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Recent Progress in Jets a.k.a. The path from Clustering to Jetography

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> Contains work done in collaboration with G. Salam, G, Soyez, J. Rojo



Introductory remarks and review

- New jet algorithms (anti-k_t, SISCone) and FastJet
- New properties/tools: areas, backreaction, filtering
- Two examples: jet quality for a mass peak and Higgs search using jet substructure

Summary/conclusions

Why jets



A jet is something that happens in high energy events:

a collimated bunch of hadrons flying roughly in the same direction

Note: hundreds of hadrons contain **a lot** of information. More than we can hope to make use of





Often you don't need a fancy algorithm to 'see' the jets

But you do to give them a **precise** and **quantitative** meaning

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Why jets

Jets are usually related to an underlying perturbative dynamics (i.e. quarks and gluons)

The purpose of a 'jet clustering' algorithm is then to reduce the complexity of the final state, simplifying many hadrons to simpler objects that one can hope to calculate

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Jet algorithm

A **jet algorithm** maps the momenta of the final state particles into the momenta of a certain number of jets:



Most algorithms contain a resolution parameter, \mathbf{R} , which controls the extension of the jet



Les Houches 2007 proceedings, arXiv:0803.0678



Reminder: running a jet definition gives a well defined physical observable, which we can measure and, hopefully, calculate

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Two main classes of jet algorithms

Sequential recombination algorithms

bottom-up approach: combine particles starting from closest ones How? Choose a distance measure, iterate recombination until few objects left, call them jets

Work because of mapping closeness ⇔ QCD divergence

Examples: Jade, kt, Cambridge/Aachen, anti-kt,

Cone algorithms

top-down approach: find coarse regions of energy flow.

How? Find stable cones (i.e. their axis coincides with sum of momenta of particles in it)

Work because QCD only modifies energy flow on small scales Examples: JetClu, MidPoint, ATLAS cone, CMS cone,

Snowmass

FERMILAB-Conf-90/249-E [E-741/CDF]

Toward a Standardization of Jet Definitions ·

* To be published in the proceedings of the 1990 Summer Study on High Energy Physics, *Research Directions for the Decade*, Snowmass, Colorado, June 25 - July 13, 1990.



Snowmass set standards, but didn't provide solutions

Cone algorithms

Finding all stable cones (and hence produce an infrared and collinear (IRC) safe cone algorithm) would naively take N2^N operations

This is roughly the age of the universe for just 100 particles

Too slow. Resort to approximate methods

Example of IC-SM: MidPoint Cone

Begin with seed particles

Cluster particles into cone if $\Delta R < R$

Iterate until stable (i.e. axis coincide with sum of momenta) cones found

Start new search cones at midpoint of stable cones

Merge jets if overlapping energy is > f times the energy of the smaller jet

Use of seeds is the most problematic issue

MidPoint infrared unsafety



G. Salam

by the MidPoint algorithm

now found

The problem is that the specific stable-cone search procedure used by MidPoint cannot find **all** possible stable cones

Example of IC-PR (e.g. CMS cone)



Begin with hardest particle as seed

Cluster	particles	into	cone	if	ΔR	<	R
---------	-----------	------	------	----	----	---	---

Iterate until stable (i.e. axis coincide with sum of momenta) cones found

Eliminate constituents of jet and start over from hardest remaining particle

NB. This is a very different algorithm from previous one. Many physics aspects differ.

IC-PR cone collinear unsafety



Splitting the hardest particle **collinearly** changes the number of final jets

A long list of cones (all eventually unsafe)

Les Houches 2007 proceedings, arXiv:0803.0678

				P	L	
S	CDF JetClu		IC_r -SM	IR ₂₊₁		
E CDF MidPoint cone		;	IC _{mp} -SM	IR ₃₊₁		
'First-generation' algorithms	CDF MidPoint searc	chcone	$IC_{se,mp}$ -SM	IR ₂₊₁		
ulgo	D0 Run II cone		IC_{mp} -SM	IR ₃₊₁		
n S						
tio	ATLAS Cone		IC-SM	IR_{2+1}		
era	PxCone		IC_{mp} -SD	IR ₃₊₁		
GU						
5 1 -8	CMS Iterative Cone		IC-PR	$Coll_{3+1}$		
	PyCell/CellJet (from	n Pythia)	FC-PR	$Coll_{3+1}$		
9	GetJet (from ISAJE	T)	FC-PR	$Coll_{3+1}$		
safety issue						
IC = Ite	rative Cone					
SM = Split-Merge		type of		IR _{n+1} : unsafe when a soft particle is addee		
SD = Split-Drop		algorithm	n hard partic	n hard particles in a common neighbourhood		
FC = Fixed Cone			Coll _{n+1} : unsa	ife when one of n	hard particles in	
PR = Pr 1atteo Cacciari - L	ogressive Removal	DESY - Septeml	a common r	neighbourhood is s	split collinearly	

Lessons

There isn't **one** cone algorithm, but rather many different cones, which can behave quite distinctly from one another

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Essentially all of the cones commonly used are <u>unsafe</u> at some point. The best ones only fail at NNLO (3+1), others already at NLO (2+1)

		Last meaningful order			
Examples:		ATLAS cone	MidPoint	CMS it. cone	
		[IC-SM]	[IC _{mp} -SM]	[IC-PR]	
	Inclusive jets	LO	NLO	NLO	
	W/Z+1 jet	LO	NLO	NLO	
	3 jets	none	LO	LO	
	W/Z + 2 jets	none	LO	LO	
	$m_{ m jet}$ in $2j+X$	none	none	none	

Calculations cost real money:

~ 100 theorists ×15 years ≈100 M€

Using unsafe jet tools essentially renders them useless

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Recombination algorithms: kt

Longitudinally invariant k_t:

S. Catani, Y. Dokshitzer, M. Seymour and B. Webber, Nucl. Phys. B406 (1993) 187 S.D. Ellis and D.E. Soper, Phys. Rev. D48 (1993) 3160

Calculate the distances between the particles: $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \frac{\Delta y^2 + \Delta \phi^2}{R^2}$

Calculate the beam distances: $d_{iB} = k_{ti}^2$

Combine particles with smallest distance or, if d_{iB} is smallest, call it a jet

Find again smallest distance and repeat procedure until no particles are left

This is infrared and collinear safe, but finding all the distances is an N² operation, to be repeated N times

 \Rightarrow naively, the k_t jet algorithm scales like N³

Faster than the cone, but still too slow: about 60 seconds for 4000 particles

FastJet and SISCone

Both the N³/speed problem of kt and the N2^N/speed/ IRC safety of the cone were solved by shifting the problem from combinatorics to geometry

k_t was made fast by reducing the problem to near-neighbour searches, and using Voronoi diagrams to reduce complexity to NInN (MC, Salam, hep-ph/0512210)

Cone was made fast (and IRC safe) by inventing circular enclosures to find stable cones and reduce complexity to N²In N (Salam, Soyez, arXiv: 0704.0292)

Both implementations (and a lot more) available via FastJet <u>www.fastjet.fr</u>

FastJet performance (k_t)

Time taken to cluster N particles:



SISCone performance



Cones Infrared (un)safety

Q: How often are the hard jets changed by the addition of a soft particle?

- Generate event with
 2 < N < 10 hard particles,
 find jets
- Add 1 < N_{soft} < 5 soft particles, find jets again
 (repeatedly)
 - If the jets are different, algorithm is IR unsafe.

Unsafety level	failure rate
2 hard + 1 soft	$\sim 50\%$
3 hard + 1 soft	$\sim 15\%$
SISCone	IR safe !

Be careful with split-merge too

	good bad	
[
	JetClu 50.1%	
	SearchCone 48.2%	
	MidPoint 16.4%	
	Midpoint-3 15.6%	
	PxCone 9.3%	
	Seedless [SM-p _t] 1.6%	ez
	0.17% Seedless [SM-MIP]	Soy
	0 (none in 4x10 ⁹) Seedless (SISCone)	Salam & Soyez
ا 10	10^{-5} 10^{-4} 10^{-3} 10^{-2} 10^{-1} 1	Sa
	Fraction of hard events failing IR safety test	

Beyond k_t

One can generalise the k_{r} distance measure:

$$d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \frac{\Delta y^2 + \Delta \phi^2}{R^2} \qquad d_{iB} = k_{ti}^{2p}$$

P = k algorithm S. Catani, Y. Dokshitzer, M. Seymour and B. Webber, Nucl. Phys. B406 (1993) 187 S.D. Ellis and D.E. Soper, Phys. Rev. D48 (1993) 3160

p = 0 Cambridge/Aachen algorithm ^{Y. Dokshitzer, G. Leder, S. Moretti and B. Webber, JHEP 08 (1997) 001 M. Wobisch and T. Wengler, hep-ph/9907280}

p = -1 anti-k_t algorithm

MC, G. Salam and G. Soyez, arXiv:0802.1189

NB: in anti-kt pairs with a **hard** particle with cluster first: if no other hard particles are close by, the algorithm will give **perfect cones**

Quite ironically, a sequential recombination algorithm is the perfect cone algorithm

The IRC safe algorithms					
k t	$SR \\ d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2 \\ hierarchical in rel P_t$	Catani et al '91 Ellis, Soper '93	NInN		
Cambridge/ Aachen	$SR \\ d_{ij} = \Delta R_{ij}^2 / R^2 \\ hierarchical in angle$	Dokshitzer et al '97 Wengler, Wobish '98	NInN		
anti-k _t	$SR \\ d_{ij} = \min(k_{ti}^{-2}, k_{tj}^{-2}) \Delta R_{ij}^{2}/R^{2} \\ gives perfectly conical hard jets$	MC, Salam, Soyez '08 (Delsart, Loch)	N ^{3/2}		
SISCone	Seedless iterative cone with split-merge gives 'economical' jets	Salam, Soyez '07	N²InN		
We call these algs 'second-generation' ones					
All are available in FastJet, <u>http://fastjet.fr</u>					

(As well as many IRC unsafe ones)

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Replacements

If you care about IRC safety but don't want to stray too far from algorithms used so far, these are possible replacements:



In addition, kt and Cambridge/Aachen can provide further flexibility

Different algorithms spanning a series of <u>different and complementary</u> <u>characteristics</u>: should be enough for most purposes

One should probably try to concentrate on these, both for analytical understanding and practical use in experiments, rather than using IRC unsafe ones

Jet areas

So far, old jet clustering, just better and/or faster

High speed and infrared safety allow for a **qualitatively new use** of jet clustering, through **new features: jet areas**

It's an example of making a different use of jets:



Jet areas: the physics case



In a realistic set-up underlying event (UE) and pile-up (PU) from multiple collisions produce many soft particles which can 'contaminate' the hard jet

$$p_T$$
 (jet) ~ p_T (parton) .

Average underlying momentum density

× 'size' of the jet



Not one, but three **<u>definitions</u>** of a jet's size:

MC, Salam, Soyez, arXiv:0802.1188



Voronoi area



Passive area Mimics effect of **pointlike** radiation



Active area

Mimics effect of **diffuse** radiation

(In the large number of particles limit all areas converge to the same value)

Details

Jet active areas

Active areas are calculated by adding thousands of `ghost' particles, clustering them with the event, and counting how many end

30 -

25

20

15

10

5





















-2

CMS Iterative Cone, R=1











Jet areas: the link to physics

The definition of **active area** mimics the behaviour of the jet-clustering algorithms in the presence of a **large number of randomly distributed soft particles**

This is like underlying event or pileup.

Tools needed to implement it:

- I. An infrared safe jet algorithm (the ghosts should not change the jets)
- 2. A reasonably **fast implementation** (we are adding thousands of ghosts) Both are available

Backreaction

"How (much) a jet changes when immersed in a background"

Without background

With background





Backreaction

MC, Salam, Soyez, arXiv:0802.1188



Anti-kt jets are much more resilient to changes from background immersion

Jet area as a tool

Underlying event and pileup determination and subtraction



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When 'measuring' the background, R should be not too small (too many empty jets) and not too large (too few jets, biased by the hard particles)

Theoretical estimates and empirical evidence point to $R \sim 0.5$ --0.6 for Underlying Event measurement (Also, a 'sensible' jet alg like kt or Cambridge/Aachen should be used)

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Background subtraction

[MC, Salam, arXiv:0707.1378]

Once measured, the background density can be used to correct the transverse momentum of the hard jets:

$$p_T^{\text{hard jet, corrected}} = p_T^{\text{hard jet, raw}} - \rho \times \text{Area}_{\text{hard jet}}$$

ρ being calculated on an event-by-event basis, this procedure will generally improve the resolution of, say, a mass peak

NB. Also be(a)ware of backreaction

(immersing a hard jet in a soft background may cause some particles belonging to the hard event to be lost from (backreaction loss) or added to (backreaction gain) the jet). Small effect for UE, larger for pileup, can be very important for heavy ions. Analytical understanding of this effect available (MC, Salam, Soyez, arXiv:0802:1188)

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Example of pileup subtraction

Let's discover a leptophobic Z' and measure its mass:



Flexibility

All IRC safe algorithms are equal, but some are more equal than others

Depending on the analysis you wish to perform, a jet **definition** might give better results than others

Which R to choose?

The value of R matters because it affects, in opposite ways, a number of things:

Small R:Limit underlying event and pileup contaminationBetter resolve many-jets events

Large R: Limit perturbative radiation loss ('out-of-cone') Limit non-perturbative hadronisation effects

The best compromise will in general depend on the specific observable

R-dependent effects

Perturbative radiation: $\Delta p_t \simeq \frac{\alpha_s(C_F, C_A)}{\pi} p_t \ln R$

Hadronisation: $\Delta p_t \simeq \frac{(C_F, C_A)}{R} \times 0.4 \text{ GeV}$

 $\label{eq:constraint} \begin{array}{ll} \mbox{Underlying Event:} & \Delta p_t \simeq \frac{R^2}{2} \times (2.5 - 15 \ {\rm GeV}) \end{array}$

Analytical estimates, Dasgupta, Magnea, Salam, arXiv:0712.3014

Best R

Minimize $\Sigma(\Delta p_t)^2$



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Cambridge/Aachen with filtering

Butterworth, Davison, Rubin, Salam, arXiv:0802.2470

An example of a **third-generation** jet algorithm



Cluster with C/A and a given R

Undo the clustering of each jet down to subjets with radius XfiltR

Retain only the **n**_{filt} hardest subjets

Aim: limit sensitivity to background while retaining bulk of perturbative radiation

Jets substructure in Higgs searches

$H \rightarrow b\overline{b}$ in the WH/ZH channels

Usually considered hopeless:

Conclusion (ATLAS TDR):

"The extraction of a signal from $H \rightarrow b\bar{b}$ decays in the WH channel will be very difficult at the LHC, even under the most optimistic assumptions [...]"

New way of going at it: use large pt (boosted Higgs), exploit jet substructure

Butterworth, Davison, Rubin, Salam, arXiv:0802.2470

#2: The jet analysis



Start with high- p_t jet

- 1. Undo last stage of clustering (\equiv reduce R): $J \rightarrow J_1, J_2$
- 2. If $max(m_1, m_2) \lesssim 0.67m$, call this a mass drop [else goto 1] Automatically detects correct $R \sim R_{bb}$ to catch angular-ordered radn.
- 3. Require $y_{12} = \frac{\min(p_{t1}^2, p_{t2}^2)}{m_{12}^2} \Delta R_{12}^2 \simeq \frac{\min(z_1, z_2)}{\max(z_1, z_2)} > 0.09$ [else goto 1] dimensionless rejection of asymmetric QCD branching
- 4. Require each subjet to have *b*-tag [else reject event] Correlate flavour & momentum structure

#3: jet filtering



At moderate p_t , R_{bb} is quite large; $UE \& pileup \ degrade \ mass \ resolution$ $\delta M \sim R^4 \Lambda_{UE} \frac{p_t}{M}$ [Dasgupta, Magnea & GPS '07]

Filter the jet

- Reconsider region of interest at smaller $R_{filt} = \min(0.3, R_{b\bar{b}}/2)$
- Take 3 hardest subjets b, \bar{b} and leading order gluon radiation

SIGNAL

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Zbb BACKGROUND

Cambridge/Aachen, R=1.2

arbitrary norm.



arbitrary norm.



arbitrary norm.





arbitrary norm.



arbitrary norm.

combine HZ and HW, $p_t > 200 \text{ GeV}$



<u>Common cuts</u>

- $p_{tV}, p_{tH} > 200 \text{ GeV}$
- ► $|\eta_H| < 2.5$
- ▶ $[p_{t,\ell} > 30 \text{ GeV}, |\eta_{\ell}| < 2.5]$
- ▶ No extra ℓ , *b*'s with $|\eta| < 2.5$
- Real/fake *b*-tag rates: 0.7/0.01

► S/\sqrt{B} from 16 GeV window

<u>3 channels combined</u> Note excellent $VZ, Z \rightarrow b\overline{b}$ peak for calibration NB: $q\overline{q}$ is mostly $t\overline{t}$

At 5.9 σ for 30 fb⁻¹ this looks like a possible new channel for light Higgs discovery. **Deserves serious exp. study!**

The IRC safe algorithms

	Speed	Regularity	UE	Backreaction	Hierarchical substructure
k t	0000	Ţ	ŢŢ		0 0
Cambridge /Aachen	000	Ţ	Ţ		000
anti-k _t	0000	00	♣/☺	00	×
SISCone	\odot	•	☺ ☺	•	×





An extensive set of fast, IRC safe jet algorithms exists, offering replacements for the IRC unsafe ones.

They offer ample flexibility in choosing the most effective jet definition for any given analysis.



They can be used to estimate the level of a uniformly distributed noise, and study its characteristics.



They can be used to subtract the noise from the hard jets, improving the quality of kinematical reconstructions.

'Third-generation' algorithms look promising.

Extra material

The FastJet algorithm

To improve the speed of the algorithm we must find more efficiently which particle is "close" to another and therefore gets combined with it

Observation (MC, G.P. Salam, hep-ph/0512210):

If i and j form the smallest $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \frac{\Delta \eta^2 + \Delta \phi^2}{R^2}$ and $k_{ti} < k_{tj}$ \Longrightarrow $\Delta R_{ij} \le \Delta R_{ik}$ $\forall k \neq j$

i.e. j is the **geometrical** nearest neighbour of i

Translation from mathematics:

When a particle gets combined with another, and has the smallest kt, its partner will be its **geometrical nearest neighbour** on the cylinder spanned by y and ϕ

This means that we need to look for partners only among the O(N) nearest neighbours of all particles (a few neighbours each × N particles)

The FastJet algorithm

Our problem has now become a **geometrical** one: how to find efficiently the (nearest) neighbour(s) of a point

Widely studied problem in computational geometry Tool: **Voronoi diagram**

Definition: each cell contains the locations which have the given point as nearest neighbour



The **dual** of a Voronoi diagram is a **Delaunay triangulation**

Key feature: once the Voronoi diagram is constructed, the nearest neighbour of a point will be in one of the O(1) cells sharing an edge with its own cell

Example : the G(eometrical) N(earest) N(eighbour) of point 7 will be found among 1,4,2,8 and 3 (it turns out to be 3)

The FastJet algorithm

MC and G.P. Salam, hep-ph/0512210

Construct the Voronoi diagram of the N particles O(N InN) using the CGAL library O(N In N of each of the N particles. Construct the d_{ij} distances, store the results in a priority queue (C++ map) O(N InN) Merge/eliminate particles appropriately repeat N Update Voronoi diagram and distances' map O(InN)

Overall, an O(N In N) algorithm

<u>NB.</u> Results identical to standard k_t algorithm. This is NOT a new jet-finder.

The SISCone algorithm

[Salam, Soyez, arXiv: 0704.0292]

Checking **all particles** in an event to test for <u>stable combinations</u>

(i.e. the axis of the cone containing a subset of particles coincides with the momentum sum) takes $O(N2^N)$ time

Solution: once more, transform into a geometrical problem

- I. Find all distinct way of enclosing a set of particles in a y- ϕ circle
- 2. Check, for each enclosure, if it corresponds to a stable cone



Finding all distinct circular enclosures of a set of points is <u>geometry</u>: move it until you hit a point, then rotate it until one of the points hits the edge <u>Result</u>: <u>Seedles Infrared Safe Cone (SISCone)</u> [runs in $O(N^2 \ln N)$ time, similar to MidPoint (N³)]

<Theoretical interlude>

Jet passive area

Passive Area

Add a **single** ghost^{*} particle to the event. Move it around. Check if it gets clustered in a given jet J.

$$a(J) \equiv \int dy d\phi f(g(y,\phi),J) \qquad \qquad f(g,J) = \begin{cases} 1 & g \in J \\ 0 & g \notin J \end{cases}$$

* ghost particle: particle with infinitesimally small momentum with respect to all other particles in the event (in practice, $O(10^{-100} \text{ GeV})$)

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Jet Active area

Active Area

Add **many** ghost particles in random configurations to the event. Cluster many times. Allow ghosts to cluster among themselves too. Count how many ghosts <u>on average</u> get clustered into a given jet J.



$$A(J) = \lim_{v_g \to \infty} \langle A(J | \{g_i\}) \rangle_g$$

Active area



Recall that 'area' is how much background a a jet can pick up. Its knowledge is essential in order to subtract it from measurements

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Jet areas: a second hard(ish) particle

 Δ_{12}

Real events have more than a single hard particle. Add a second (soft) one at a distance Δ_{12}



Passive areas (and SISCone's active area) can be calculated analytically, while the others are obtained numerically

Jet areas: anomalous dimensions

Finally, weigh the probability of emission of the soft particle with the leading-order QCD matrix element:

$$\langle \Delta area \rangle = \int C_1 \frac{\alpha_s(p_{t2}\Delta_{12})}{\pi} \frac{dp_{t2}}{p_{t2}} \left[\frac{d\Delta_{12}}{\Delta_{12}} \right]_+ \begin{pmatrix} 1 & \Delta_{12} & 2\\ \bullet & --- & \bullet\\ hard & soft \end{pmatrix}$$

The result is an **anomalous dimension**.

Areas change with transverse momentum of the jet in a predictable way:

$$\langle \Delta area
angle = \mathbf{d} \; \; rac{C_1}{\pi b_0} \ln rac{lpha_s(Q_0)}{lpha_s(Rp_{t1})}$$

In a similar way one can also predict the evolution of the dispersion, calculating

$$\langle \Delta area^2 \rangle = s^2 \frac{C_1}{\pi b_0} \ln \frac{\alpha_s(Q_0)}{\alpha_s(Rp_{t1})}$$

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Passive areas: analytical results

MC, Salam, Soyez, arXiv:0802.1188

$$\begin{aligned} d_{k_{t},R} &= \left(\frac{\sqrt{3}}{8} + \frac{\pi}{3} + \xi\right) R^{2} \simeq 0.5638 \,\pi R^{2} \,, \\ d_{\text{Cam},R} &= \left(\frac{\sqrt{3}}{8} + \frac{\pi}{3} - 2\xi\right) R^{2} \simeq 0.07918 \,\pi R^{2} \,, \\ d_{\text{SISCone},R} &= \left(-\frac{\sqrt{3}}{8} + \frac{\pi}{6} - \xi\right) R^{2} \simeq -0.06378 \,\pi R^{2} \,, \\ \begin{array}{l} \text{Negative!} \\ \text{SISCone} \\ \text{jets shrink!} \end{array}$$

$$s_{k_t,R}^2 = \left(\frac{\sqrt{3}\pi}{4} - \frac{19}{64} - \frac{15\zeta(3)}{8} + 2\pi\xi\right)R^4 \simeq (0.4499 \pi R^2)^2,$$

$$s_{\text{Cam},R}^2 = \left(\frac{\sqrt{3}\pi}{6} - \frac{3}{64} - \frac{\pi^2}{9} - \frac{13\zeta(3)}{12} + \frac{4\pi}{3}\xi\right)R^4 \simeq (0.2438 \pi R^2)^2,$$

$$s_{\text{SISCone},R}^2 = \left(\frac{\sqrt{3}\pi}{12} - \frac{15}{64} - \frac{\pi^2}{18} - \frac{13\zeta(3)}{24} + \frac{2\pi}{3}\xi\right)R^4 \simeq (0.09142 \pi R^2)^2.$$

with
$$\xi \equiv \frac{\psi'(1/6) + \psi'(1/3) - \psi'(2/3) - \psi'(5/6)}{48\sqrt{3}} \simeq 0.507471$$

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d:

Jet areas: passive v. active

		-						
	area/ π R ²		dispersion		d or D		s or S	
	passive	active	passive	active	passive	active	passive	active
	a(1PJ)	$A(1\mathrm{PJ})$	$\sigma(1PJ)$	$\Sigma(1\rm{PJ})$	d	D	<i>s</i>	S
k_t	1	0.81	0	0.28	0.56	0.52	0.45	0.41
Cam/Aachen	1	0.81	0	0.26	0.08	0.08	0.24	0.19
SISCone	1	1/4	0	0	-0.06	0.12	0.09	0.07
anti- k_t	1	1	0	0	0	0	0	0
	si	ngle har	emission of a second perturbative particle (coeff. of anomalous dimension)					

Some remarkable features

- SISCone has very small active area
- SISCone's anomalous dimension changes from negative for passive area to positive for active area
- kt has largest anomalous dimension
- anti-kt has constant area (null anomalous dimension): it's a perfect cone

Jet areas scaling violations



Averages and dispersions evolution from Monte Carlo simulations (dijet events at LHC) in good agreement with simple LL calculations



(Though it might not be the best place where to measure α_{s} )

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Jet areas scaling violations

MC, Salam, Soyez, arXiv:0802.1189

Check anti-k, behaviour: scaling violations indeed absent, as predicted



</Theoretical interlude>

Underlying event measurement



Marchesini-Webber idea: look at transverse region to measure underlying event



Topological selection

The jets are classified as belonging to the noise on the ground of their **position**

Area v. рт

LHC: dijet event + high-lumi pilup

a few hard particles and many softer ones

(a similar picture applies to the Underlying Event)



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The key observation

 p_{T} /Area is fairly constant, except for the hard jets

