

# Exotic Mesons, XYZ, as tetraquarks

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# 1. Introduction

Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc.

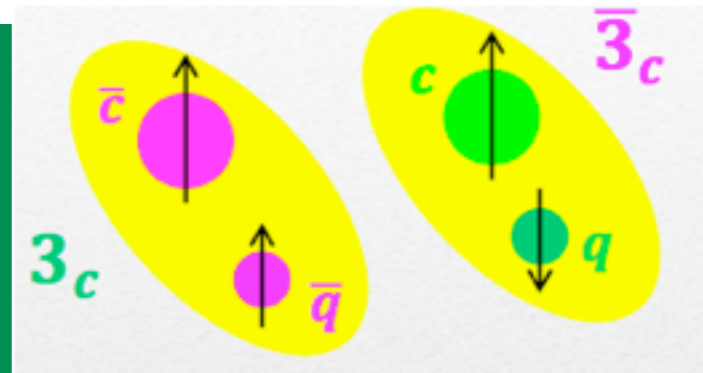
M. Gell-Mann, A Schematic Model of Baryons and Mesons, PL **8**, 214, 1964

- For long, we lived with the simplest paradigm:

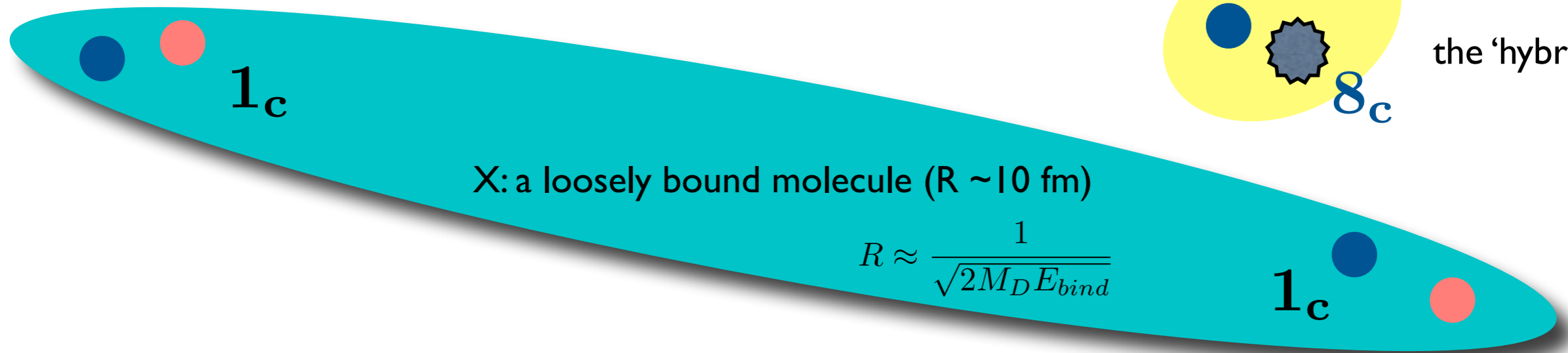
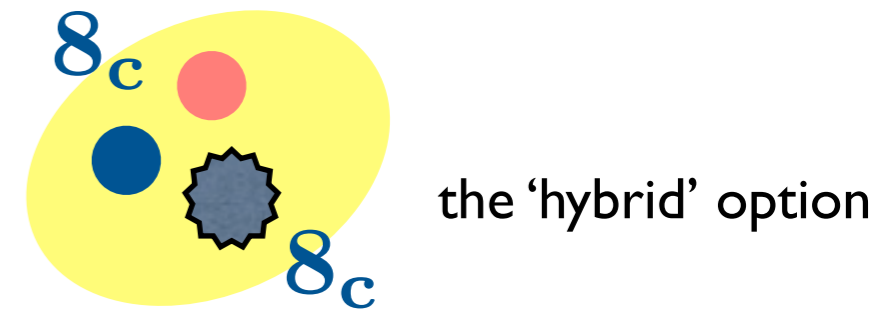
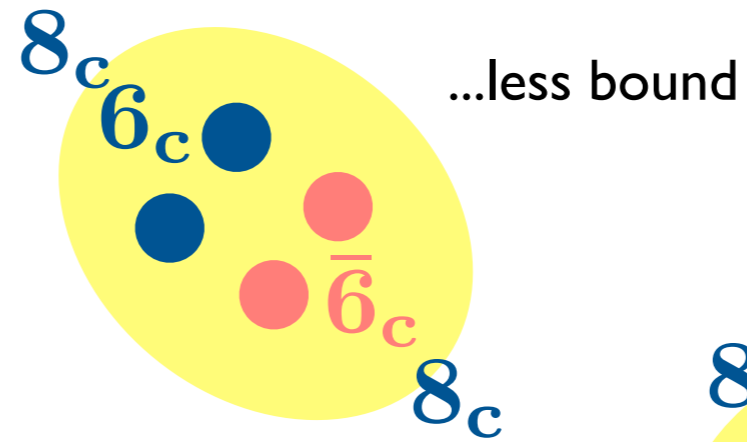
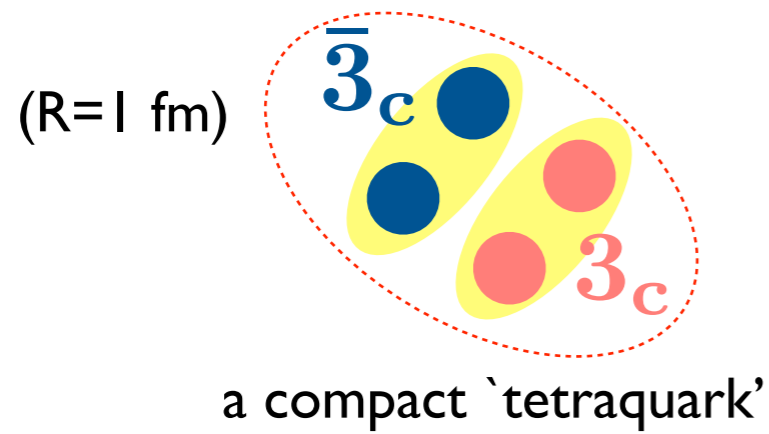
$$\text{mesons} = q\bar{q}, \quad \text{baryons} = qqq$$

- Paradigm rested on the absence of  $I=2$ ,  $\pi\pi$  resonances and of  $S>0$  baryons.
- The case had to be revisited, because the lowest lying, octet of scalar mesons-  $f_0(980)$ ,  $a_0(980)$ ,  $\kappa(800)$  and  $\sigma(600)$ - does not fit in the picture.
- The  $X(3872)$ , narrow width, with decays into  $J/\Psi + 2\pi/3\pi$ , discovered by Belle in 2003, does not fit into the “charmonium” states,
- since then, Belle, BaBar, BES and LHCb have reported many other states that do not fit the charmonium picture, called  $X(1^{++})$  and  $Y(1^{-})$  states: molecules? hybrids? tetraquarks?
- In 2007, Belle observed a charged “charmonium”,  $Z^+(4430) \rightarrow \psi(2S) + \pi$ , that could not be interpreted as molecule, but later Babar suggested it was simply a reflection of  $K^*$  states
- LHCb has confirmed the  $Z^+(4430)$  while other similar states,  $Z^+(3900)$  and  $Z^+(4020)$ , have been established.

I shall follow the idea that  $X$ ,  $Y$ , and  $Z$  states belong to a new spectroscopy of mesons, made by diquark-antidiquark pairs. For Beauty see also A. Ali, Belle II TIP, Krakov (slides available).



# Models for X Y Z mesons

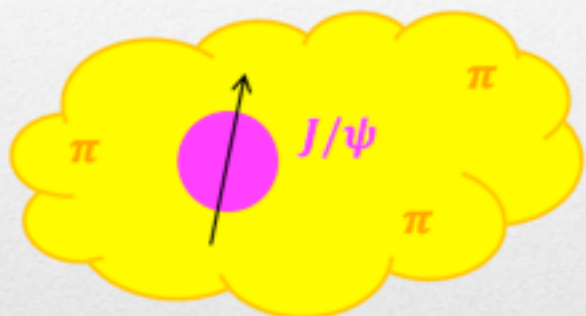





## Hadro-charmonium

Voloshin arXiv:1304.0380

A  $c\bar{c}$  state surrounded by light matter

Decay into  $\eta_c \rho$  forbidden by HQSS



-  quark (heavy or light)
-  antiquark
-  gluon

# X(3872) production @ LHC

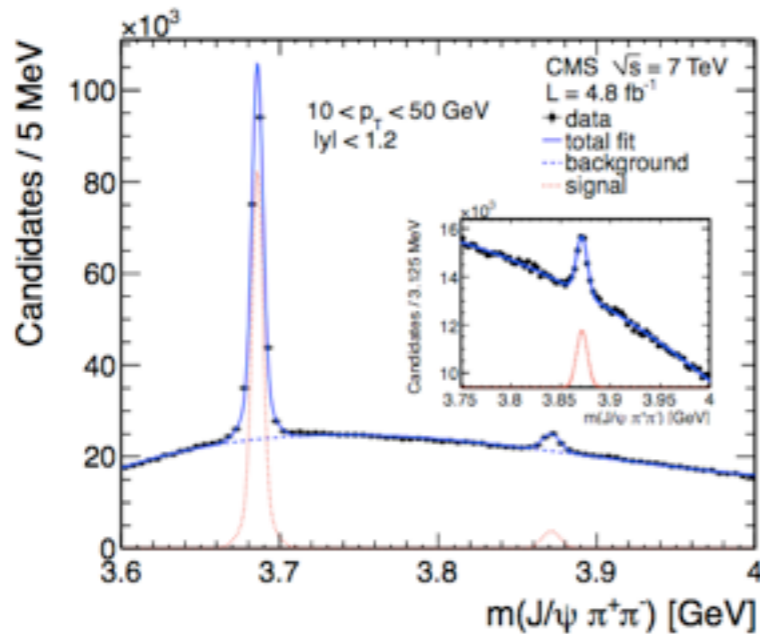
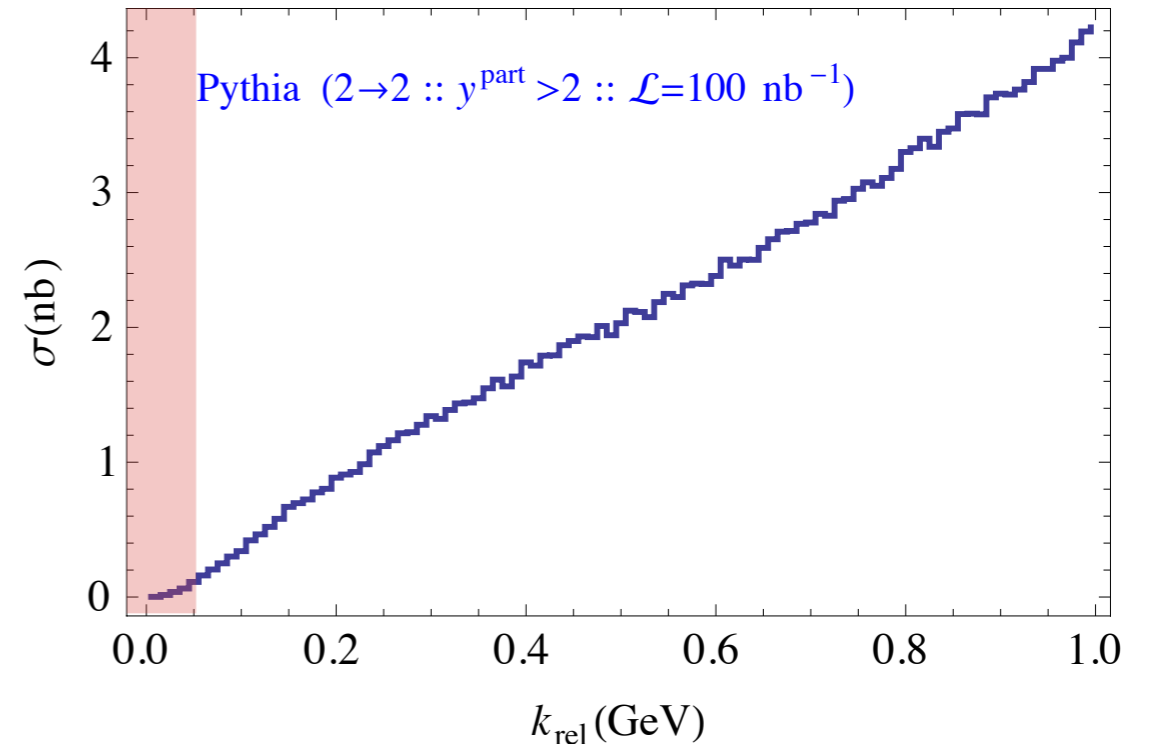
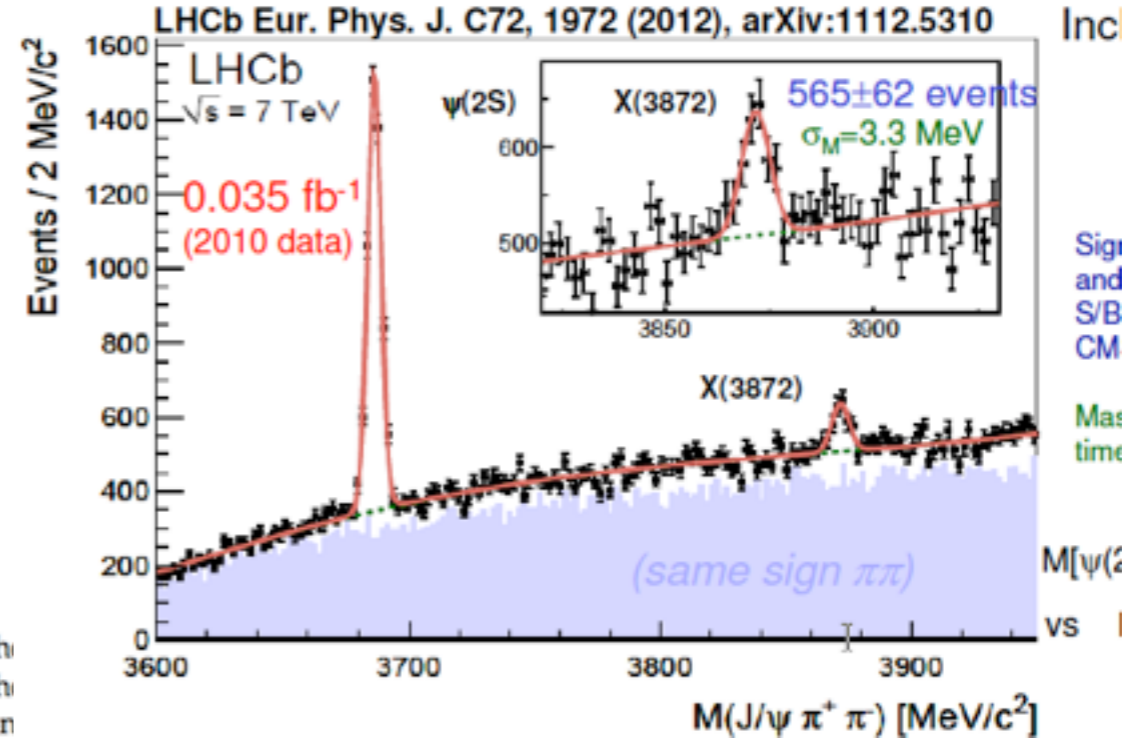


Figure 1: The  $J/\psi\pi^+\pi^-$  invariant-mass spectrum for  $10 < p_T < 50 \text{ GeV}$  and  $|y| < 1.2$ . The lines represent the signal-plus-background fits (solid), the background-only (dashed), and the signal-only (dotted) components. The inset shows an enlargement of the X(3872) mass region

- Production at Colliders speaks against extended objects;
- using Pythia to estimate the probability to find a D-Dbar pair in the relevant phase space, factors of  $10^{-2}$  are found with respect to the X(3872) cross section measured by CDF ( $\sim 30 \text{ nb}$ ).



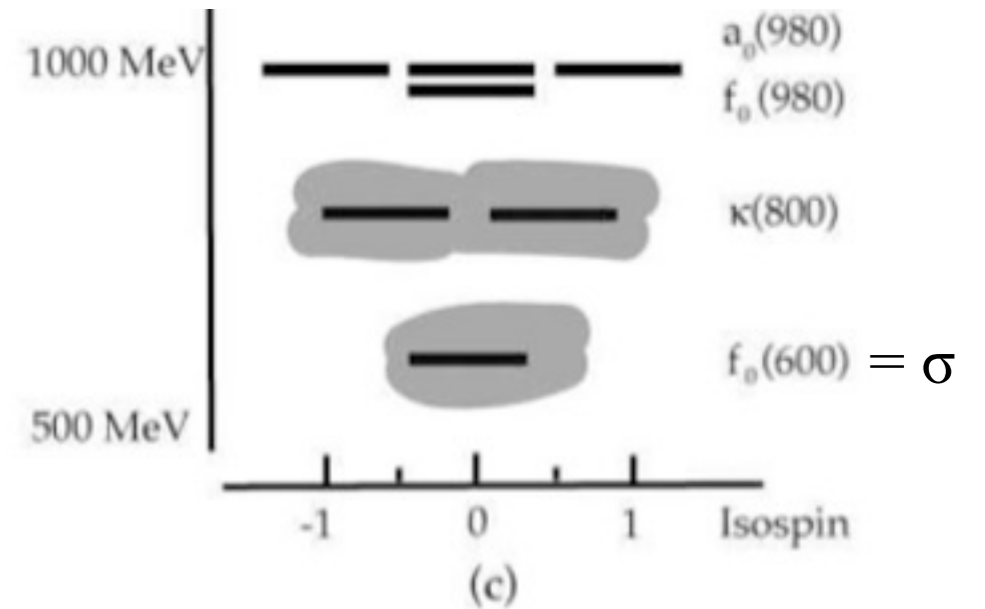
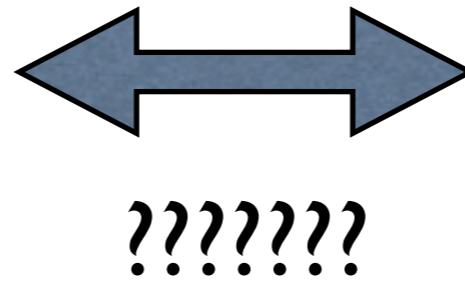
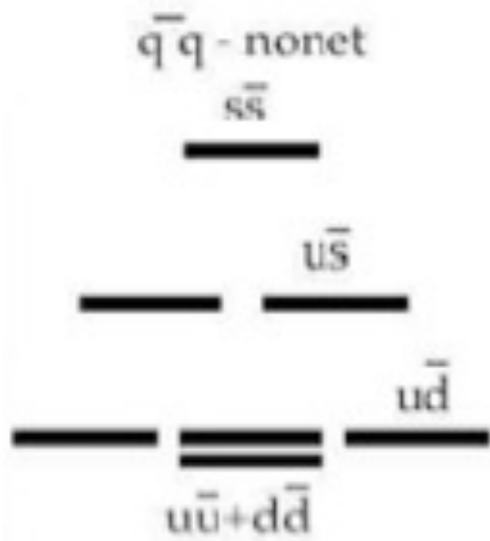
Few think X, Y, Z are only kinematic effects due to the opening of new channels. For one, see:

E. S. Swanson, Cusps and Exotic Charmonia, arXiv:1504.07952 [hep-ph]

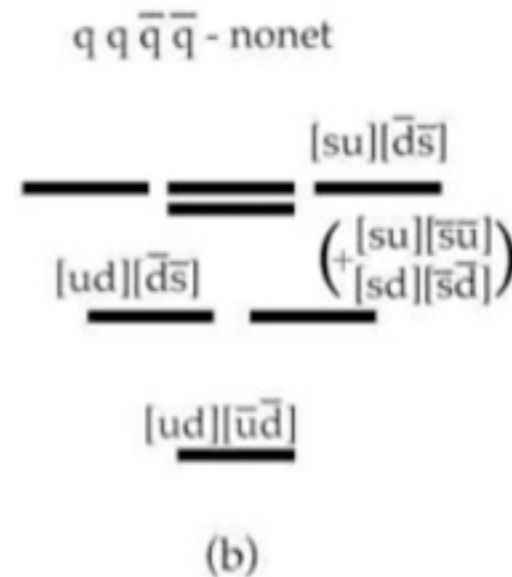
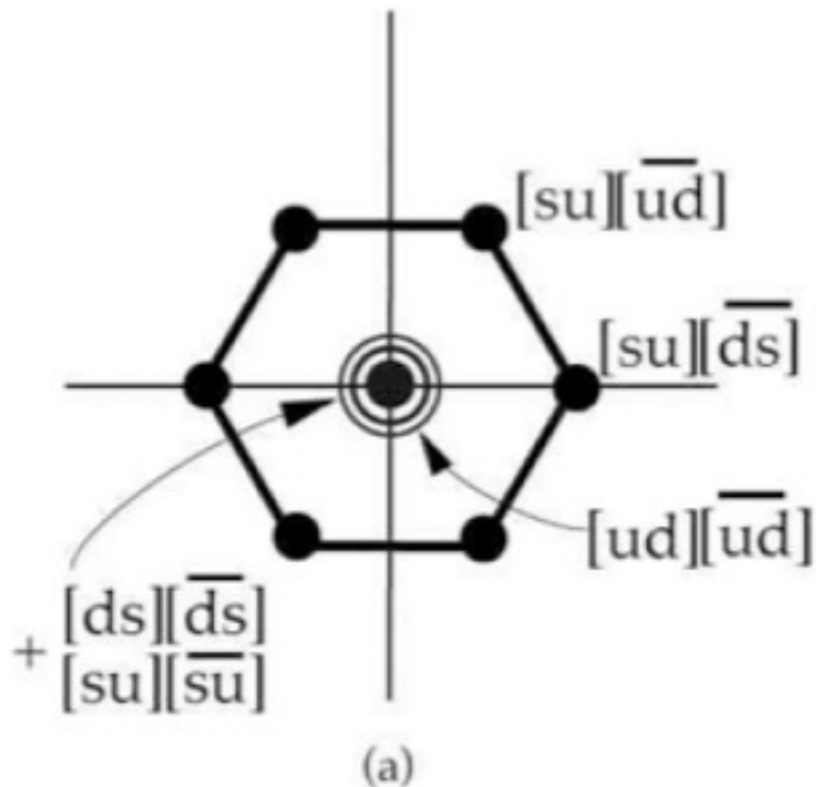
I think it takes a lot of unconventional dynamics to produce the X(3872) as a “cusp”

Also, the phase of Z(4430) seems to go at  $90^0$  at the peak, like a well-behaved Breit-Wigner resonance...

# 2. The octet of light scalar mesons and diquarks



Antisymmetric tetraquarks work better





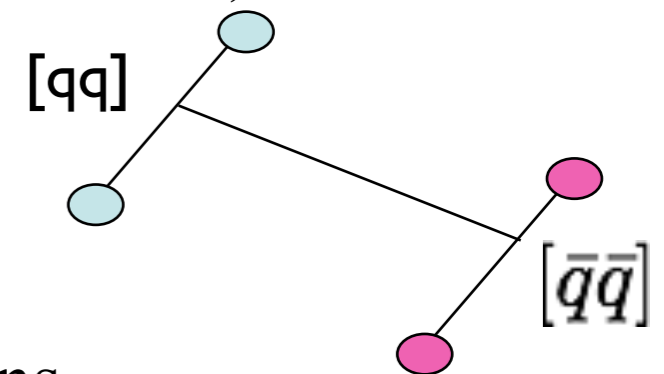
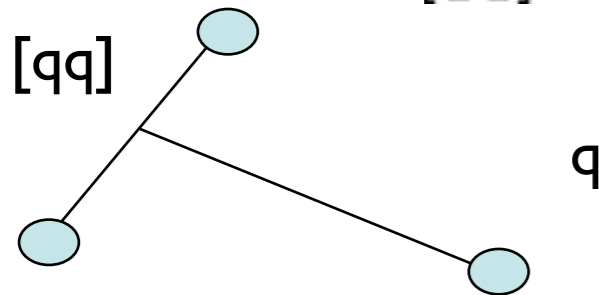
# Diquarks vs molecules

QCD forces are attractive (in 1 gluon approx.) for diquark  $[qq']$ : color =  $3\bar{b}$ , SU(3) flavour =  $3\bar{b}$ , spin=0, spin-spin force also attractive: *good diquark* (Jaffe, 1977)  
 - makes a simple unit to form color singlets (Jaffe & Wilcezcck, 2003)  
 -  $[cq]$  may make a stable configuration even for spin 1, *bad diquark*, since spin-spin interactions, repulsive in spin 1, decrease with mass)

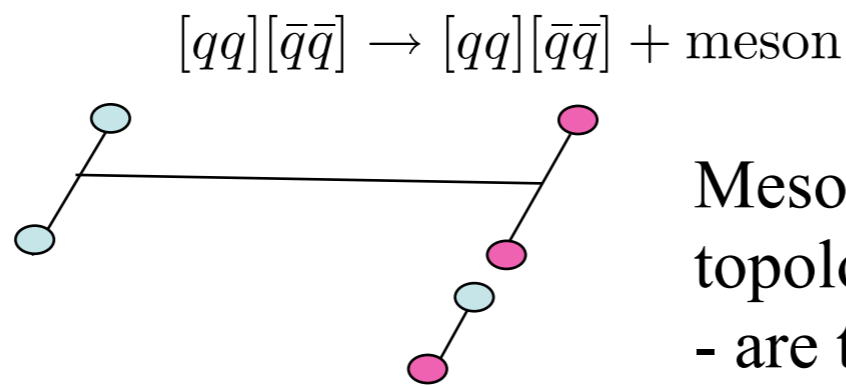
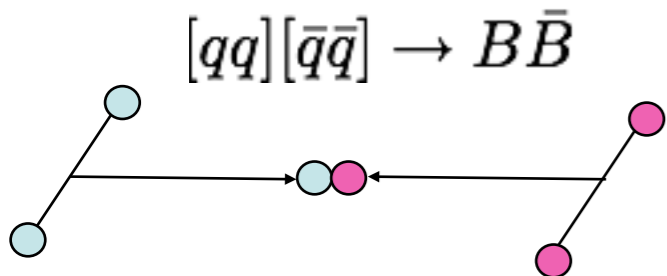
Diquark needs to combine with other colored objects:

with  $q \rightarrow$  baryon (e.g.  $\Lambda$ ), Y-shape

with  $[\bar{q}\bar{q}] \rightarrow$  scalar meson, H-shape (Rossi & Veneziano, 1980)



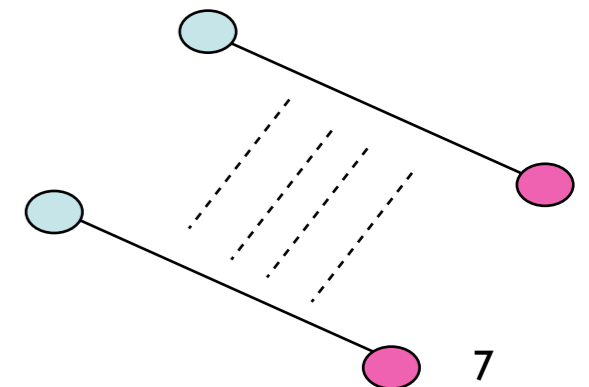
Many states: tetraquarks may have radial and orbital excitations  
 string topology is more related to Baryon-antiBaryon:  
 if you break the string,



A. De Rujula, H. Georgi and S. L. Glashow,  
 Phys. Rev. Lett. 38 (1977) 317.

Meson-meson molecules have a different string topology:

- are they bound?
- very few states



# 3. Conventional and less conventional Quarkonia

- The accuracy with which the spectra of  $Q\bar{Q}$  states ( $Q=c, b$ ) are predicted and measured makes it possible to discover new states “by difference”
- Terminology of  $Q\bar{Q}$  states in S and P wave:

spin =  $S$ , orb. ang. mom. =  $L$ , tot. ang. mom. =  $J$ :  $2S+1 L_J$

radial excitation =  $n$

$\eta_c(1S) = {}^1S_0$ ;  $J/\Psi(1S) = {}^3S_1$

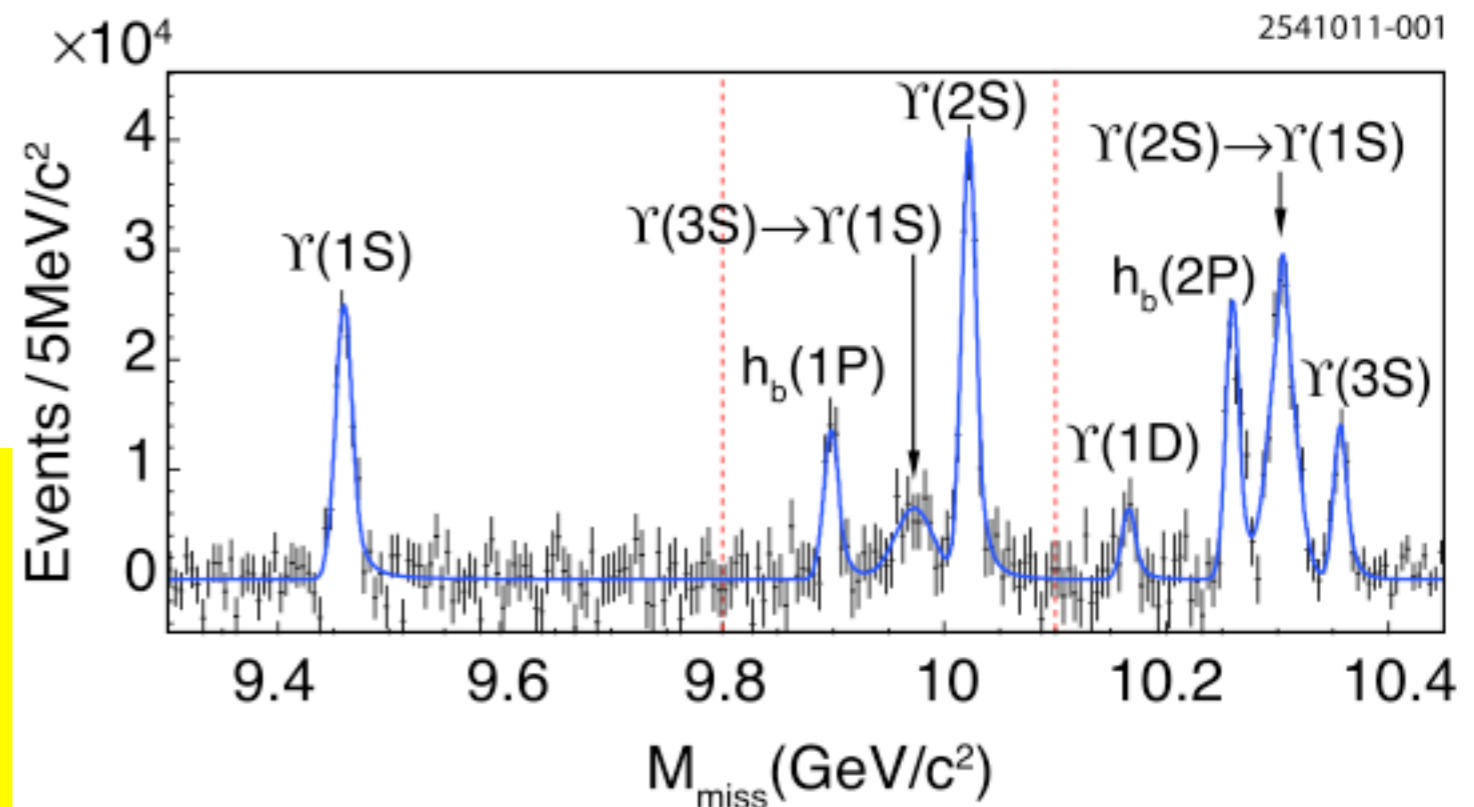
$h_c(1P) = {}^1P_1$ ,  $\chi_c(1P) = {}^3P_J$

Particle Data Group:

S. Eidelman et al., DEVELOPMENTS IN HEAVY QUARKONIUM SPECTROSCOPY  
Updated March 2014;

Quarkonium Working Group:

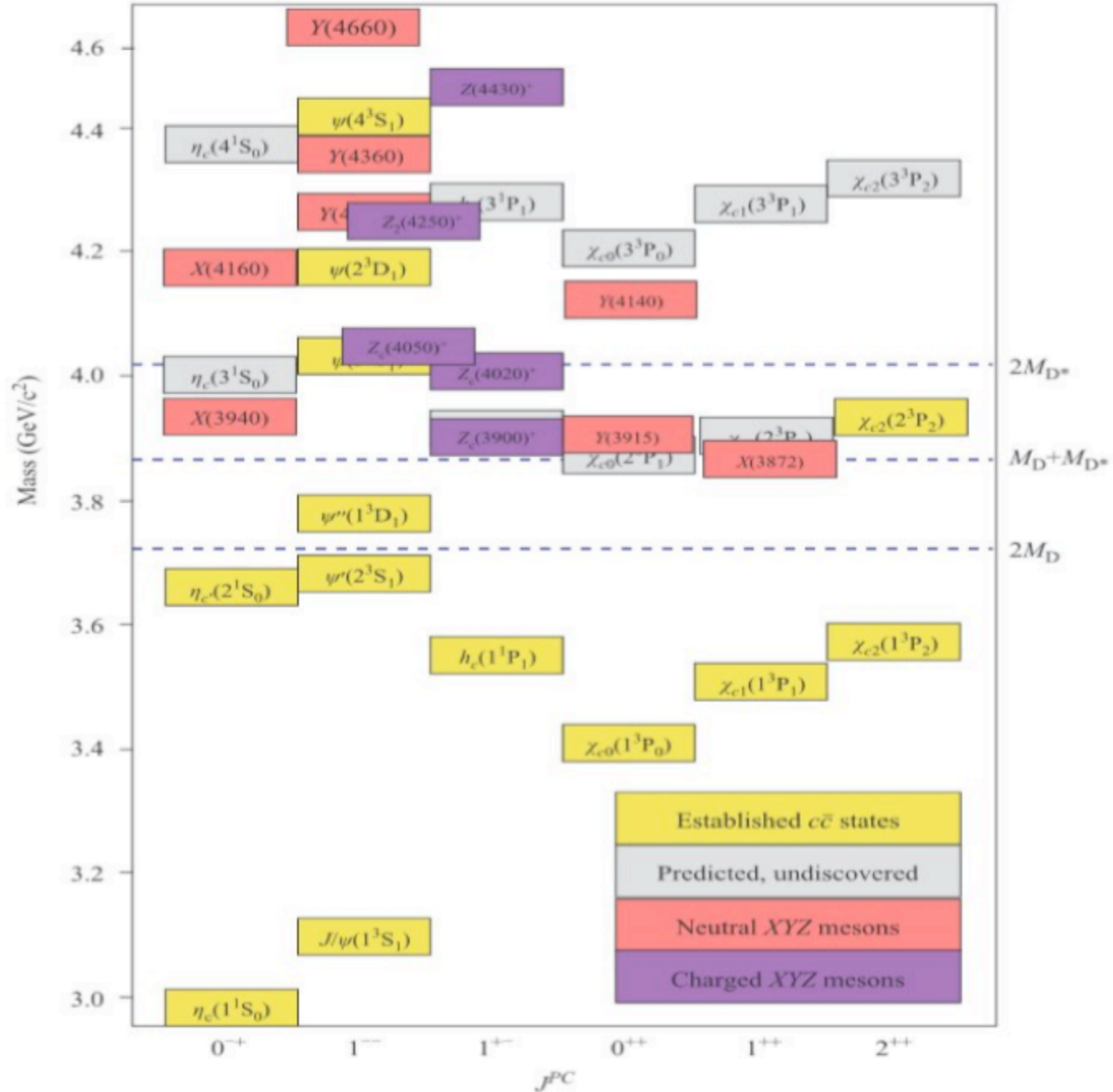
N. Brambilla et al., arXiv:1404.3723v1  
[hep-ph] 14 Apr 2014



**Figure 1:** From Belle [31], the mass recoiling against  $\pi^+\pi^-$  pairs,  $M_{\text{miss}}$ , in  $e^+e^-$  collision



# Charmonia and Charmonium-like Hadrons (Olsen, arxiv:1411.7738)



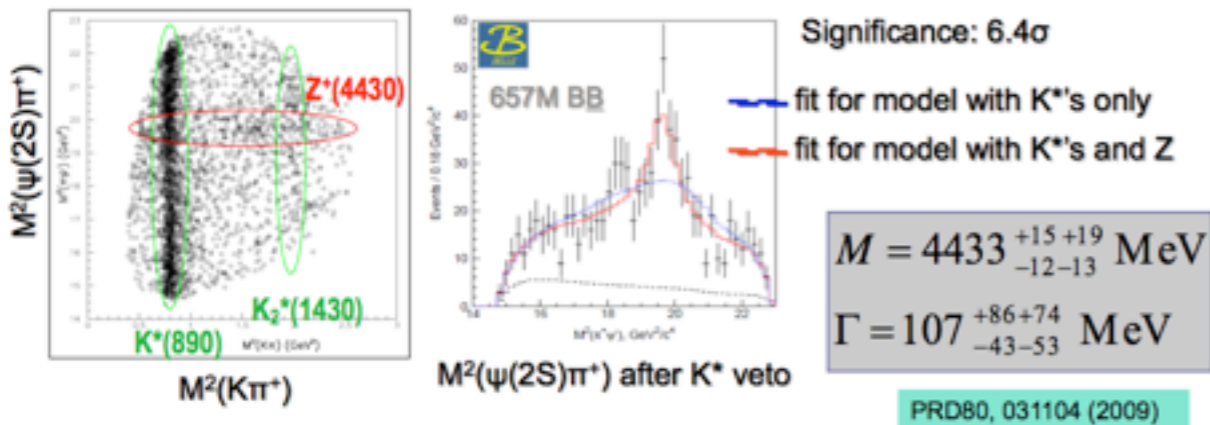
# terminology of unanticipated charmonia

- X, e.g. X(3872): neutral, typically seen in J/Psi+pions, positive parity,  $J^{PC}=0^{++}, 1^{++}, 2^{++}$
- Y, e.g. Y(4260): neutral, seen in  $e^+e^-$  annihilation with Initial State Radiation, therefore  $J^{PC}=1^{--}$
- Z, eg. Z(4430): charged/neutral, typically positive parity, mostly seen in J/Psi+pion and some in  $h_c(1P) + \text{pion}$

- Found in  $\psi(2S)\pi^+$  from  $B \rightarrow \psi(2S)\pi^+K$ . Z parameters from fit to  $M(\psi(2S)\pi^+)$
- Confirmed through Dalitz-plot analysis of  $B \rightarrow \psi(2S)\pi^+K$
- $B \rightarrow \psi(2S)\pi^+K$  amplitude: coherent sum of Breit-Wigner contributions

**Models: all known  $K^* \rightarrow K\pi^+$  resonances only**

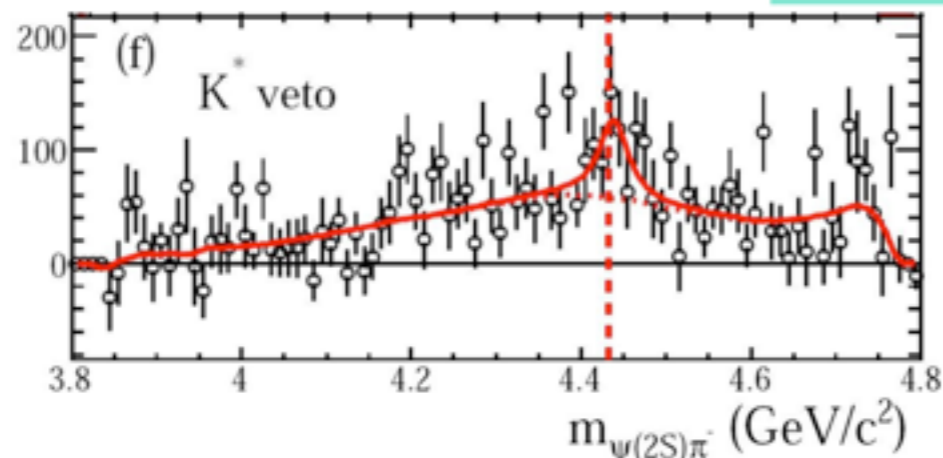
**all known  $K^* \rightarrow K\pi^+$  and  $Z^+ \rightarrow \psi(2S)\pi^+$   $\Rightarrow$  favored by data**



- [cu][cd] tetraquark? neutral partner in  $\psi'\pi^0$  expected**
- $D^*D_1(2420)$  molecule? should decay to  $D^*D^*\pi$**



**BaBar doesn't see a significant  $Z(4430)^+$**



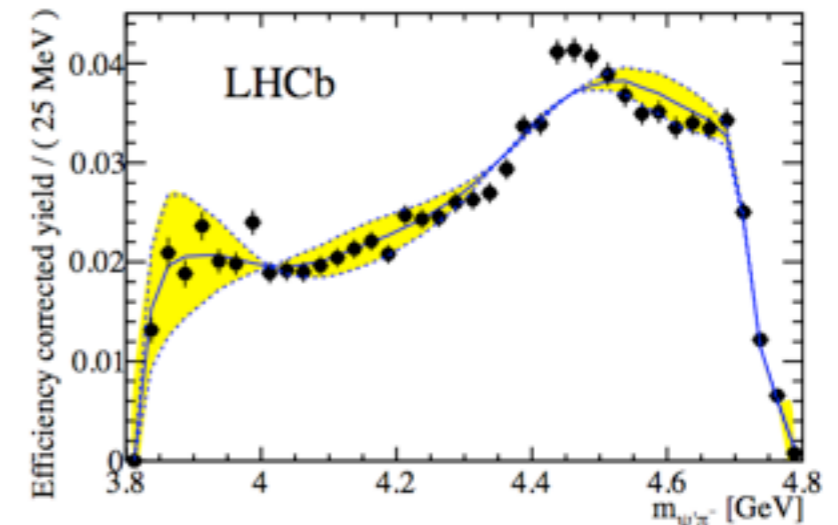
"For the fit ... equivalent to the Belle analysis...we obtain mass & width values that are consistent with theirs,... but only  $\sim 1.9\sigma$  from zero; fixing mass and width increases this to only  $\sim 3.1\sigma$ ."

$BF(B^0 \rightarrow Z^+K) \times BF(Z^+ \rightarrow \psi(2S)\pi^+) < 3.1 \times 10^{-5}$

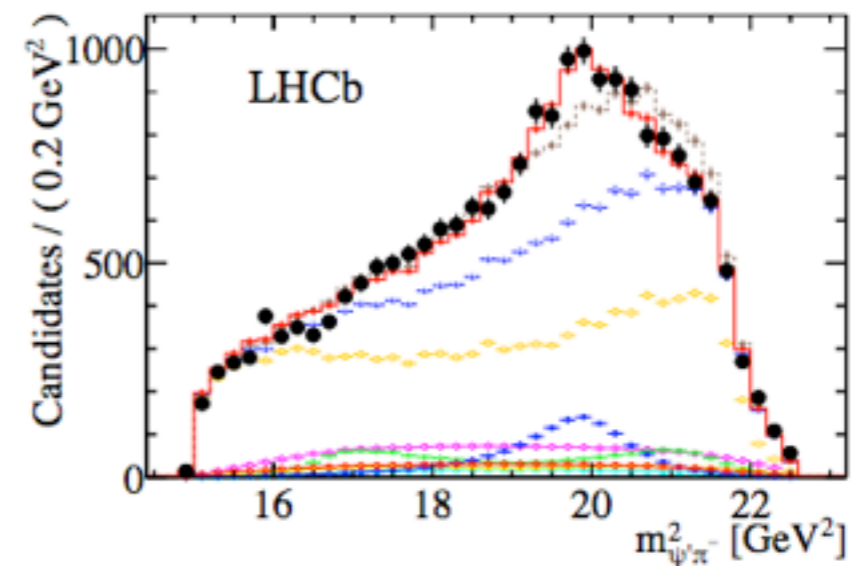
Belle PRL:  $(4.1 \pm 1.0 \pm 1.4) \times 10^{-5}$

- Babar inserts in the fit all  $K^*$  resonances
- is Belle effect due to  $K^*$  reflections ???

# 4. The $Z^\pm(4430)$ saga



no Z



with Z

- $D^*D_1 =$  in S-Wave: may have  $J=1$  but has negative parity
- Argand Plot shows  $90^\circ$  phase: Z is a genuine resonance

# Z(4430) as a radially excited tetraquark

- There *are* 4 quarks in Z(4430)
- in 2007 we classified the Z(4430) as a tetraquark, the radial excitation of the S-wave companion of X(3872)
- this was because of its decay into  $\psi(2S)^+ \pi$  and its mass  $\sim 550$  MeV larger than the X
- We noted then: *A crucial consequence of a Z(4430) charged particle is that a charged state decaying into  $\psi(1S) \pi^\pm$  or  $\eta_c \rho^\pm$  should be found around 3880 MeV (i.e. almost degenerate with X(3872))*
- The  $Z_c(3900)$  has been seen later by BES III and Belle with the anticipated decay:
  - $Z^+(3900) \rightarrow \psi(1S) \pi^+$
- a neutral partner was suggested by CLEO,
- The further observation of Z(4020) by the BES III Collaboration reinforces the tetraquark picture, which looks more attractive and constrained as compared to some years ago
- The Z(4430) decay into  $\psi(2S)$  as indication of a radially excited tetraquark has been confirmed by S. Brodski *et al.* (arXiv:1406.7281 [hep-ph])



# Radial excitations

Spacing of radial excitations are the same in Charmonia and Bottomonia;

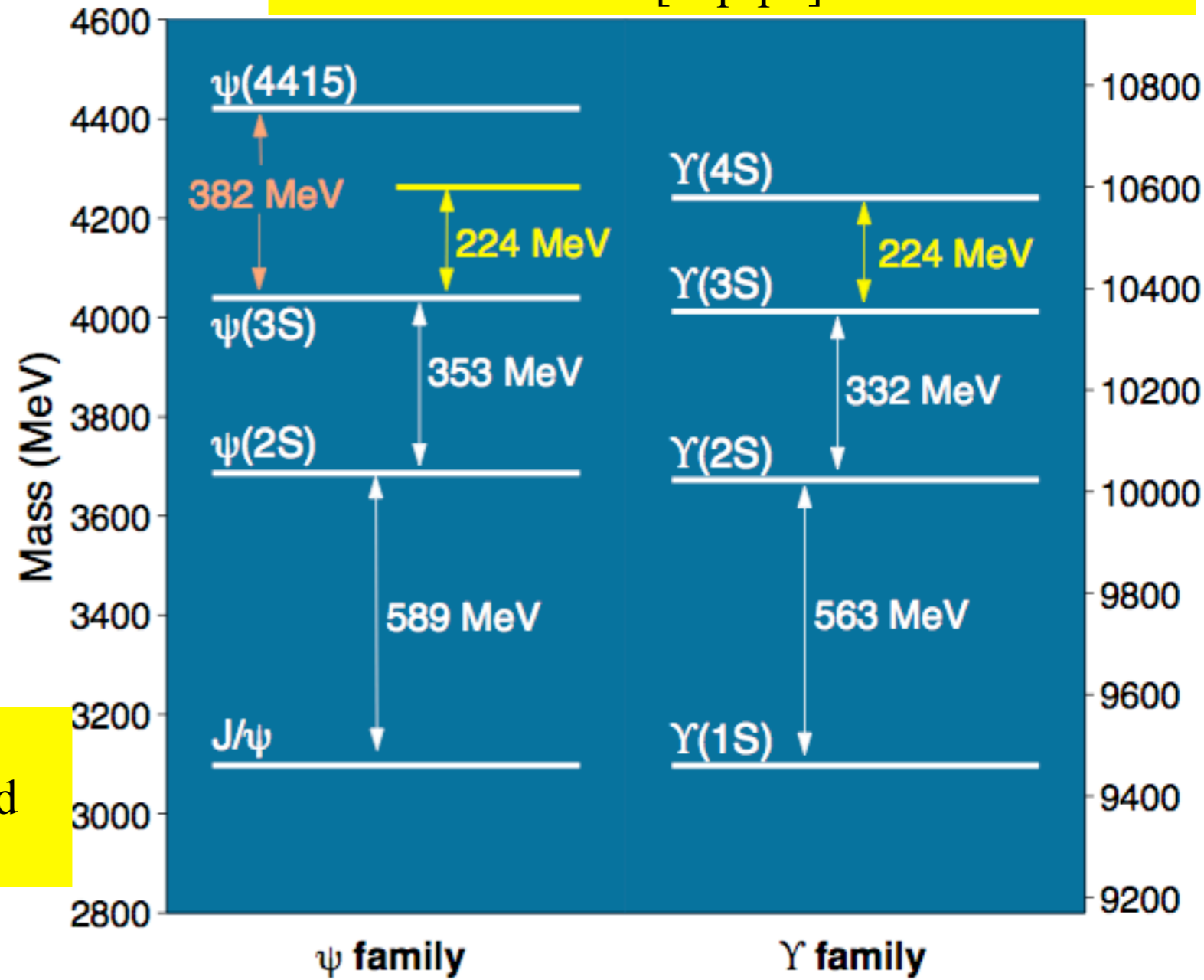
- gap between 1P-2P states is smaller :

$$\chi_{bJ}(2P) - \chi_{bJ}(1P) \approx 360 \text{ MeV}$$

$$\chi_{cJ}(2P) - \chi_{cJ}(1P) \approx 437 \text{ MeV}$$

Is a diquark-antidiquark pair similar to a quark-antiquark pair? a very tightly bound diquark?

L.-P. He, D.-Y. Chen, X. Liu and T. Matsuki  
arXiv:1405.3831 [hep-ph].





## 5. Tetraquarks in the large N expansion

- Reputation of tetraquarks was somehow tarnished by a theorem of S. Coleman: *tetraquarks correlators for  $N \rightarrow \infty$  reduce to disconnected meson-meson propagators*

S. Coleman, *Aspects of Symmetry* (Cambridge University Press, Cambridge, England, (1985), pp. 377–378

- The argument was reexamined by S. Weinberg who argued that if the connected tetraquark correlator develops a pole, it will be irrelevant that it is of order  $1/N$  with respect to the disconnected part: *at the pole the connected part will dominate anyhow;*

S. Weinberg, PRL 110, 261601 (2013)

- the real issue is the width of the tetraquark pole: it may increase for large N, to the point of making the state undetectable;
- Weinberg's conclusion is that the decay rate goes like  $1/N$ , making tetraquarks a respectable possibility.
- Weinberg's discussion has been enlarged by M. Knecht and S. Peris (arXiv:1307.1273) and further considered by T. Cohen and R. Lebed et al. (arXiv: 1401.1815, arXiv: 1403.8090).

What is not forbidden is NECESSARY

# Decay amplitudes in 1/N expansion

- By Fierz rearrangements, tetraquark operators can be reduced to products of color singlet bilinears;
- interpolating field operators have to be multiplied by powers of N, such as to make the connected two-point correlators to be normalized to unity;
- one loop amplitude with insertions of quark color singlet operators gives a factor N.

$$Q = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}] \left\{ \begin{array}{l} \frac{1}{\sqrt{N}} (\bar{u}c) (D, D^*) \\ \frac{1}{\sqrt{N}} (\bar{c}u) (\bar{D}, \bar{D}^*) \\ + (c \leftrightarrow u) \\ \frac{1}{\sqrt{N}} (\bar{c}c) (\eta_c, J/\Psi, \chi_c, h_c, \dots) \\ \frac{1}{\sqrt{N}} (\bar{u}u) (\pi, \eta, \rho, \omega, \dots) \end{array} \right. \quad \bullet \text{ two independent amplitudes}$$

- The result is that *decay amplitudes into two mesons are of order:*  $\frac{1}{N^{3/2}} N = \frac{1}{\sqrt{N}}$
- These two amplitudes were introduced long ago for tetraquark light scalar decay: reassuringly, they turn out both to be leading in 1/N.

L. Maiani, F. Piccinini, A. D. Polosa, V. Riquer, PRL **B93**, 212002 (2004)

# further decay amplitudes

- tetraquark de-excitation amplitudes by meson emission, e.g.  $Y(4260) \rightarrow Z_c(3900) + \pi$ , are also of order  $1/\sqrt{N}$

$$Y(4260) = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}] \left\{ \begin{array}{l} \bar{c}u \\ \bar{u}c \end{array} \right. \left. \begin{array}{l} u \\ u \end{array} \right\} \left\{ \begin{array}{l} \bar{u}c \\ \bar{c}d \\ \bar{d}u \end{array} \right. \left. \begin{array}{l} c \\ d \end{array} \right\}$$

$$Z_c^-(3900) = \frac{1}{\sqrt{N}} [cd][\bar{c}\bar{u}]$$

$$\pi^+ = \frac{1}{\sqrt{N}} (u\bar{d})$$

- however, e.m. currents need no normalization factor, so that the de-excitation amplitudes via photon emission are of order  $eQ \times 1$ .

$$Y(4260) = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}] \left\{ \begin{array}{l} \bar{c}u \\ \bar{u}c \end{array} \right. \left. \begin{array}{l} u \\ u \end{array} \right\} \left\{ \begin{array}{l} \bar{u}c \\ \bar{c}u \end{array} \right. \left. \begin{array}{l} c \\ u \end{array} \right\}$$

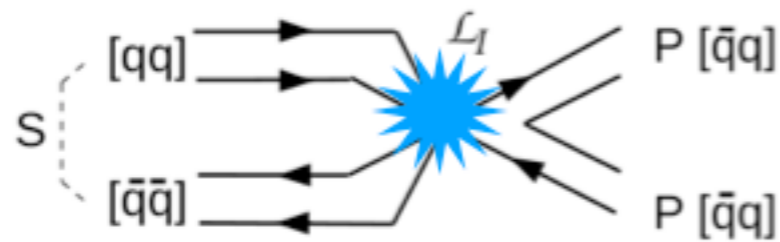
$$X(3872) = \frac{1}{\sqrt{N}} [cu][\bar{c}\bar{u}]$$

$$eQ \quad \gamma$$

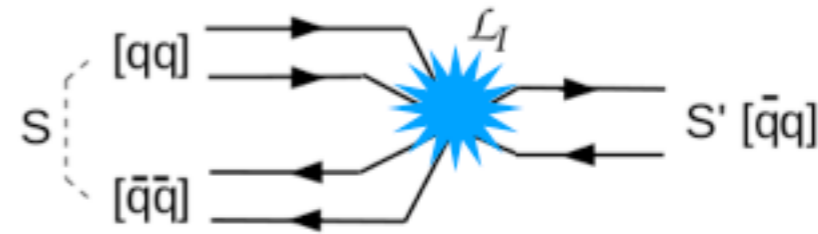
# Non-perturbative instantons: may explain two or three further puzzles

G. 't Hooft, G. Isidori, L. Maiani, A. D. Polosa and V. Riquer, PL **B662** (2008) 424.

A. H. Fariborz, R. Jora and J. Schechter, PR **D77** (2008) 094004.



(a)



(b)

- (a) the decay  $f_0(980) \rightarrow 2\pi$  ( $f_0 = \frac{([su][\bar{s}\bar{u}] + u \rightarrow d)}{\sqrt{2}}$ )
- (b) the mixing of light (tetraquark) scalar mesons with  $q$ - $q$ bar mesons, the latter being made by  $a_0(1474)$  ( $I=1$ ),  $K_0(1412)$ , ( $I=1/2$ ), and three isosinglets:  $f_0(1370)$ ,  $f_0(1507)$  and  $f_0(1714)$  (one could be a glueball);
- (c)= (b) in the reverse:

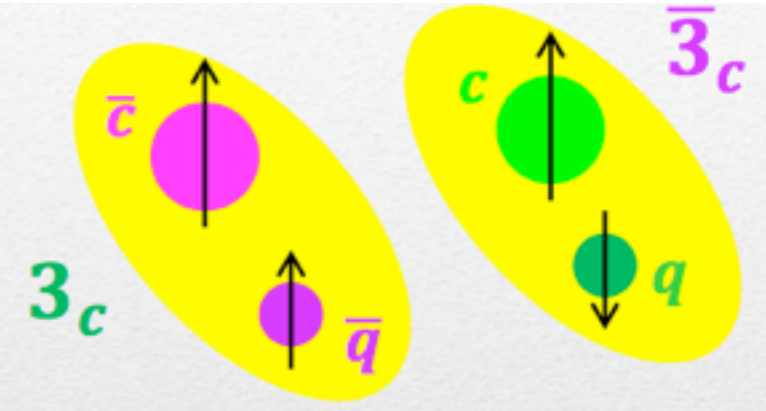
- with:  $Y(4260) = \frac{([cu][\bar{c}\bar{u}] + u \rightarrow d)}{\sqrt{2}}$ , the  $u$ - $u$ bar or  $d$ - $d$ bar pair in  $Y$  may give rise to the observed decay:

$$Y(4260) \rightarrow J/\Psi + f_0(q\bar{q})_{off-shell} \rightarrow J/\Psi + f_0([qq][\bar{q}\bar{q}])$$

# 6. Tetraquark picture of unexpected quarkonia

L.Maiani, F.Piccinini, A.D.Polosa and V.Riquer, Phys. Rev. D 71 (2005) 014028

$$[cQ]_{s=0,1} [\bar{c}\bar{q}']_{\bar{s}=0,1}$$



- $I=1, 0$
- S-wave: positive parity
- total spin of each diquark,  $S=1, 0$
- neutral states may be mixtures of isotriplet and isosinglet
- mass splitting due to spin-spin interactions (e.g. the non-relativistic constituent quark model)

$$H = 2M_{diquark} - 2 \sum_{i<j} \kappa_{ij} (\vec{s}_i \cdot \vec{s}_j) \frac{\lambda_i^A}{2} \frac{\lambda_j^A}{2}$$

## The S-wave, $J^P=1^+$ charmonium tetraquarks

- use the basis  $|s, \bar{s}\rangle_J$

$$J^P = 0^+ \quad C = + \quad X_0 = |0, 0\rangle_0, \quad X'_0 = |1, 1\rangle_0$$

$$J^P = 1^+ \quad C = + \quad X_1 = \frac{1}{\sqrt{2}} (|1, 0\rangle_1 + |0, 1\rangle_1)$$

$$J^P = 1^+ \quad C = + \quad Z = \frac{1}{\sqrt{2}} (|1, 0\rangle_1 - |0, 1\rangle_1), \quad Z' = |1, 1\rangle_1$$

$$J^P = 2^+ \quad C = + \quad X_2 = |1, 1\rangle_2$$

$$X(3872)=X_1$$

Z(3900), Z(4020)=lin. combs. of Z&Z' that diagonalize H

$$X(3940)=X_2 ??$$



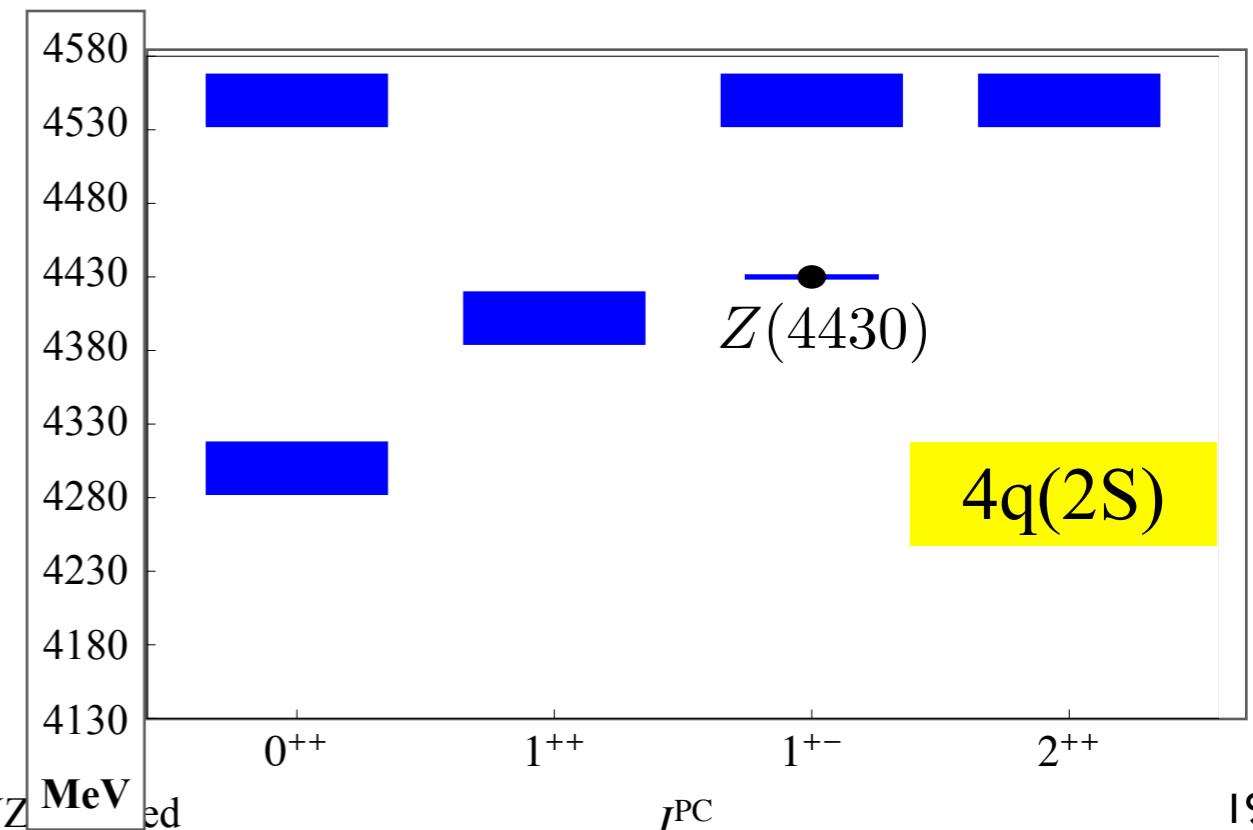
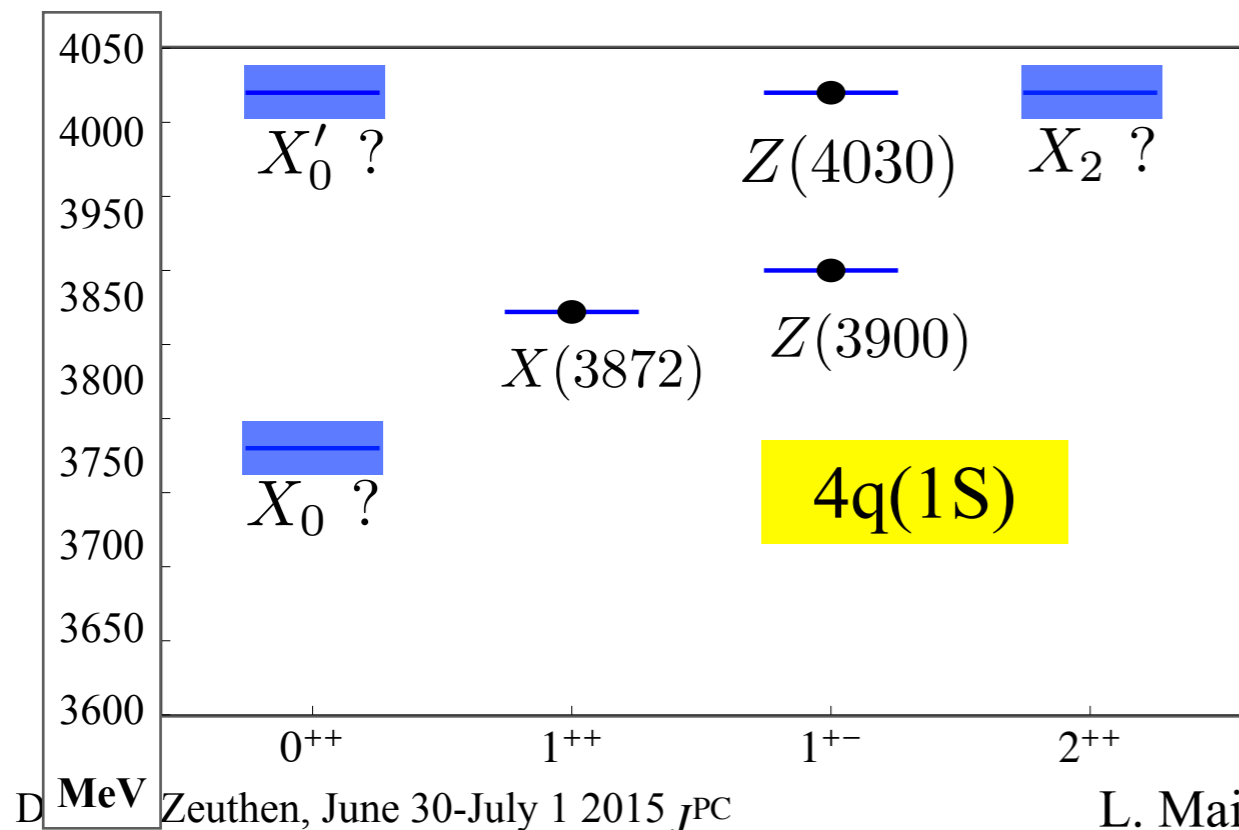
# Mass spectrum: the new paradigm

A. Polosa, V. Riquer, F. Piccinini, PRD **89**, 114010 (2014)

- A tentative mass spectrum for the S-wave tetraquarks was derived in the 2005 paper, based on an extrapolation of the spin-spin interactions in conventional S-wave mesons and baryons.
- Does NOT agree with the observed level ordering of X(3872), Z(3900) and Z(4020)
- A new, simple paradigm accounts for the observed pattern: dominant interactions are those *between quarks in the same (tightly bound?) diquark* (or antiquarks in the same antidiquark):

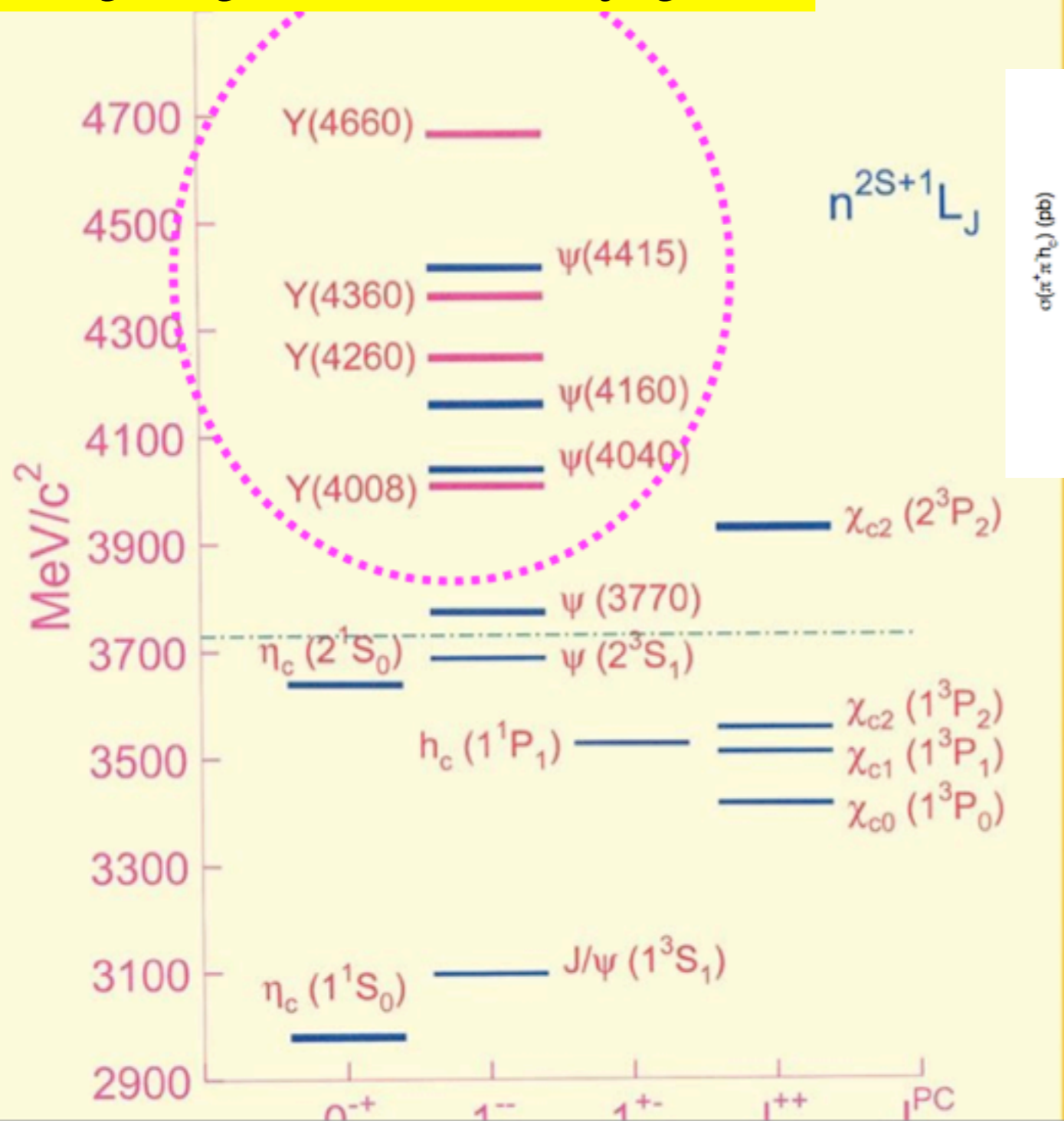
$$H \approx 2\kappa_{qc} (s_q \cdot s_c + s_{\bar{q}} \cdot s_{\bar{c}}) = \kappa_{qc} [s(s+1) + \bar{s}(\bar{s}+1) - 3]$$

- H is diagonal in the basis of diquark total spin and counts the number of spin=1 diquarks
- one Z is degenerate with X(3872), the other is heavier;
- $\kappa_{qc} \sim 60$  MeV from fit (larger than  $\kappa_{qc}$  in baryons).

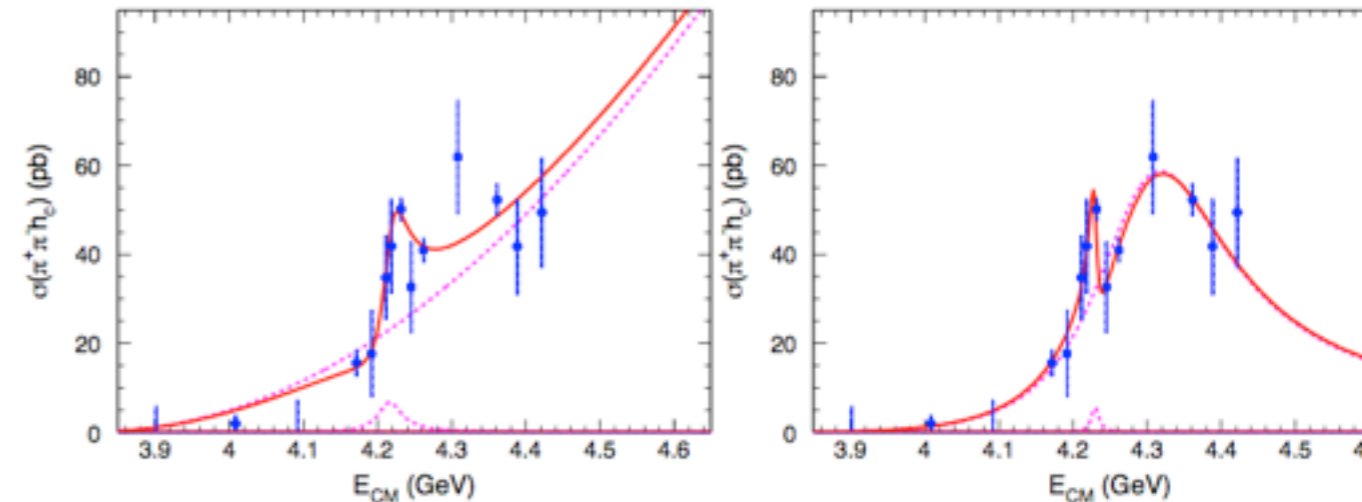


# 7. What are the Y states?

Changzheng YUAN, IHEP Beijing, 2014



later BES III has observed another one: Y(4230) which decays in  $h_c \pi \pi$



or maybe two? (narrow and wide)

Our survey:

- Y(4660) and Y(4360), decaying into  $\psi(2S)\pi$
- Y(4630) decaying into  $\Lambda_c \bar{\Lambda}_c$
- Y(4220), narrow (and Y(4290), wide ???) in  $h_c(1P) + \pi$ , BES III
- Y(4260) and Y(4008) decaying into  $J/\psi + \pi$ ,

# Y- tetraquarks

- Tetraquark states with  $J^{PC}=1^-$  can be obtained with odd values of the orbital angular momentum  $L=1, 3$  and diquark and antidiquark spins  $s, \bar{s}=0,1$ .
- use the notation:  $|s, \bar{s}; S, L\rangle_{J=1}$ , and charge conjugation invariance we get four states with  $L=1$ :

	spin composition: $ s, \bar{s}, S, L\rangle_J$	$P(s_{c\bar{c}} = 1)$	$P(s_{c\bar{c}} = 0)$	assign.
$Y_1$	$ 0, 0; 0, 1\rangle_1$	0.75	0.25	$Y(4008)$
$Y_2$	$\frac{1}{\sqrt{2}}( 1, 0; 1, 1\rangle_1 +  0, 1; 1, 1\rangle_1)$	1	0	$Y(4260)$
$Y_3$	$ 1, 1; 0, 1\rangle_1$	0.25	0.75	$Y(4230)$
$Y_4$	$ 1, 1; 2, 1\rangle_1$	1	0	$Y(4630)$

## Interpretation of Y states:

- leave aside the  $L = 3$  state (too heavy);
- $Y(4360)$  and  $Y(4660)$  = radial excitations of  $Y(4008)$  and  $Y(4260)$  (decay into  $\psi(2S)$ ,  $\Delta M \sim 350, 400$  MeV in the range of  $\Delta M$  of  $L = 1$  charmonia and bottomonia);
- the 4 states  $Y_{1-4}$  identified with  $Y(4008)$ ,  $Y(4260)$ ,  $Y(4220)$  (the narrow structure in the  $h_c$  channel) and  $Y(4630)$ .

# Selection rules

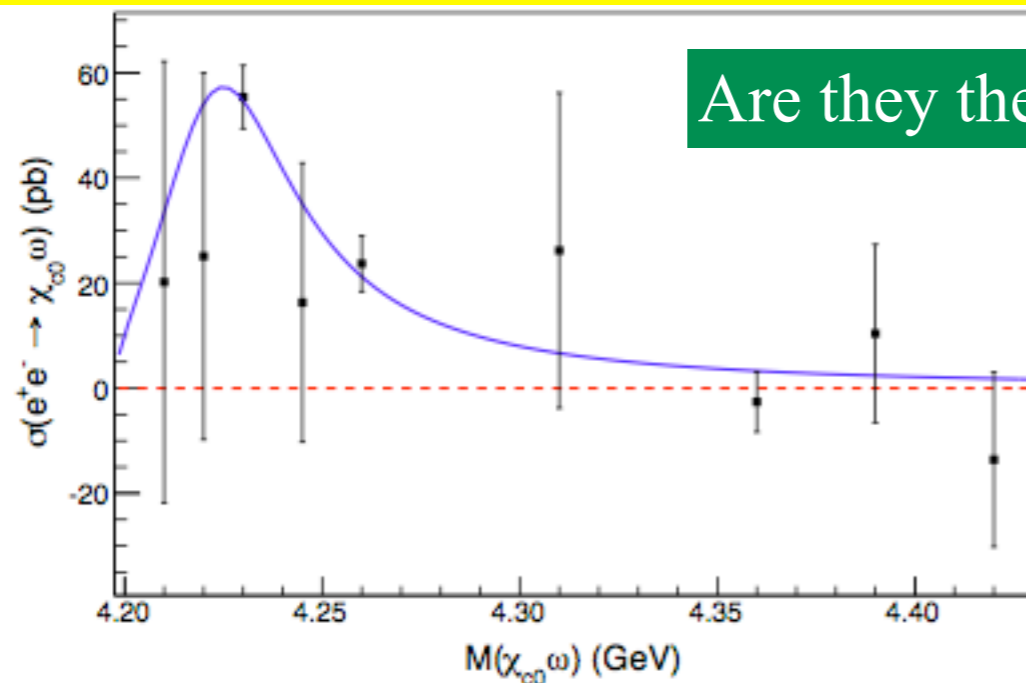
- Conservation of the heavy quark spin is well established in QCD: decays indicate the value of c-cbar spin in the initial wave function:
  - X(3872):  $S(c\text{-cbar})=1 \rightarrow J/\Psi$  yes, but no  $\eta_c$
  - Y(4230): both  $\chi_c$  ( $S(c\text{-cbar})=1$ ) and  $h_c$  ( $S(c\text{-cbar})=0$ )
- conservation of light quark spin is not reliable:
  - initial spin composition not necessarily reflected in  $K K^*$  vs  $K^* K^*$  decay modes
- observed X, Y, Z in the new paradigm of spin-spin coupling respect these rules, as far as we can see !
- more precise measurements of different decay channel will be of the utmost importance.

# Y states, decay patterns and very tentative assignments

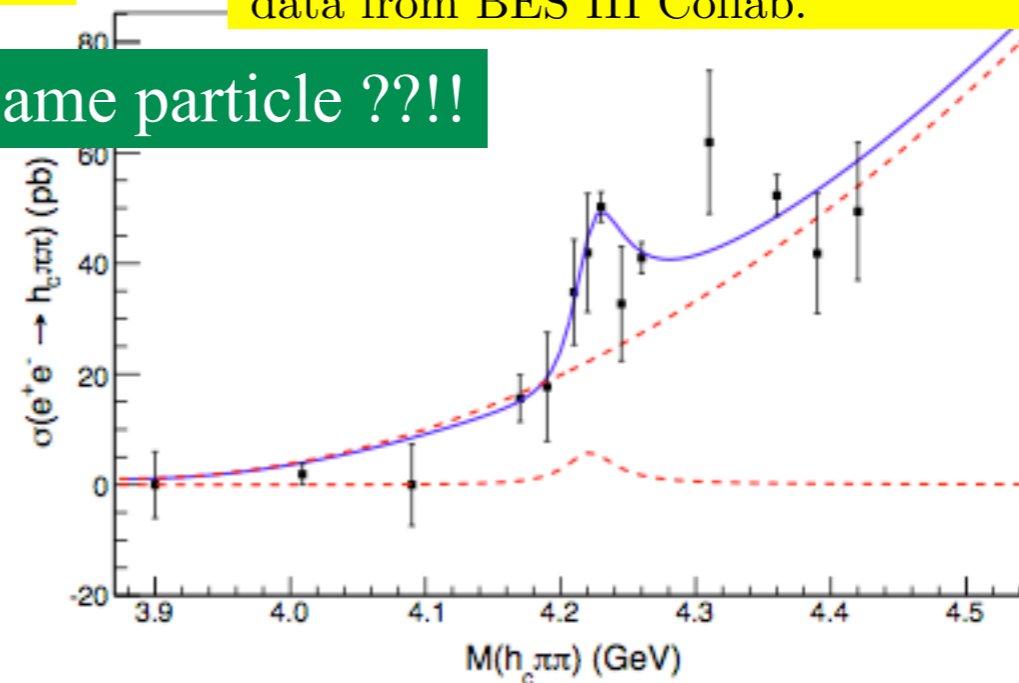
	$J/\Psi + \pi\pi$	$\psi(2S) + \pi\pi$	$h_c + \pi\pi$	$\chi_{c0} + \omega$	$\Lambda_c + \bar{\Lambda}_c$		$P(S_{c\bar{c}}=1)$	$P(S_{c\bar{c}}=0)$
$S_{c\bar{c}}$	1	1	0	1	1			
Y(4008)	seen	-	-	-	-	$Y_1$	0.75	0.25
Y(4230)	-	-	seen	seen	-	$Y_3$	0.25	0.75
Y(4260)	seen	-	-	-	-	$Y_2$	1	0
Y(4360)	-	seen	-	-	-	$Y'_1$	1	0
Y(4630)	-	-	-	-	seen	$Y_4$	1	0
Y(4660)	-	seen	-	-	-	$Y'_2$	1	0

M. Ablikim *et al.* [BESIII Collaboration], arXiv:1410.6538 [hep-ex].

C. Z. Yuan, Chin. Phys. C **38** (2014) 043001  
data from BES III Collab.



$$Y(4230) \rightarrow \chi_c + \omega$$



$$Y(4230) \rightarrow h_c + \pi^+ + \pi^-$$

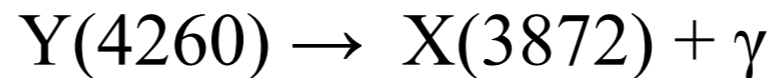
Are they the same particle ???!

Y(4230) has  $S_{c\bar{c}} = 1$  and  $S_{c\bar{c}} = 0$  decays, as required by  $Y_3$



# Radiative decays

- The identical spin structure implied in the model for  $Y(4260)$  and  $X(3872)$  suggests the decay



M.Ablikim et al. [BESIII Collaboration], arXiv:1310.4101 [hep-ex]

to be an *unsuppressed  $E_1$  transition*, with  $\Delta L=1$  and  $\Delta \text{Spin}=0$ , similar to the observed transitions of charmonium  $\chi$  states.

- The decay rate could provide a first estimate of the radius of the tetraquark.
- A comparison of the spin structures in  $Y$  and  $X$  states provides selection rules for  $E_1$  transitions that should provide a better identification of the levels.
- The assignments we have made produce the table:

$$Y_4 = Y(4630) \rightarrow \gamma + X_2 \quad (J^{PC} = 2^{++}) = \gamma + X(3940), \quad ??$$

$$Y_3 = Y(4220) \rightarrow \gamma + X'_0 \quad (J^{PC} = 0^{++}) = \gamma + X(3916), \quad ??$$

$$Y_2 = Y(4260) \rightarrow \gamma + X_1 \quad (J^{PC} = 1^{++}) = \gamma + X(3872), \quad \text{seen}$$

$$Y_1 = Y(4008) \rightarrow \gamma + X_0 \quad (J^{PC} = 0^{++}) = \gamma + X(3770 ??), \quad ??$$

# Basic formulae

*Hua-Xing Chen, Luciano Maiani, Antonio Polosa*

*PRELIMINARY, NOT TO BE QUOTED*

$$Y(4260) \rightarrow \gamma + X(3872)$$

ED1 transition from a Y tetraquark, P-wave, to a X tetraquark, S-wave, with the same spin structure. can be computed in the approximation where diquarks are treated as pointlike objects of electric charge Q:

$$Q = \left\{ \begin{array}{l} +\frac{4}{3}, \text{ for } [cu] \\ +\frac{1}{3}, \text{ for } [cd] \end{array} \right\}$$

pointlike approx. introduced by: A. Ali, C. Hambrock and S. Mishima, Phys. Rev. Lett. **106** (2011) 092002

$$\Gamma = \alpha \frac{\omega^3}{9\pi} \sum_{mki} |\langle X, m | Q x^i | Y, k \rangle|^2$$

- First estimate (not to be quoted):

$$\Gamma(Y4260 \rightarrow \gamma + X3872) \sim 40 \text{ keV}$$

$$B(Y4260 \rightarrow \gamma + X3872) \sim 3 \cdot 10^{-4}$$

- Basic formula:  $\sigma_{peak}(e^+ + e^- \rightarrow V \rightarrow f) = \frac{12\pi}{M^2} B(V \rightarrow e^+ e^-) B(V \rightarrow f)$

- BES III measures:  $5 \cdot 10^{-3} = \frac{\sigma(e^+ e^- \rightarrow \gamma + [J/\Psi \pi\pi]_X)}{\sigma(e^+ e^- \rightarrow J/\Psi \pi\pi)} \approx \frac{B(Y \rightarrow \gamma X) B(X \rightarrow J/\Psi \pi\pi)}{B(Y \rightarrow J/\Psi \pi\pi)}$

- our result implies:  $B(Y \rightarrow J/\Psi \pi\pi) \sim 0.06 B(X \rightarrow J/\Psi \pi\pi)$

that is:  $B(Y \rightarrow J/\Psi \pi\pi) \sim 3 \cdot 10^{-3}$ , assuming  $B(X \rightarrow J/\Psi \pi\pi) \sim 5 \cdot 10^{-2}$

or  $\Gamma(Y \rightarrow J/\Psi \pi\pi) \sim 7 \Gamma(X \rightarrow J/\Psi \pi\pi)$  for  $\Gamma(X) \sim 1 \text{ MeV} \dots$  can be tested ???

# 8. Hidden beauty tetraquarks

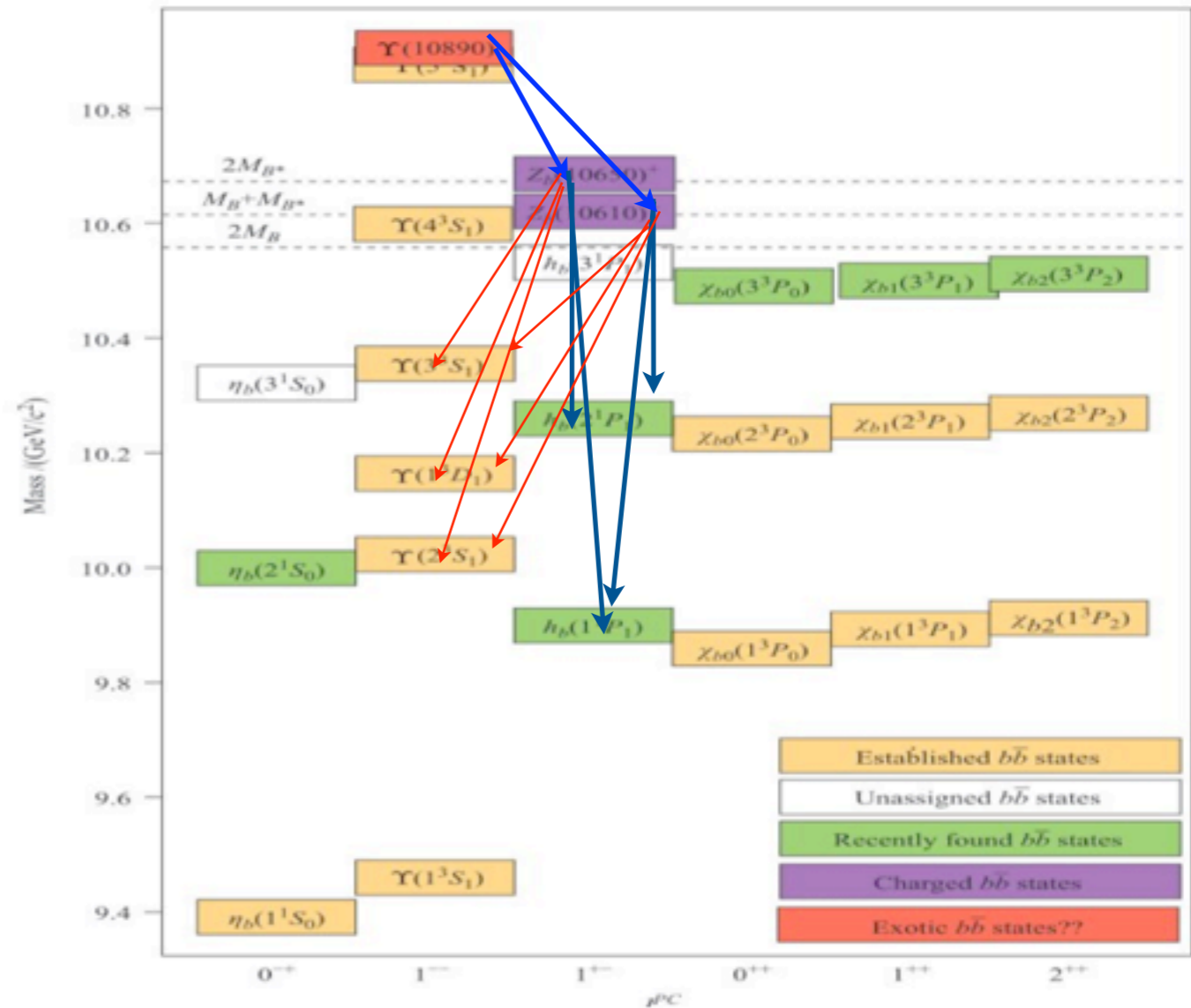
A. Ali, C. Hambrock, I. Ahmed and M. J. Aslam, Phys. Lett. B 684, 28 (2010);

A. Ali, C. Hambrock and M. J. Aslam, Phys. Rev. Lett. 104, 162001 (2010) [Erratum-ibid. 107, 049903 (2011)];

A. Ali, BELLE II ITIP, Krakow, 2015

Bottomonia and Bottomonium-like Hadrons (Olsen, arxiv:1411.7738)

- note:  $\Delta M(Z_b)/\Delta M(Z_c) \sim m_c/m_b$ , as expected
- Y(10850) usually identified with Y(5S)
- however Ali et al suggest Y(5S) is superimposed to the b-analog of Y(4260) with the decays:
  - $Y_b \rightarrow Z_b/Z_b' \pi \rightarrow h_b(nP) \pi \pi$
  - $Y_b \rightarrow Z_b/Z_b' \pi \rightarrow Y(nS) \pi \pi$
- simultaneous decay in  $h_b$  and Y *is compatible* with heavy quark spin conservation, since  $Z_b$  are not degenerate and each has both  $S_{(b \bar{b})} = 0, 1$  components



Ahmed Ali (DESY, Hamburg)

$$|Z_b\rangle = \frac{|1_{bq}, 0_{\bar{b}\bar{q}}\rangle - |0_{bq}, 1_{\bar{b}\bar{q}}\rangle}{\sqrt{2}} = \frac{\alpha|1_{q\bar{q}}, 0_{b\bar{b}}\rangle - \beta|0_{q\bar{q}}, 1_{b\bar{b}}\rangle}{\sqrt{2}}$$

$$|Z'_b\rangle = |1_{bq}, 1_{\bar{b}\bar{q}}\rangle_{J=1} = \frac{\beta|1_{q\bar{q}}, 0_{b\bar{b}}\rangle + \alpha|0_{q\bar{q}}, 1_{b\bar{b}}\rangle}{\sqrt{2}}$$

$$\alpha \approx \beta \approx 1$$

- heavy quark spin conservation implies:

- $Y \rightarrow h_b (nP) \quad S = 1 \rightarrow S = 0$ :

$$g_Z = g(\Upsilon \rightarrow Z_b \pi) g(Z_b \rightarrow h_b \pi) \propto -\alpha \beta \langle h_b | 1_{q\bar{q}}, 0_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle$$

$$g_{Z'} = g(\Upsilon \rightarrow Z'_b \pi) g(Z'_b \rightarrow h_b \pi) \propto \alpha \beta \langle h_b | 1_{q\bar{q}}, 0_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle = -g_Z$$

- $Y \rightarrow Y(nS)$

$$f_Z = f(\Upsilon \rightarrow Z_b \pi) f(Z_b \rightarrow \Upsilon(nS) \pi) \propto |\beta|^2 \langle \Upsilon(nS) | 0_{q\bar{q}}, 1_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle$$

$$f_{Z'} = f(\Upsilon \rightarrow Z'_b \pi) f(Z'_b \rightarrow \Upsilon(nS) \pi) \propto |\alpha|^2 \langle \Upsilon(nS) | 0_{q\bar{q}}, 1_{b\bar{b}} \rangle \langle 0_{q\bar{q}}, 1_{b\bar{b}} | \Upsilon \rangle = \frac{\alpha^2}{\beta^2} f_Z$$

- in agreement, within still large errors, with Belle data:

Final State	$\Upsilon(1S)\pi^+\pi^-$	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$	$h_b(2P)\pi^+\pi^-$
Rel. Norm.	$0.57 \pm 0.21^{+0.19}_{-0.04}$	$0.86 \pm 0.11^{+0.04}_{-0.10}$	$0.96 \pm 0.14^{+0.08}_{-0.05}$	$1.39 \pm 0.37^{+0.05}_{-0.15}$	$1.6^{+0.6+0.4}_{-0.4-0.6}$
Rel. Phase	$58 \pm 43^{+4}_{-9}$	$-13 \pm 13^{+17}_{-8}$	$-9 \pm 19^{+11}_{-26}$	$187^{+44+3}_{-57-12}$	$181^{+65+74}_{-105-109}$

Table 1: Relative normalizations and relative phases (in degrees), for  $s_{b\bar{b}} : 1 \rightarrow 1$  and  $1 \rightarrow 0$  transitions, as reported by Belle.

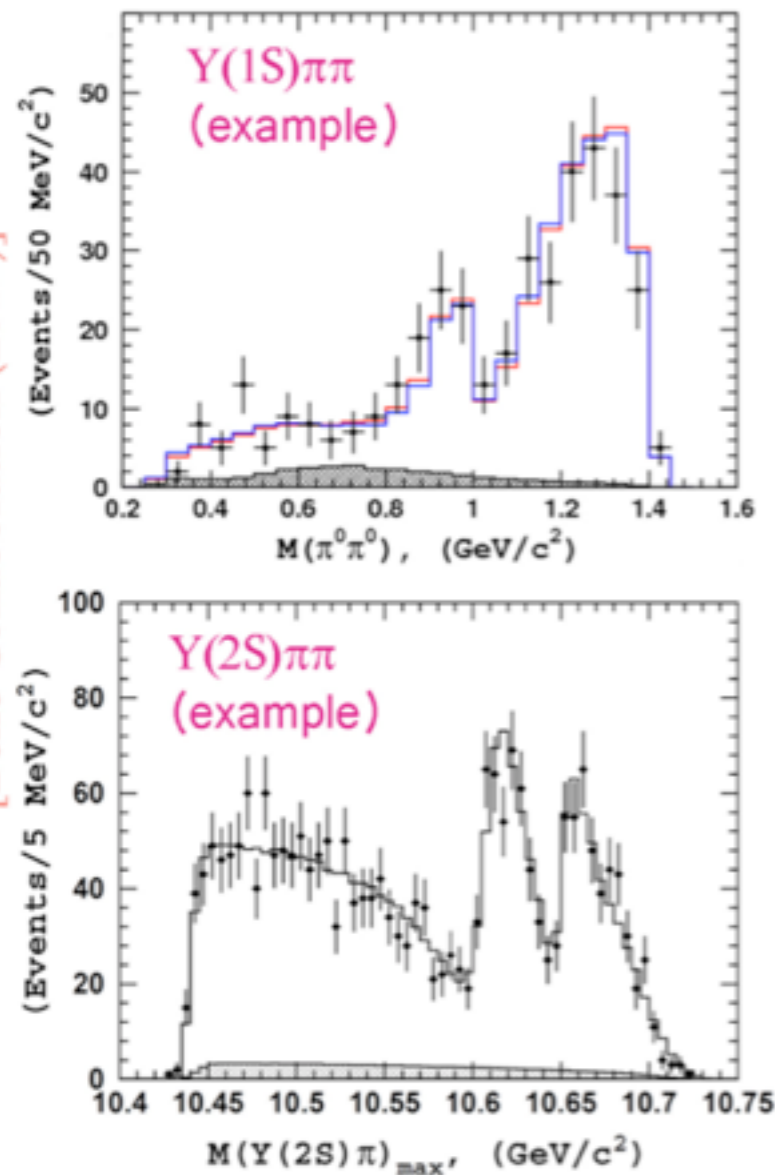
$$\begin{aligned} \overline{s_{b\bar{b}} : 1 \rightarrow 1 \text{ transition}} : \\ \overline{\text{Rel.Norm.}} &= 0.85 \pm 0.08 = |\alpha|^2 / |\beta|^2 \\ \overline{\text{Rel.Phase}} &= (-8 \pm 10)^\circ \end{aligned}$$

$$\begin{aligned} \overline{s_{b\bar{b}} : 1 \rightarrow 0 \text{ transition}} : \\ \overline{\text{Rel.Norm.}} &= 1.4 \pm 0.3 \\ \overline{\text{Rel.Phase}} &= (185 \pm 42)^\circ \end{aligned}$$

has the  $Y_b(10850)$  bump a 4quark component, besides the  $Y(5S)$  one, as proposed by Ali and coworkers?

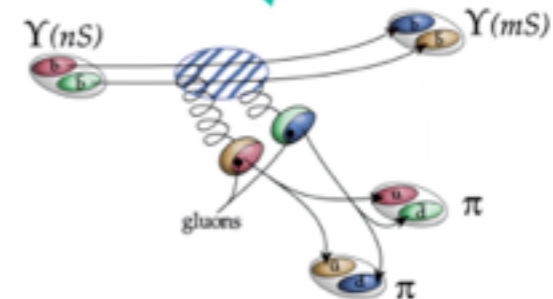
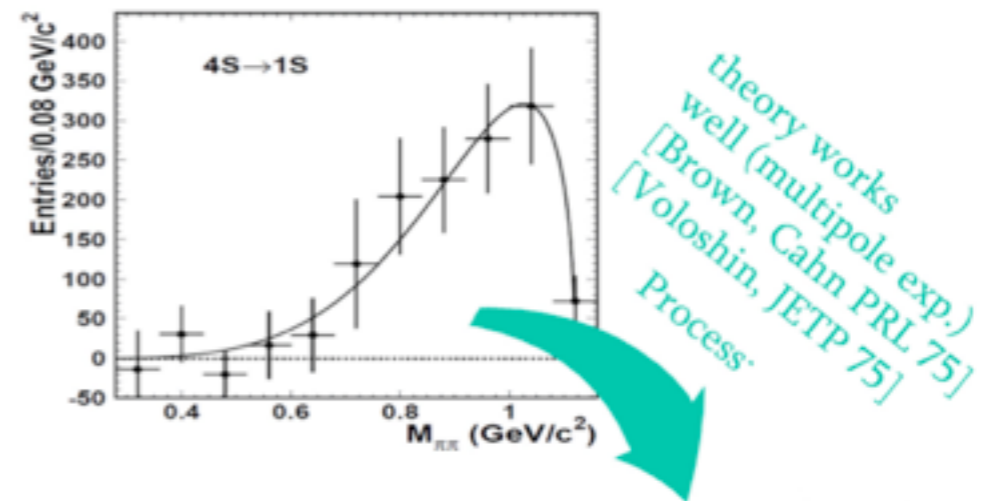
Dipion mass distributions in  $Y(5S) \rightarrow Y(nS)\pi\pi$  decays?

[Belle Collaboration (2012)]



Ahmed Ali (DESY, Hamburg)

- the dipion spectrum strongly suggestive of the characteristic processes:
  - 4quark decay in  $Y(1S)+q \bar{q} \rightarrow f_2(1270)$
  - same with  $f_0(1370) \rightarrow f_0(990)$  by instanton mixing [ $f_0(1370)$  goes essentially in  $4\pi$  only]
  - hint of de-excitation in  $Y_b(b \bar{b})+4\text{quark } f_0(500)$
  - note the difference w.r.t. the 2 pion spectrum in the decay of  $Y_b(4S)!!$

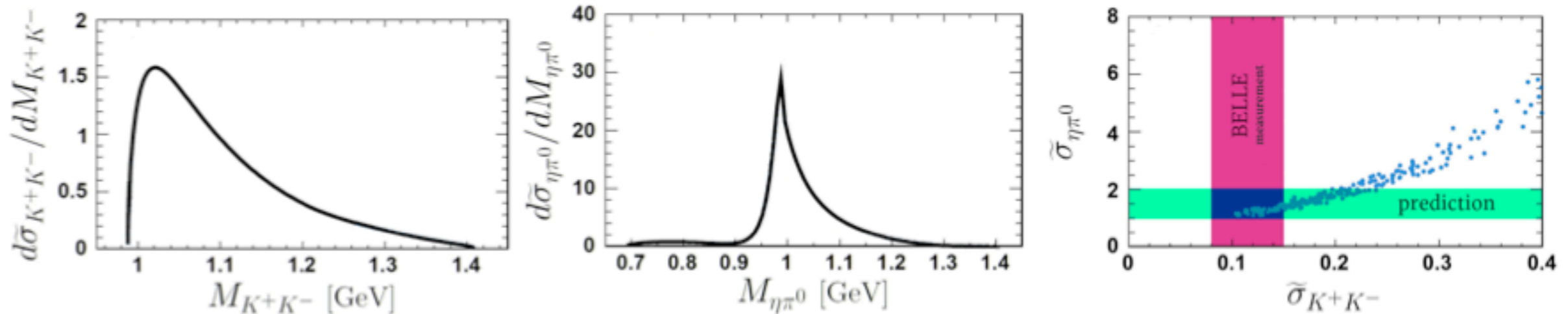




# Predictions for : $Y(10850) \rightarrow Y(1S) + K^+ K^-$ , or $\eta \pi^0$

Fit determines couplings (assume  $SU(3)$  flavor symmetry for couplings  $(\sigma(500), f_0(980), a_0(980)) \rightarrow PP'$ , [’t Hooft, Isidori, Maiani, Polosa, Riquer, PLB 08] )

↪ predictions for spectra:



■ Agreement with  $\tilde{\sigma}_{K+K^-} = 0.11^{+0.04}_{-0.03}$  (BELLE)

↪  $1.0 \lesssim \tilde{\sigma}_{\eta\pi^0} \lesssim 2.0$  predicted

■ Resonance dominance

↪ Characteristic shape

↪ **Good tests (relying on  $Y_b$  has 2 flavor states)**

## 9. To be convinced that we *do see* a new spectroscopy....

- $Z_c(3900)^0$  has been found: BES III, arXiv:1506.06018
- Is there the  $I=1$  (i.e. charged) companion of  $X(3872)$ ? is it very wide? are there more neutral  $Z$  ?
- Complete the 1S tetraquark multiplet (masses estimated with  $\pm 40$  MeV ?):
  - $X_0$ : 3780,  $X_0$ ,  $X_2$ : 4020, decay:  $J/\Psi \pi \pi$
- Fill the 2S multiplet
  - $Z'(2S)$ : 4550, decay  $\psi(2S) \pi$ ,  $h_c(2S) \pi$
  - $X(2S)$ : 4430
  - $X_0(2S)$ : 4310,  $X'_0(2S)$ ,  $X_2(2S)$ : 4550 decay  $\psi(2S) \pi$
- $Y(4660) \rightarrow \psi(2S) \pi \pi$  decay:
  - does it go via  $Z(4430) + \pi$  ? and there is a trace of  $Z'(2S) + \pi$  ?
- $Y(4660) \rightarrow \gamma + \dots$  to discover  $X(2S)$  ??
- are there  $Y_b(10850) \rightarrow Y(1S) \eta \pi^0$  decays?
- Can LHCb see the  $X, Y, Z$  states seen by Belle and BES?
- ....

Many Thanks !!