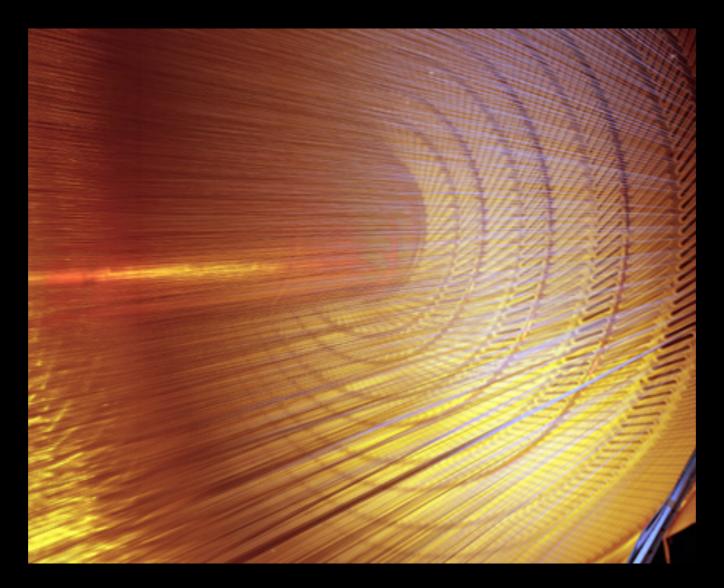
# High-precision measurement of the W boson mass with the CDF II detector



**Chris Hays, Oxford University** 



DESY Colloquium 24 May, 2022



### Electroweak gauge boson masses

#### Gauge field potential

$$V = -\frac{g^{2}v^{2}}{8}[(W_{\mu}^{+})^{2} + (W_{\mu}^{-})^{2}]$$
$$-\frac{v^{2}(g^{2} + g^{2})}{8}Z^{\mu}Z_{\mu}$$

$$m_W = \frac{v}{2}g$$

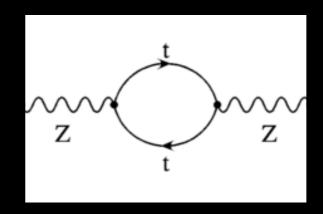
$$m_- =$$

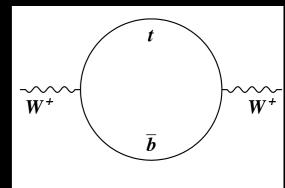
$$m_Z = \frac{v}{2} \sqrt{g^2 + g^2}$$

$$v = 246$$
 GeV and  $g = 0.64$ :

$$m_W = 78.7 \; \mathrm{GeV}$$

#### Quantum corrections





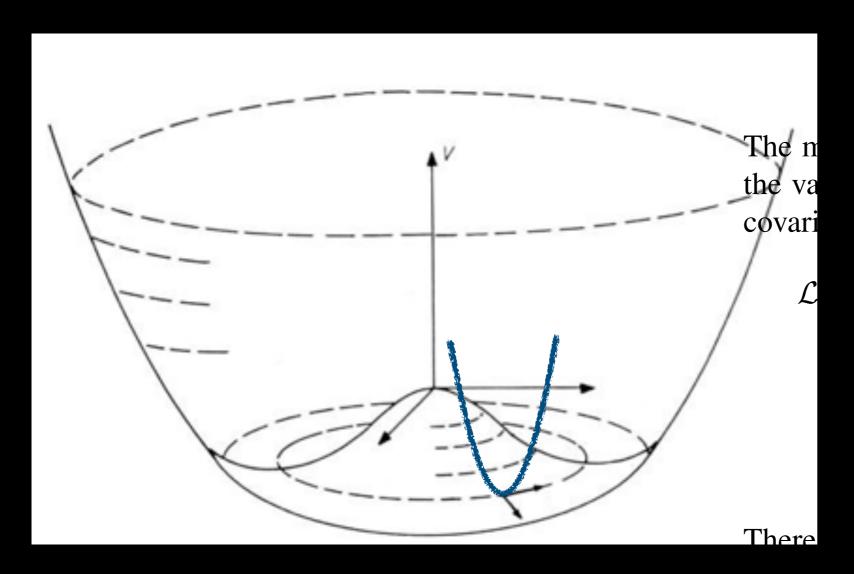
$$m_W^2 = \frac{\hbar^3}{c} \frac{\pi \alpha_{EM}}{\sqrt{2}G_F(1 - m_W^2/m_Z^2)(1 - \Delta r)}$$

$$\Delta r_{tb} = \frac{c}{\hbar^3} \frac{-3G_F m_W^2}{8\sqrt{2}\pi^2 (m_Z^2 - m_W^2)} \times \left[ m_t^2 + m_b^2 - \frac{2m_t^2 m_b^2}{m_t^2 - m_b^2} \ln(m_t^2/m_b^2) \right]$$

Global fit to SM measurements yields indirect W boson mass of  $81354 \pm 7$  MeV

### Higgs boson mass

#### Higgs field potential



$$m_H = v\sqrt{2\lambda} = 125 \text{ GeV}$$
  $\lambda \approx 0.1$ 

#### Quantum corrections

$$\mathcal{L}(\phi) = \frac{1}{2} (D_{\mu} \phi^* D^{\mu} \phi + \mu)$$
 of  $V(\phi)$  has not changed, d obtain the terms in equa

Naively integrating to a cutoff scale  $\Lambda$ :

$$\Delta m_H = \frac{3g^2 m_t^2}{16\pi^2 m_W^2} \Lambda^2$$

If there is no new physics up to scale  $\Lambda$  then we need 'fine-tuning' to cancel the quantum corrections

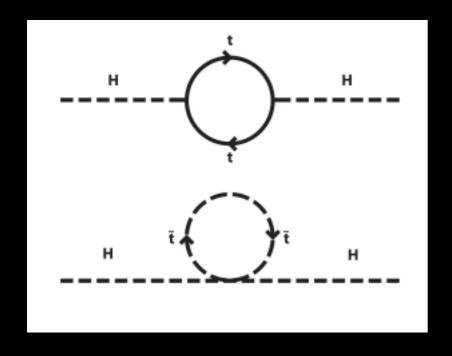
1% fine tuning:  $\Lambda = 6.6$  TeV

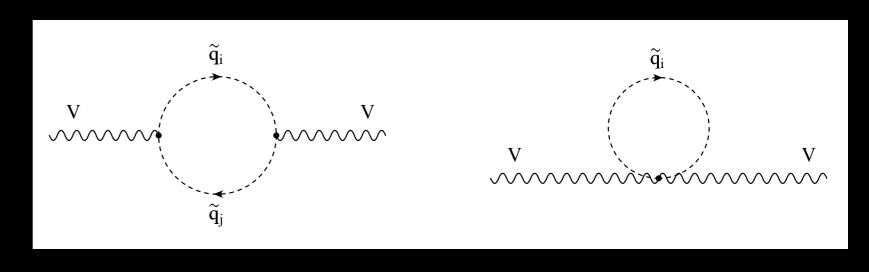
Motivates TeV-scale new physics

### W boson mass

The W boson mass is the most sensitive observable to sources of 'naturalness'

Classic example: Supersymmetry

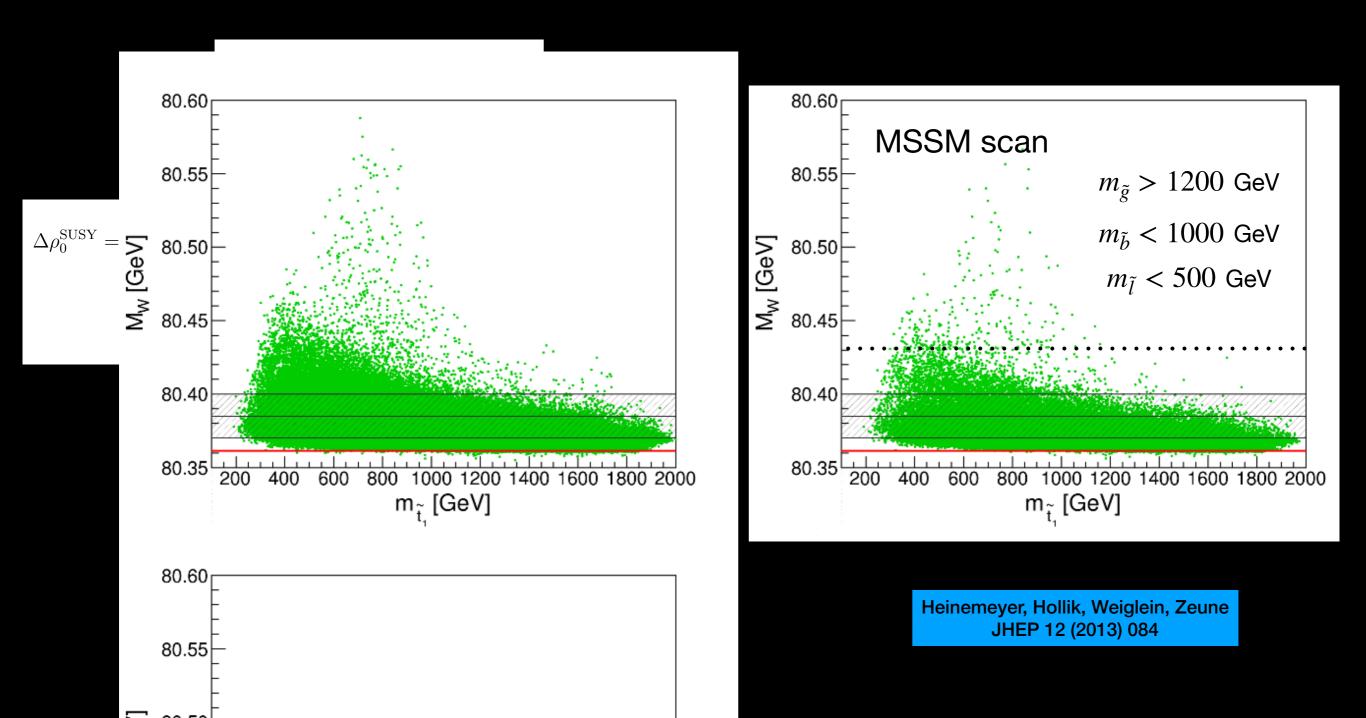




Mass splittings in supersymmetric isospin doublets: different mass shifts for W & Z bosons

### W boson mass

Difference in corrections to W and Z propagators encapsulated by  $\rho$  parameter

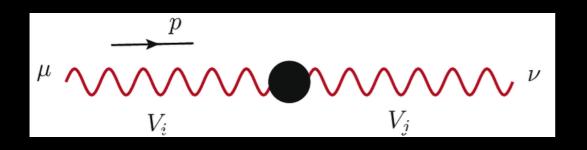


#### W boson mass

More generally the SM effective field theory parameterizes high-scale effects

$$\mathcal{L}_{\textit{SMEFT}} = \mathcal{L}_{\textit{SM}} + \mathcal{L}^{(5)} + \mathcal{L}^{(6)} + \mathcal{L}^{(7)} + \cdots, \qquad \mathcal{L}^{(d)} = \sum_{i=1}^{n_d} \frac{C_i^{(d)}}{\Lambda^{d-4}} Q_i^{(d)} \quad \text{for } d > 4.$$

I. Brivio and M. Trott, Phys. Rep. 793 (2019) 1



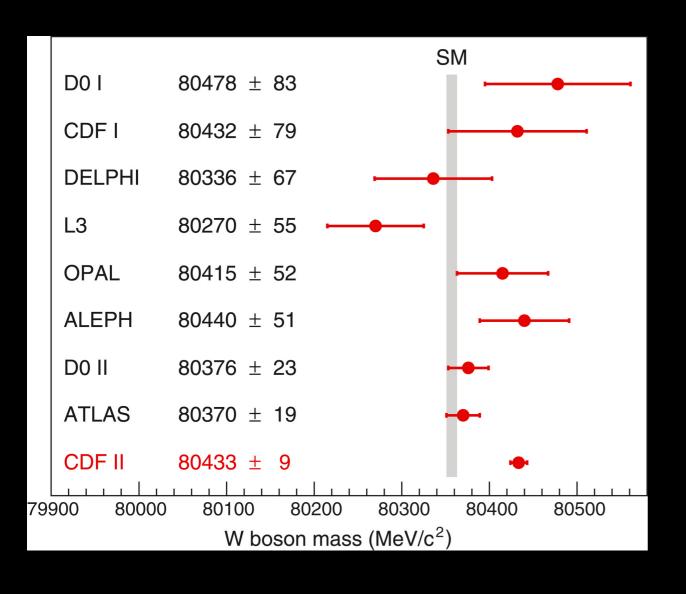
$$\frac{\delta m_W}{m_W} = \left(0.34c_{HD} + 0.72c_{HWB} + 0.37c_{Hl3} - 0.19c_{ll1}\right) \frac{v^2}{\Lambda^2}$$

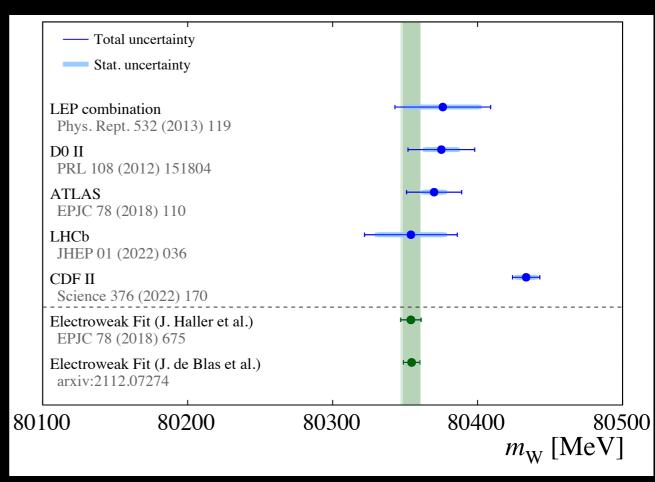
For 
$$\delta m_W/m_W=0.1\,\%$$
 and c<sub>HD</sub>=1,  $\Lambda=4.5\,{\rm TeV}$  e.g. Z' boson

For 
$$\delta m_W/m_W=0.1\,\%$$
 and chwb=1,  $\Lambda=6.6\,\text{TeV}$  e.g. compositeness

Smaller  $c_i \rightarrow smaller \Lambda$ 

### W boson mass measurements





### **CDF II measurement of the W boson mass**



 $\sqrt{s} = 1.96$  TeV proton-antiproton collisions from the Fermilab Tevatron

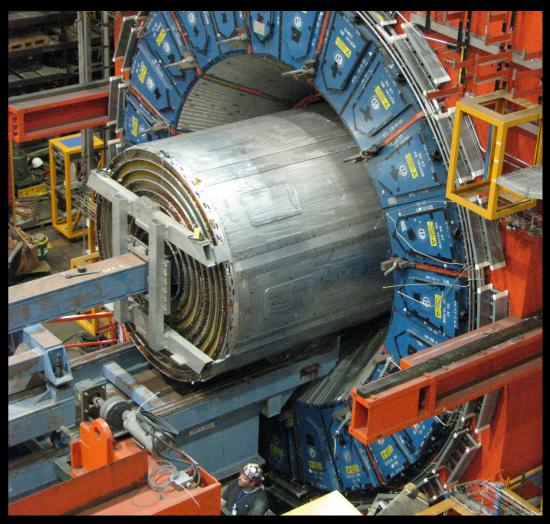
CDF II detector consists of

silicon vertex detector

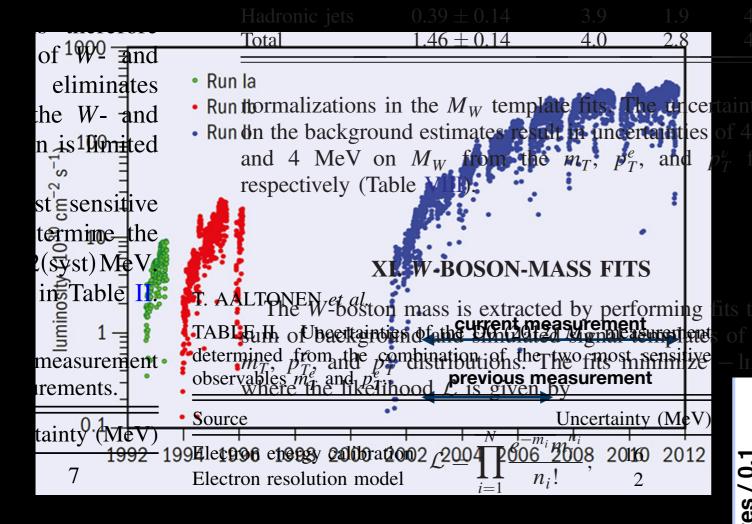
large drift chamber

coarse calorimeter towers

outer muon chambers

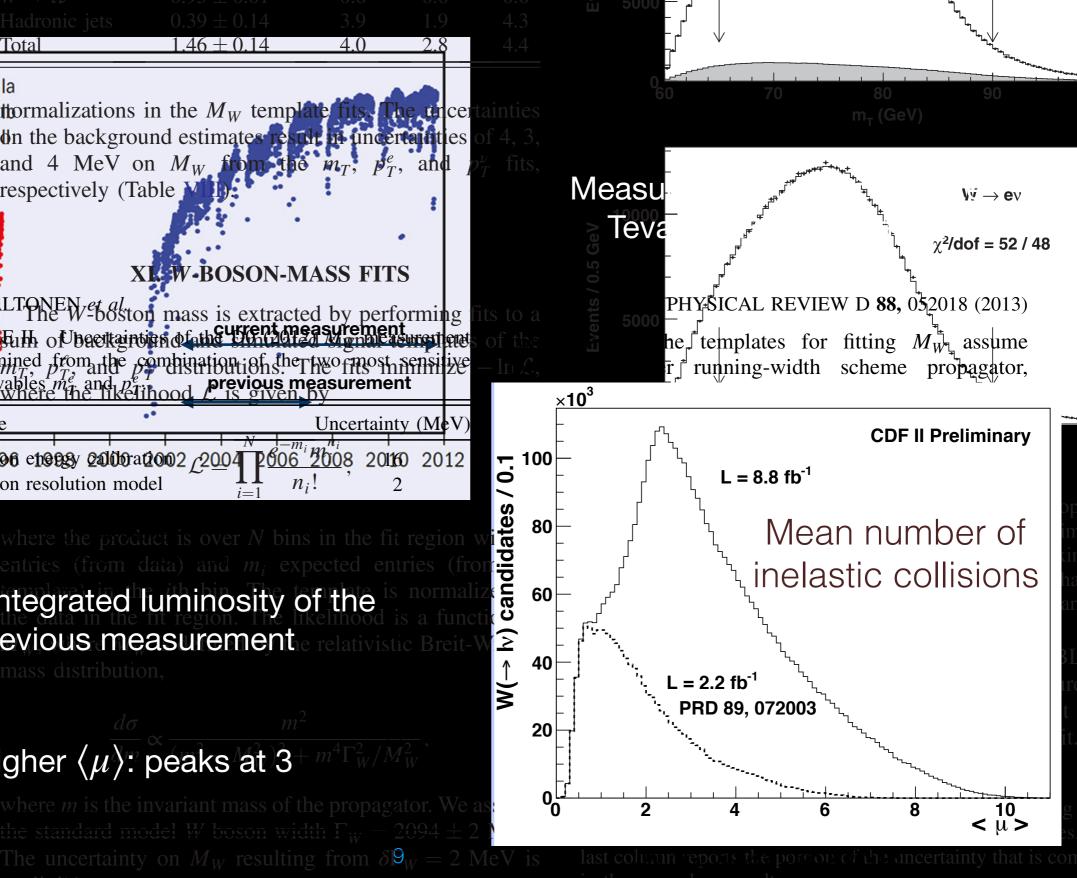


# CDF II measurement of the W



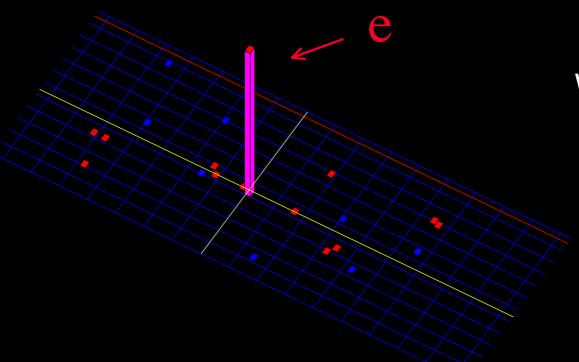
4x the integrated luminosity of the previous measurement relativistic Breit-

Higher  $\langle \mu \rangle$ : peaks at 3



 $\chi^2$ /dof = 58 / 48

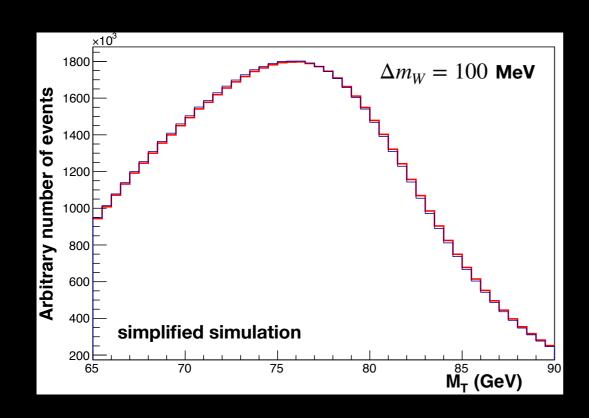
### **CDF II measurement of the W boson mass**

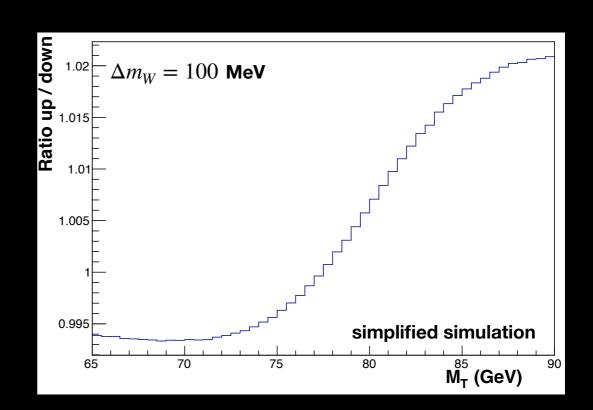


W bosons identified in their decays to  $e\nu$  and  $\mu\nu$ 

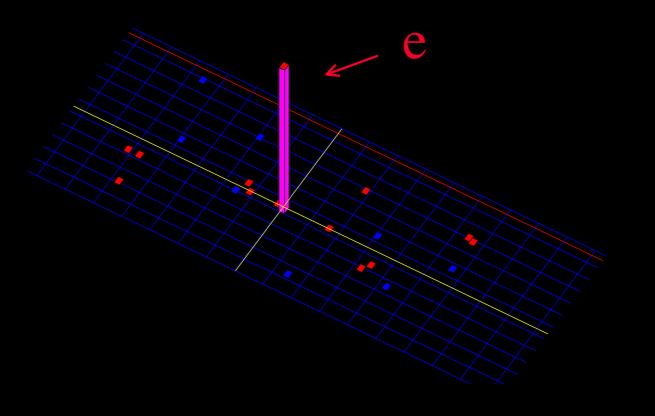
Mass measured by fitting template distributions of transverse momentum and mass

$$m_T = \sqrt{2p_T^{\ l} p_T (1 - \cos \Delta \phi)}$$



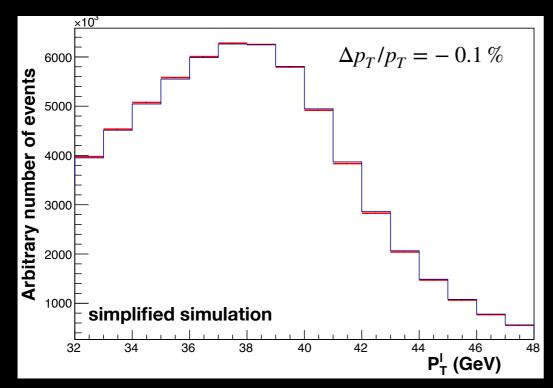


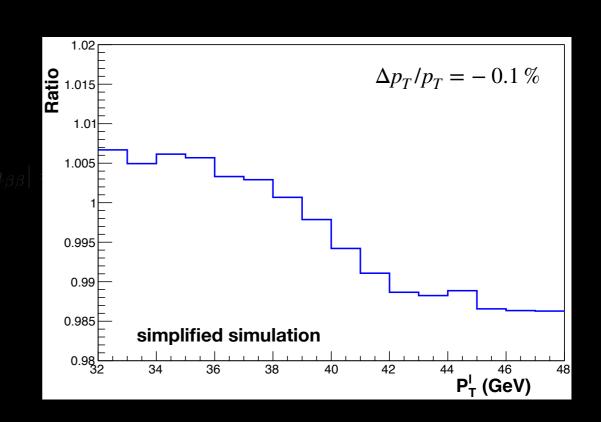
### **Calibrations**



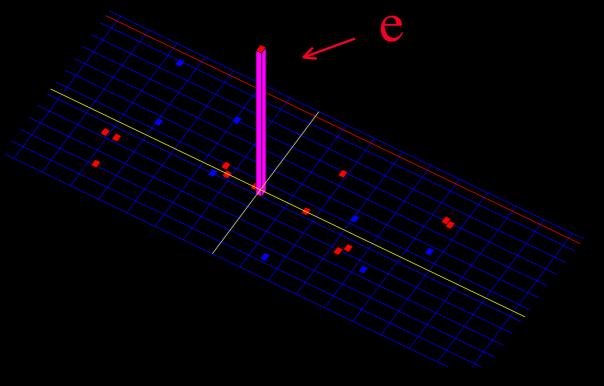
Measurement requires precise calibrations and momentum scale and resoution

Charged lepton scale





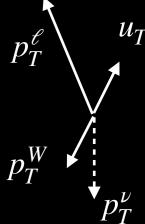
### **Calibrations**

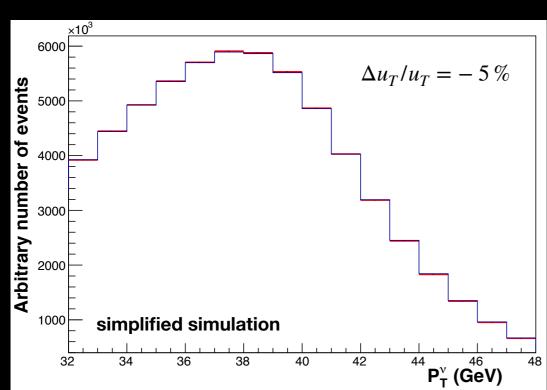


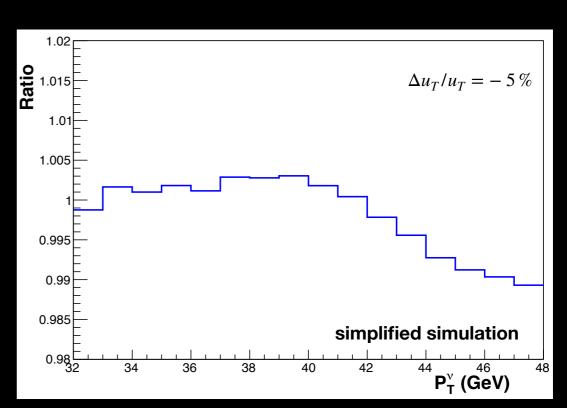
Measurement requires precise calibrations and momentum scale and resoution

$$\vec{p}_T = -(\vec{p}_T^{l} + \vec{u}_T)$$

Recoil scale







#### **Detector simulation**

#### **Developed custom simulation for analysis**

Models ionization energy loss, multiple scattering, bremsstrahlung, photon conversion, Compton scattering

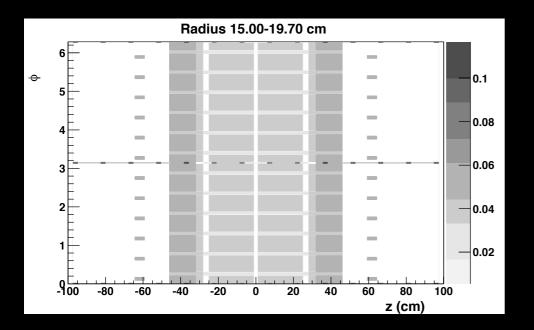
Acceptance map for muon detectors

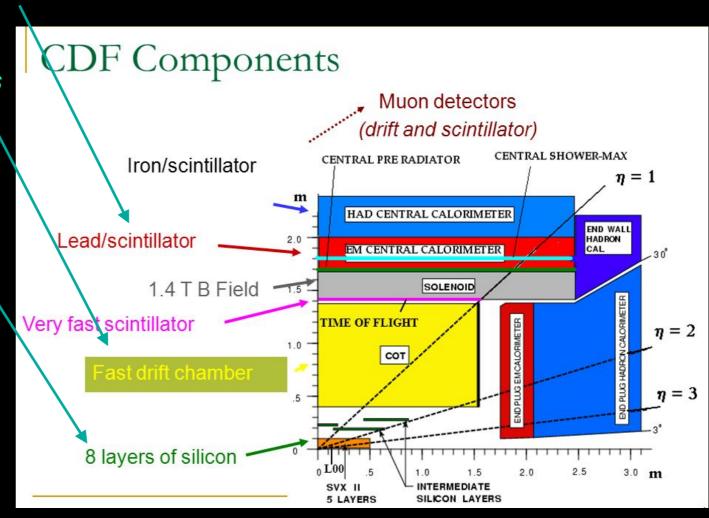
Parameterized GEANT4 model of electromagnetic calorimeter showers Includes shower losses due to finite calorimeter thickness

Kotwal & CH, NIMA 729, 25 (2013)

Hit-level model of central outer tracker Layer-by-layer resolution functions and efficiencies

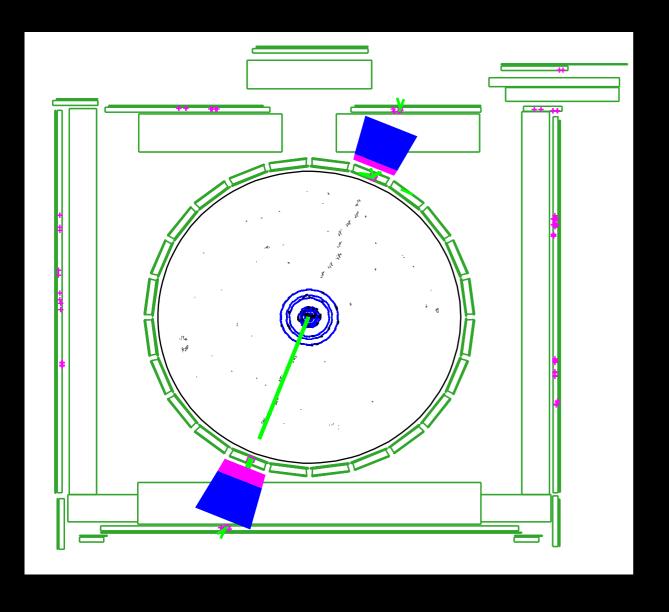
Material map of inner silicon detector Includes radiation lengths and Bethe-Bloch terms

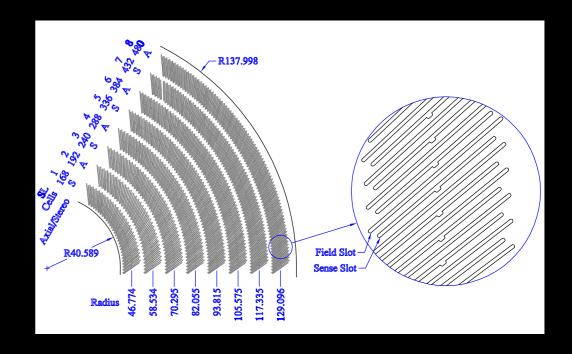


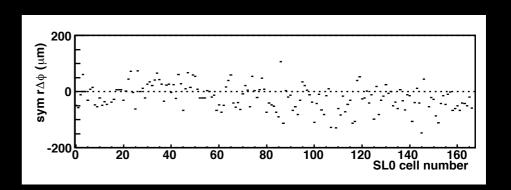


First step is to align the drift chamber (the "central outer tracker" or COT)

Two degrees of freedom (shift & rotation) for each of 2520 cells made up of twelve sense wires constrained using hit residuals from cosmic-ray tracks



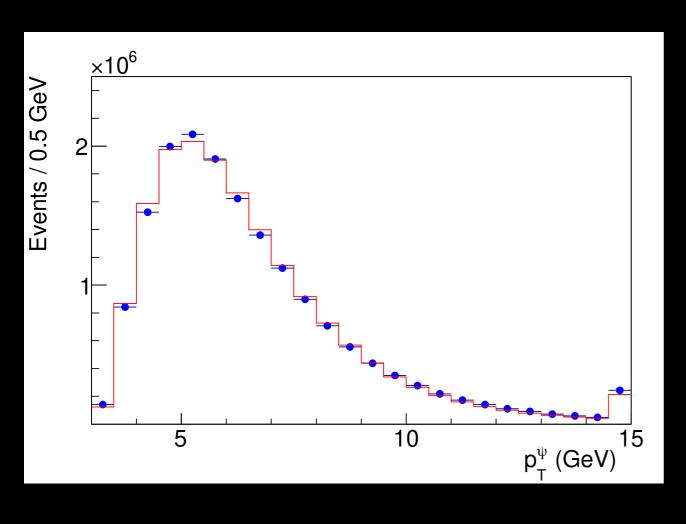


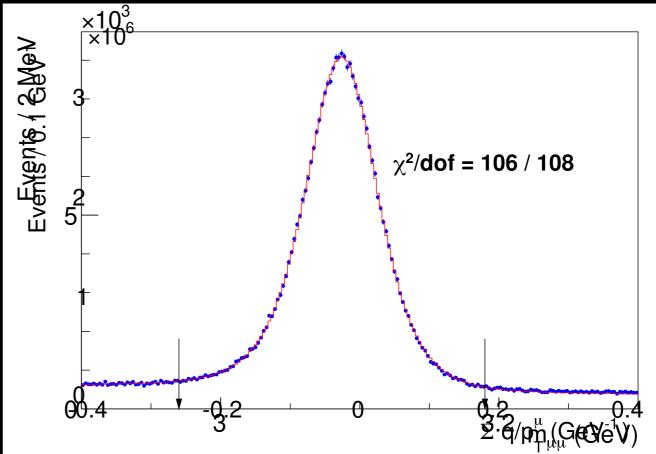


Second step is to calibrate the momentum scale using  $J/\psi$  decays to muons

#### **Simulation:**

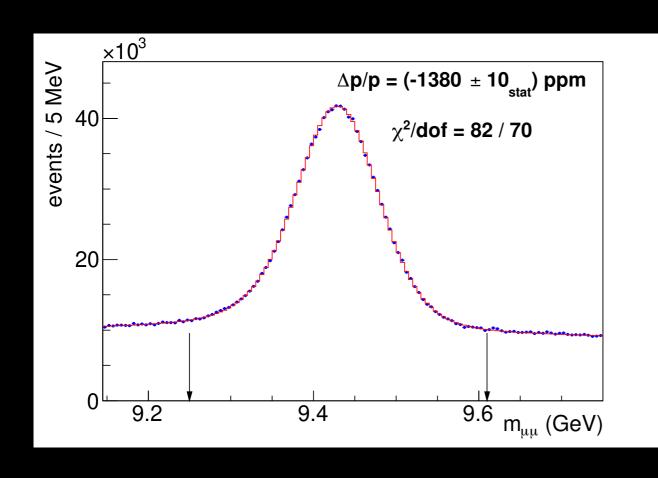
Adjust kinematics to match the data Model resonance shape using hit-level simulation and NLO form factor for QED radiation

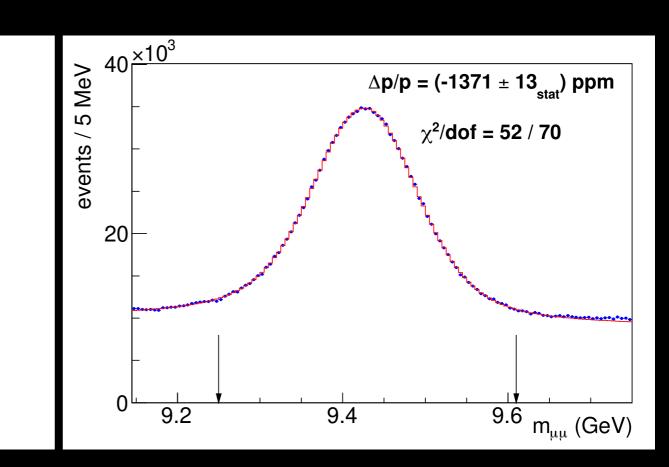




Third step is to calibrate the scale using  $\Upsilon$  decays to muons

Compare fit results with and without constraining the track to the collision point





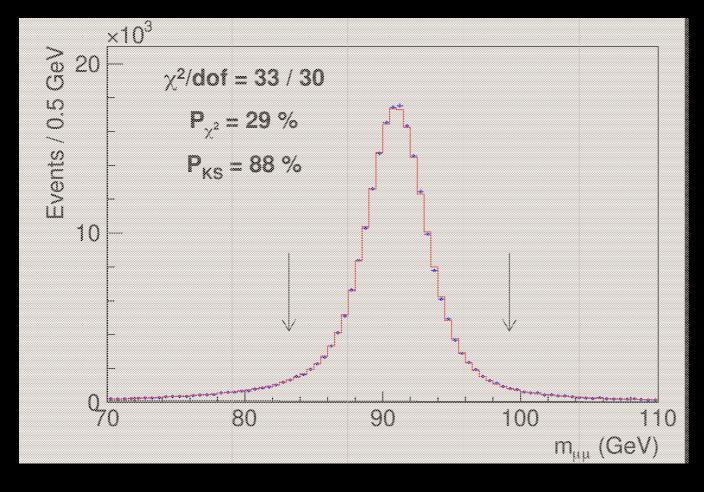
with constraint

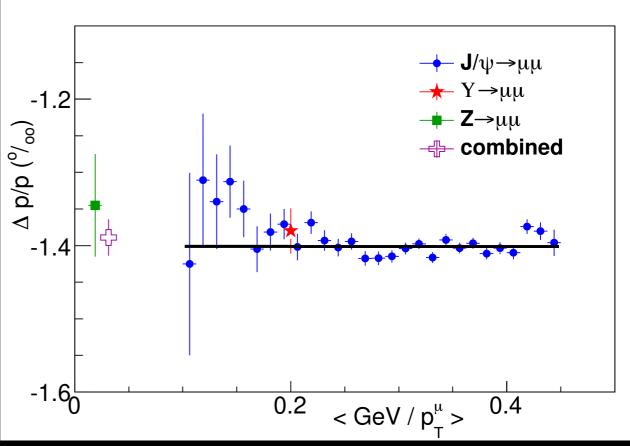
without constraint

Final step is to measure the Z boson mass

$$M_Z = 91\ 192.0 \pm 6.4_{stat} \pm 4.0_{sys} \, \mathrm{MeV}$$

Result blinded with [-50,50] MeV offset until previous steps were complete Combine all measurements into a final charged-track momentum scale



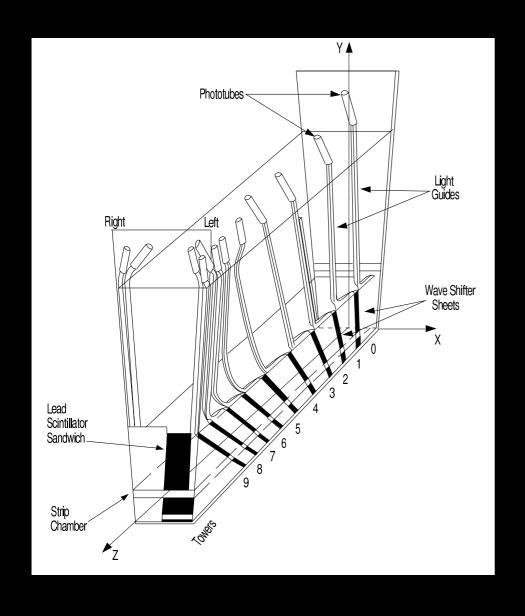


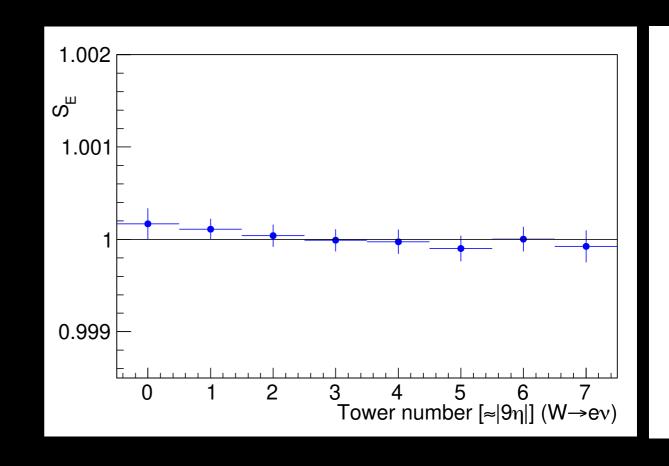
#### Electron momentum calibration

First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

#### **Data corrections:**

Use mean E/p to remove time dependence & response variations in tower Fit ratio of calorimeter energy to track momentum to correct each tower in  $\eta$ 





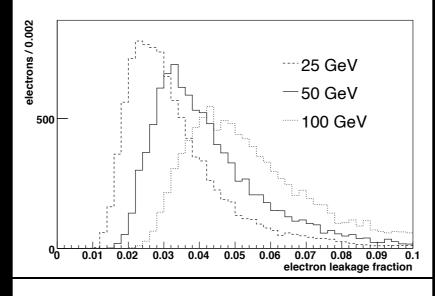
Events / 0.007

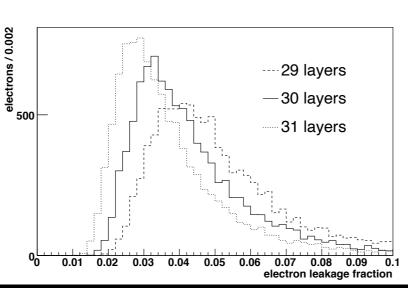
#### Electron momentum calibration

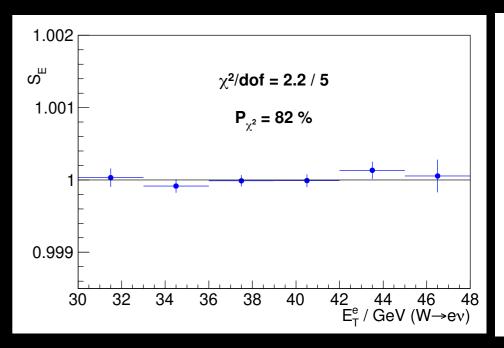
First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Parameterize calorimeter shower deposition and leakage based on GEANT4 Determine small calorimeter thickness corrections using region of low E/p in data Fit calorimeter scale as a function of  $E_T$  to correct for any remaining energy dependence

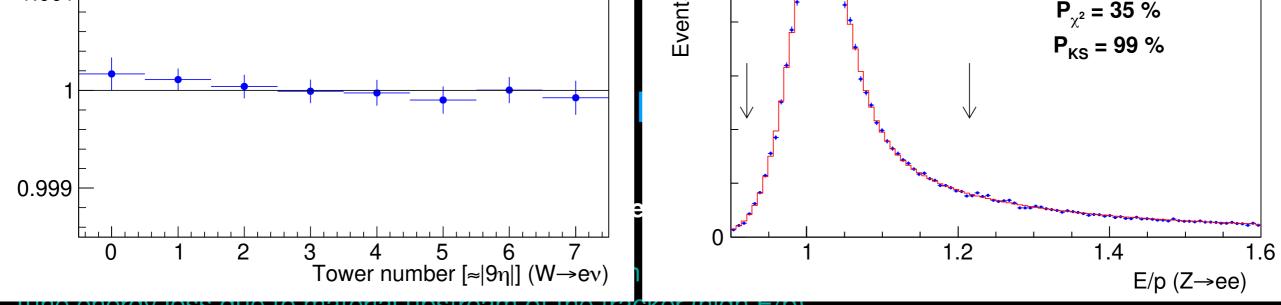
Tower	Thickness $(x_0)$	Number of lead sheets
0	17.9	30
1	18.2	30
2	18.2	29
3	17.8	27
4	18.0	26
5	17.7	24
6	18.1	23
7	17.7	21
8	18.0	20





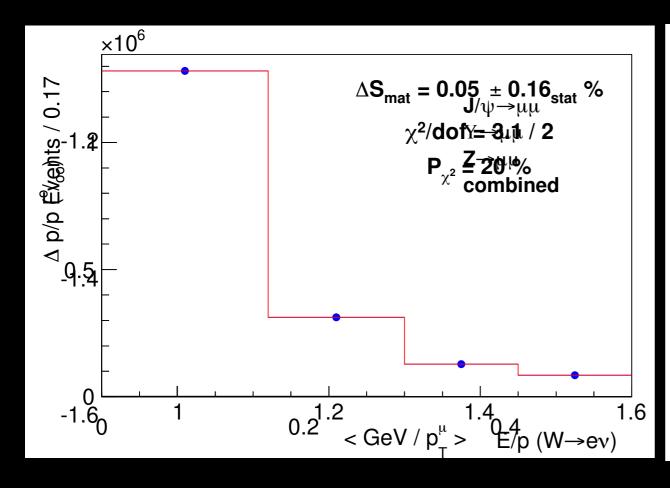


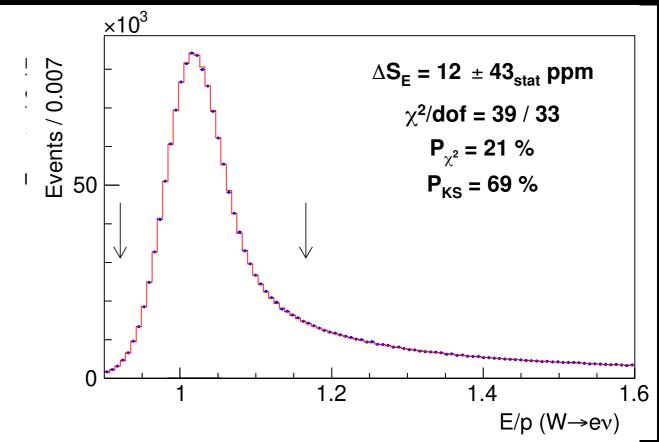
Kotwal & CH, NIMA 729, 25 (2013)



Tune energy loss due to material upstream of the tracker (high E/p)

Sampling resolution given by 
$$\sigma_E/E = \sqrt{\frac{12.6 \,\%}{E_T}} + \kappa^2$$
 with  $\kappa = 0.7 - 1.1 \,\%$  increasing with tower  $\eta$ 





#### Electron momentum calibration

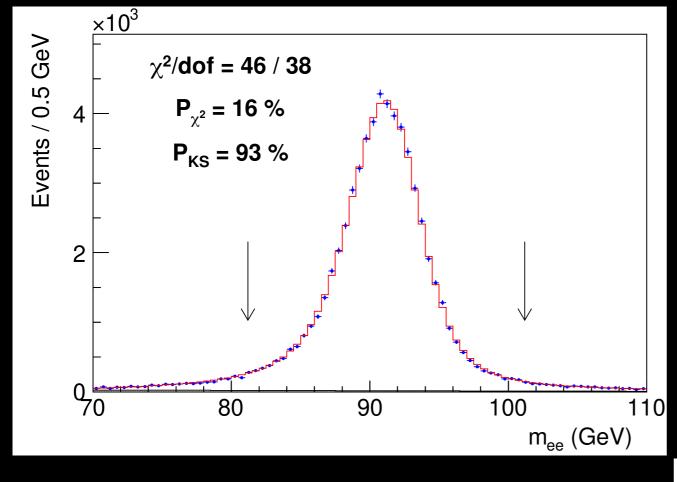
Second step is the measurement of the Z boson mass

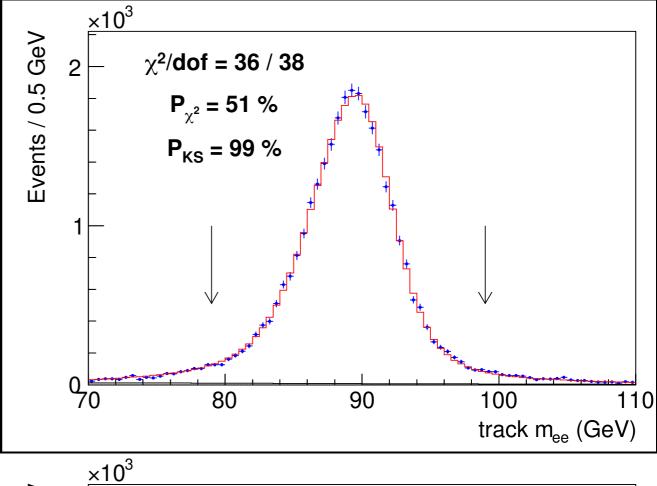
$$M_Z = 91\ 194.3 \pm 13.8_{stat} \pm 7.6_{sys} \text{ MeV}$$

As a consistency check measure mass using only track information

e.g.  $M_Z = 91\ 215.2 \pm 22.4$  MeV for non-radiative electrons (E/p<1.1)

Same blinding as for muon channel



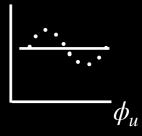


 $\sqrt{2}$ /dof - 62 / 58

### Recoil momentum calibration

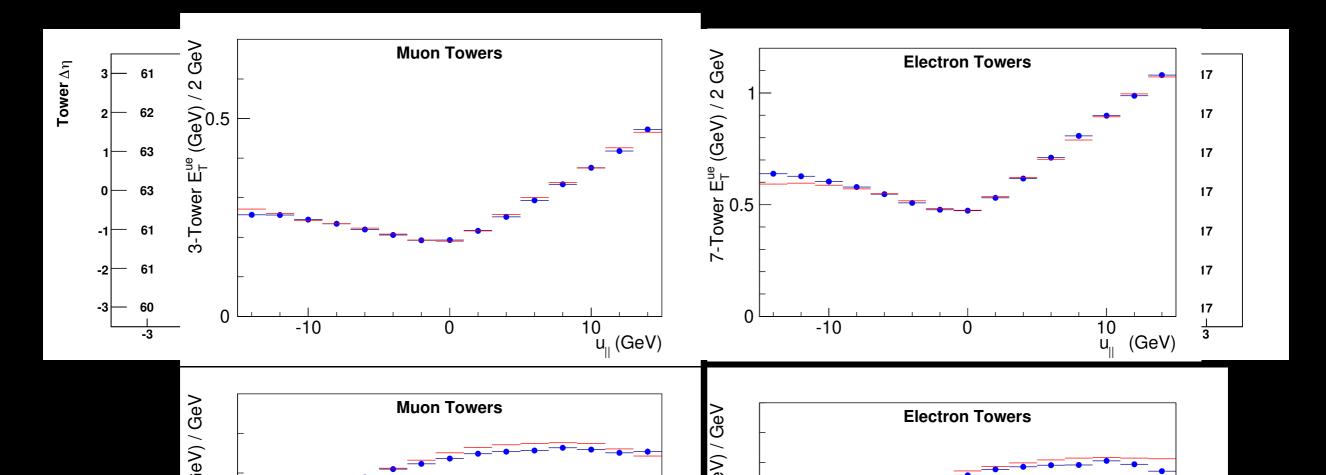
#### First step is the alignment of the calorimeters

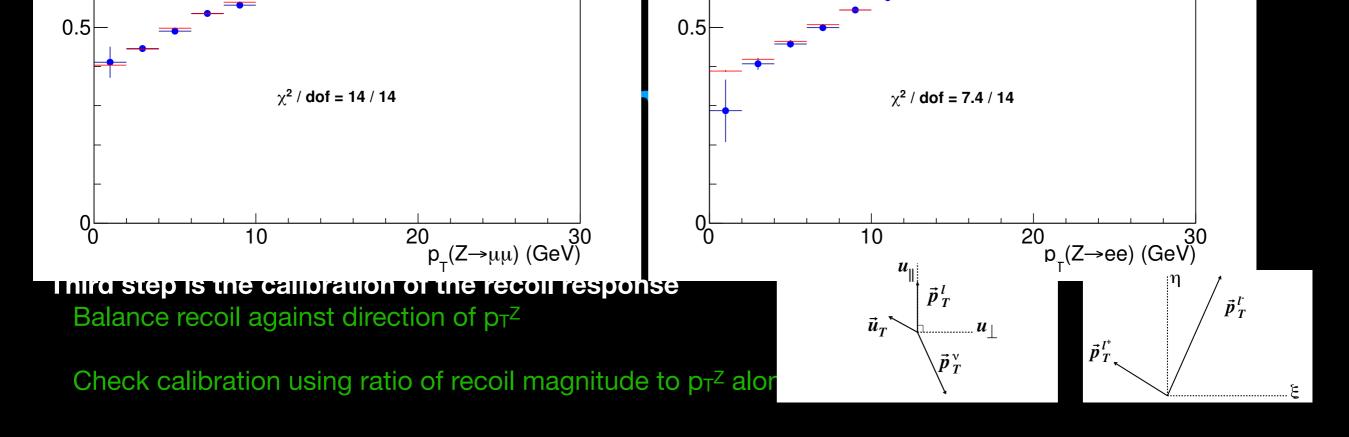
Misalignments relative to the beam axis cause a modulation in the recoil direction Alignment performed separately for each run period using minimum-bias data

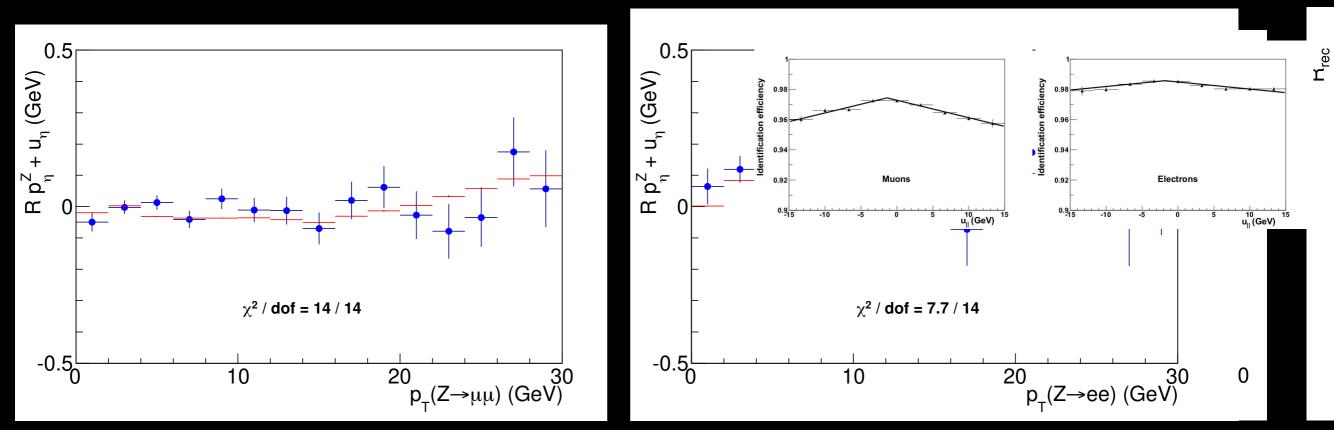


#### Second step is the reconstruction of the recoil

Remove towers traversed by identified leptons
Remove corresponding recoil energy in simulation using towers rotated by 90° validate using towers rotated by 180°



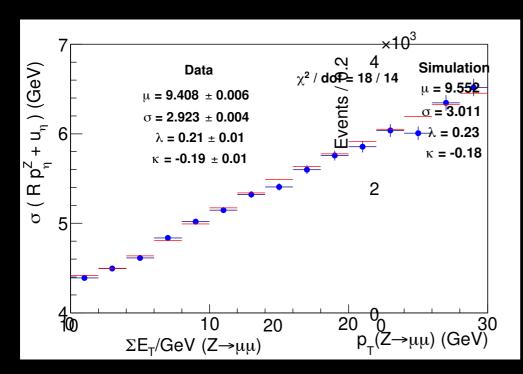


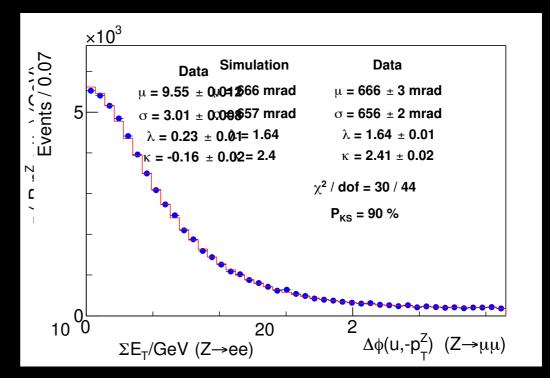


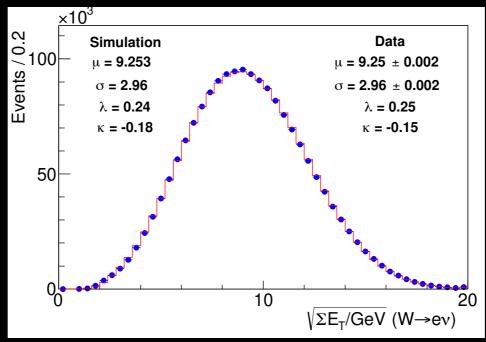
### Recoil momentum calibration

#### Fourth step is the calibration of the recoil resolution

Includes jet-like energy and angular resolution, additional dijet fraction term, and pileup





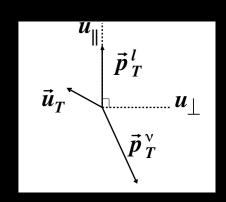


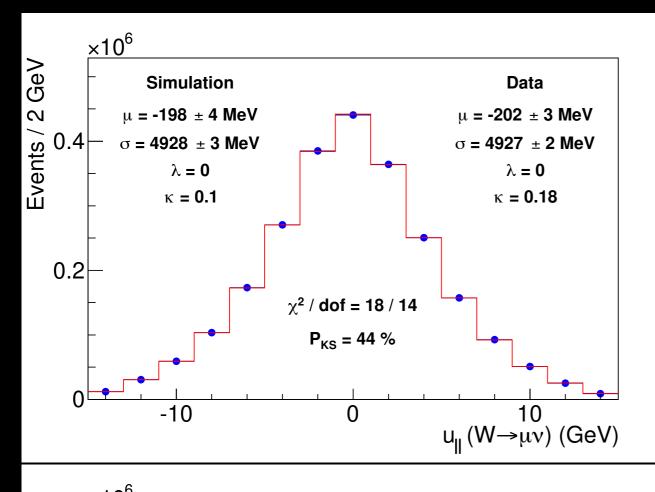
### **Recoil momentum validation**

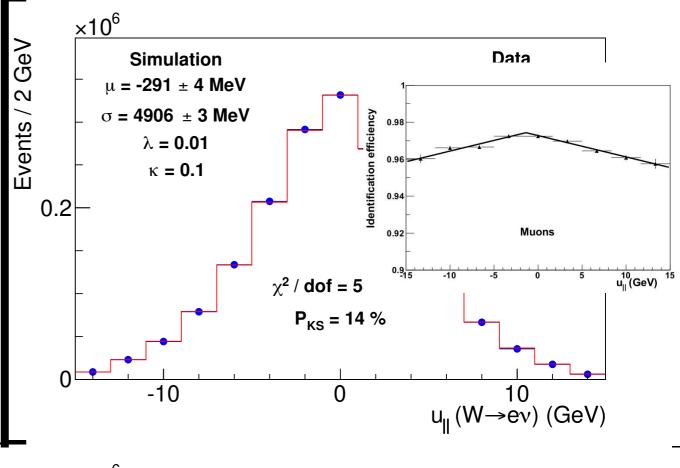
#### W boson recoil distributions validate the model

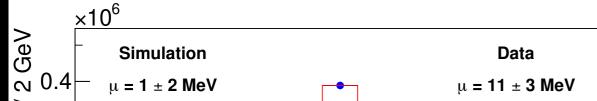
Most important is the recoil projected along the charged-lepton's momentum  $(u_{||})$ 

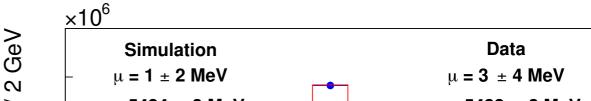
$$m_T \approx 2p_T \sqrt{1 + u_{||}/p_T} \approx 2p_T + u_{||}$$

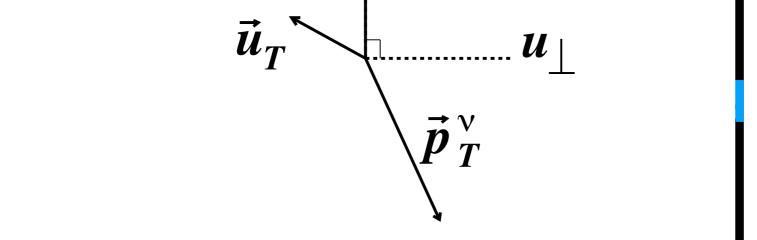


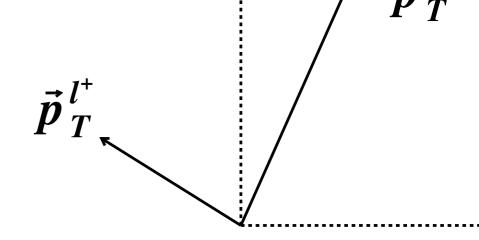








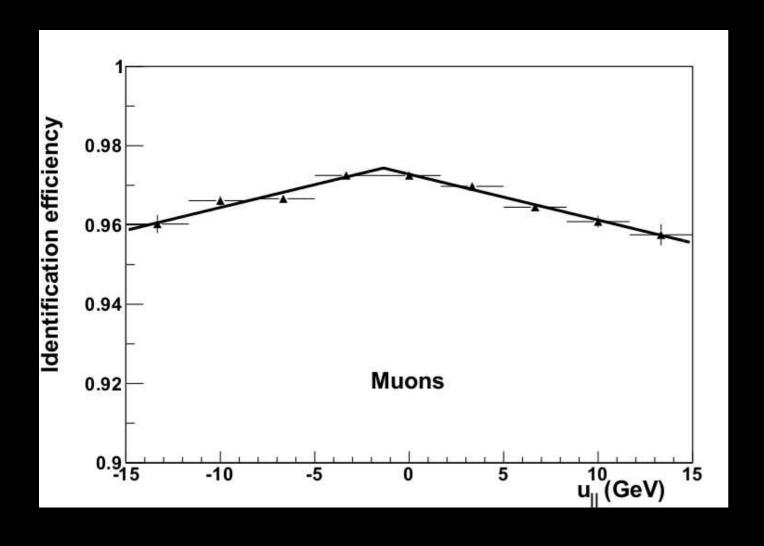


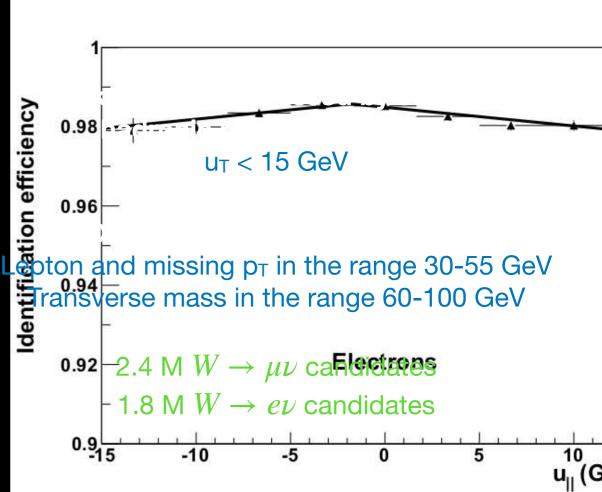


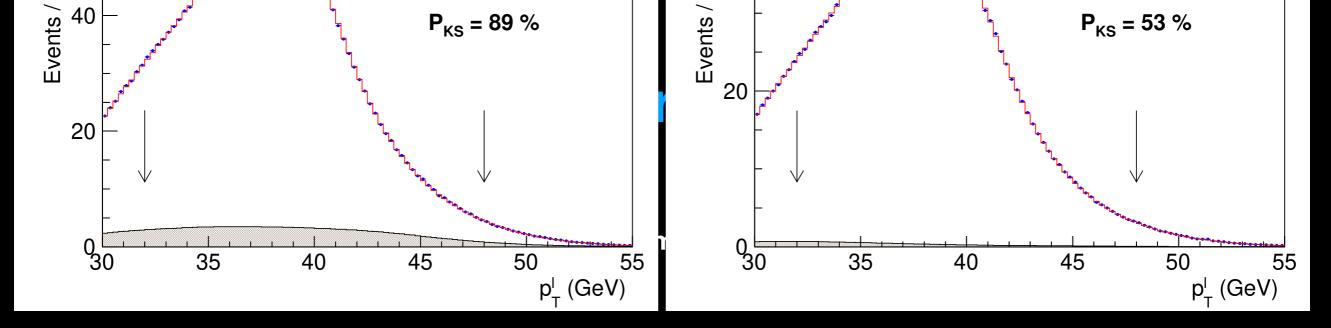
Triggers with low momentum thresholds (18 GeV) and very loose lepton id

Offline id also loose, efficiencies vary by 2% as hadronic recoil direction changes

#### No lepton isolation requirement in trigger or offline selection

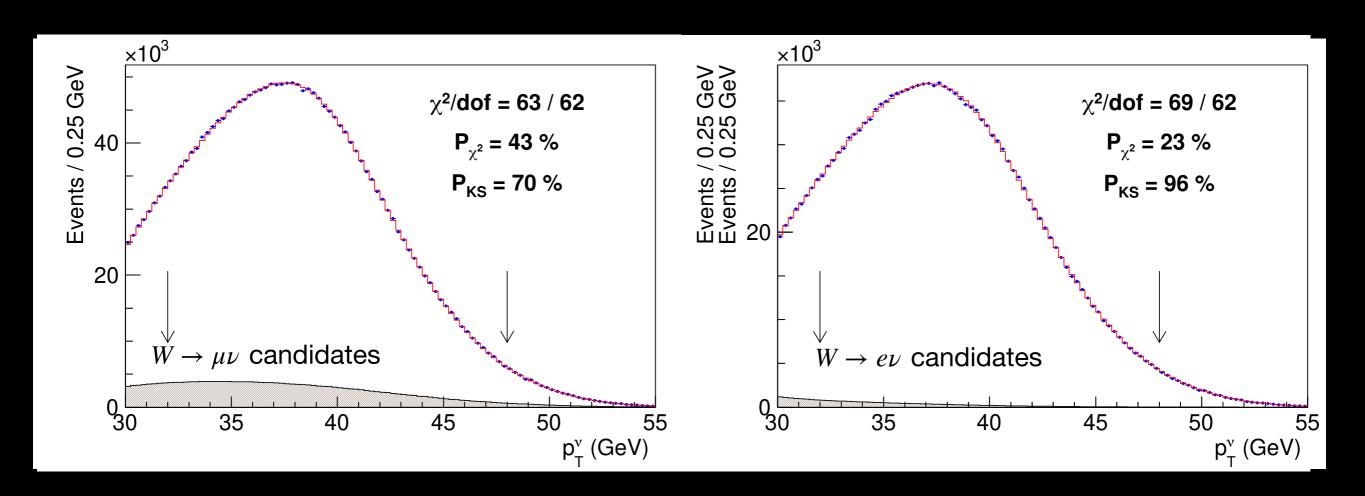






Largest background is  $Z \to \mu\mu$  with one unreconstructed muon: **7.4% of data sample**  $W \to \tau\nu$  background is ~1% in each channel: largest background in electron sample

Background from hadrons misreconstructed as leptons estimated using data: 0.2-0.3%

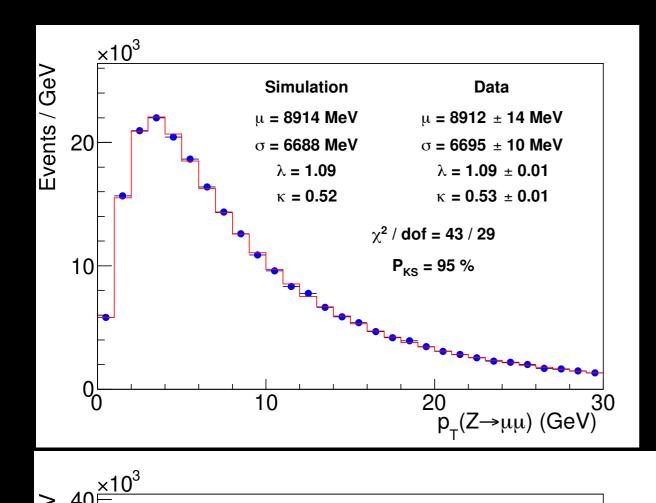


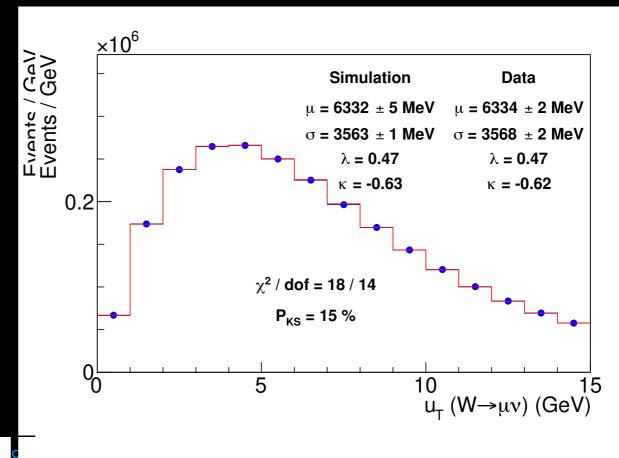
#### Boson p<sub>T</sub> impacts the p<sub>T</sub> distributions of the decay leptons

Resbos used to generate events with non-perturbative parameters and NNLL resummation to model the region of low boson  $p_T$ 

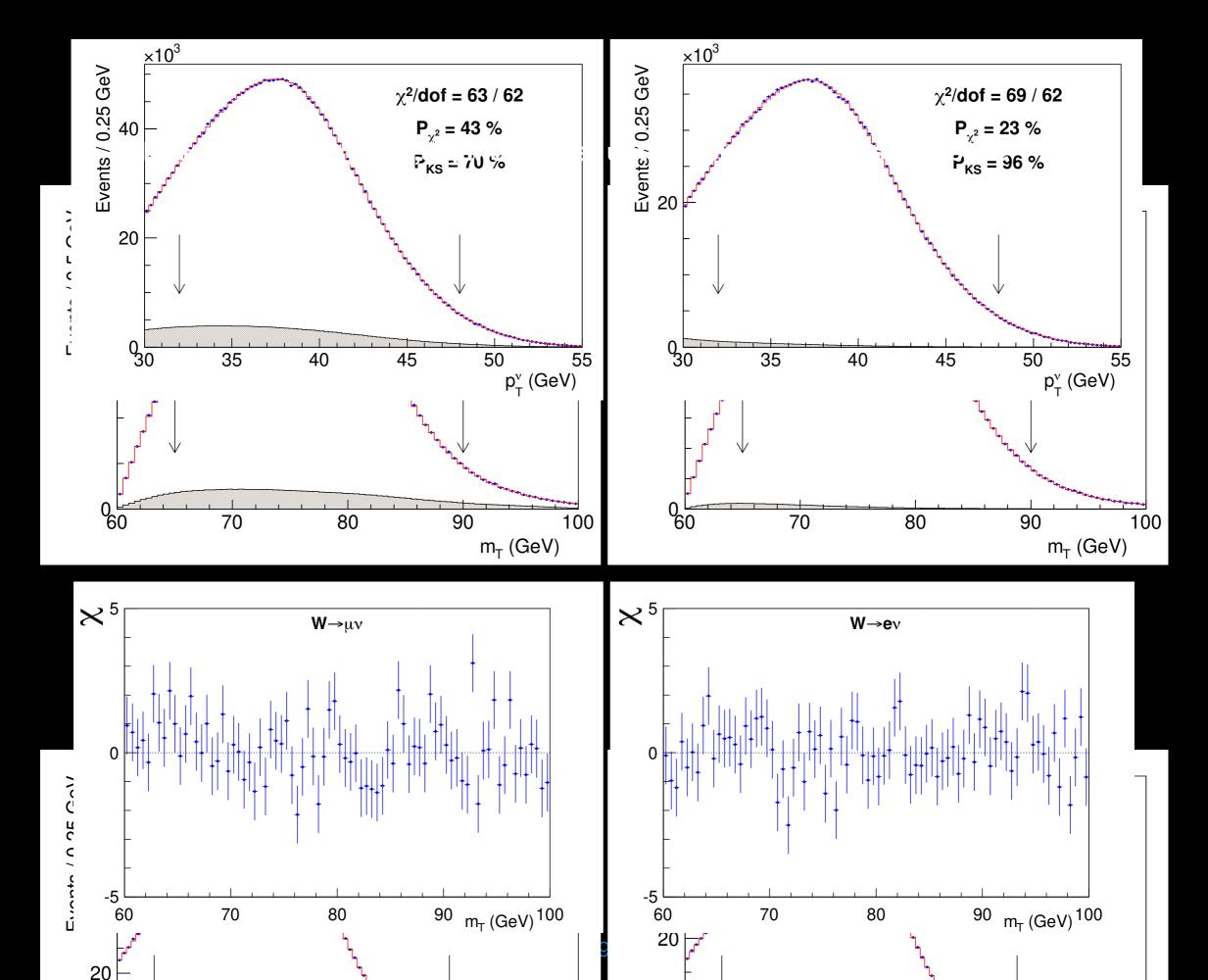
Z boson  $p_T$  used to constrain the non-perturbative parameter  $g_2$  and the perturbative coupling  $\alpha_s$ 

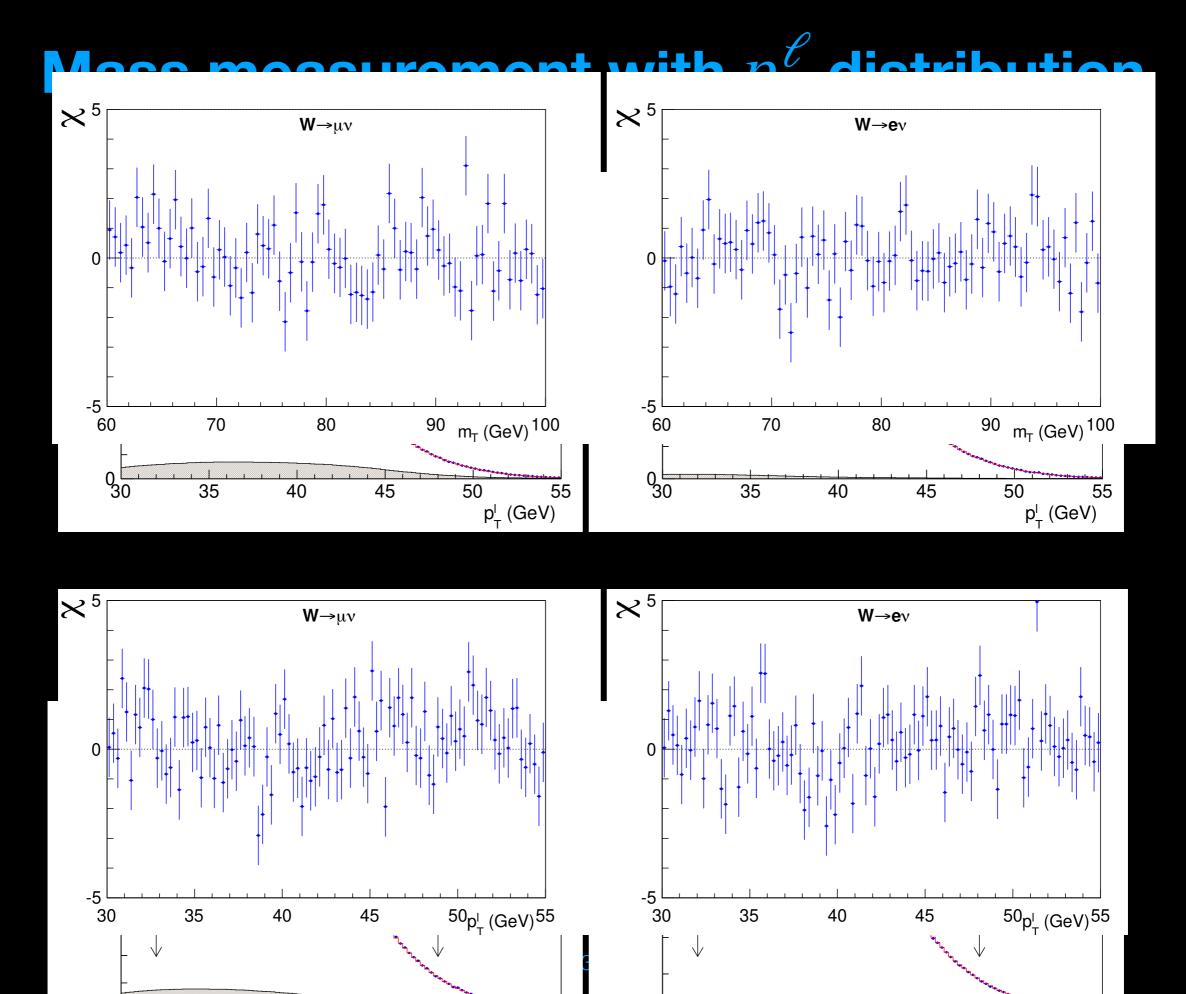
Resbos models W boson p<sub>T</sub> well uncertainty estimated using DYQT and constrained with data



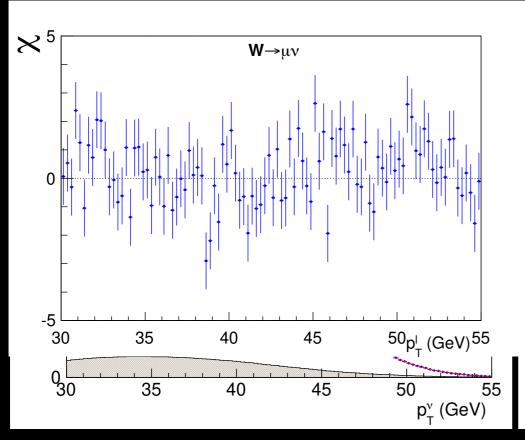


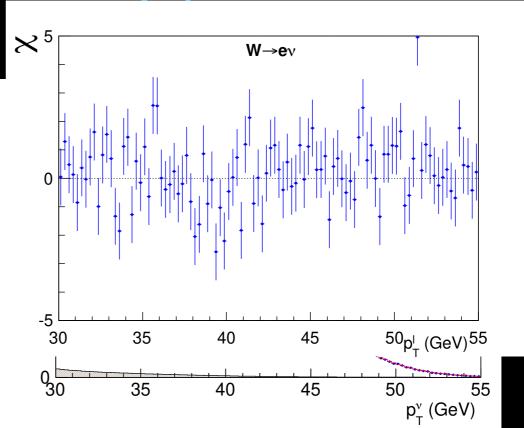
Events / GeV

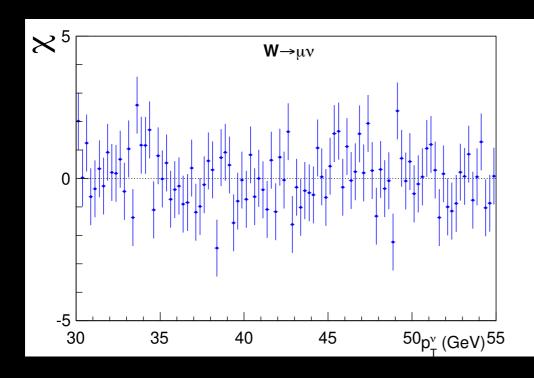


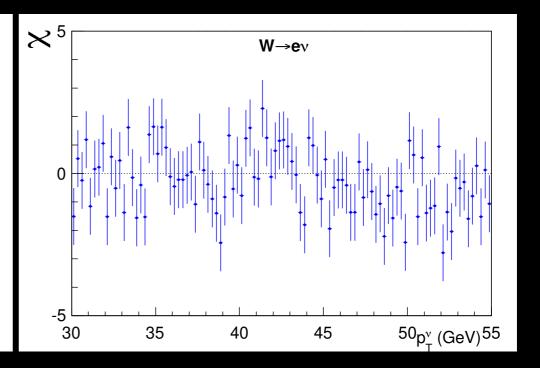


# Mass measurement with $p_T^{\nu}$ distribution









## W boson mass measurement

Combination	$m_T$ :	fit	$p_T^\ell$ f	it	$p_T^ u$ fi	it	Value (MeV)	$\chi^2/\mathrm{dof}$	Probability
	Electrons	Muons	Electrons	Muons	Electrons	Muons			(%)
$\overline{m_T}$	✓	<b>√</b>					$80\ 439.0 \pm 9.8$	1.2 / 1	28
$p_T^\ell$			✓	$\checkmark$			$80\ 421.2 \pm 11.9$	0.9 / 1	36
$p_T^ u$					✓	$\checkmark$	$80\ 427.7 \pm 13.8$	0.0 / 1	91
$m_T \ \& \ p_T^\ell$	✓	$\checkmark$	✓	$\checkmark$			$80\ 435.4 \pm 9.5$	4.8 / 3	19
$m_T~\&~p_T^{ u}$	✓	$\checkmark$			✓	$\checkmark$	$80\ 437.9 \pm 9.7$	2.2  / 3	53
$p_T^\ell \ \& \ p_T^ u$			✓	$\checkmark$	✓	$\checkmark$	$80\ 424.1 \pm 10.1$	1.1 / 3	78
Electrons	✓		✓		✓		$80\ 424.6 \pm 13.2$	3.3 / 2	19
Muons		$\checkmark$		$\checkmark$		$\checkmark$	$80\ 437.9 \pm 11.0$	3.6 / 2	17
All	✓	$\checkmark$	✓	$\checkmark$	<b>√</b>	$\checkmark$	$80\ 433.5 \pm 9.4$	7.4 / 5	20

Fit difference	Muon channel	Electron channel
$\overline{M_W(\ell^+)} - M_W(\ell^-)$	$-7.8\pm18.5_{\rm stat}\pm12.7_{\rm COT}$	$14.7 \pm 21.3_{\rm stat} \pm 7.7_{\rm stat}^{\rm E/p} \ (0.4 \pm 21.3_{\rm stat})$
$M_W(\phi_\ell > 0) - M_W(\phi_\ell < 0)$	$24.4 \pm 18.5_{\rm stat}$	$9.9 \pm 21.3_{\rm stat} \pm 7.5_{\rm stat}^{\rm E/p} \ (-0.8 \pm 21.3_{\rm stat})$
$M_Z(\text{run} > 271100) - M_Z(\text{run} < 271100)$	$5.2 \pm 12.2_{\rm stat}$	$63.2 \pm 29.9_{\rm stat} \pm 8.2_{\rm stat}^{\rm E/p} \ (-16.0 \pm 29.9_{\rm stat})$

### **Summary**

The W boson mass is an important parameter in particle physics

Measurement of W boson mass with <10 MeV precision achieved with complete CDF data set

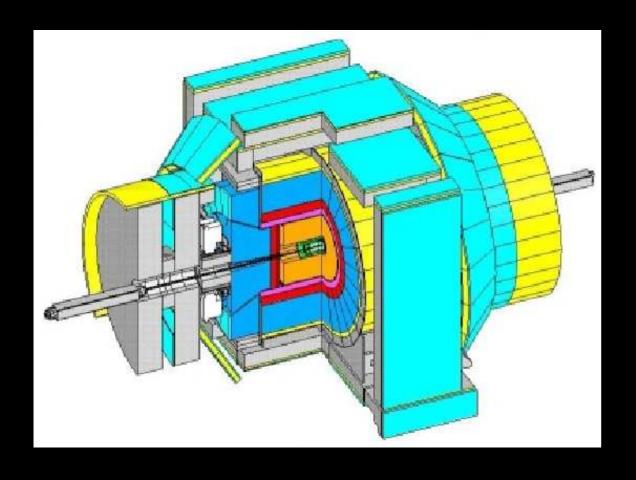
Result of >20 years of experience with the CDF II detector

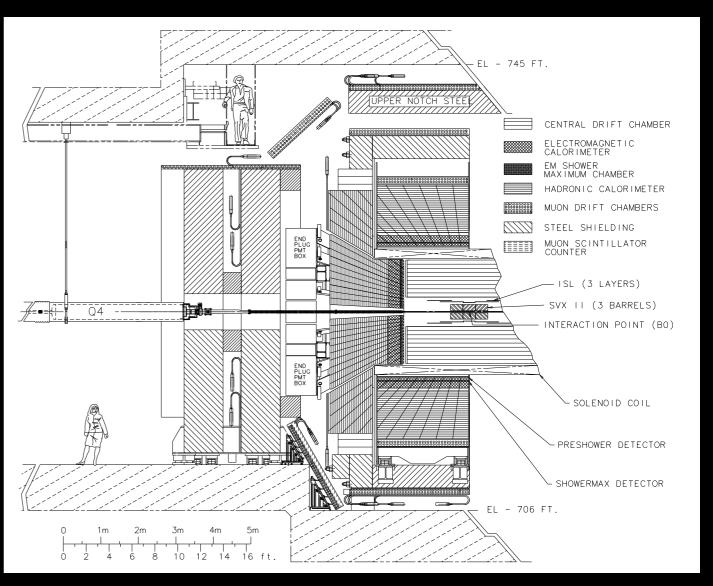
0.01% precision required flexibility: all experimental aspects controlled by the analysis team Reconstruction, alignment, calibration, simulation, analysis

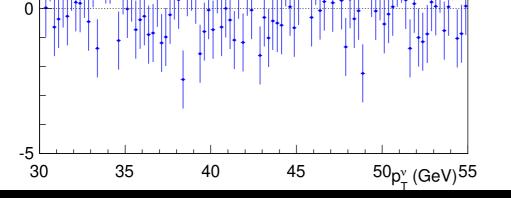
Analysis procedures approved pre-unblinding and frozen

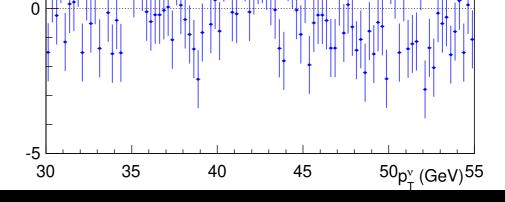
Surprising 0.1% deviation from SM motivates expanded study of mw measurements and procedures

# Backup









Source of systematic		$m_T$ fit			$p_T^\ell$ fit			$p_T^{\nu}$ fit	
uncertainty	Electrons	Muons	Common	Electrons	Muons	Common	Electrons	Muons	Common
Lepton energy scale	5.8	2.1	1.8	5.8	2.1	1.8	5.8	2.1	1.8
Lepton energy resolution	0.9	0.3	-0.3	0.9	0.3	-0.3	0.9	0.3	-0.3
Recoil energy scale	1.8	1.8	1.8	3.5	3.5	3.5	0.7	0.7	0.7
Recoil energy resolution	1.8	1.8	1.8	3.6	3.6	3.6	5.2	5.2	5.2
Lepton $u_{  }$ efficiency	0.5	0.5	0	1.3	1.0	0	2.6	2.1	0
Lepton removal	1.0	1.7	0	0	0	0	2.0	3.4	0
Backgrounds	2.6	3.9	0	6.6	6.4	0	6.4	6.8	0
$p_T^Z$ model	0.7	0.7	0.7	2.3	2.3	2.3	0.9	0.9	0.9
$p_T^W/p_T^Z$ model	0.8	0.8	0.8	2.3	2.3	2.3	0.9	0.9	0.9
Parton distributions	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9
QED radiation	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7
Statistical	10.3	9.2	0	10.7	9.6	0	14.5	13.1	0
Total	13.5	11.8	5.8	16.0	14.1	7.9	18.8	17.1	7.4

# **Background fractions**

	$\delta M_W \; ({ m MeV})$				
Source	(%)	$m_T$ fit	$p_T^\mu$ fit	$p_T^{\nu}$ fit	
$Z/\gamma^* \to \mu\mu$	$7.37 \pm 0.10$	1.6 (0.7)	3.6 (0.3)	0.1 (1.5)	
W  o  au  u	$0.880\pm0.004$	0.1(0.0)	0.1(0.0)	0.1(0.0)	
Hadronic jets	$0.01 \pm 0.04$	0.1(0.8)	-0.6 (0.8)	2.4 (0.5)	
Decays in flight	$0.20 \pm 0.14$	1.3(3.1)	1.3(5.0)	-5.2 (3.2)	
Cosmic rays	$0.01 \pm 0.01$	0.3(0.0)	0.5(0.0)	0.3(0.3)	
Total	$8.47 \pm 0.18$	2.1 (3.3)	3.9(5.1)	5.7 (3.6)	

	Fraction	$\delta M_W \; ({ m MeV})$					
Source	(%)	$m_T$ fit	$p_T^e$ fit	$p_T^{\nu}$ fit			
$Z/\gamma^* \to ee$	$0.134 \pm 0.003$	0.2 (0.3)	0.3 (0.0)	0.0(0.6)			
$W \to  au  u$	$0.94 \pm 0.01$	0.6(0.0)	0.6(0.0)	0.6(0.0)			
Hadronic jets	$0.34 \pm 0.08$	2.2(1.2)	0.9(6.5)	6.2 (-1.1)			
Total	$1.41 \pm 0.08$	2.3 (1.2)	1.1 (6.5)	6.2(1.3)			

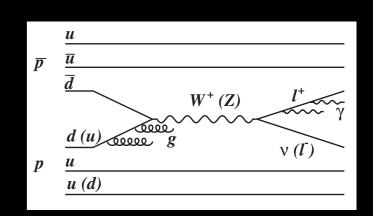
## W boson production and decay

Parton distributions impact the measurement through lepton acceptance

Restriction in  $\eta$  reduces the fraction of low-p<sub>T</sub> leptons

#### Small correction applied to update to NNPDF3.1 NNLO PDF

The set with the most W charge asymmetry measurements at the time



#### Uncertainty determined using a principal component analysis on the replica set

Measurement sensitive to ~15 eigenvectors

Leading 25 eigenvectors used to estimate uncertainty (3.9 MeV)

Three general NNLO PDF sets (NNPDF3.1, CT18, and MMHT14) have a range of  $\pm 2.1$  MeV from mean

#### Photos resummation with ME corrections used to model final-state photon radiation

validated by studying the average radiation in EM towers around the charged lepton, and with the Z mass measurement

## **Initial state LO & NLO**

W+ initial	Туре	Pythia LO	Madgraph LO	Madgraph NLO
u dbar	V-V	81.7%	82.0%	82.7%
dbar u	S-S	8.9%	9.0%	8.8%
u sbar	V-S	1.6%	1.9%	1.8%
sbar u	S-S	0.3%	0.3%	0.3%
c sbar	S-S	2.9%	2.9%	-
sbar c	S-S	2.9%	2.9%	-
c dbar	S-V	0.7%	0.7%	-
dbar c	S-S	0.2%	0.2%	-
u g	v-g		-	3.7%
g dbar	g-v		-	1.8%
g u	g-s		-	0.4%
dbar g	s-g		-	0.5%
g sbar	g-s		-	0.02%
sbar g	s-g		-	0.02%

## W boson mass fit results

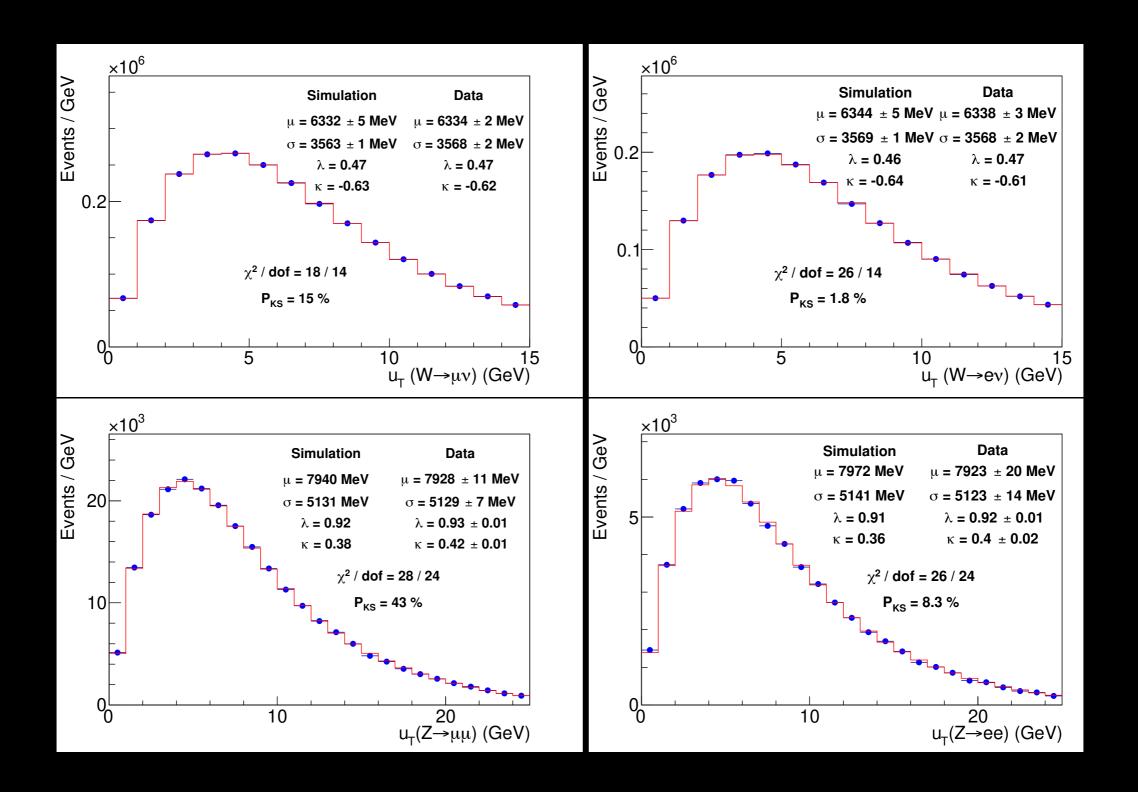
Distribution	W-boson mass (MeV)	$\chi^2/\mathrm{dof}$
$m_T(e, u)$	$80\ 429.1 \pm 10.3_{\rm stat} \pm 8.5_{\rm syst}$	39/48
$p_T^\ell(e)$	$80\ 411.4 \pm 10.7_{\rm stat} \pm 11.8_{\rm syst}$	83/62
$p_T^{ u}(e)$	$80\ 426.3 \pm 14.5_{\rm stat} \pm 11.7_{\rm syst}$	69/62
$m_T(\mu, u)$	$80\ 446.1 \pm 9.2_{\rm stat} \pm 7.3_{\rm syst}$	50/48
$p_T^\ell(\mu)$	$80\ 428.2 \pm 9.6_{\rm stat} \pm 10.3_{\rm syst}$	82/62
$p_T^{ u}(\mu)$	$80\ 428.9 \pm 13.1_{\rm stat} \pm 10.9_{\rm syst}$	63/62
combination	$80\ 433.5 \pm 6.4_{\rm stat} \pm 6.9_{\rm syst}$	7.4/5

Distribution	$M_W$ (MeV)	$\chi^2/\text{d.o.f}$
$W \to e\nu$		
$m_T$	$80408 \pm 19$	52/48
$p_T^{ ilde{\ell}}$	$80393 \pm 21$	60/62
$p_T^{\nu}$	$80431 \pm 25$	71/62
$W \to \mu\nu$		•
$m_T$	$80379 \pm 16$	57/48
$p_T^{\hat{\ell}}$	$80348 \pm 18$	58/62
$p_T^{\nu}$	$80406 \pm 22$	82/62

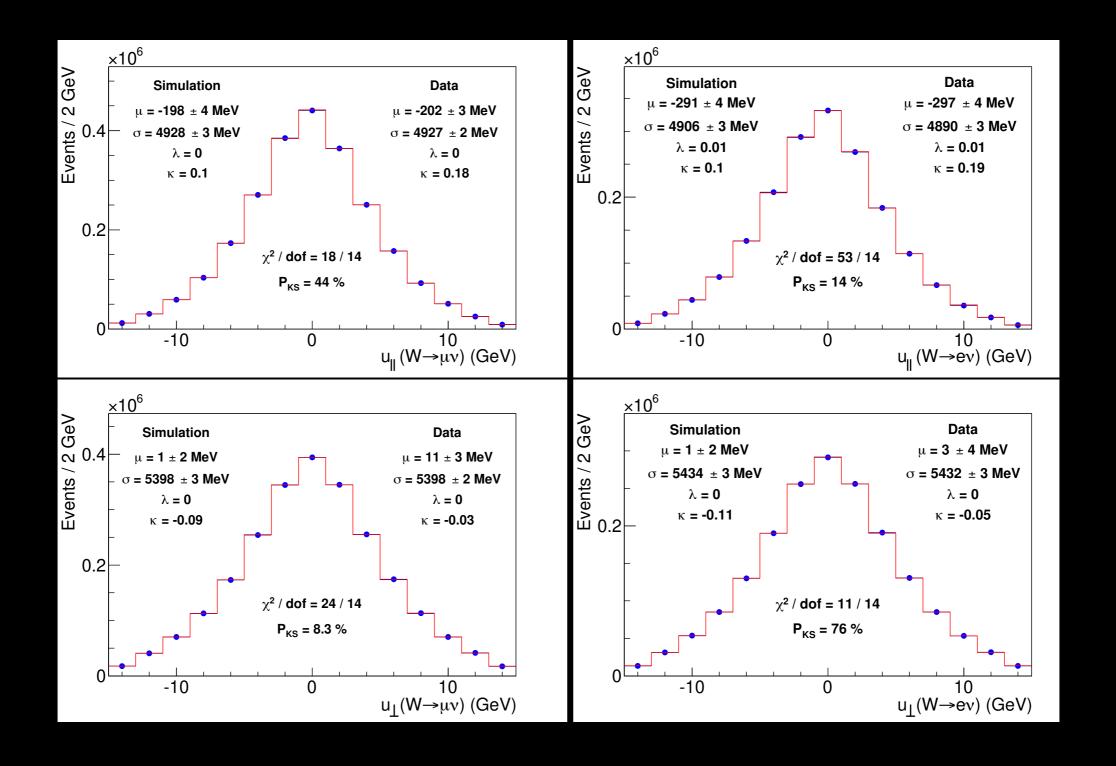
# Measurement updates

Method or technique	impact
Detailed treatment of parton distribution functions	+3.5  MeV
Resolved beam-constraining bias in CDF reconstruction	+10 MeV
Improved COT alignment and drift model [65]	uniformity
Improved modeling of calorimeter tower resolution	uniformity
Temporal uniformity calibration of CEM towers	uniformity
Lepton removal procedure corrected for luminosity	uniformity
Higher-order calculation of QED radiation in $J/\psi$ and $\Upsilon$ decays	accuracy
Modeling kurtosis of hadronic recoil energy resolution	accuracy
Improved modeling of hadronic recoil angular resolution	accuracy
Modeling dijet contribution to recoil resolution	accuracy
Explicit luminosity matching of pileup	accuracy
Modeling kurtosis of pileup resolution	accuracy
Theory model of $p_T^W/p_T^Z$ spectrum ratio	accuracy
Constraint from $p_T^W$ data spectrum	robustness
Cross-check of $p_T^Z$ tuning	robustness

## Recoil in W & Z events



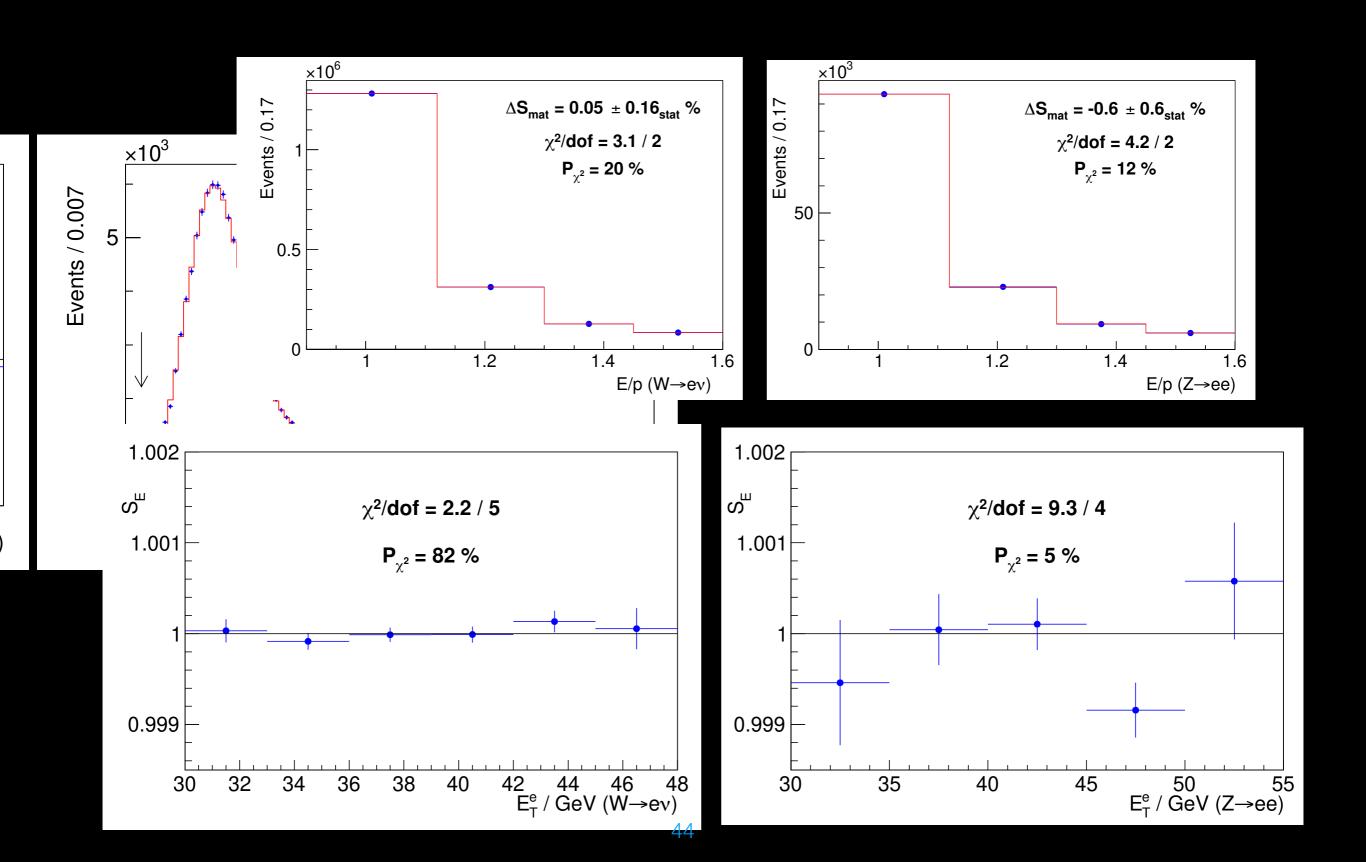
## Recoil projections in W events



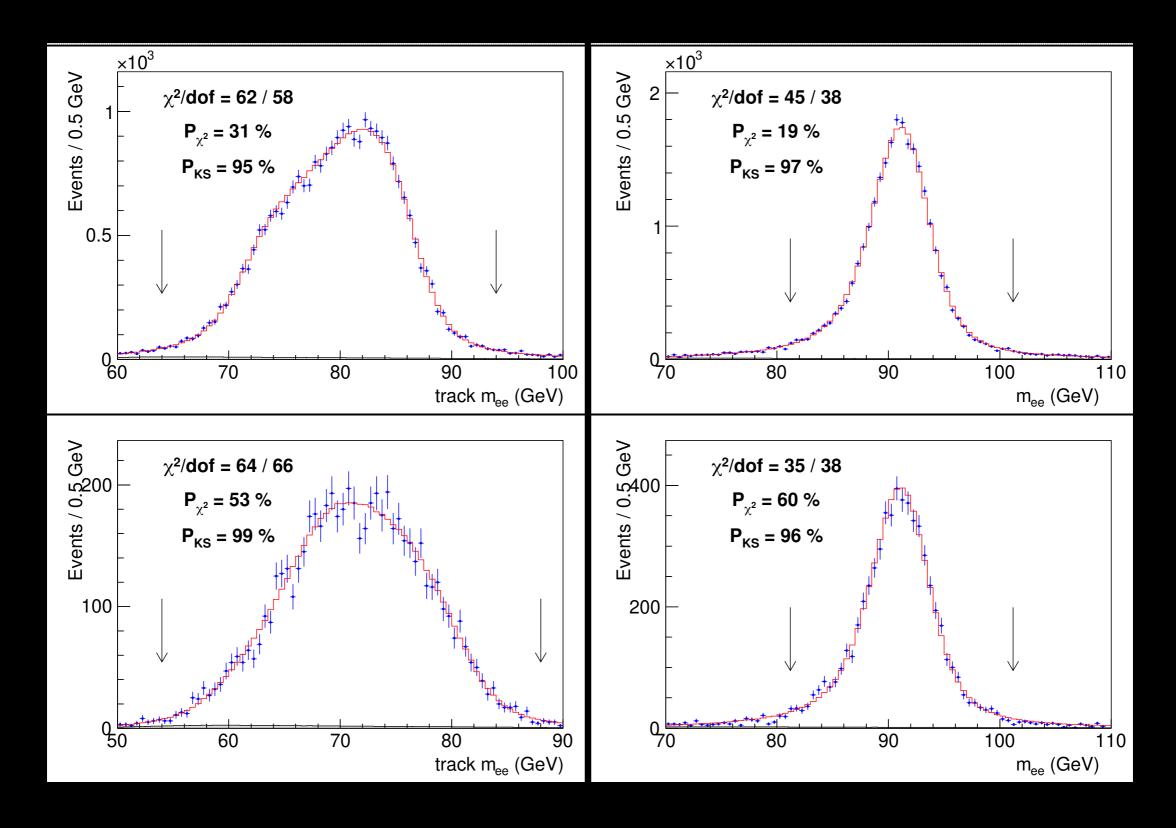
# Recoil model parameters

Parameter	Description	Source	$m_T$	$p_T^\ell$	$p_T^{ u}$
a	average response	Fig. S23	-1.6	-2.9	-0.2
b	response non-linearity	Fig. S23	-0.8	-2.0	0.7
Response			1.8	3.5	0.7
$N_V$	spectator interactions	Fig. S24	0.5	-3.2	3.6
$s_{ m had}$	sampling resolution	Fig. S24	0.3	0.3	0.8
$f_{\pi^0}^4$	EM fluctuations at low $u_T$	Fig. S25	-0.3	-0.2	-1.0
$f_{\pi^0}^{15}$	EM fluctuations at high $u_T$	Fig. S25	-0.3	-0.3	-0.2
$\alpha$	angular resolution at low $u_T$	Fig. S26	1.4	0.1	2.5
$\beta$	angular resolution at intermediate $u_T$	Fig. S26	0.2	0.1	0.7
$\gamma$	angular resolution at high $u_T$	Fig. S26	0.3	0.3	0.7
$f_2^a$	average dijet component	Fig. S27	0.1	-1.1	0.8
$f_2^s$	variation of dijet component with $u_T$	Fig. S27	-0.1	-0.2	-0.1
$k_{\xi}$	average dijet resolution	Fig. S28	-0.1	0.1	-0.3
$\delta_{\xi}$	fluctuations in dijet resolution	Fig. S28	-0.2	0.2	-1.1
$A_{\xi}$	higher-order term in dijet resolution	Fig. S28	0.1	-1.0	0.7
$\mu_{\xi}$		Fig. S28	-0.5	-0.4	-0.9
$\epsilon_{\xi}$		Fig. S28	0.1	-0.2	0.4
$S_{\xi}^{+}$		Fig. S28	0.5	-0.4	1.4
$S_{\xi}^{-}$		Fig. S28	-0.3	-0.2	-0.5
$q_{\xi}$		Fig. S28	-0.2	0.0	0.2
Resolution			1.8	3.6	5.2

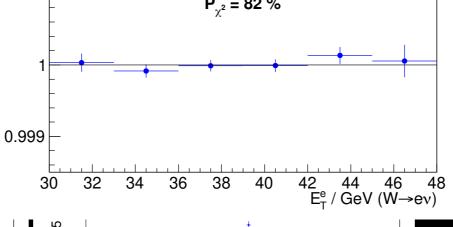
## **Electron momentum calibration**

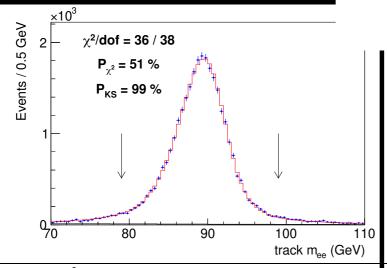


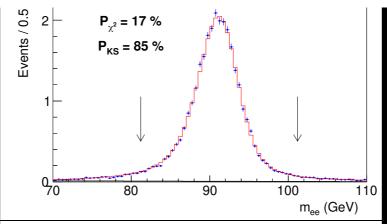
## Electron momentum calibration

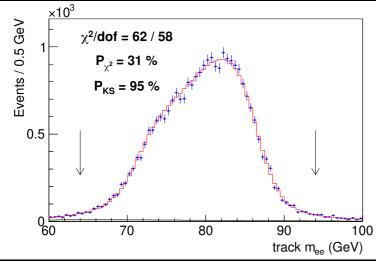


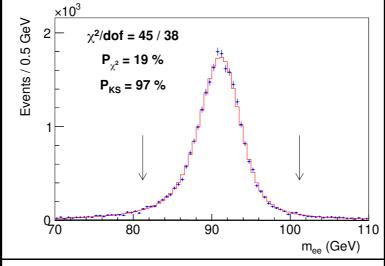
## **Z** mass fit

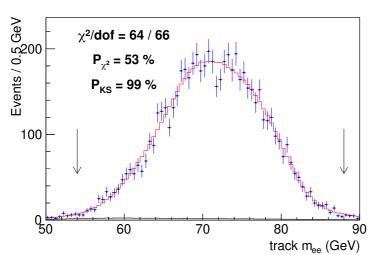


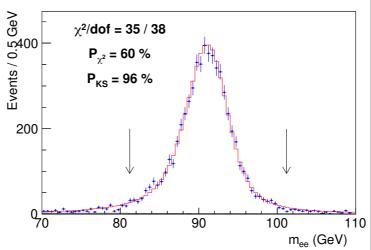


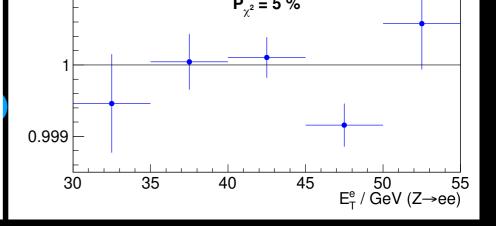












Electrons	Calorimeter	Track
E/p < 1.1 only	$91190.9\pm19.7$	$91215.2\pm22.4$
E/p > 1.1  and  E/p < 1.1	$91201.1\pm21.5$	$91259.9 \pm 39.0$
E/p > 1.1 only	$91184.5 \pm 46.4$	$91167.7\pm109.9$

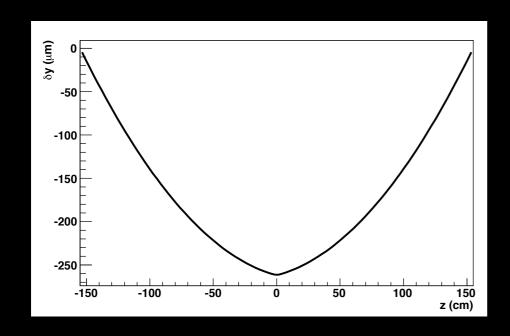
## Muon momentum calibration

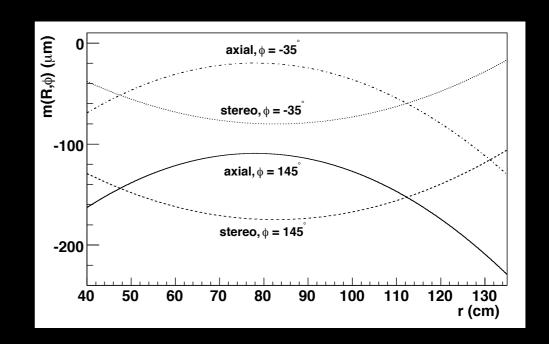
Source	$J/\psi$ (ppm)	Υ (ppm)	Correlation (%)
QED	1	1	100
Magnetic field non-uniformity	13	13	100
Ionizing material correction	11	8	100
Resolution model	10	1	100
Background model	7	6	0
COT alignment correction	4	8	0
Trigger efficiency	18	9	100
Fit range	2	1	100
$\Delta p/p$ step size	2	2	0
World-average mass value	4	27	0
Total systematic	29	34	16 ppm
Statistical NBC (BC)	2	13(10)	0
Total	29	36	16 ppm

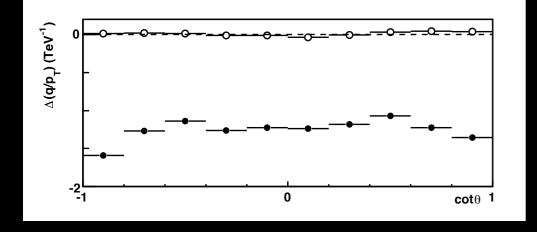
### Muon momentum calibration

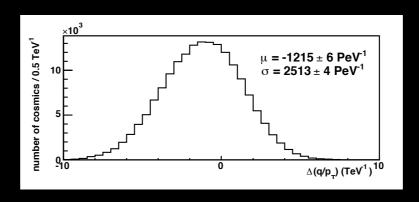
First step is to align the drift chamber (the "central outer tracker" or COT)

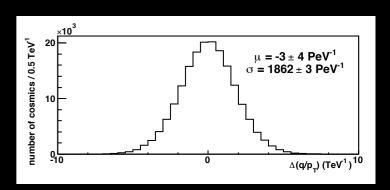
Two parameters for the electrostatic deflection of the wire within the chamber constrained using difference between fit parameters of incoming and outgoing cosmic-ray tracks











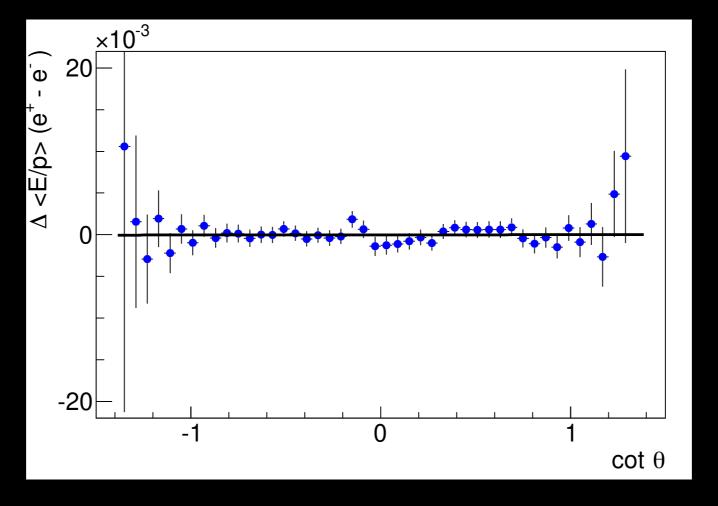
### Track momentum calibration

Residual tracker misalignments studied using difference in E/p between electrons and positrons

Correction as a function of polar angle applied to measured tracks from W and Z decays

Linear dependence on cot theta would cause a bias in the mw mass fit

No linear correction required, statistical precision from E/p constrains the bias to <0.8 MeV

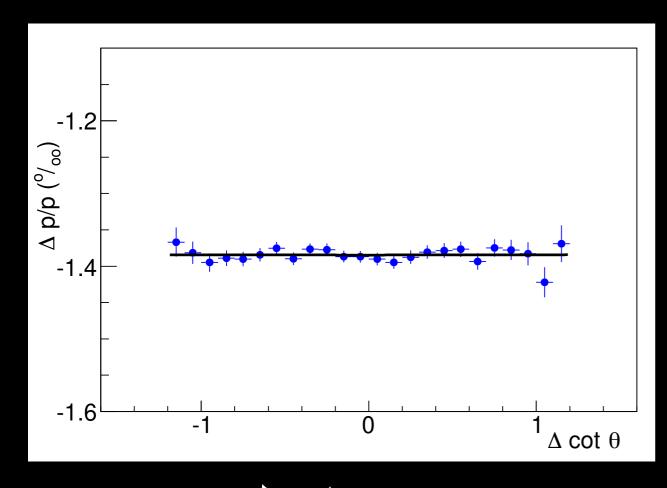


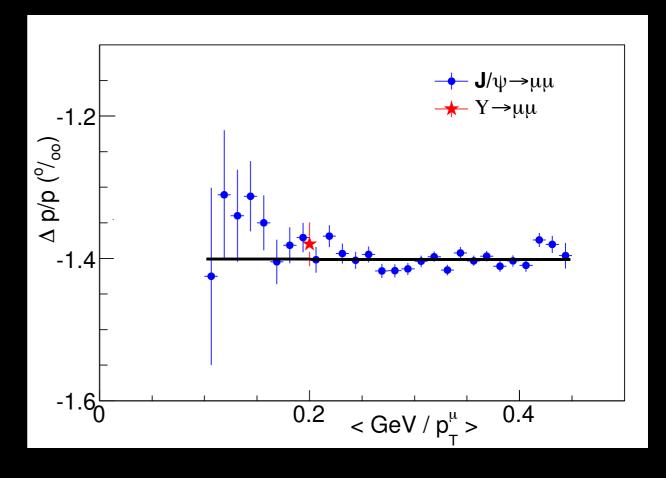
### Muon momentum calibration

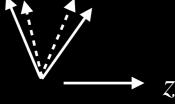
Second step is to calibrate the momentum scale using  $J/\psi$  decays to muons

#### **Simulation corrections:**

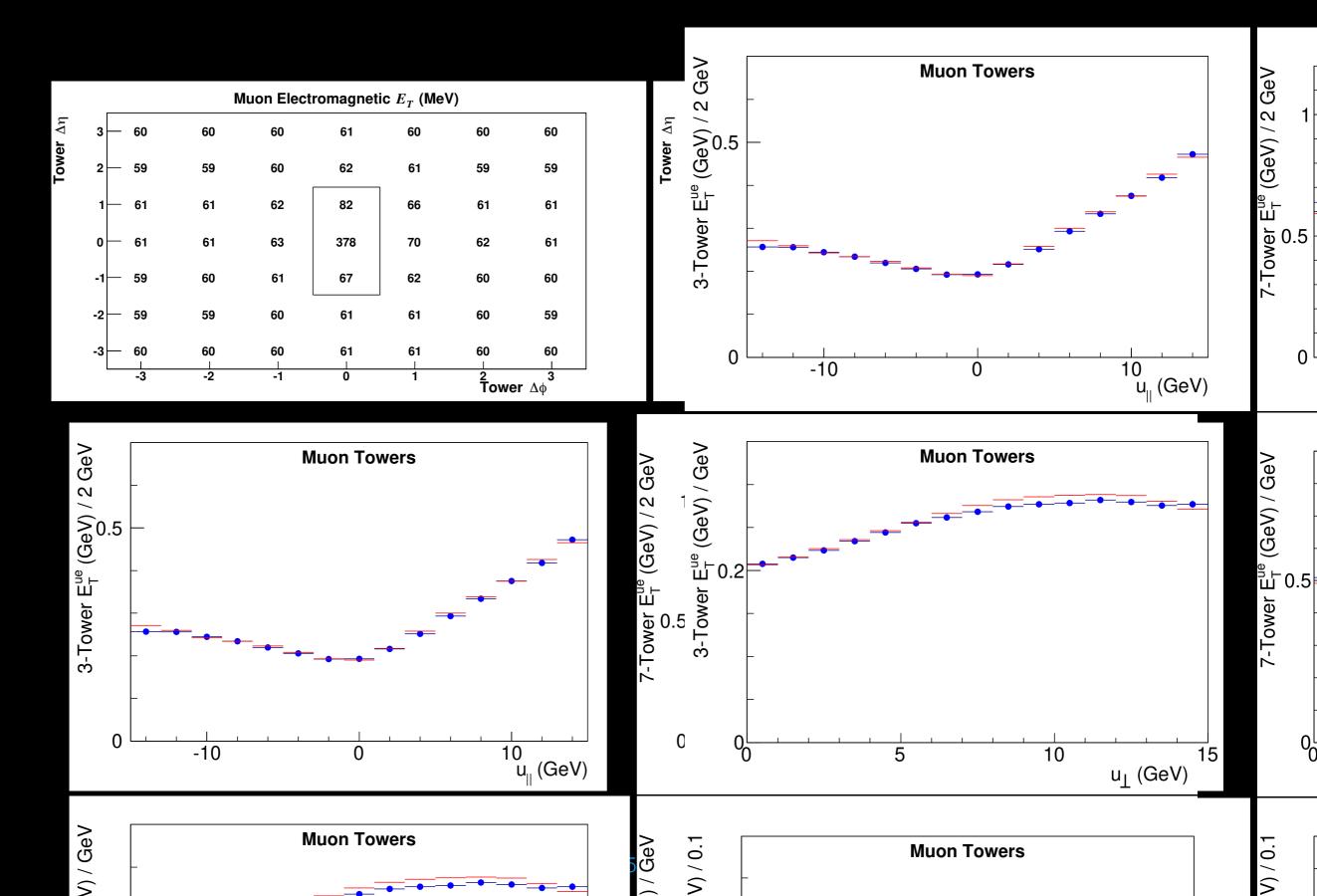
Correct the length scale of the tracker with mass measurement as a function of  $\Delta \cot \theta$  Correct the amount of upstream material with mass measurement as a function of  $p_T^{-1}$ 

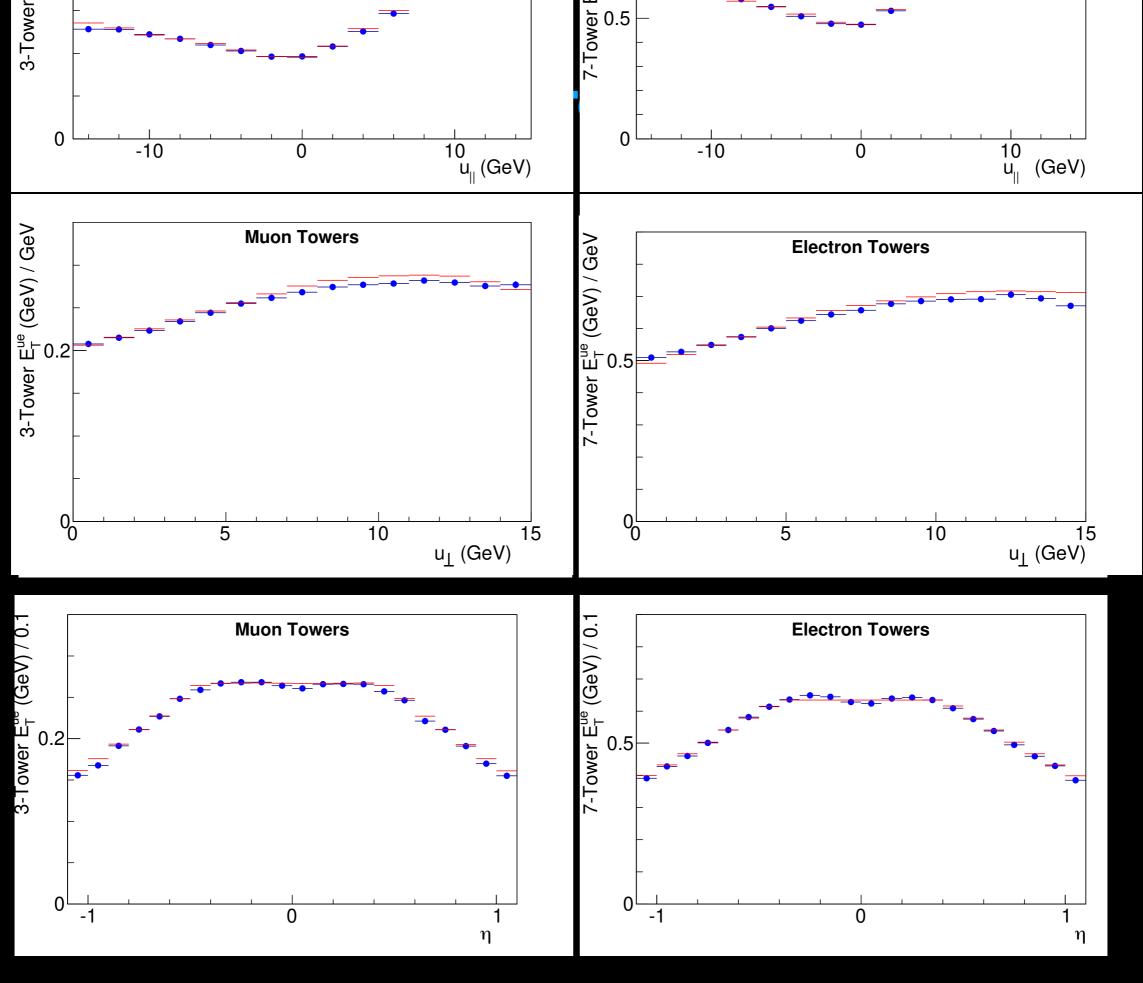




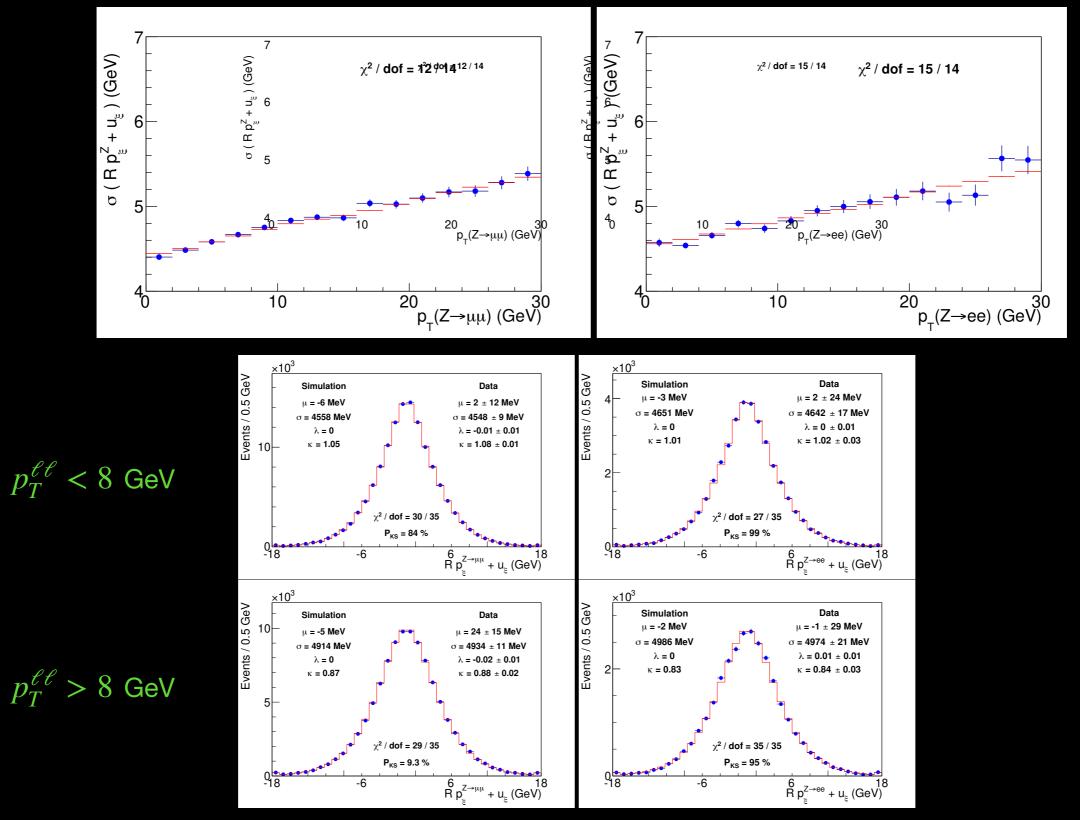


## Recoil reconstruction in muon channel





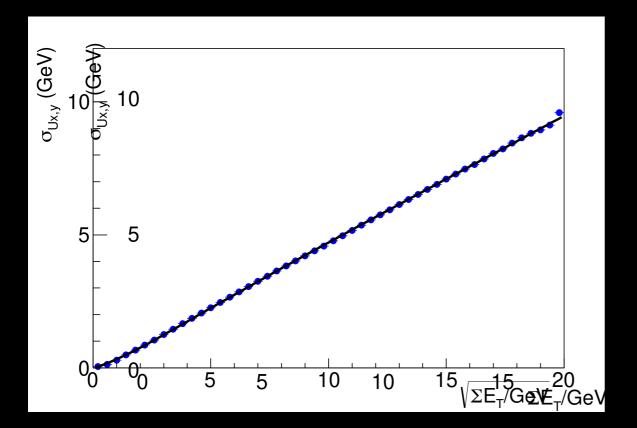
## **Recoil resolution**



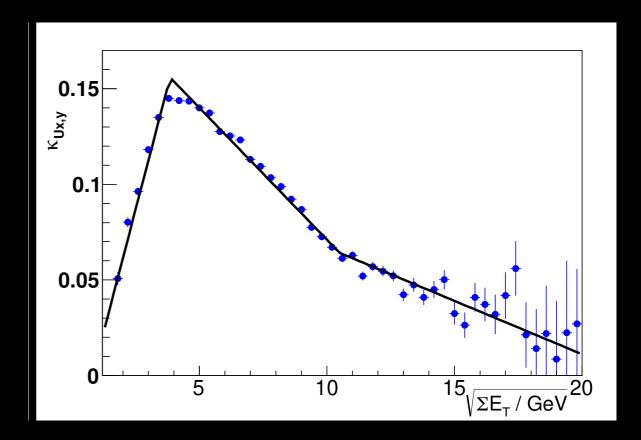
## Pileup and underlying event resolution

#### Resolution extracted from minimum bias data

### Root mean square

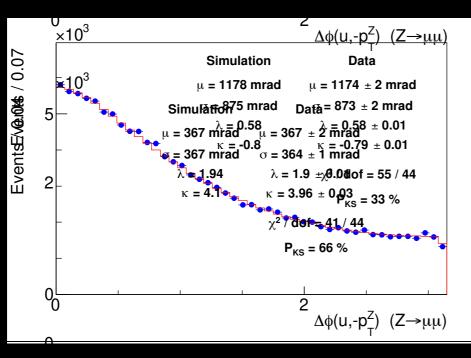


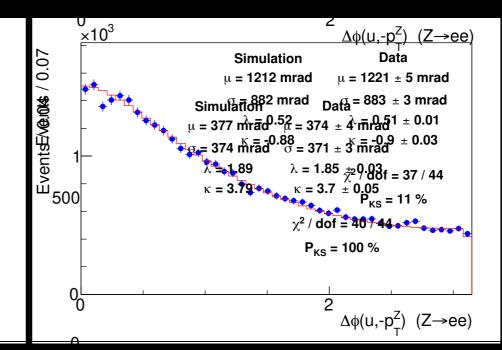
#### kurtosis



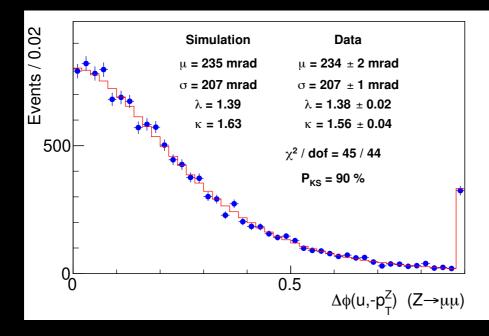
## Recoil angular resolution

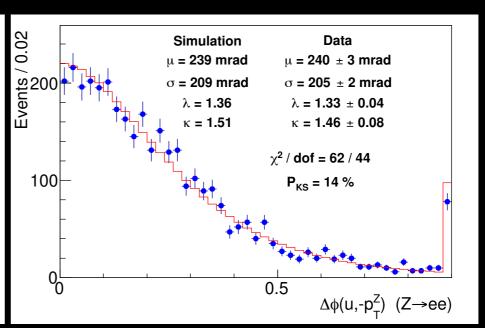
### $p_T^{\ell\ell} < 8~{ m GeV}$



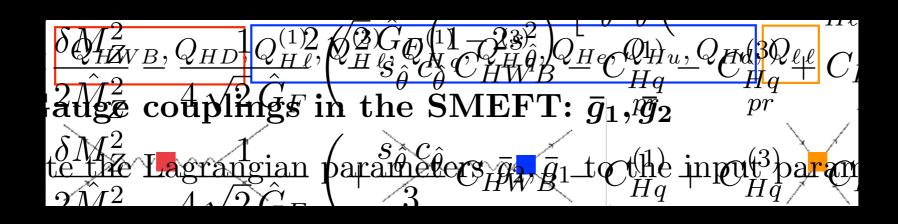


### $p_T^{\ell\ell} > 23 \text{ GeV}$





### Electroweak observables at dimension 6



Parameter	Input Value
$\hat{m}_Z$	$91.1875 \pm 0.0021$
$\hat{G}_F$	$1.1663787(6) \times 10^{-5}$
$\hat{lpha}_{ew}$	1/137.035999074(94)

$$\frac{\delta m_W^2}{\hat{m}_W^2} = \hat{\Delta} \left[ 4 C_{HWB} + \frac{c_{\hat{\theta}}}{s_{\hat{\theta}}} C_{HD} + 4 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{H\ell}^{(3)} - 2 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{\ell \ell} \right]$$

Experimental Value	Ref.	SM Theoretical Value	Ref.
$91.1875 \pm 0.0021$	[19]	_	_
$80.385 \pm 0.015$	[49]	$80.365 \pm 0.004$	[50]
$2.4952 \pm 0.0023$	[19]	$2.4942 \pm 0.0005$	[48]
$20.767 \pm 0.025$	[19]	$20.751 \pm 0.005$	[48]
$0.1721 \pm 0.0030$	[19]	$0.17223 \pm 0.00005$	[48]
$0.21629 \pm 0.00066$	[19]	$0.21580 \pm 0.00015$	[48]
$41.540 \pm 0.037$	[19]	$41.488 \pm 0.006$	[48]
$0.0171 \pm 0.0010$	[19]	$0.01616 \pm 0.00008$	[32]
$0.0707 \pm 0.0035$	[19]	$0.0735 \pm 0.0002$	[32]
$0.0992 \pm 0.0016$	[19]	$0.1029 \pm 0.0003$	[32]
	$91.1875 \pm 0.0021$ $80.385 \pm 0.015$ $2.4952 \pm 0.0023$ $20.767 \pm 0.025$ $0.1721 \pm 0.0030$ $0.21629 \pm 0.00066$ $41.540 \pm 0.037$ $0.0171 \pm 0.0010$ $0.0707 \pm 0.0035$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

