DESY Zeuthen September 23, 2009

## Recent Progress in Jets a.k.a.

## The path from Clustering to Jetography

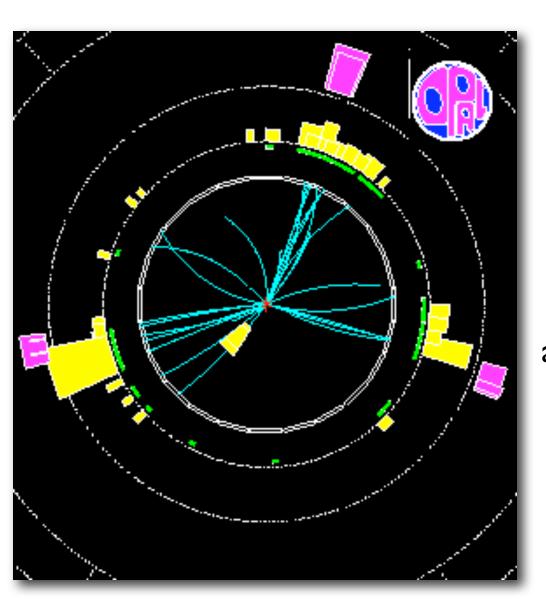
Matteo Cacciari LPTHE - Paris 6,7 and CNRS

Contains work done in collaboration with G. Salam, G, Soyez, J. Rojo

#### Outline

- Introductory remarks and review
- New jet algorithms (anti-kt, SISCone) and FastJet
- New properties/tools: areas, backreaction, filtering
- Two examples: jet quality for a mass peak and Higgs search using jet substructure
- Summary/conclusions

#### Why jets

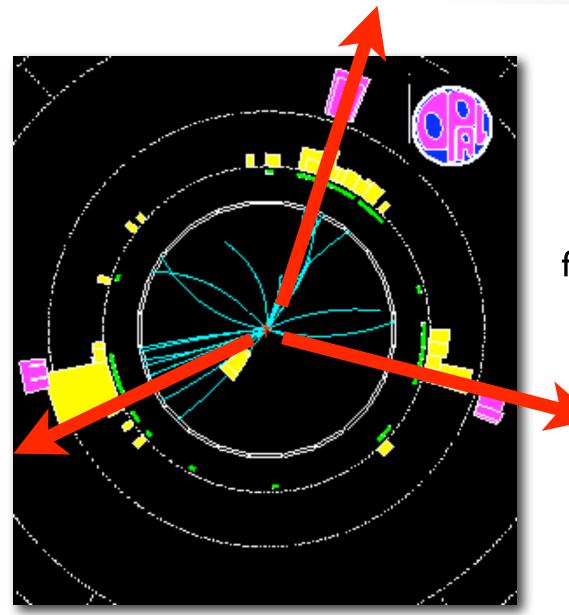


A jet is something that happens in high energy events:

a collimated bunch of hadrons flying roughly in the same direction

Note: hundreds of hadrons contain **a lot** of information. More than we can hope to make use of

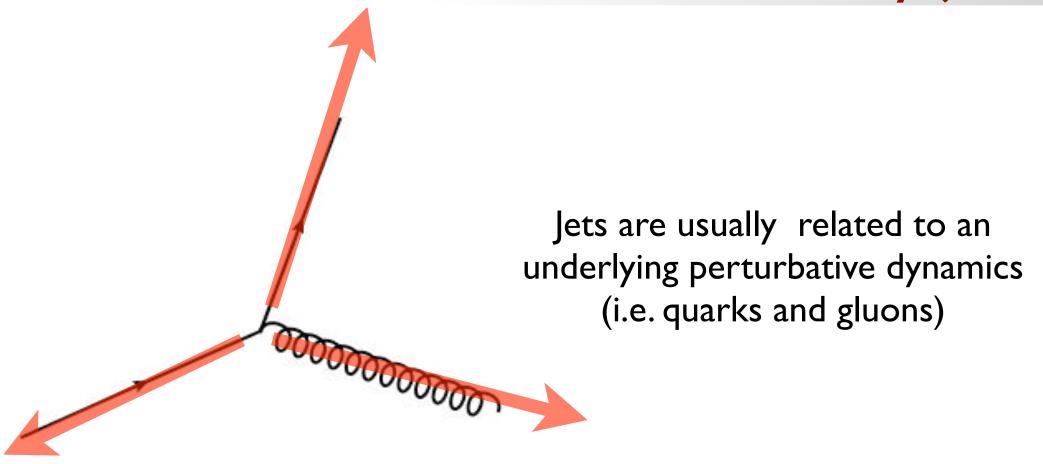
Why jets



Often you don't need a fancy algorithm to 'see' the jets

But you do to give them a **precise** and **quantitative** meaning

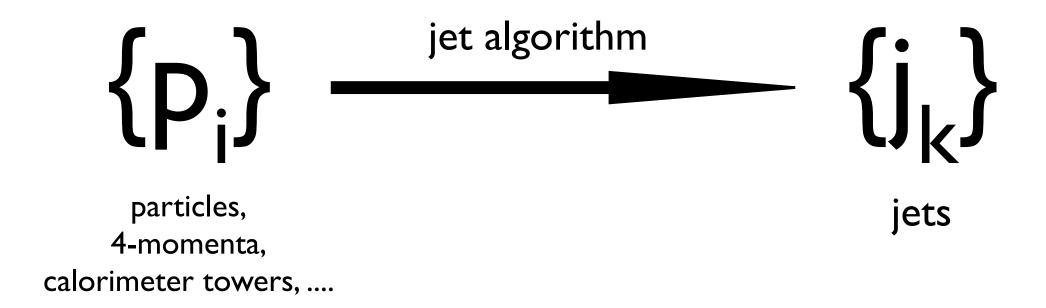
#### Why jets



The purpose of a 'jet clustering' algorithm is then to reduce the complexity of the final state, simplifying many hadrons to simpler objects that one can hope to calculate

### Jet algorithm

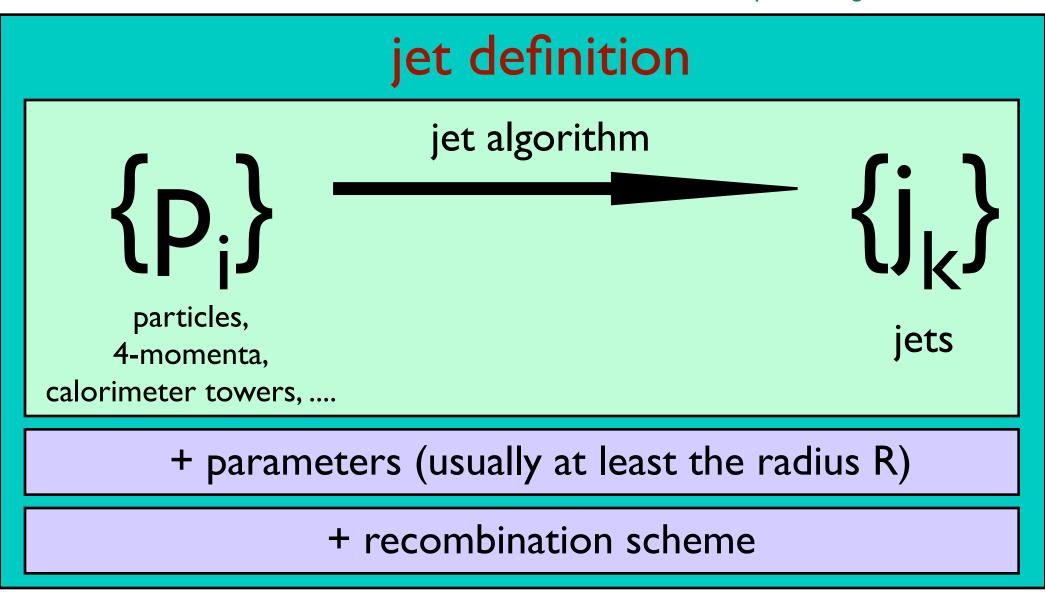
A **jet algorithm** maps the momenta of the final state particles into the momenta of a certain number of jets:



Most algorithms contain a resolution parameter, **R**, which controls the extension of the jet

## Jet definition

Les Houches 2007 proceedings, arXiv:0803.0678



Reminder: running a jet definition gives a well defined physical observable, which we can measure and, hopefully, calculate

#### Two main classes of jet algorithms

#### Sequential recombination algorithms

bottom-up approach: combine particles starting from closest ones

**How?** Choose a **distance measure**, iterate recombination until few objects left, call them jets

Work because of mapping closeness  $\Leftrightarrow$  QCD divergence Examples: Jade,  $k_t$ , Cambridge/Aachen, anti- $k_t$ , .....

#### **Cone algorithms**

top-down approach: find coarse regions of energy flow.

How? Find stable cones (i.e. their axis coincides with sum of momenta of particles in it)

Work because QCD only modifies energy flow on small scales Examples: JetClu, MidPoint, ATLAS cone, CMS cone, ......

#### Snowmass

#### FERMILAB-Conf-90/249-E [E-741/CDF]

#### Toward a Standardization of Jet Definitions .

\* To be published in the proceedings of the 1990 Summer Study on High Energy Physics, Research Directions for the Decade, Snowmass, Colorado, June 25 - July 13, 1990.

Several important properties that should be met by a jet definition are [3]:

- 1. Simple to implement in an experimental analysis;
- 2. Simple to implement in the theoretical calculation;
- 3. Defined at any order of perturbation theory;
- 4. Yields finite cross section at any order of perturbation theory;
- 5. Yields a cross section that is relatively insensitive to hadronization.

**Speed** 

Infrared and collinear safety

[Addition of a soft particle or a collinear splitting should not change final hard jets]

Snowmass set standards, but didn't provide solutions

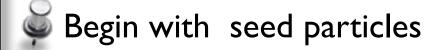
#### Cone algorithms

Finding all stable cones (and hence produce an infrared and collinear (IRC) safe cone algorithm) would naively take N2<sup>N</sup> operations

This is roughly the age of the universe for just 100 particles

Too slow.
Resort to approximate methods

### Example of IC-SM: MidPoint Cone



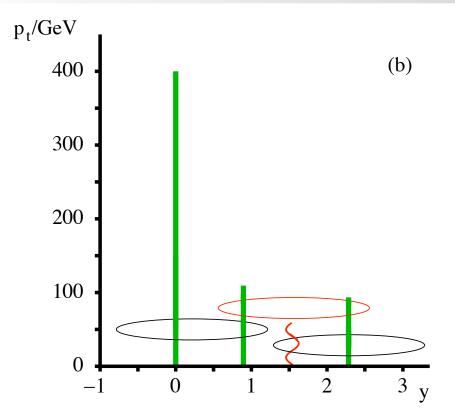
ightharpoonup Cluster particles into cone if  $\Delta R < R$ 

lterate until stable (i.e. axis coincide with sum of momenta) cones found

Start new search cones at midpoint of stable cones

Merge jets if overlapping energy is > f times the energy of the smaller jet

Use of seeds is the most problematic issue



Three hard particles clustered into **two** cones by the MidPoint algorithm

Addition of a **soft** particle changes the hard jets: **three** stable cones are now found

The problem is that the specific stable-cone search procedure used by MidPoint cannot find **all** possible stable cones

G. Sal

## Example of IC-PR (e.g. CMS cone)



ightharpoonup Cluster particles into cone if  $\Delta R < R$ 

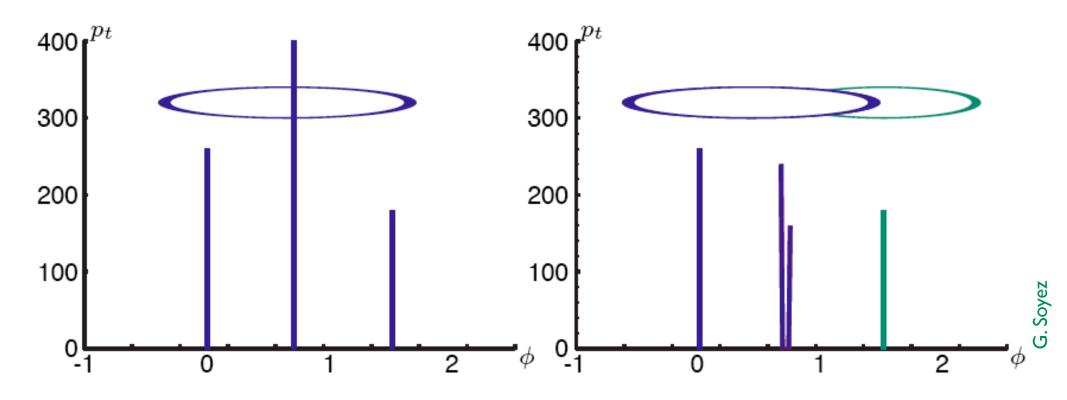
Iterate until stable (i.e. axis coincide with sum of momenta) cones found

Eliminate constituents of jet and start over from hardest remaining particle

NB. This is a very different algorithm from previous one.

Many physics aspects differ.

#### IC-PR cone collinear unsafety



Splitting the hardest particle **collinearly** changes the number of final jets

#### A long list of cones (all eventually unsafe)

Les Houches 2007 proceedings, arXiv:0803.0678

		ı'
CDF JetClu	$IC_r$ -SM	$IR_{2+1}$
CDF MidPoint cone	$IC_{mp}$ -SM	IR <sub>3+1</sub>
CDF MidPoint searchcone	$IC_{se,mp}$ -SM	$IR_{2+1}$
D0 Run II cone	$IC_{mp}$ -SM	IR <sub>3+1</sub>
ATLAS Cone	IC-SM	$IR_{2+1}$
PxCone	$IC_{mp}$ -SD	IR <sub>3+1</sub>
CMS Iterative Cone	IC-PR	Coll <sub>3+1</sub>
PyCell/CellJet (from Pythia)	FC-PR	Coll <sub>3+1</sub>
GetJet (from ISAJET)	FC-PR	Coll <sub>3+1</sub>
<u> </u>		

IC = Iterative Cone

SM = Split-Merge

SD = Split-Drop

FC = Fixed Cone

PR = Progressive Removal

type of algorithm IR<sub>n+1</sub>: unsafe when a soft particle is added to n hard particles in a common neighbourhood

Coll<sub>n+1</sub>: unsafe when one of n hard particles in

a common neighbourhood is split collinearly

DESY - September 12-23, 2009

safety issue



There isn't one cone algorithm, but rather many different cones, which can behave quite distinctly from one another



Essentially all of the cones commonly used are unsafe at some point. The best ones only fail at NNLO (3+1), others already at NLO (2+1)

		Last meaningful order			
Examples:		ATLAS cone	MidPoint	CMS it. cone	
		[IC-SM]	$[IC_{mp}\text{-SM}]$	[IC-PR]	
	Inclusive jets	LO	NLO	NLO	
	W/Z+1 jet	LO	NLO	NLO	
	3 jets	none	LO	LO	
	W/Z+2 jets	none	LO	LO	
	$m_{\rm jet}$ in $2j + X$	none	none	none	

Calculations cost real money:

~ 100 theorists ×15 years ≈100 M€

Using unsafe jet tools essentially renders them useless

## Recombination algorithms: kt

#### Longitudinally invariant k<sub>t</sub>:

S. Catani, Y. Dokshitzer, M. Seymour and B. Webber, Nucl. Phys. B406 (1993) 187 S.D. Ellis and D.E. Soper, Phys. Rev. D48 (1993) 3160

- Calculate the distances between the particles:  $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \frac{\Delta y^2 + \Delta \phi^2}{R^2}$
- $\mathbf{\hat{\mathbf{\mathcal{G}}}}$  Calculate the beam distances:  $d_{iB}=k_{ti}^2$
- Combine particles with smallest distance or, if dib is smallest, call it a jet
- Find again smallest distance and repeat procedure until no particles are left

This is infrared and collinear safe, but finding all the distances is an  $N^2$  operation, to be repeated N times

 $\Rightarrow$  naively, the  $k_t$  jet algorithm scales like  $N^3$ 

Faster than the cone, but still too slow: about 60 seconds for 4000 particles

#### FastJet and SISCone

Both the N<sup>3</sup>/speed problem of kt and the N<sup>2</sup>N/speed/IRC safety of the cone were solved by shifting the problem from combinatorics to geometry

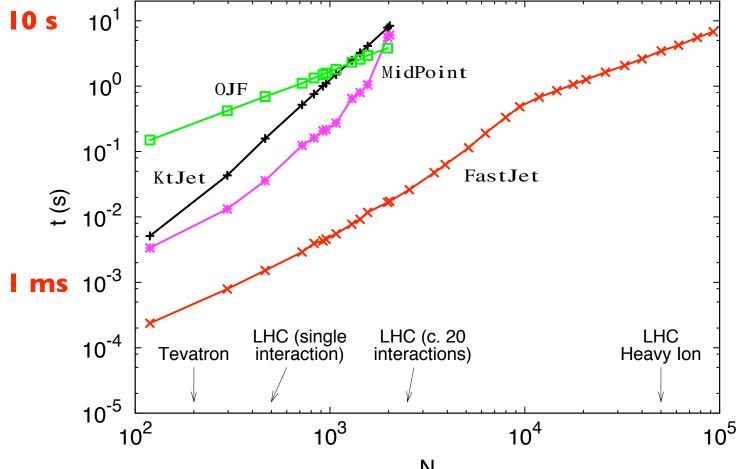
- k<sub>t</sub> was made fast by reducing the problem to near-neighbour searches, and using Voronoi diagrams to reduce complexity to NInN (MC, Salam, hep-ph/0512210)
- Cone was made fast (and IRC safe) by inventing circular enclosures to find stable cones and reduce complexity to N2In N

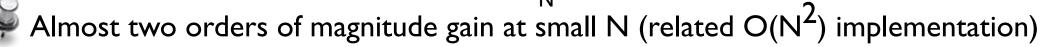
(Salam, Soyez, arXiv: 0704.0292)

Both implementations (and a lot more) available via FastJet <a href="https://www.fastjet.fr">www.fastjet.fr</a>

## FastJet performance (kt)

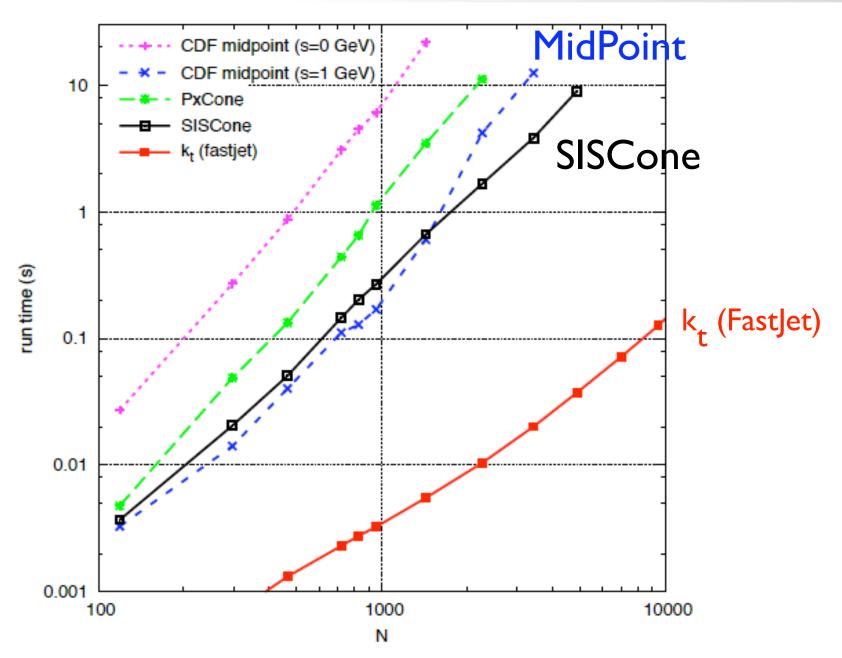
#### **Time** taken to cluster N particles:





Large-N region now reachable

#### SISCone performance



SISCone as fast as MidPoint → no penalty for infrared safety!

## Cones Infrared (un)safety

Q: How often are the hard jets changed by the addition of a soft particle?

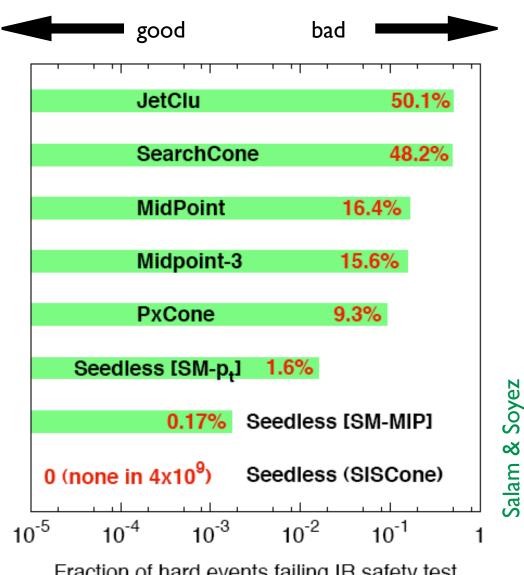
- Generate event with 2 < N < 10 hard particles, find jets
- ightharpoonup Add  $1 < N_{soft} < 5$  soft particles, find jets again

#### [repeatedly]

If the jets are different, algorithm is IR unsafe.

Unsafety level	failure rate
2  hard + 1  soft	$\sim 50\%$
3  hard + 1  soft	$\sim 15\%$
SISCone	IR safe!

Be careful with split-merge too



Fraction of hard events failing IR safety test

Matteo Cacciari - LPTHE

#### Beyond kt

One can generalise the k<sub>t</sub> distance measure:

$$d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \frac{\Delta y^2 + \Delta \phi^2}{R^2} \qquad d_{iB} = k_{ti}^{2p}$$

$$p = I k_t algorithm$$

S. Catani, Y. Dokshitzer, M. Seymour and B. Webber, Nucl. Phys. B406 (1993) 187 S.D. Ellis and D.E. Soper, Phys. Rev. D48 (1993) 3160

p = 0 Cambridge/Aachen algorithm

Y. Dokshitzer, G. Leder, S.Moretti and B. Webber, JHEP 08 (1997) 001 M.Wobisch and T.Wengler, hep-ph/9907280

$$p = -1$$
 anti- $k_t$  algorithm

MC, G. Salam and G. Soyez, arXiv:0802.1189

NB: in anti-kt pairs with a **hard** particle with cluster first: if no other hard particles are close by, the algorithm will give **perfect cones** 

Quite ironically, a sequential recombination algorithm is the perfect cone algorithm

The	<b>IRC</b>	safe	a	lgor	ithn	ns
				.0		

23

<b>k</b> <sub>t</sub>	$SR$ $d_{ij} = min(k_{ti}^{2}, k_{tj}^{2}) \Delta R_{ij}^{2}/R^{2}$ hierarchical in rel P <sub>t</sub>	Catani et al '91 Ellis, Soper '93	NInN
Cambridge/ Aachen	$SR$ $d_{ij} = \Delta R_{ij}^2 / R^2$ hierarchical in angle	Dokshitzer et al '97 Wengler, Wobish '98	NInN
anti-k <sub>t</sub>	$SR$ $d_{ij} = min(k_{ti}^{-2}, k_{tj}^{-2}) \Delta R_{ij}^{2}/R^{2}$ gives perfectly conical hard jets	MC, Salam, Soyez '08 (Delsart, Loch)	N <sup>3/2</sup>
SISCone	Seedless iterative cone with split-merge gives 'economical' jets	Salam, Soyez '07	N <sup>2</sup> InN

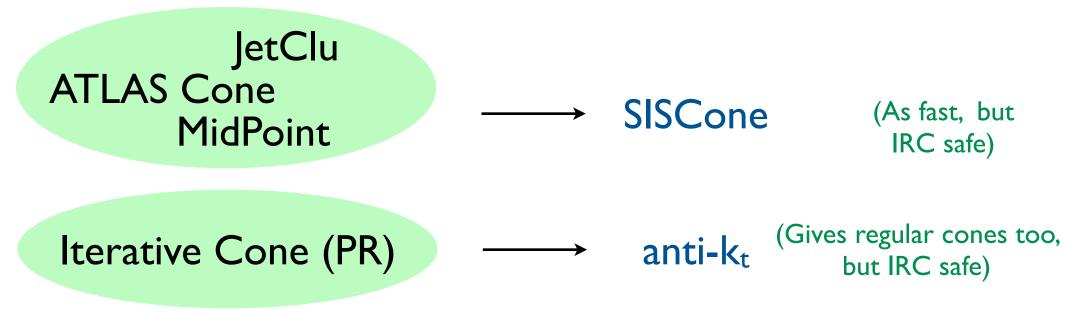
#### We call these algs 'second-generation' ones

All are available in FastJet, <a href="http://fastjet.fr">http://fastjet.fr</a>

(As well as many IRC unsafe ones)

#### Replacements

If you care about IRC safety but don't want to stray too far from algorithms used so far, these are possible replacements:



In addition, kt and Cambridge/Aachen can provide further flexibility

Different algorithms spanning a series of <u>different and complementary</u> <u>characteristics</u>: should be enough for most purposes

One should probably try to concentrate on these, both for analytical understanding and practical use in experiments, rather than using IRC unsafe ones

#### Jet areas

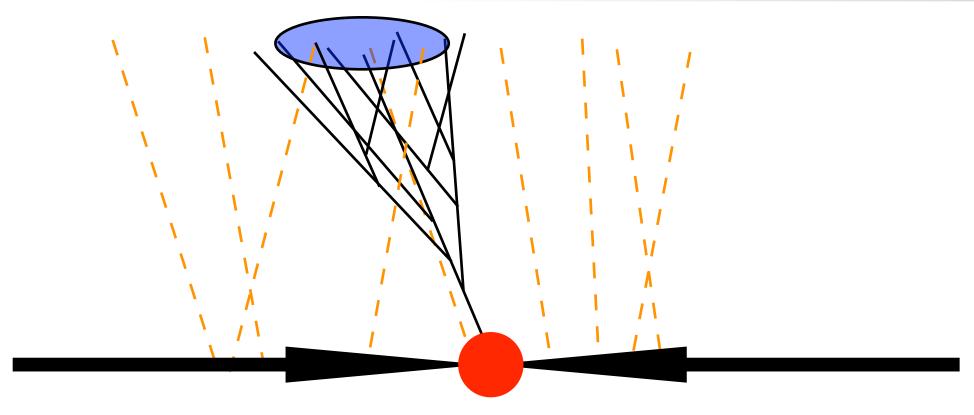
So far, old jet clustering, just better and/or faster

High speed and infrared safety allow for a qualitatively new use of jet clustering, through new features: jet areas

It's an example of making a different use of jets:



## Jet areas: the physics case



In a realistic set-up underlying event (UE) and pile-up (PU) from multiple collisions produce many soft particles which can 'contaminate' the hard jet

$$p_T$$
 (jet) ~  $p_T$  (parton) +

Average underlying momentum density

× 'size' of the jet

#### Jet areas

#### Not one, but three **definitions** of a jet's size:

MC, Salam, Soyez, arXiv:0802.1188



Passive area

Mimics effect of **pointlike** radiation

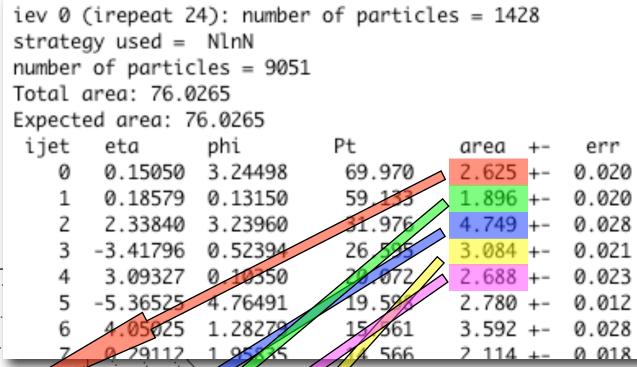
Active area

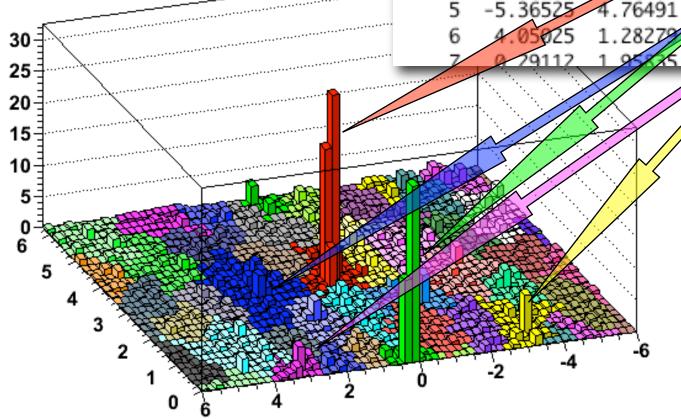
Mimics effect of diffuse radiation

(In the large number of particles limit all areas converge to the same value)

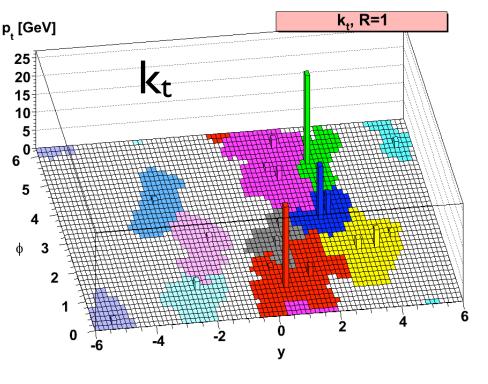
#### Jet active areas

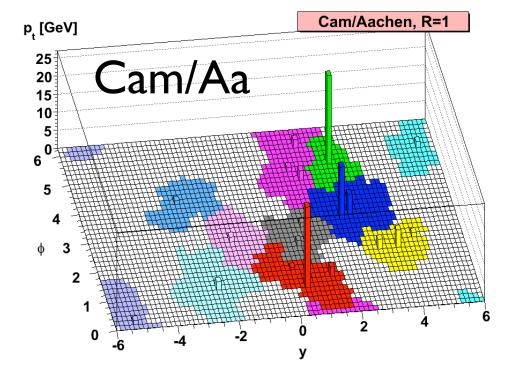
Active areas are calculated by adding thousands of `ghost' particles, clustering them with the event, and counting how many end up in a given jet

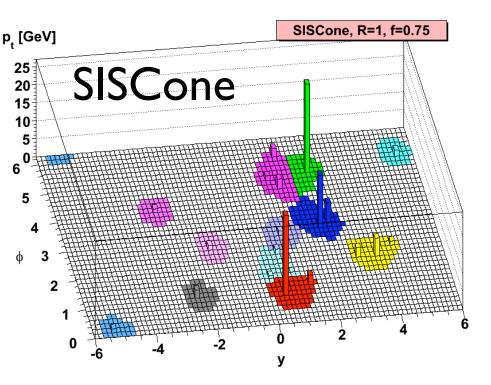


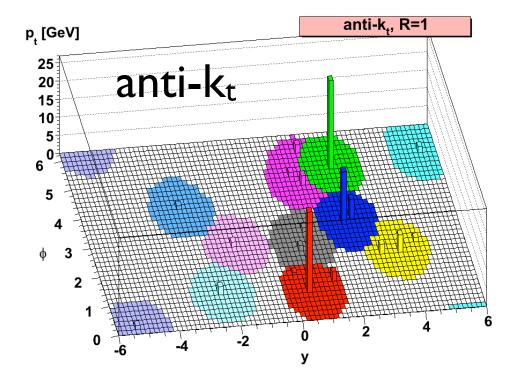


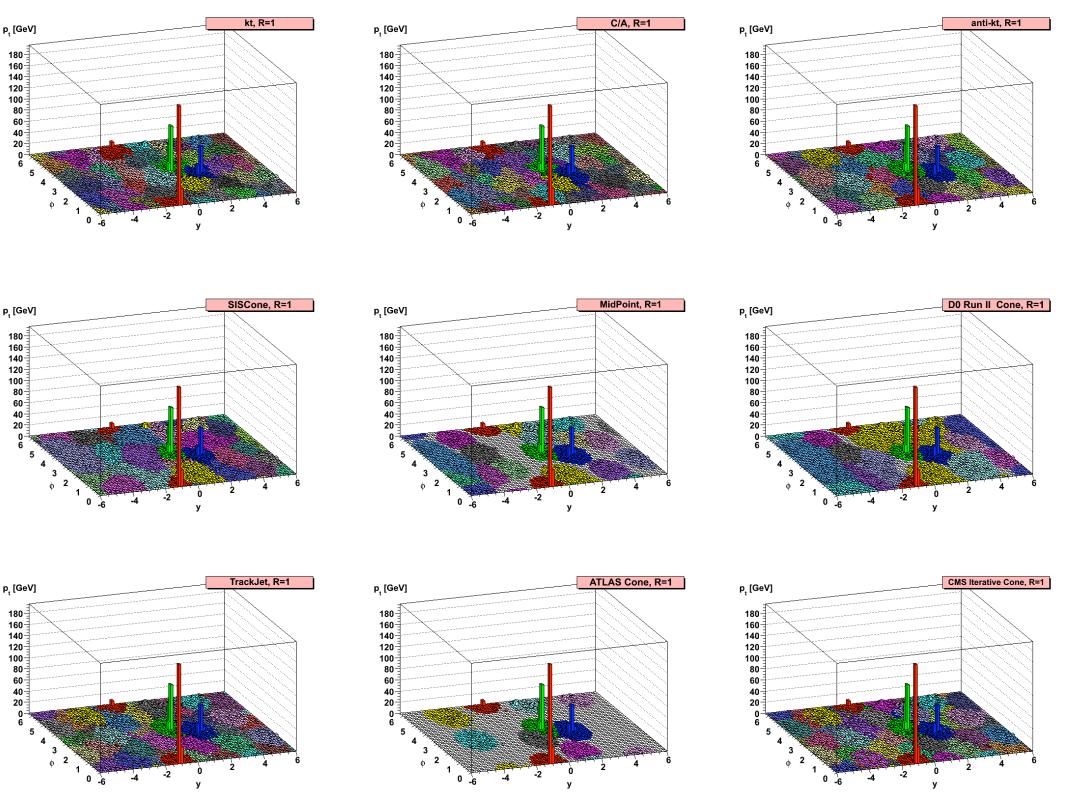
The ghost can also give a visual impression of the reach of each jet











#### Jet areas: the link to physics

The definition of active area mimics the behaviour of the jet-clustering algorithms in the presence of a large number of randomly distributed soft particles

This is like underlying event or pileup.

#### Tools needed to implement it:

- I. An infrared safe jet algorithm (the ghosts should not change the jets)
- 2. A reasonably fast implementation (we are adding thousands of ghosts)

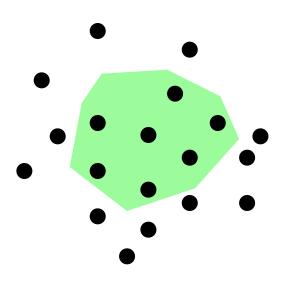
Both are available

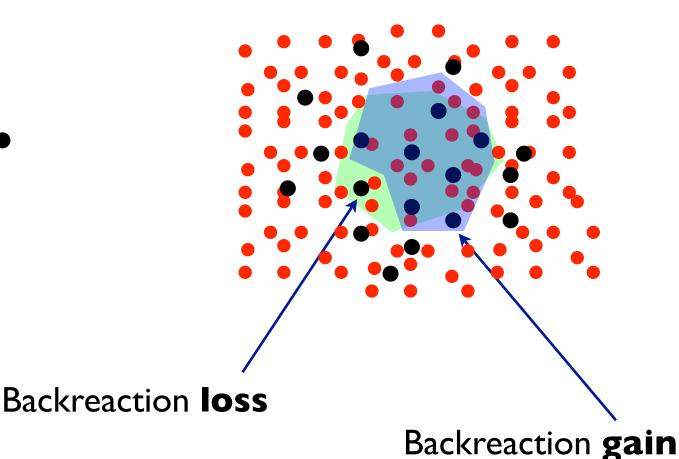
#### Backreaction

"How (much) a jet changes when immersed in a background"

Without background

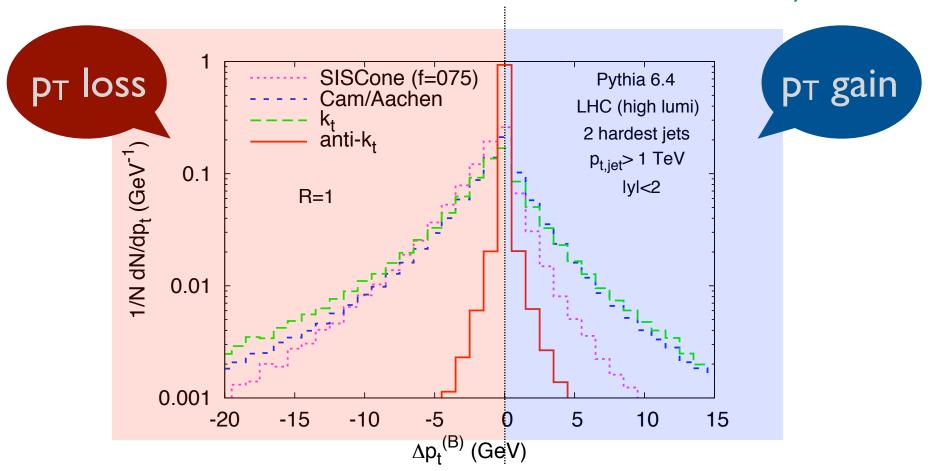
With background





#### Backreaction

MC, Salam, Soyez, arXiv:0802.1188



## Anti-kt jets are much more resilient to changes from background immersion

#### Jet area as a tool

# Underlying event and pileup determination and subtraction

## Measurement of background level

MC, Salam, arXiv:0707.1378

$$\rho \equiv \underset{\text{(over a single event)}}{\text{median}} \left[ \left\{ \frac{p_t^{jet}}{\text{Area}_{jet}} \right\} \right]$$

Taking the median of the distribution is a way to get rid of (part of the) possible bias from the few hard jets

(This can still be tweaked/improved)

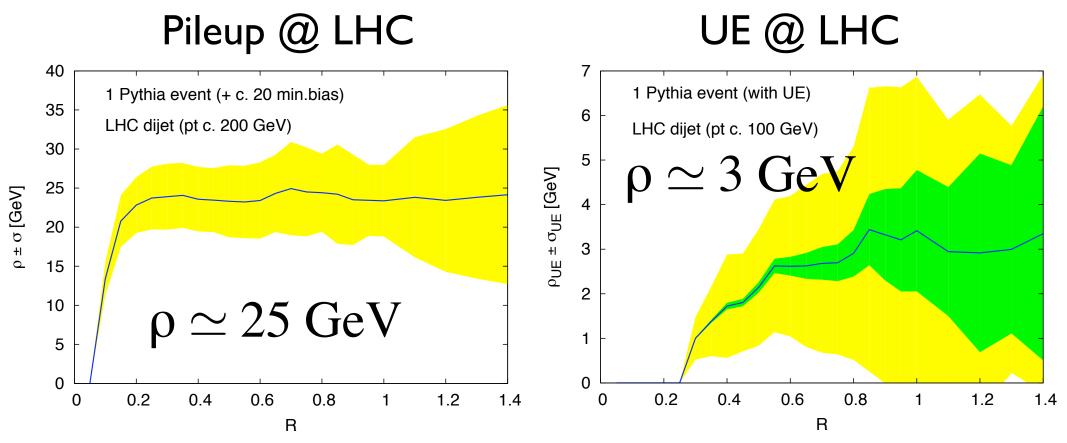
For  $\rho$  to be non-zero at the *perturbative* level one would need at least as many hard jets as 'empty jets'. This can be shown to happen at order  $\alpha_s^n$ , with

$$n \simeq \frac{4y_{\text{max}}}{(x_{\text{pg}} + x_{\text{sp}})R^2} \simeq 2.94 \frac{y_{\text{max}}}{R^2}$$

Factors related to typical areas of pure-ghost and single-particle jets

This gives n ~ 24--47 for  $y_{max} = 4$  and R = 0.5--0.7

### Examples of background measurements



When 'measuring' the background, R should be not too small (too many empty jets) and not too large (too few jets, biased by the hard particles)

Theoretical estimates and empirical evidence point to  $R \sim 0.5$ --0.6 for Underlying Event measurement (Also, a 'sensible' jet alg like  $k_t$  or Cambridge/Aachen should be used)

# Background subtraction

[MC, Salam, arXiv:0707.1378]

Once measured, the background density can be used to correct the transverse momentum of the hard jets:

$$p_T^{\text{hard jet, corrected}} = p_T^{\text{hard jet, raw}} - \rho \times \text{Area}_{\text{hard jet}}$$

ρ being calculated on an event-by-event basis, this procedure will generally improve the resolution of, say, a mass peak

NB. Also be(a)ware of backreaction

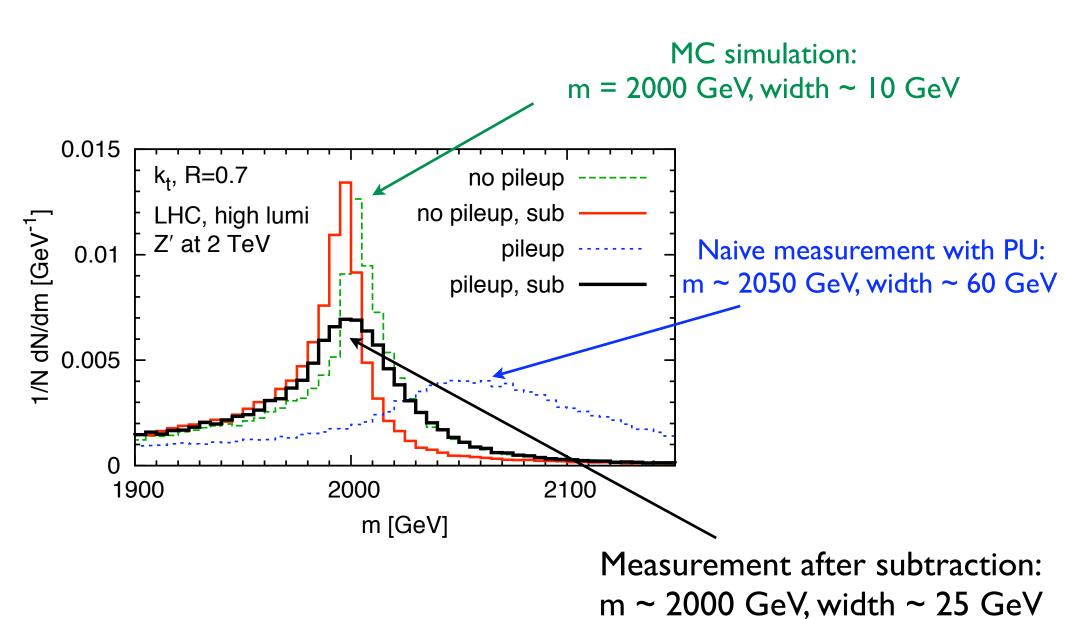
(immersing a hard jet in a soft background may cause some particles belonging to the hard event to be lost from (backreaction loss) or added to (backreaction gain) the jet).

Small effect for UE, larger for pileup, can be very important for heavy ions.

Analytical understanding of this effect available (MC, Salam, Soyez, arXiv:0802:1188)

# Example of pileup subtraction

Let's discover a leptophobic Z' and measure its mass:



# All IRC safe algorithms are equal, but some are more equal than others

Depending on the analysis you wish to perform, a jet **definition** might give better results than others

### Which R to choose?

The value of R matters because it affects, in opposite ways, a number of things:

**Small R:** 

Limit underlying event and pileup contamination Better resolve many-jets events



Limit perturbative radiation loss ('out-of-cone') Limit non-perturbative hadronisation effects

The best compromise will in general depend on the specific observable

# R-dependent effects

Perturbative radiation: 
$$\Delta p_t \simeq \frac{\alpha_s(C_F, C_A)}{\pi} p_t \ln R$$



Hadronisation: 
$$\Delta p_t \simeq \frac{(C_F, C_A)}{R} \times 0.4 \; \mathrm{GeV}$$



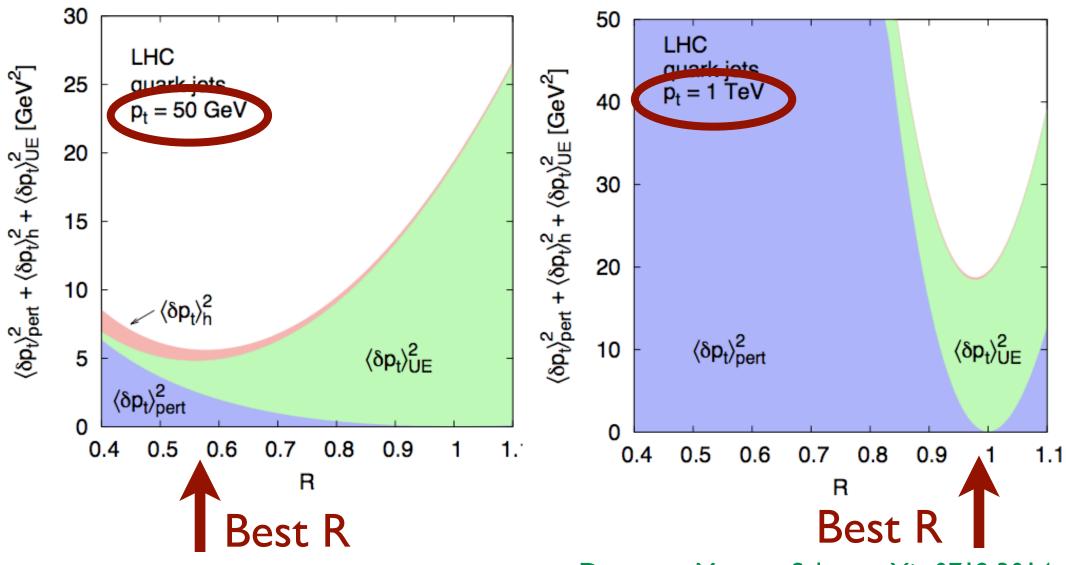
Underlying Event: 
$$\Delta p_t \simeq \frac{R^2}{2} \times (2.5 - 15 \ {\rm GeV})$$

Analytical estimates,

Dasgupta, Magnea, Salam, arXiv:0712.3014

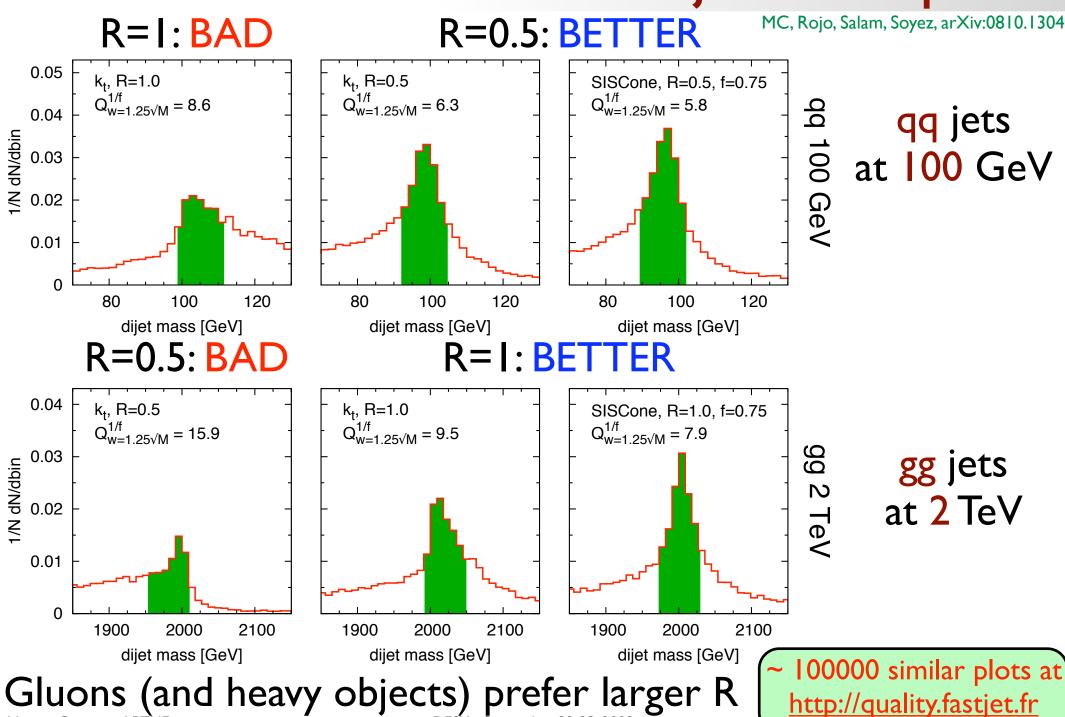
### Best R

### Minimize $\Sigma(\Delta p_t)^2$



Dasgupta, Magnea, Salam, arXiv:0712.3014

# Reconstruction of a di-jet mass peak



DESY - September 22-23, 2009

Matteo Cacciari - LPTHE

Effective luminosity ratios anti-k+ SISCone C/A-filt k<sub>t</sub> C/A Example of a 엵 2.0 'third-generation' algorithm 100 GeV 1.5 Lower is 2.0 better g N 1.5 e۷ 1.0 Best 99 2.0 8 1.5 GeV 1.0 2.0 Different algs, gg different R, 1.5 e۷ different performances 1.0 1.5 0.2 0.5 1.50.20.5 Matteo Cacciari - RTHE R DESY - Septembe 22-23, 2009

# Cambridge/Aachen with filtering

Butterworth, Davison, Rubin, Salam, arXiv:0802.2470

#### An example of a third-generation jet algorithm



Cluster with C/A and a given R



Undo the clustering of each jet down to subjets with radius Xfilt R



Retain only the nfilt hardest subjets

# Aim: limit sensitivity to background while retaining bulk of perturbative radiation

# Jets substructure in Higgs searches

 $H \to b \bar b$  in the WH/ZH channels

Usually considered hopeless:

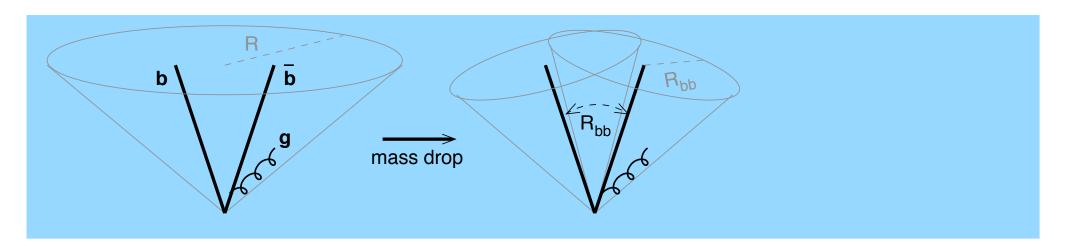
#### **Conclusion (ATLAS TDR):**

"The extraction of a signal from  $H \rightarrow b\bar{b}$  decays in the WH channel will be very difficult at the LHC, even under the most optimistic assumptions [...]"

New way of going at it: use large pt (boosted Higgs), exploit jet substructure

Butterworth, Davison, Rubin, Salam, arXiv:0802.2470

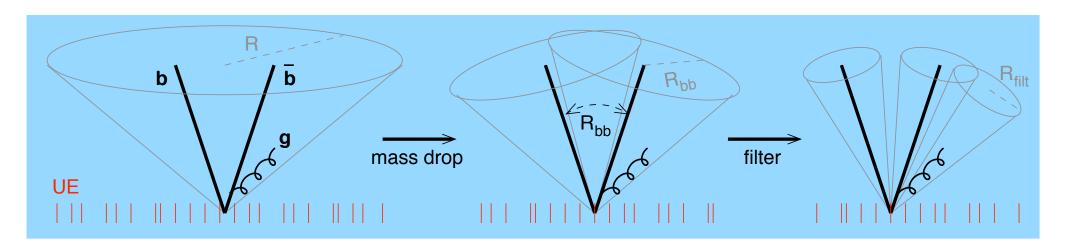
#### #2: The jet analysis



#### Start with high- $p_t$ jet

- 1. Undo last stage of clustering ( $\equiv$  reduce R):  $J \rightarrow J_1, J_2$
- 2. If  $\max(m_1, m_2) \lesssim 0.67m$ , call this a mass drop [else goto 1] Automatically detects correct  $R \sim R_{bb}$  to catch angular-ordered radn.
- 3. Require  $y_{12} = \frac{\min(p_{t1}^2, p_{t2}^2)}{m_{12}^2} \Delta R_{12}^2 \simeq \frac{\min(z_1, z_2)}{\max(z_1, z_2)} > 0.09$  [else goto 1] dimensionless rejection of asymmetric QCD branching
- 4. Require each subjet to have *b*-tag [else reject event]

  Correlate flavour & momentum structure



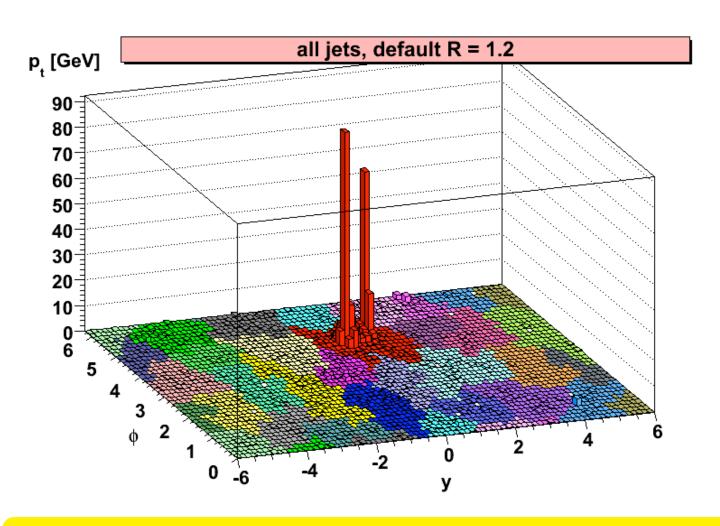
At moderate  $p_t$ ,  $R_{bb}$  is quite large; UE & pileup degrade mass resolution  $\delta M \sim R^4 \Lambda_{UE} \frac{p_t}{M}$  [Dasgupta, Magnea & GPS '07]

#### Filter the jet

- ▶ Reconsider region of interest at smaller  $R_{filt} = \min(0.3, R_{b\bar{b}}/2)$
- ▶ Take 3 hardest subjets b,  $\bar{b}$  and leading order gluon radiation

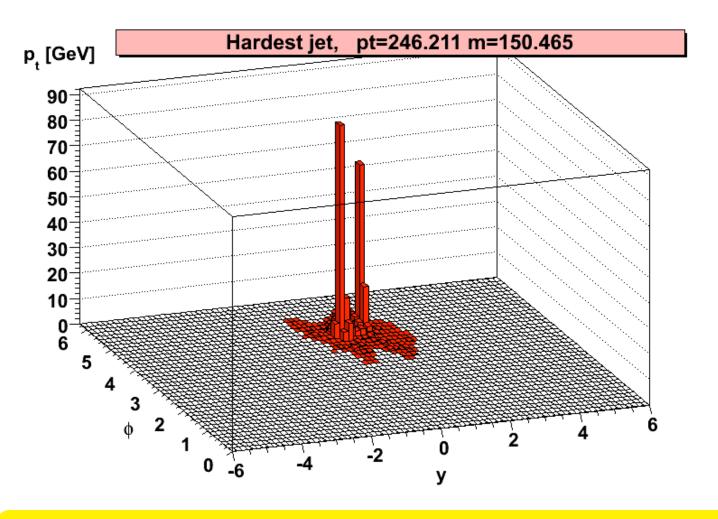
SIGNAL

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

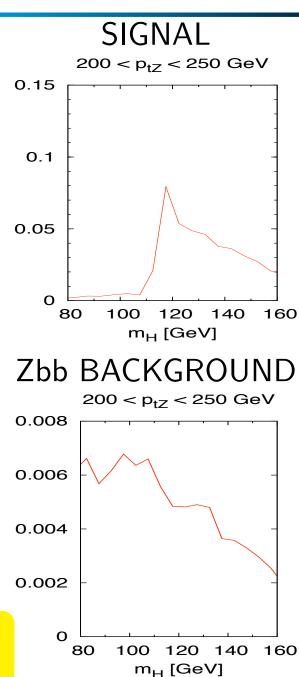


Zbb BACKGROUND

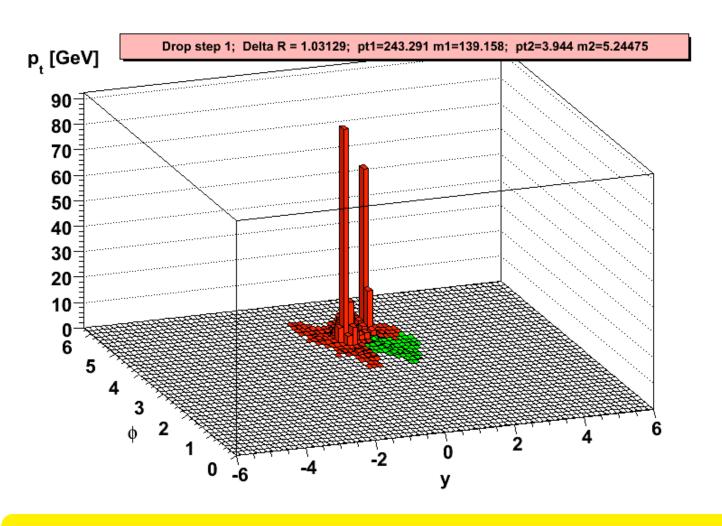
Cambridge/Aachen, R=1.2



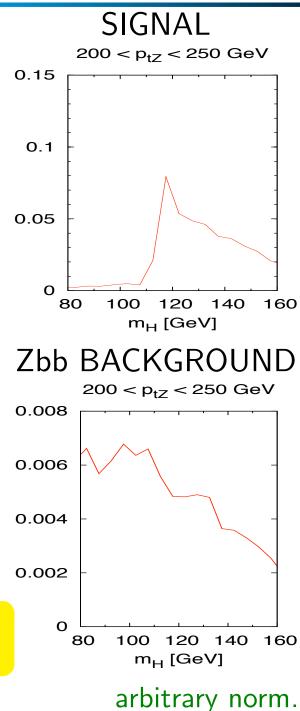
Consider hardest jet, m = 150 GeV

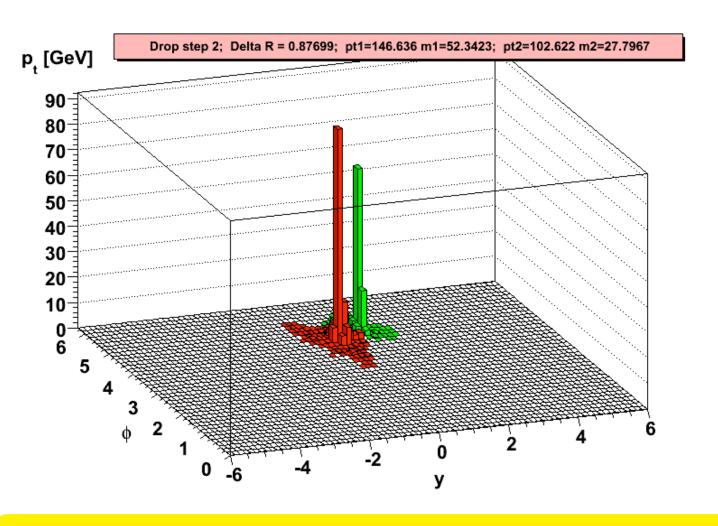


arbitrary norm.

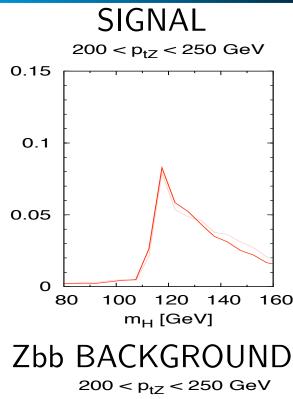


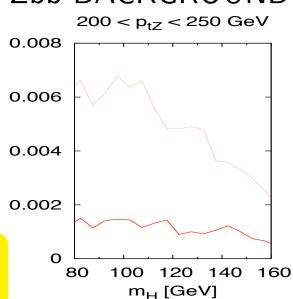
split:  $m=150~{\rm GeV}, \; \frac{\max(m_1,m_2)}{m}=0.92 \to {\rm repeat}$ 



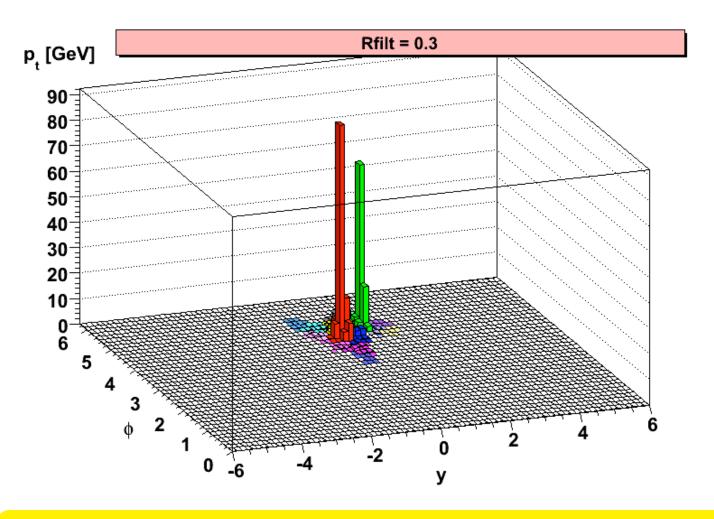


split: m = 139 GeV,  $\frac{\max(m_1, m_2)}{m} = 0.37 \rightarrow \text{mass drop}$  $y_{12} = 0.7$  -- OK

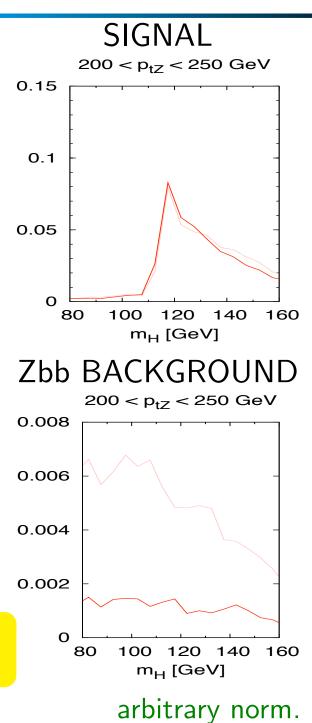


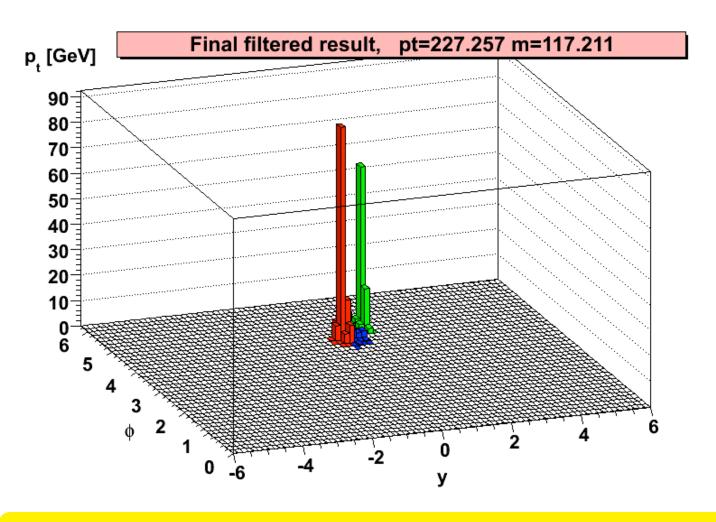


arbitrary norm.

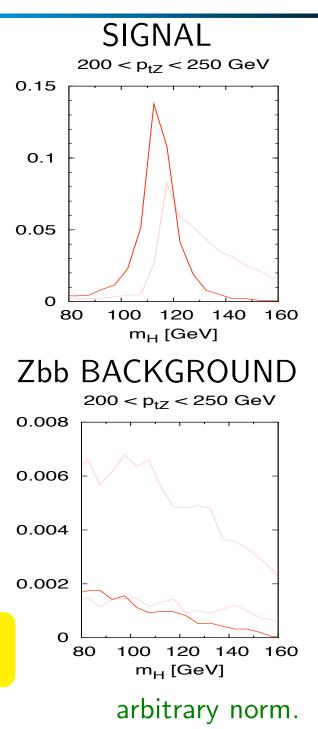




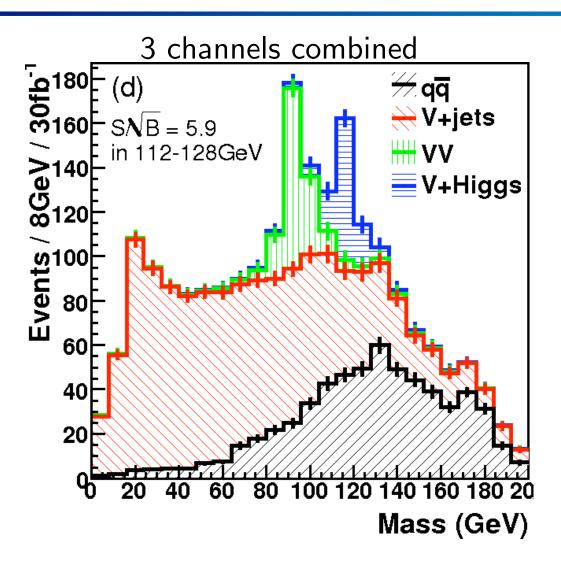




 $R_{filt} = 0.3$ : take 3 hardest,  $\mathbf{m} = 117 \text{ GeV}$ 



#### combine HZ and HW, $p_t > 200 \text{ GeV}$



#### Common cuts

- $ho_{tV}, p_{tH} > 200 \text{ GeV}$
- ▶  $|\eta_H| < 2.5$
- $ightharpoonup [p_{t,\ell} > 30 \text{ GeV}, |\eta_{\ell}| < 2.5]$
- ▶ No extra  $\ell$ , b's with  $|\eta| < 2.5$
- ► Real/fake *b*-tag rates: 0.7/0.01
- ►  $S/\sqrt{B}$  from 16 GeV window

#### 3 channels combined

Note excellent VZ,  $Z \rightarrow b\bar{b}$  peak for calibration

NB:  $q\bar{q}$  is mostly  $t\bar{t}$ 

At  $5.9\sigma$  for 30 fb<sup>-1</sup> this looks like a possible new channel for light Higgs discovery. **Deserves serious exp. study!** 

# The IRC safe algorithms

	Speed	Regularity	UE	Backreaction	Hierarchical substructure	
<b>k</b> <sub>t</sub>	© © ©	<b>**</b>	<b>T</b>	•••	⊕ ⊕	
Cambridge /Aachen	⊕ ⊕ ⊕	<b>†</b>	<b>†</b>	**	⊕ ⊕ ⊕	
anti-k <sub>t</sub>	◎ ◎ ◎	◎ ◎	♣/ ⓒ	◎ ◎	×	
SISCone	☺	•	⊕ ⊕	•	×	

## Conclusions



An extensive set of fast, IRC safe jet algorithms exists, offering replacements for the IRC unsafe ones.



They offer ample flexibility in choosing the most effective jet definition for any given analysis.



They can be used to estimate the level of a uniformly distributed noise, and study its characteristics.



They can be used to subtract the noise from the hard jets, improving the quality of kinematical reconstructions.



'Third-generation' algorithms look promising.

# Extra material

# The FastJet algorithm

To improve the speed of the algorithm we must find more efficiently which particle is "close" to another and therefore gets combined with it

Observation (MC, G.P. Salam, hep-ph/0512210):

If i and j form the smallest 
$$d_{ij} = \min(k_{ti}^2, k_{tj}^2) \frac{\Delta \eta^2 + \Delta \phi^2}{R^2}$$

and
$$k_{ti} < k_{ti}$$

$$\Delta R_{ij} \leq \Delta R_{ik} \quad \forall \quad k \neq j$$

i.e. j is the **geometrical** nearest neighbour of i

Translation from mathematics:

When a particle gets combined with another, and has the smallest kt, its partner will be its **geometrical nearest neighbour** on the cylinder spanned by y and φ

This means that we need to look for partners only among the O(N) nearest neighbours of all particles (a few neighbours each  $\times$  N particles)

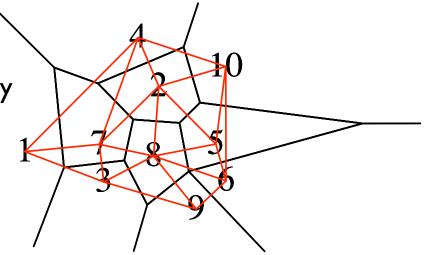
# The FastJet algorithm

Our problem has now become a **geometrical** one: how to find efficiently the (nearest) neighbour(s) of a point

Widely studied problem in computational geometry

Tool: Voronoi diagram

Definition: each cell contains the locations which have the given point as nearest neighbour



The dual of a Voronoi diagram is a Delaunay triangulation

Key feature: once the Voronoi diagram is constructed, the nearest neighbour of a point will be in one of the O(1) cells sharing an edge with its own cell

Example: the G(eometrical) N(earest) N(eighbour) of point 7 will be found among 1,4,2,8 and 3 (it turns out to be 3)

# The FastJet algorithm

MC and G.P. Salam, hep-ph/0512210

Construct the Voronoi diagram of the N particles using the CGAL library

O(N InN)

Find the GNN of each of the N particles. Construct the distances, store the results in a priority queue (C++ map)

O(N InN)

Merge/eliminate particles appropriately

Update Voronoi diagram and distances' map



repeat N times

#### Overall, an O(N In N) algorithm

**NB.** Results identical to standard  $k_t$  algorithm. This is NOT a new jet-finder.

# The SISCone algorithm

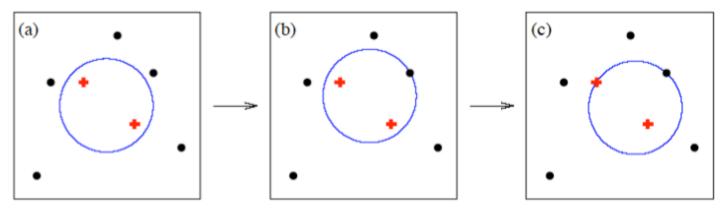
[Salam, Soyez, arXiv: 0704.0292]

#### Checking all particles in an event to test for stable combinations

(i.e. the axis of the cone containing a subset of particles coincides with the momentum sum) takes  $O(N2^N)$  time

#### Solution: once more, transform into a geometrical problem

- I. Find all distinct way of enclosing a set of particles in a y- $\phi$  circle
- 2. Check, for each enclosure, if it corresponds to a stable cone



Finding all distinct circular enclosures of a set of points is geometry: move it until you hit a point, then rotate it until one of the points hits the edge

Result: Seedles Infrared Safe Cone (SISCone)

[runs in  $O(N^2lnN)$  time, similar to MidPoint  $(N^3)$ ]

# <Theoretical interlude>

# Jet passive area

#### Passive Area

Add a **single** ghost\* particle to the event.

Move it around.

Check if it gets clustered in a given jet J.

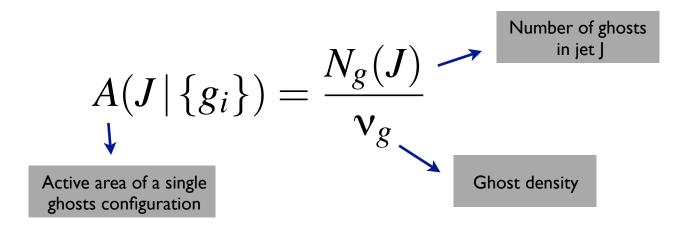
$$a(J) \equiv \int dy \, d\phi \, f(g(y, \phi), J) \qquad \qquad f(g, J) = \begin{cases} 1 & g \in J \\ 0 & g \notin J \end{cases}$$

<sup>\*</sup> ghost particle: particle with infinitesimally small momentum with respect to all other particles in the event (in practice,  $O(10^{-100}~\text{GeV})$ )

# Jet Active area

#### **Active Area**

Add **many** ghost particles in random configurations to the event. Cluster many times. Allow ghosts to cluster among themselves too. Count how many ghosts on average get clustered into a given jet J.



$$A(J) = \lim_{\mathbf{v}_g o \infty} raket{A(J | \{g_i\})}_g$$
Active area

# Jet areas: the single hard particle case

[MC, Salam, Soyez]

# A jet of 'radius' R will surely have area $\pi R^2$ , right?

Well, it depends.....

**Passive** areas of a single hard particle are indeed  $\pi R^2$ 

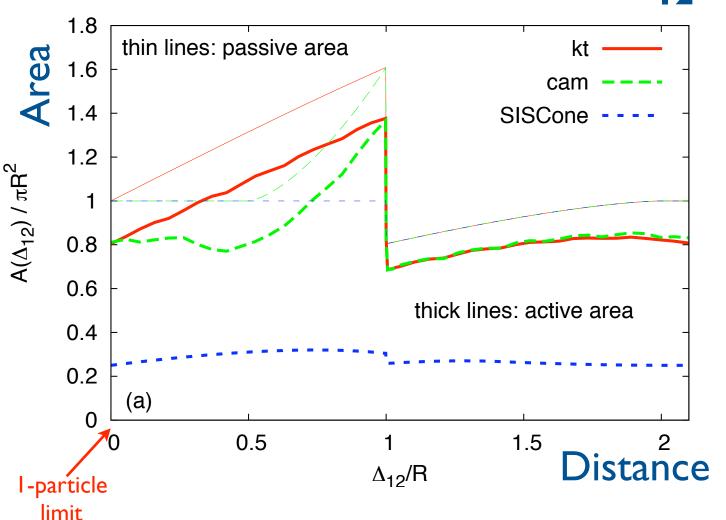
However, **active** areas are not: 
$$\begin{cases} k_t \rightarrow 0.81 \ \pi R^2 \\ Cam/Aa \rightarrow 0.81 \ \pi R^2 \\ SISCone \rightarrow \pi R^2 / 4 \\ anti-k_t \rightarrow \pi R^2 \end{cases}$$

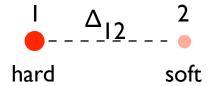
Recall that 'area' is how much background a a jet can pick up. Its knowledge is essential in order to subtract it from measurements

# Jet areas: a second hard(ish) particle

Real events have more than a single hard particle.

#### Add a second (soft) one at a distance $\Delta_{12}$





The jet area depends on the distance between the particles

Note very small active area for SISCone!

Passive areas (and SISCone's active area) can be calculated analytically, while the others are obtained numerically

# Jet areas: anomalous dimensions

Finally, weigh the probability of emission of the soft particle with the leading-order QCD matrix element:

$$\langle \Delta area \rangle = \int C_1 \frac{\alpha_s(p_{t2}\Delta_{12})}{\pi} \frac{dp_{t2}}{p_{t2}} \left[ \frac{d\Delta_{12}}{\Delta_{12}} \right]_{+} \begin{pmatrix} \frac{1}{2} & \Delta_{12} & 2\\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$$

The result is an anomalous dimension.

Areas change with transverse momentum of the jet in a predictable way:

$$\langle \Delta area 
angle = d \frac{C_1}{\pi b_0} \ln \frac{\alpha_s(Q_0)}{\alpha_s(Rp_{t1})}$$

In a similar way one can also predict the evolution of the dispersion, calculating

$$\langle \Delta \, area^2 
angle = \, {\sf s^2} \, \, rac{C_1}{\pi b_0} \ln rac{lpha_s(Q_0)}{lpha_s(Rp_{t1})}$$

# Passive areas: analytical results

MC, Salam, Soyez, arXiv:0802.1188

$$d_{k_t,R} = \left(\frac{\sqrt{3}}{8} + \frac{\pi}{3} + \xi\right) R^2 \simeq 0.5638 \, \pi R^2 \,,$$
 
$$d_{\mathrm{Cam},R} = \left(\frac{\sqrt{3}}{8} + \frac{\pi}{3} - 2\xi\right) R^2 \simeq 0.07918 \, \pi R^2 \,,$$
 
$$d_{\mathrm{SISCone},R} = \left(-\frac{\sqrt{3}}{8} + \frac{\pi}{6} - \xi\right) R^2 \simeq -0.06378 \, \pi R^2 \,,$$
 Negative! SISCone jets shrink!

$$s_{k_t,R}^2 = \left(\frac{\sqrt{3}\pi}{4} - \frac{19}{64} - \frac{15\zeta(3)}{8} + 2\pi\xi\right)R^4 \simeq (0.4499\,\pi R^2)^2\,,$$
 
$$s_{\text{Cam},R}^2 = \left(\frac{\sqrt{3}\pi}{6} - \frac{3}{64} - \frac{\pi^2}{9} - \frac{13\zeta(3)}{12} + \frac{4\pi}{3}\xi\right)R^4 \simeq (0.2438\,\pi R^2)^2\,,$$
 
$$s_{\text{SISCone},R}^2 = \left(\frac{\sqrt{3}\pi}{12} - \frac{15}{64} - \frac{\pi^2}{18} - \frac{13\zeta(3)}{24} + \frac{2\pi}{3}\xi\right)R^4 \simeq (0.09142\,\pi R^2)^2\,.$$

with 
$$\xi \equiv \frac{\psi'(1/6) + \psi'(1/3) - \psi'(2/3) - \psi'(5/6)}{48\sqrt{3}} \simeq 0.507471$$

d:

# Jet areas: passive v. active

	area/πR <sup>2</sup>		dispe	ersion	d or D		s or S	
	passive	active	passive	active	passive	active	passive	active
	$a(1\mathrm{PJ})$	$A(1\mathrm{PJ})$	$\sigma(1PJ)$	$\Sigma(1\mathrm{PJ})$	d	D	s	S
$k_t$	1	0.81	0	0.28	0.56	0.52	0.45	0.41
Cam/Aachen	1	0.81	0	0.26	0.08	0.08	0.24	0.19
SISCone	1	1/4	0	0	-0.06	0.12	0.09	0.07
anti- $k_t$	1	1	0	0	0	0	0	0

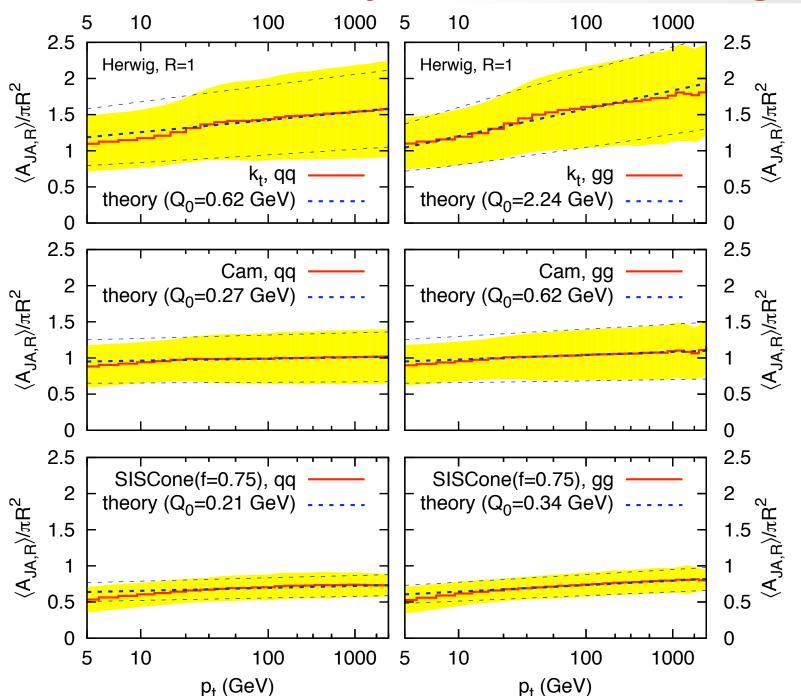
single hard particle

emission of a second perturbative particle (coeff. of anomalous dimension )

#### Some remarkable features

- SISCone has very small active area
- SISCone's anomalous dimension changes from negative for passive area to positive for active area
- kt has largest anomalous dimension
- anti-k<sub>t</sub> has constant area (null anomalous dimension): it's a perfect cone

# Jet areas scaling violations



Averages and dispersions evolution from Monte Carlo simulations (dijet events at LHC) in good agreement with simple LL calculations

Area scaling violations are a legitimate observable.

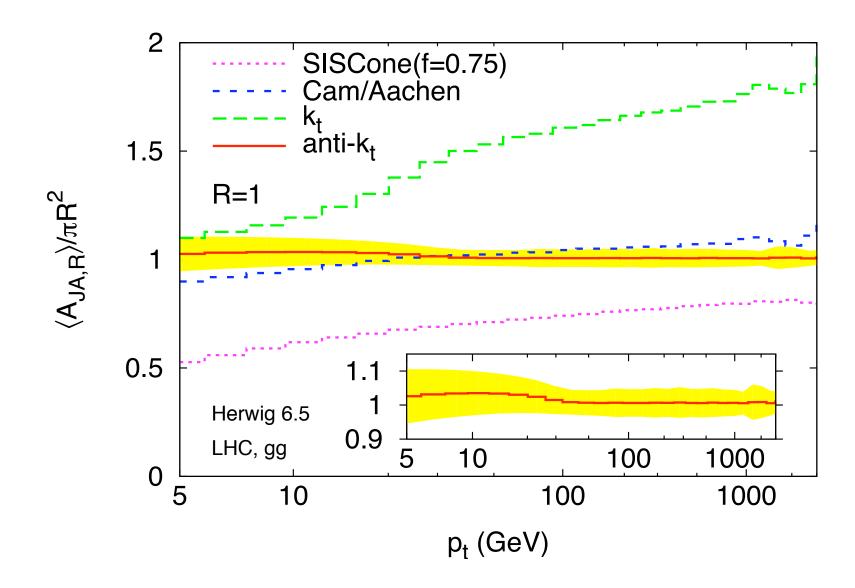
(Though it might not be the best place where to measure  $\alpha_s$  ....)

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# Jet areas scaling violations

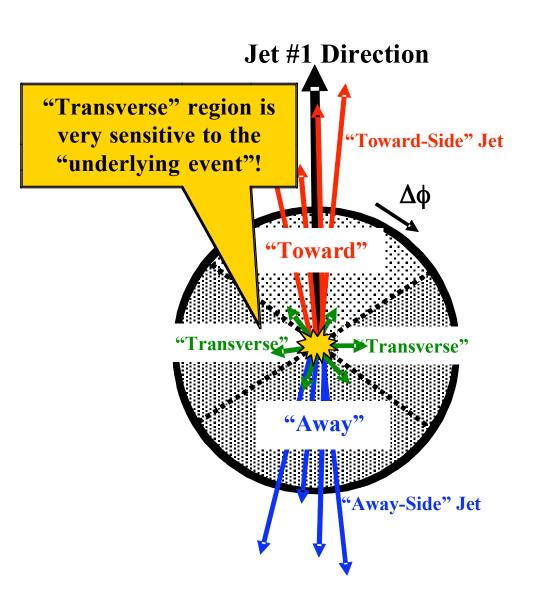
MC, Salam, Soyez, arXiv:0802.1189

Check anti-k, behaviour: scaling violations indeed absent, as predicted

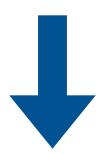


# </Theoretical interlude>

# Underlying event measurement



Marchesini-Webber idea: look at transverse region to measure underlying event



#### **Topological selection**

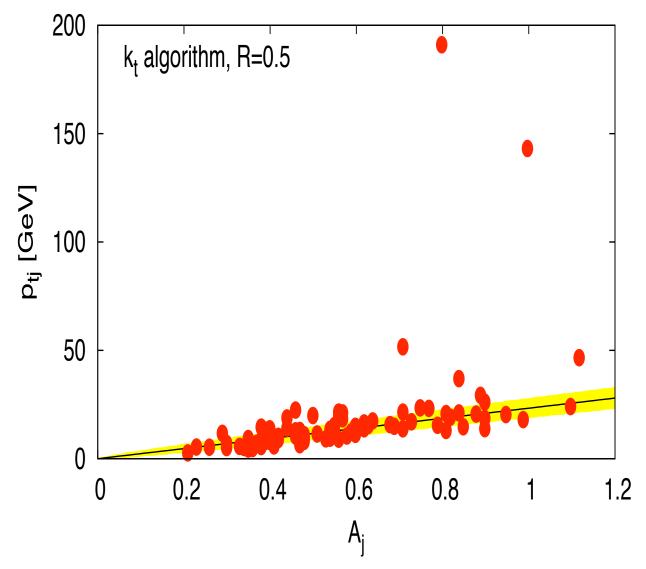
The jets are classified as belonging to the noise on the ground of their **position** 

# Area v. pt

#### LHC: dijet event + high-lumi pilup

a few hard particles and many softer ones

(a similar picture applies to the Underlying Event)



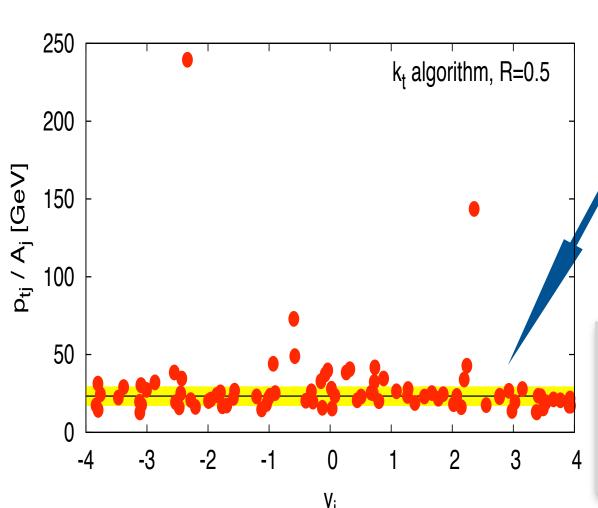
The jets adapt to the surrounding environment



They can have very different areas

# The key observation

#### p<sub>T</sub>/Area is fairly constant, except for the hard jets



The distribution of background jets establishes its own average momentum density  $\rho$ 

(NB. this is true on an event-by-event basis)

#### **Dynamical selection**

The jets are classified as belonging to the noise on the ground of their **characteristics** 

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