

A conclusive test of the cold dark matter model

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... or how to rule out CDM – or alternative models

The new Ogden
Centre at Durham



The Λ CDM model of cosmogony


Cosmological constant Cold dark matter

- Proposed in 1980s, it is an *ab initio*, **fully specified** model of **cosmic evolution** and the formation of cosmic structure
- Has strong **predictive** power and can, in principle, be **ruled out**
- Has made a number of **predictions** that were subsequently **verified** empirically (e.g. CMB, LSS, galaxy formation)

Three Nobel Prizes in Physics since 2006, including 2019

The big Bang

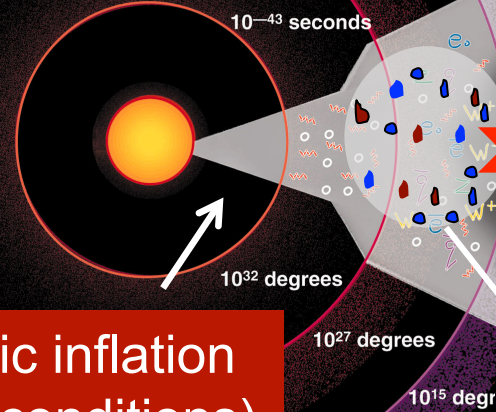
The cosmic microwave background is emitted
($t \sim 350,000$ yrs)

Production of particle dark matter
($t \sim 10^{-10}$ s)

Cosmic inflation
(initial conditions)
($t \sim 10^{-35}$ s)

The first light in our Universe

$t = 13.7$ billion yrs



- | | |
|---|--------------------------------|
| radiation | e^+ positron (anti-electron) |
| particles | p proton |
| W^+ heavy particles carrying the weak force | n neutron |
| W^- | m meson |
| Z | H hydrogen |
| quark | D deuterium |
| anti-quark | He helium |
| e^- electron | Li lithium |

3 minutes

300 thousand years

15 thousand million years

18 degrees

3 degrees K

Non-baryonic dark matter candidates

From the early 1980s:

Type	example	mass
hot	neutrino	few tens of eV
warm	sterile ν	keV-MeV
cold	axion neutralino	$10^{-5}\text{eV} - 100 \text{ GeV}$

The dark matter power spectrum

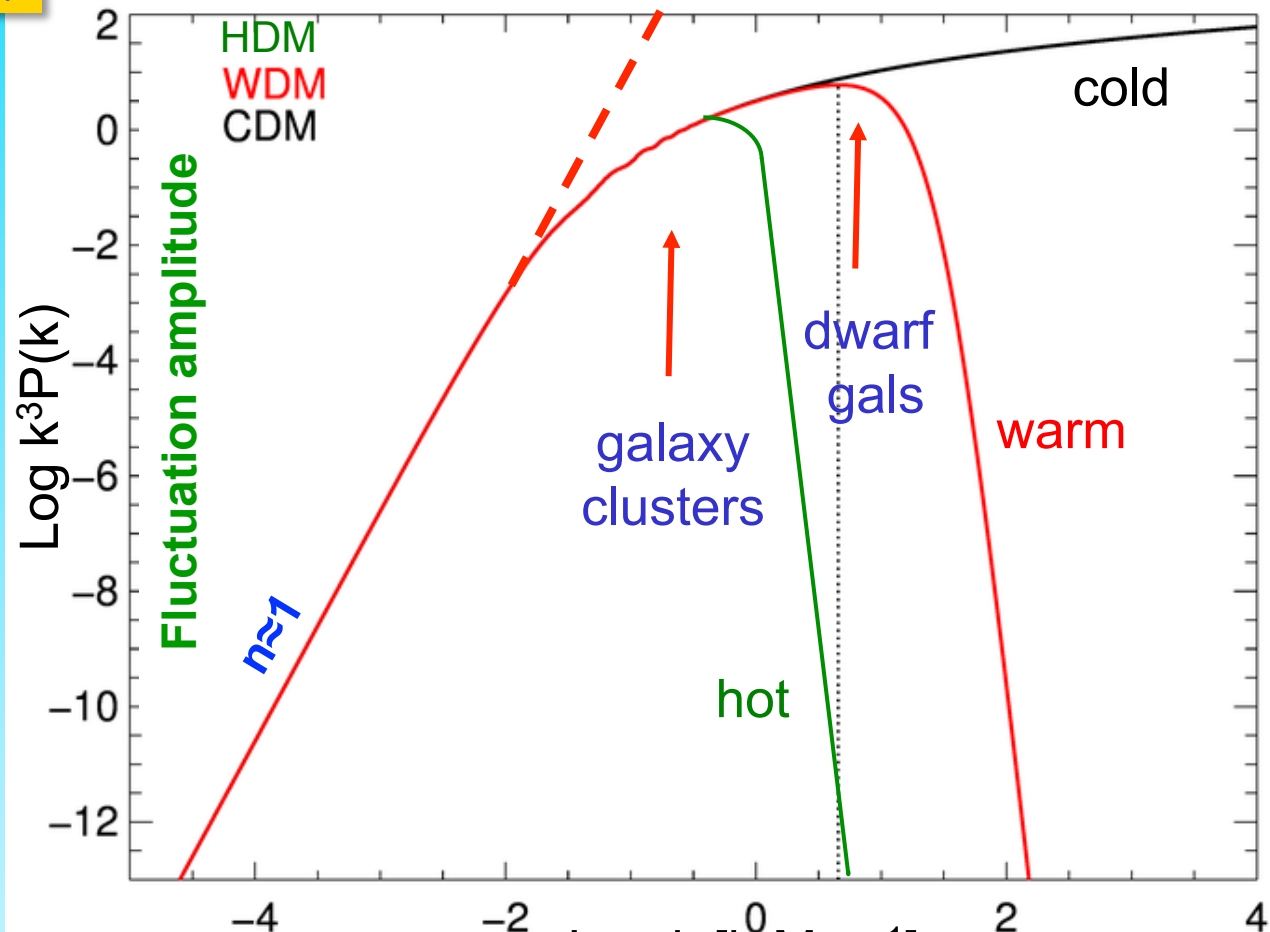
$k^3 P(k)$

The linear power spectrum (“power per octave”)

Free streaming →

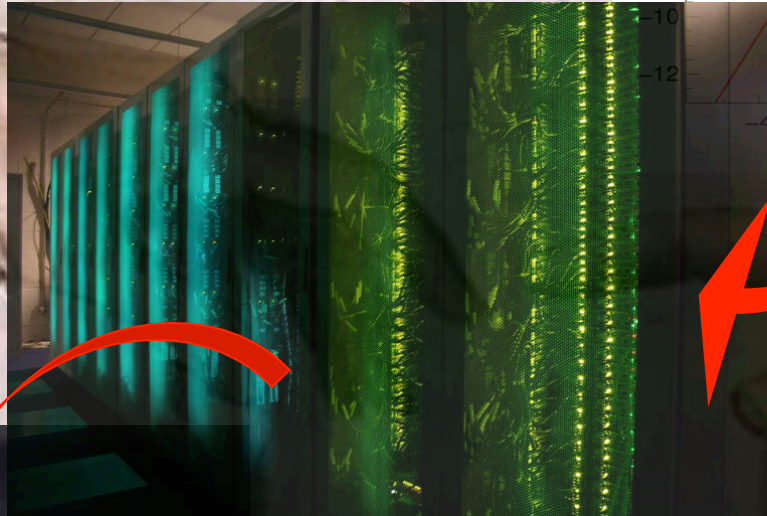
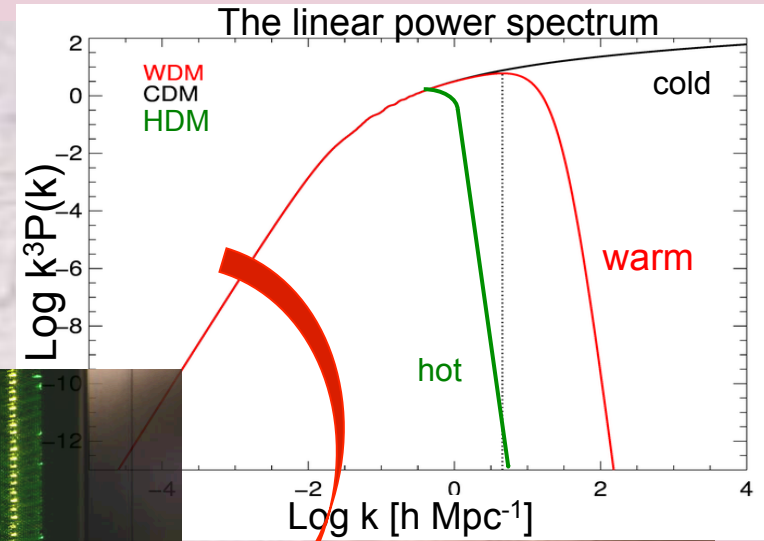
$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for a thermal relic



These possibilities can be tested with astrophysics

Non-linear evolution

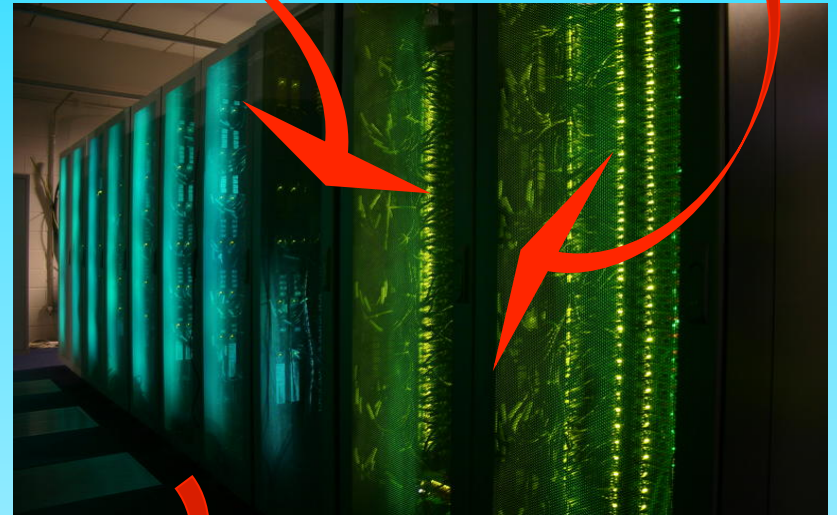


Non-linear evolution: simulations

Assumption about content of Universe → Initial conditions

Relevant equations:

Collisionless Boltzmann;
Poisson; Friedmann eqns;
Radiative hydrodynamics
Subgrid astrophysics



How to make a virtual universe

Hot dark matter

-7-

LUBIMOV

$$m_\nu = 30 \text{ eV} \rightarrow \Omega_m = 1$$

1981

HAS THE NEUTRINO A NON-ZERO REST MASS?
(Tritium β -Spectrum Measurement)*

V. Lubimov, E. Novikov, V. Nozik, E. Tretyakov
Institute for Theoretical and Experimental Physics, Moscow, U.S.S.R.

V. Kosik
Institute of Molecular Genetics, Moscow, U.S.S.R.

ABSTRACT

The high energy part of the β -spectrum of tritium in the molecule was measured with high precision by a toroidal β -spectrometer. The results give evidence for a non-zero electron anti-neutrino mass.

Fifty years ago Pauli introduced the neutrino to explain the β -spectrum shape. Pauli made the first estimate of the neutrino mass ($E_{\beta \text{ max}} \approx \text{nuclei mass defect}$): it should be very small or maybe zero. Up to now the study of the β -spectrum shape is the most sensitive, direct method of neutrino mass measurement.

For allowed β -transitions, if $M_\nu = 0$, then $S \approx (E - E_0)^2$. The Kurie plot is then a straight line with the only kinematic parameter being $E_k = E_0$ (total β -transition energy). If $M_\nu \neq 0$, then $S \approx (E_0 - E) \sqrt{(E_0 - E)^2 - M_\nu^2}$. The Kurie plot is then distorted, especially near the endpoint.

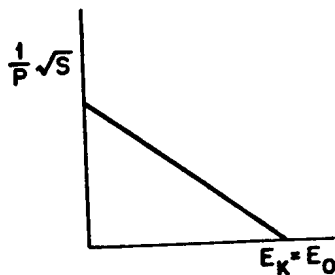


Fig. 1. Kurie plot for $M_\nu = 0$.

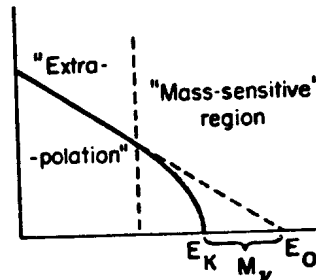
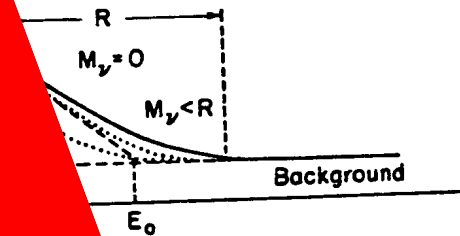


Fig. 2. Kurie plot for $M_\nu \neq 0$.

The method for the neutrino mass measurement is to obtain E_0 from the extrapolation and obtain E_k from the spectrum intercept. Then $M_\nu = E_0 - E_k$. Qualitatively, $M_\nu \neq 0$ if the β -spectrum near the endpoint runs below the extrapolated curve.

* Paper presented by Oleg Egorov.

things are more complicated. The apparatus resolution strongly affects the spectrum endpoint and rather the spectrum slope.



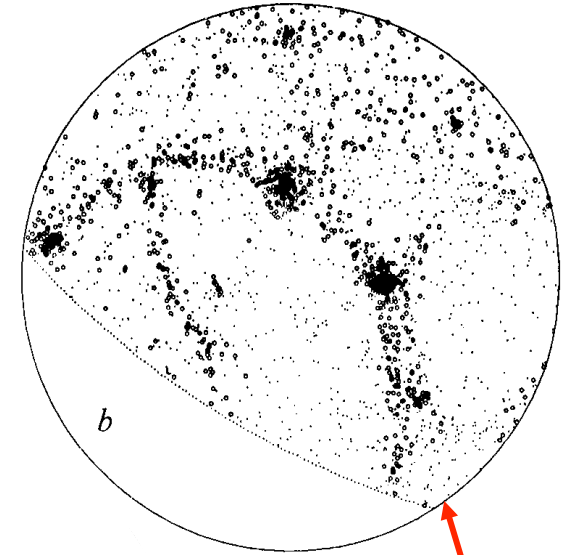
Realistic Kurie plot.

extrapolation. However, we are unable to determine M_ν , then once again the lack of counts near the endpoint indicate that $M_\nu \neq 0$. If $M_\nu \leq R$, the changes due to M_ν and the influence of R are indistinguishable. For $M_\nu > R$, the determination of the knowledge of R is compulsory. The background determines the statistical accuracy near the endpoint, i.e., in the region of the highest sensitivity to the ν mass. So: 1) R should be $\sim M_\nu$, 2) the smaller M_ν is, the smaller the background ($\sim M_\nu^2$) must be and the higher the statistics ($\sim M_\nu^{-3}$) must be. For example, suppose that for $M_\nu = 100 \text{ eV}$ we need resolution R , background Q , and statistics N . If $M_\nu = 30 \text{ eV}$, to achieve the same $\Delta M/M$ they should be $R/3$, $Q/10$, and $N \times 30$, respectively.

The shorter the β -spectrum, the less it is spread due to R (as $R \sim \Delta p/p \approx \text{const.}$). A classical example is ^3H β -decay, which has 1) the smallest $E_0 \sim 18.6 \text{ keV}$, 2) an allowed β -transition, simple nucleus, and simple theoretical interpretation, 3) highly reduced radioactivity. The first experiments with ^3H were by S. Curran et al. (1948) and G. Hanna, B. Pontecorvo (1949). Using ^3H gas in a proportional counter, they obtained $M_\nu \leq 1 \text{ keV}$. Further progress required magnetic spectrometer development. This allowed the resolution to be improved considerably, and L. Langer and R. Moffat (1952) obtained $M_\nu \leq 250 \text{ eV}$. The best value was obtained by K. Bergqvist (1972): $R \sim 50 \text{ eV}$ and $M_\nu \leq 55 \text{ eV}$.

The ITEP spectrometer is of a new type: ironless, with toroidal magnetic field (E. Tretyakov, 1973). The principle of the toroidal magnetic field focusing systems was proposed by V. Vladimirov et al. (An example is a "Horn" of ν -beams.) It turns out that a rectilinear conductor (current) has a focusing ability for particles emitted perpendicular to the rotation axis. This system has infinite periodical focusing structure. The ITEP spectrometer is based on this principle.

Non-baryonic dark matter cosmologies



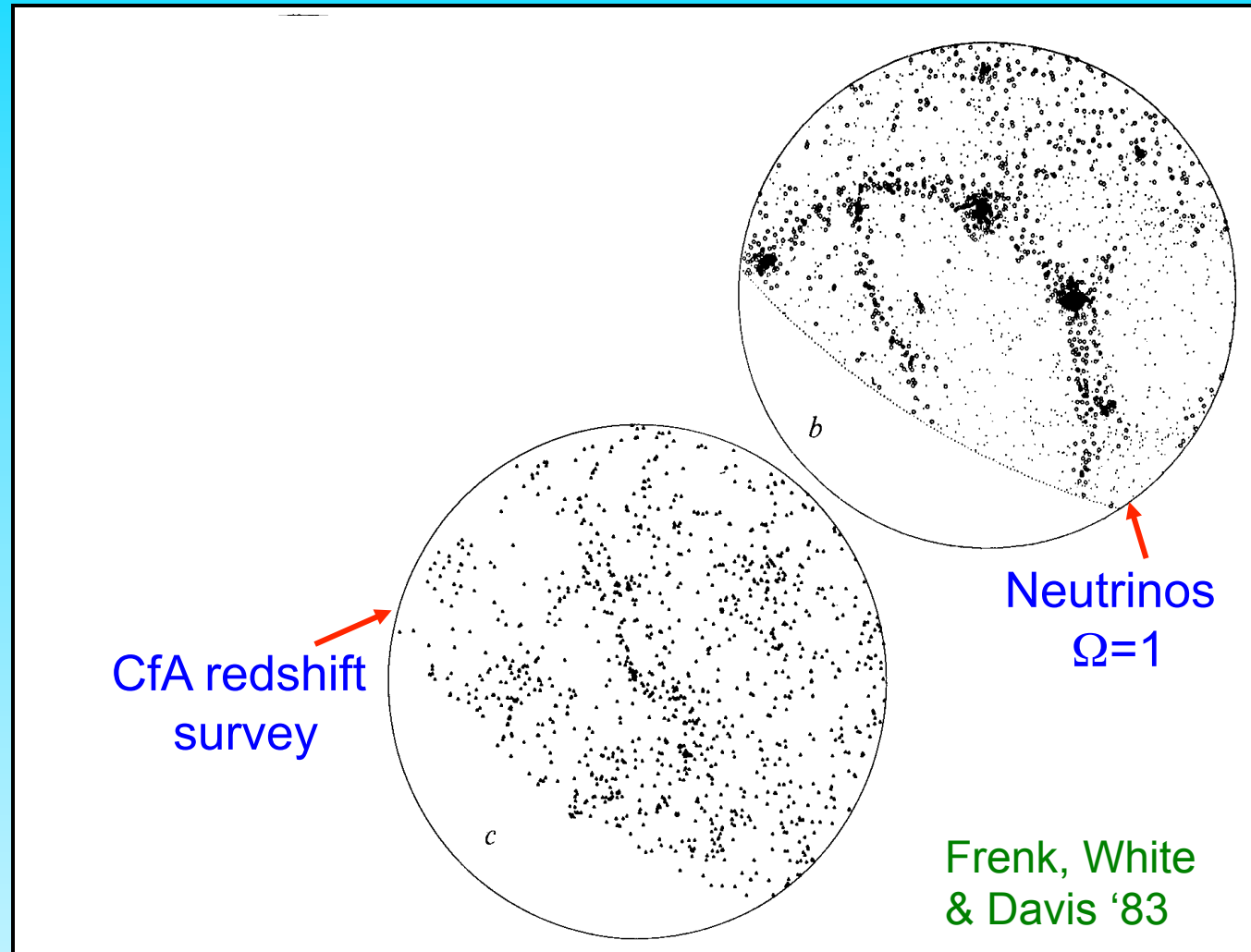
Neutrinos
 $\Omega=1$

Frenk, White
& Davis '83

Non-baryonic dark matter cosmologies

Neutrino DM →
wrong clustering

Neutrinos cannot
make appreciable
contribution to Ω
→ $m_\nu \ll 30 \text{ eV}$



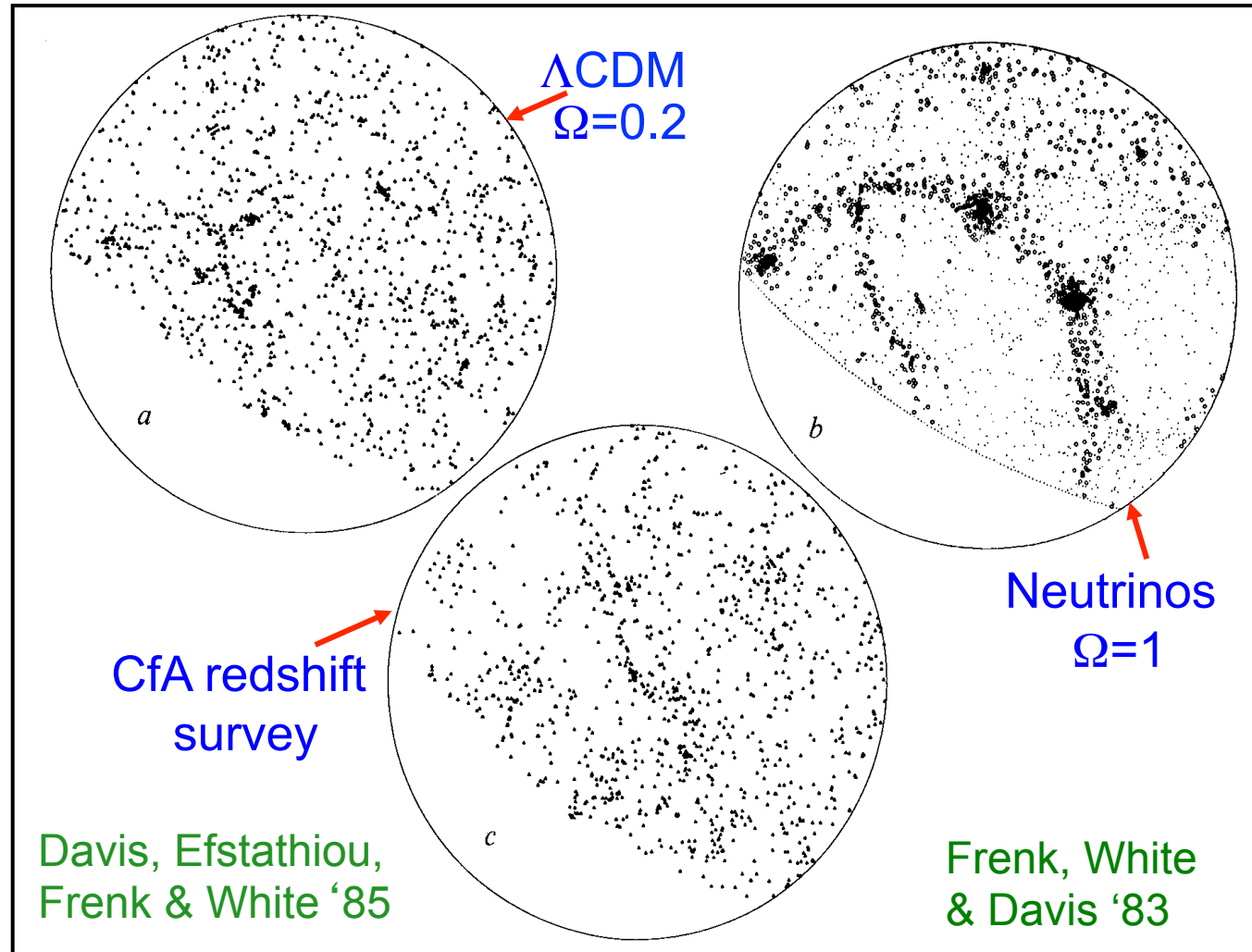
Non-baryonic dark matter cosmologies

Neutrino DM →
wrong clustering

Neutrinos cannot
make appreciable
contribution to Ω
→ $m_\nu \ll 30$ eV

Early CDM N-body
simulations gave
promising results

In CDM structure
forms hierarchically



The big Bang



300 thousand

3 minutes

15 thousand million years

The temperature of this radiation should show small irregularities

Production of particle dark matter
($t \sim 10^{-10}$ s)

10^{-43} seconds

10^{32} degrees

10^{27} degrees

10^{15} degrees

1 degrees

18 degrees

3 degrees K

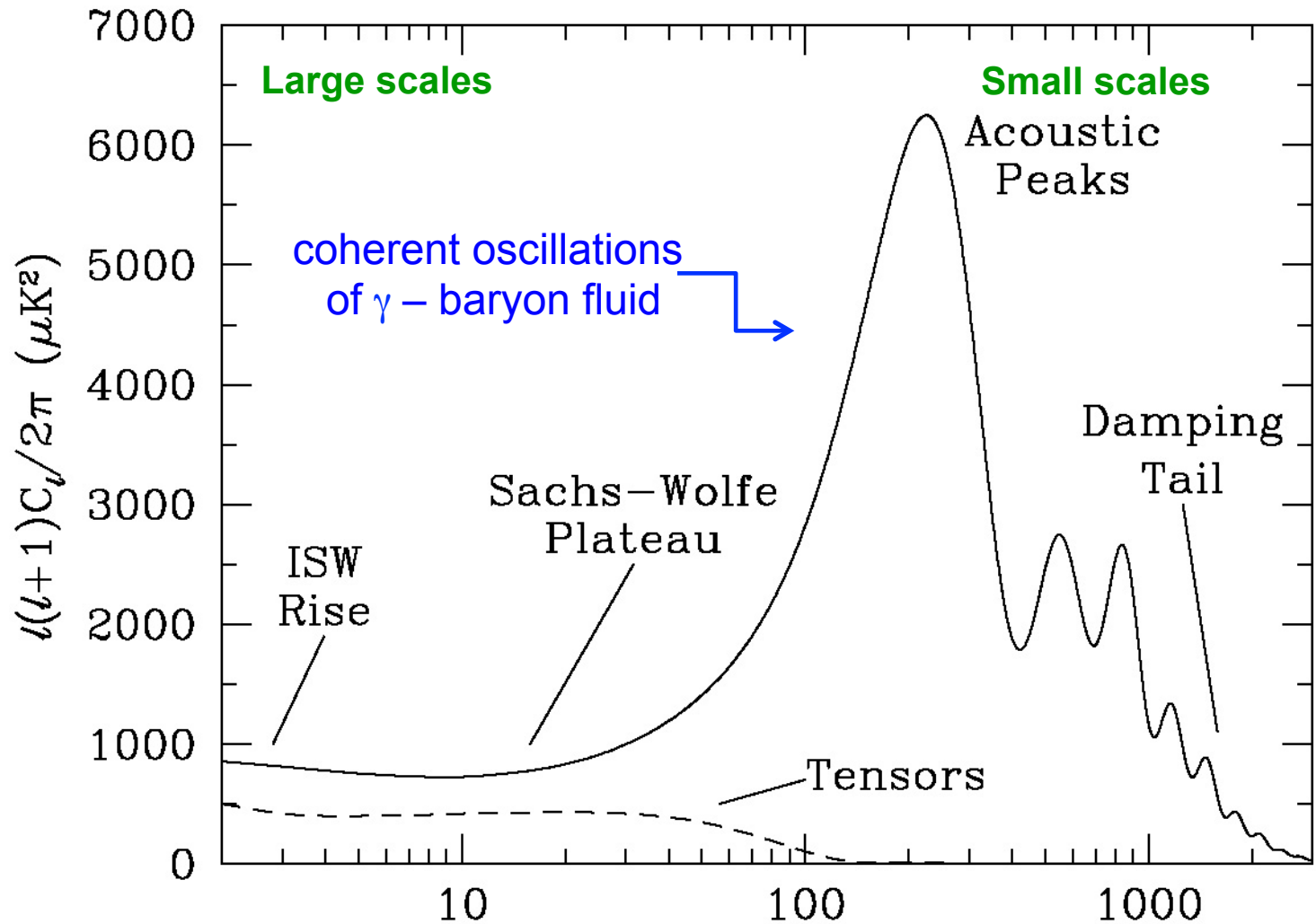
$t = 13.7$ billion yrs

Cosmic inflation
(initial conditions)
($t \sim 10^{-35}$ s)

- radiation
- particles
- W^+ heavy particles carrying the weak force
- W^-
- Z
- quark
- anti-quark
- electron
- positron (anti-proton)
- neutron
- meson
- hydrogen
- deuterium
- helium
- lithium

Temperature anisotropies in CMB

2D power spectrum



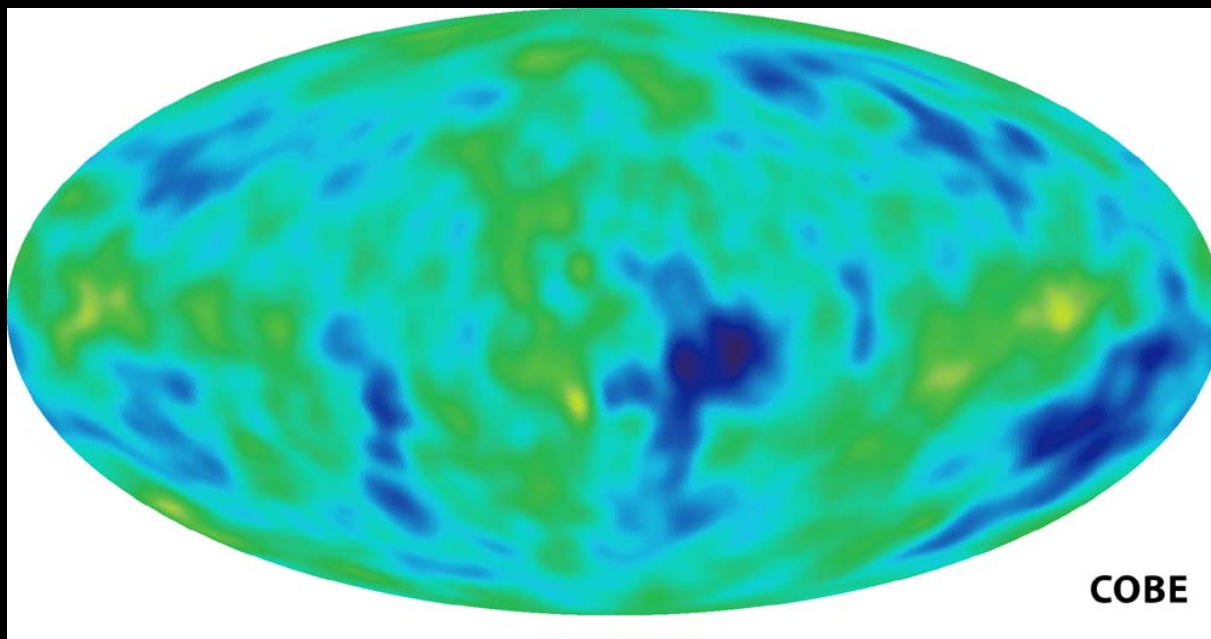
Peebles & Yu '70 Sunyev & Zel'dovich '70

For CDM: Peebles '82; Bond & Efstathiou '84

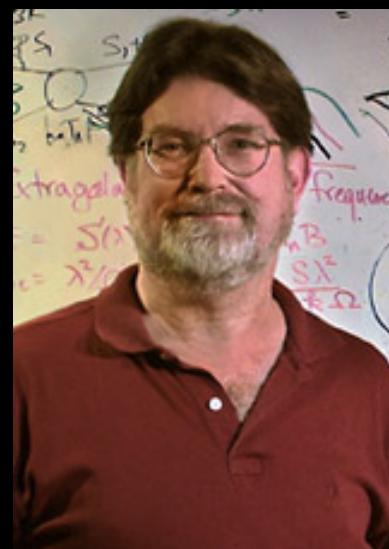
Jim Peebles
Nobel prize 2019



1992



George Smoot - Nobel Prize 2006

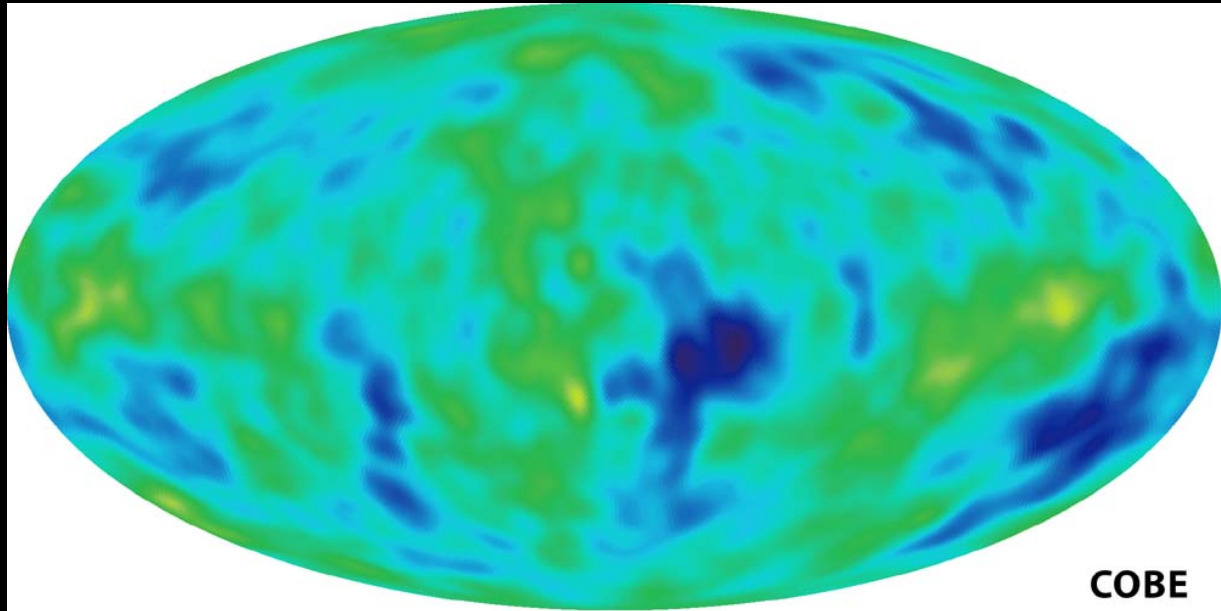
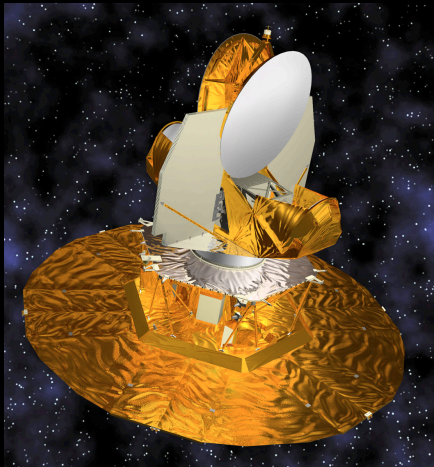


The CMB

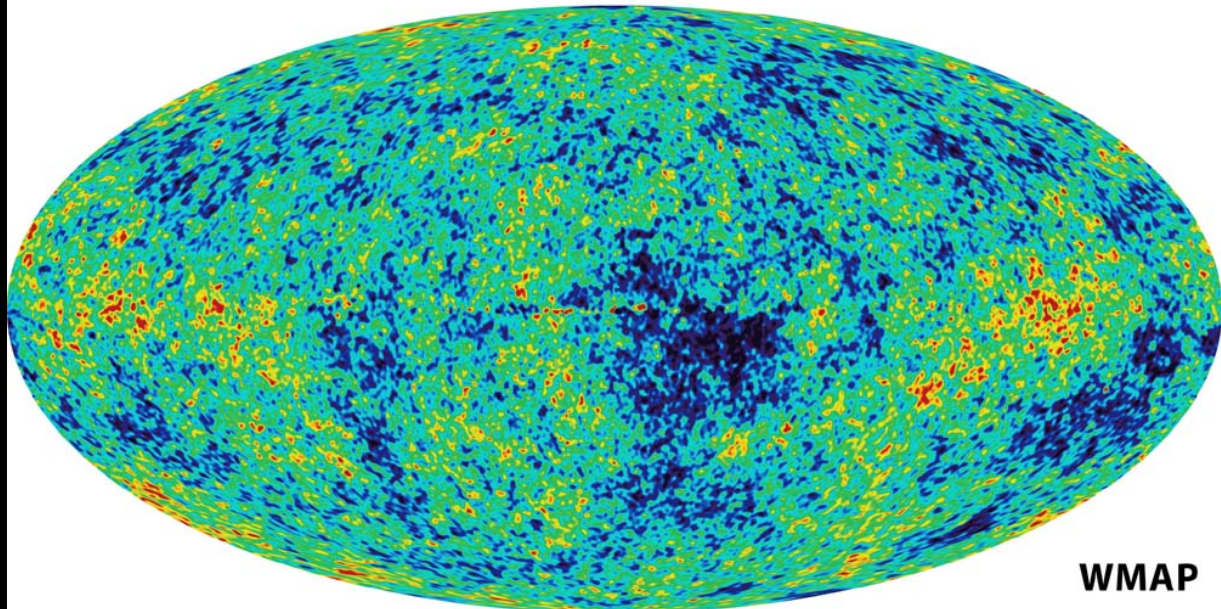
1992



2003



COBE

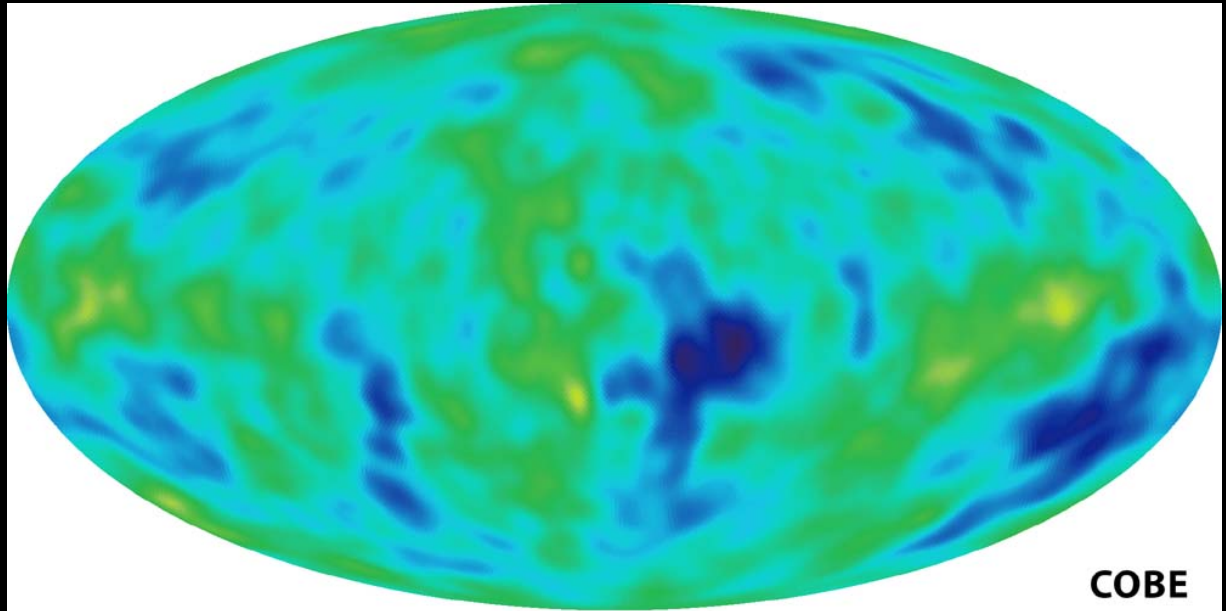


WMAP

ICC

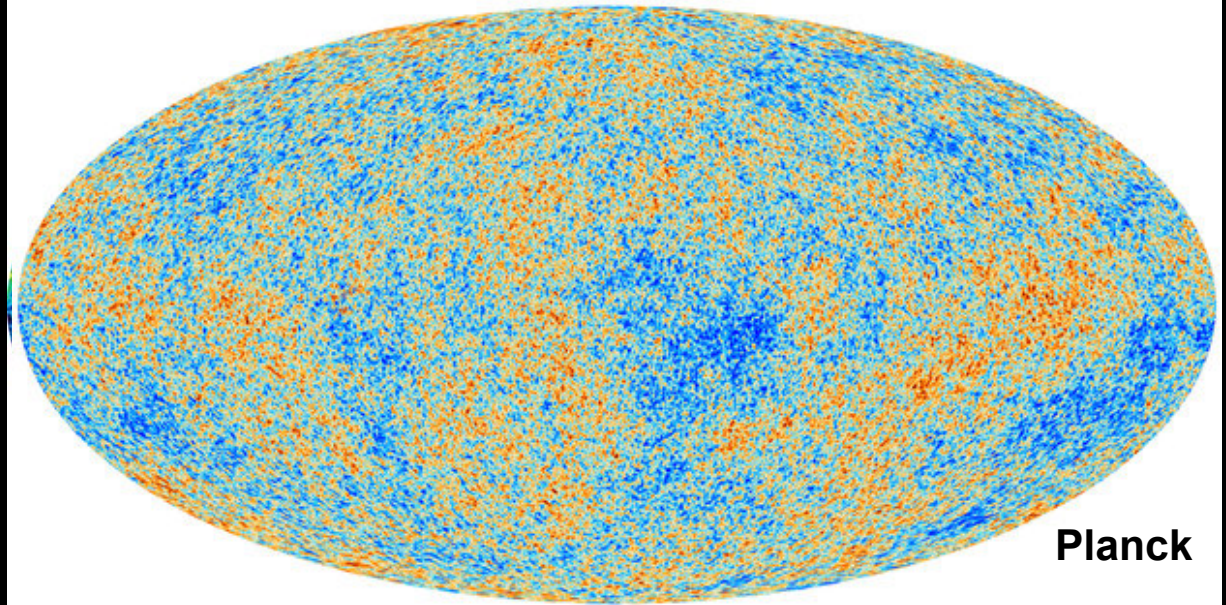
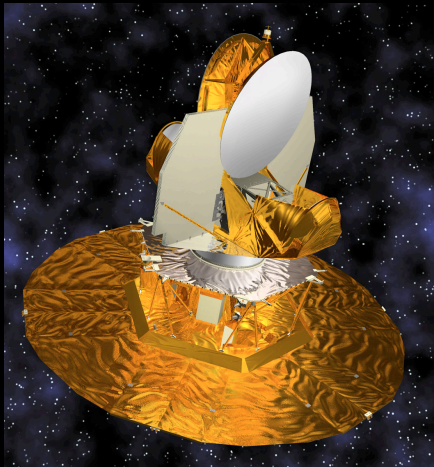
The CMB

1992



COBE

2012



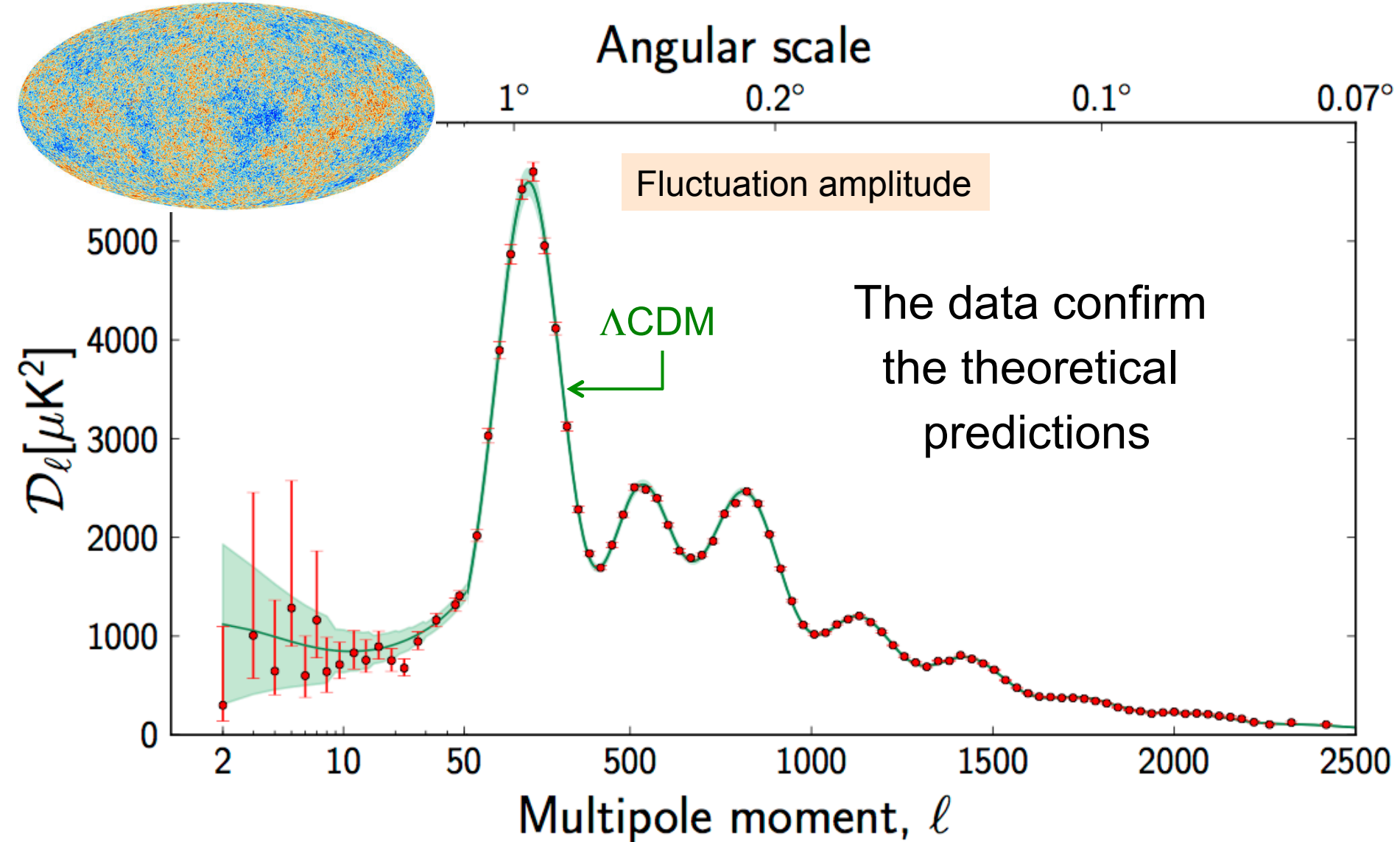
Planck

The initial conditions for galaxy formation



Quantum fluctuations from inflation

Planck: CMB temperature anisotropies



The six parameters of minimal Λ CDM model

		<i>Planck</i> +WP	
Parameter		Best fit	68% limits
6 model parameters	$\Omega_b h^2$. density of baryons .	0.022032	0.02205 \pm 0.00028
	$\Omega_c h^2$. density of CDM .	0.12038	0.1199 \pm 0.0027
	$100\theta_{MC}$	1.04119	1.04131 \pm 0.00063
	τ	0.0925	0.089 $^{+0.012}_{-0.014}$
	n_s	0.9619	0.9603 \pm 0.0073
	$\ln(10^{10} A_s)$	3.0980	3.089 $^{+0.024}_{-0.027}$

A 40 σ detection of non-baryonic dark matter!

N-body simulations of large-scale structure in Λ CDM

Davis, Efstathiou, Frenk
& White '85

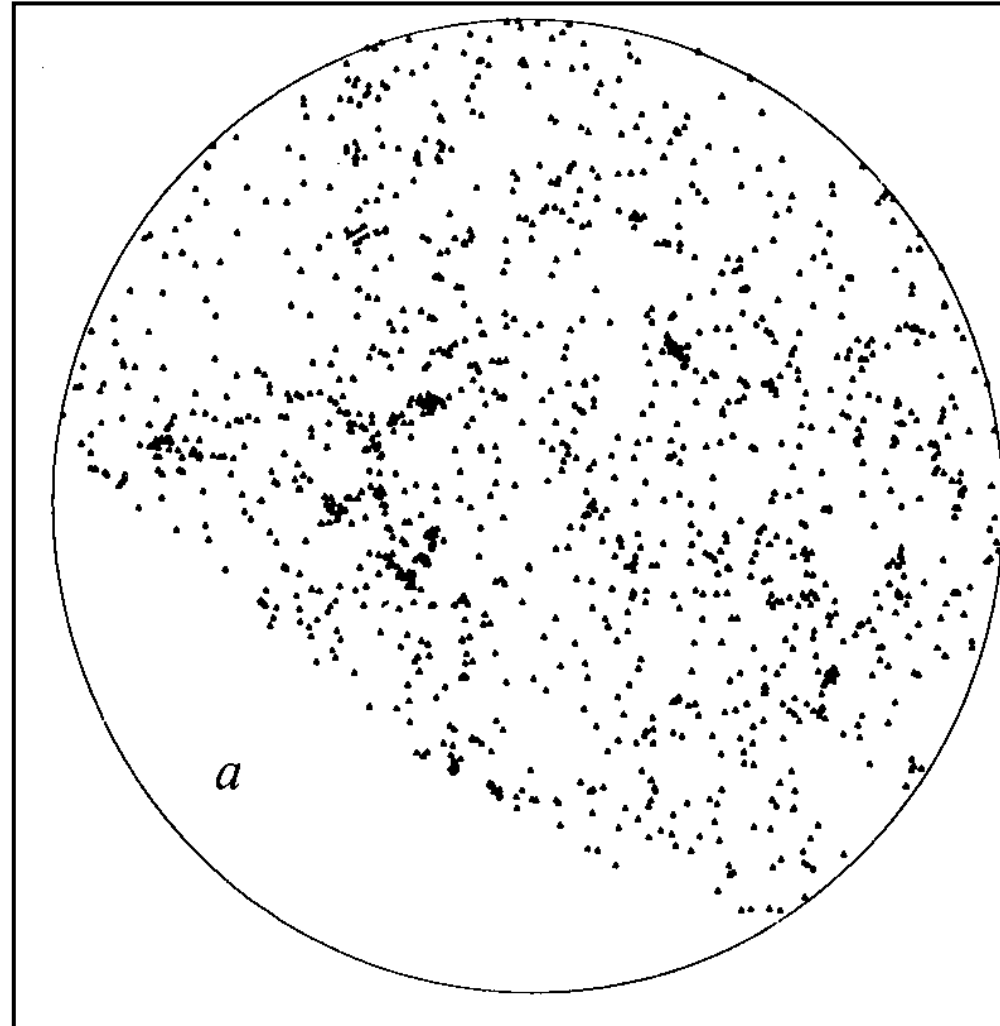
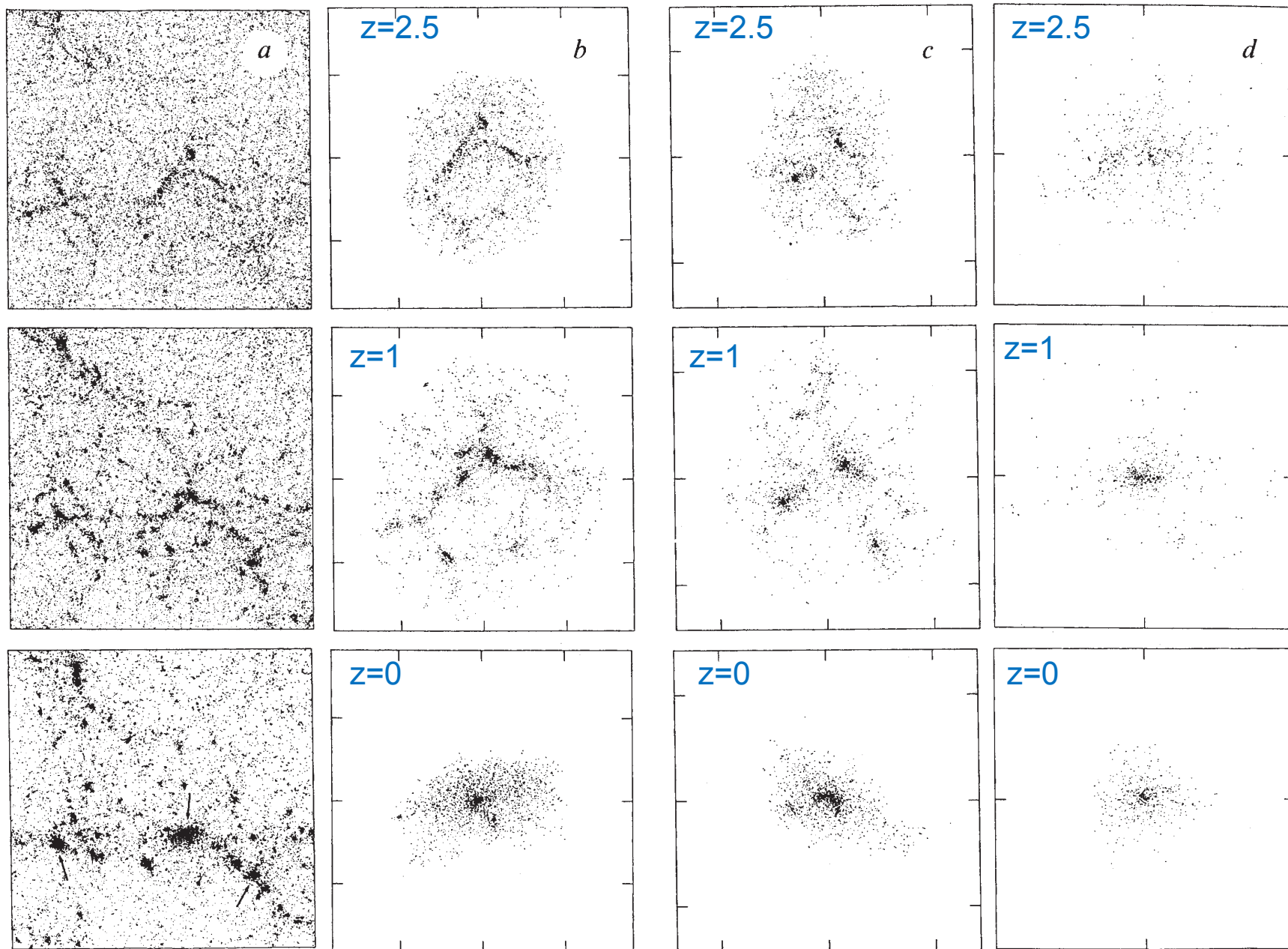


Fig. 1

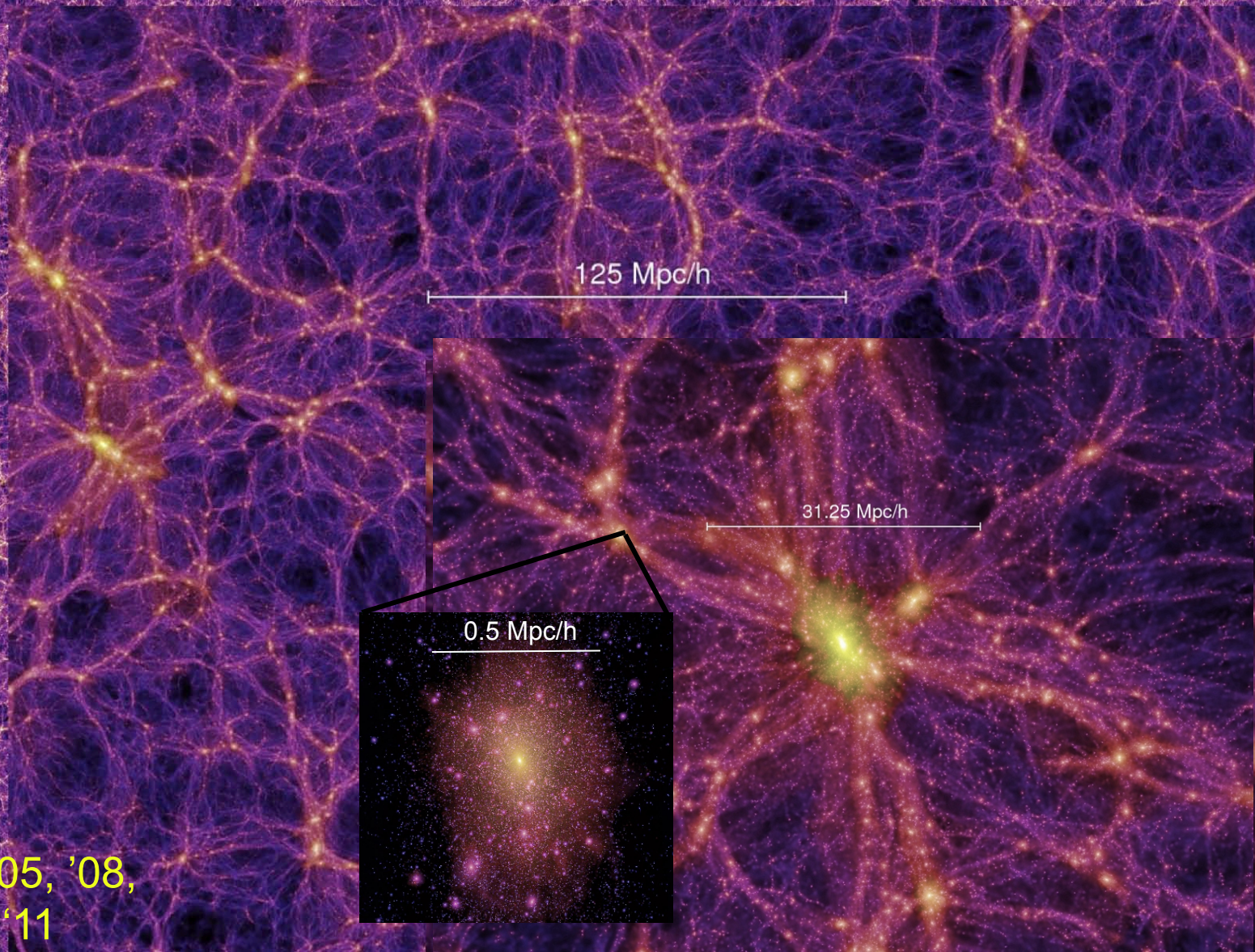
Formation of CDM halos



Frenk et al 1985

VIRGO

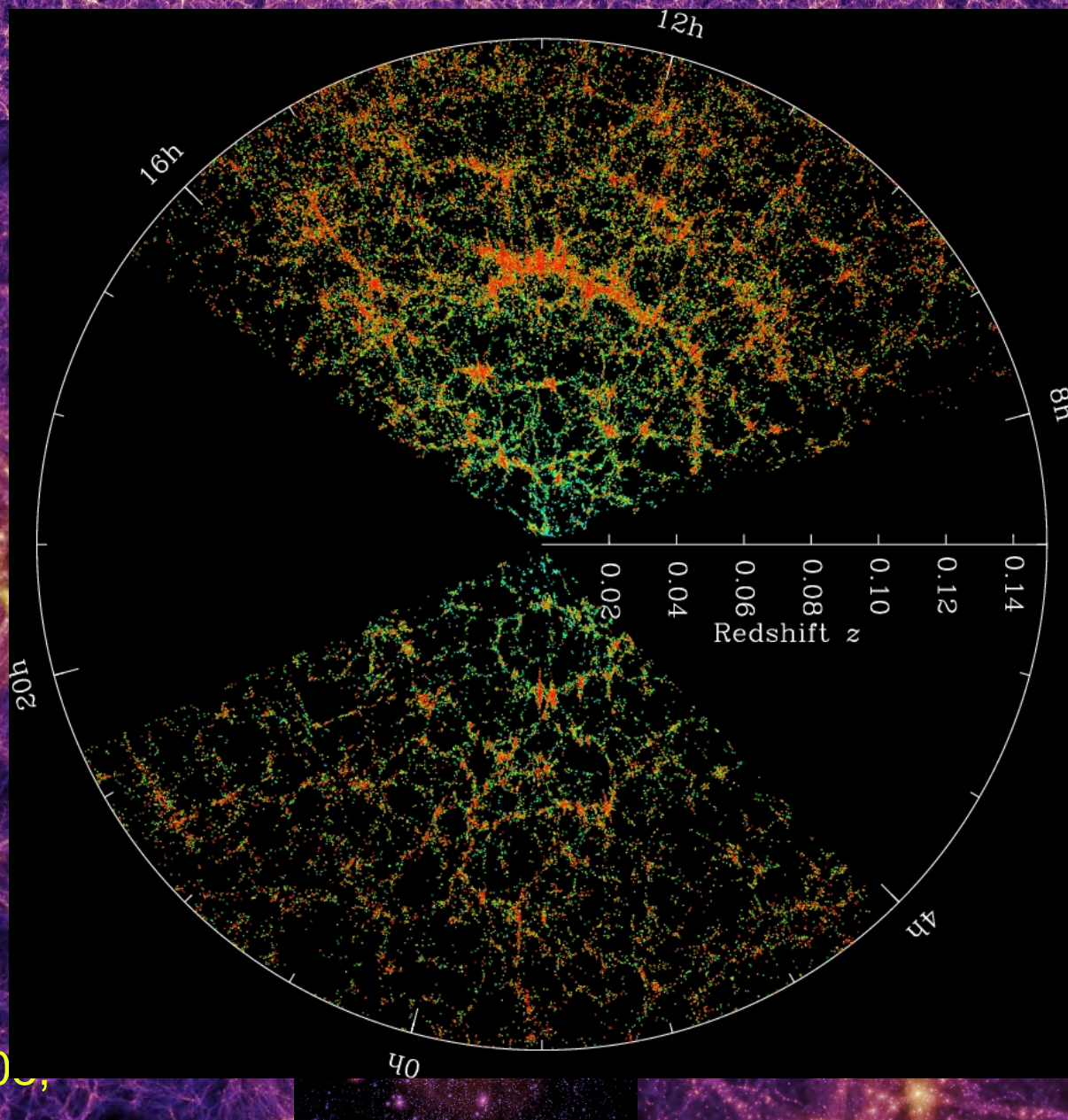
The Millennium/Aquarius/Phoenix simulation series



Springel et al '05, '08,
Gao et al '11

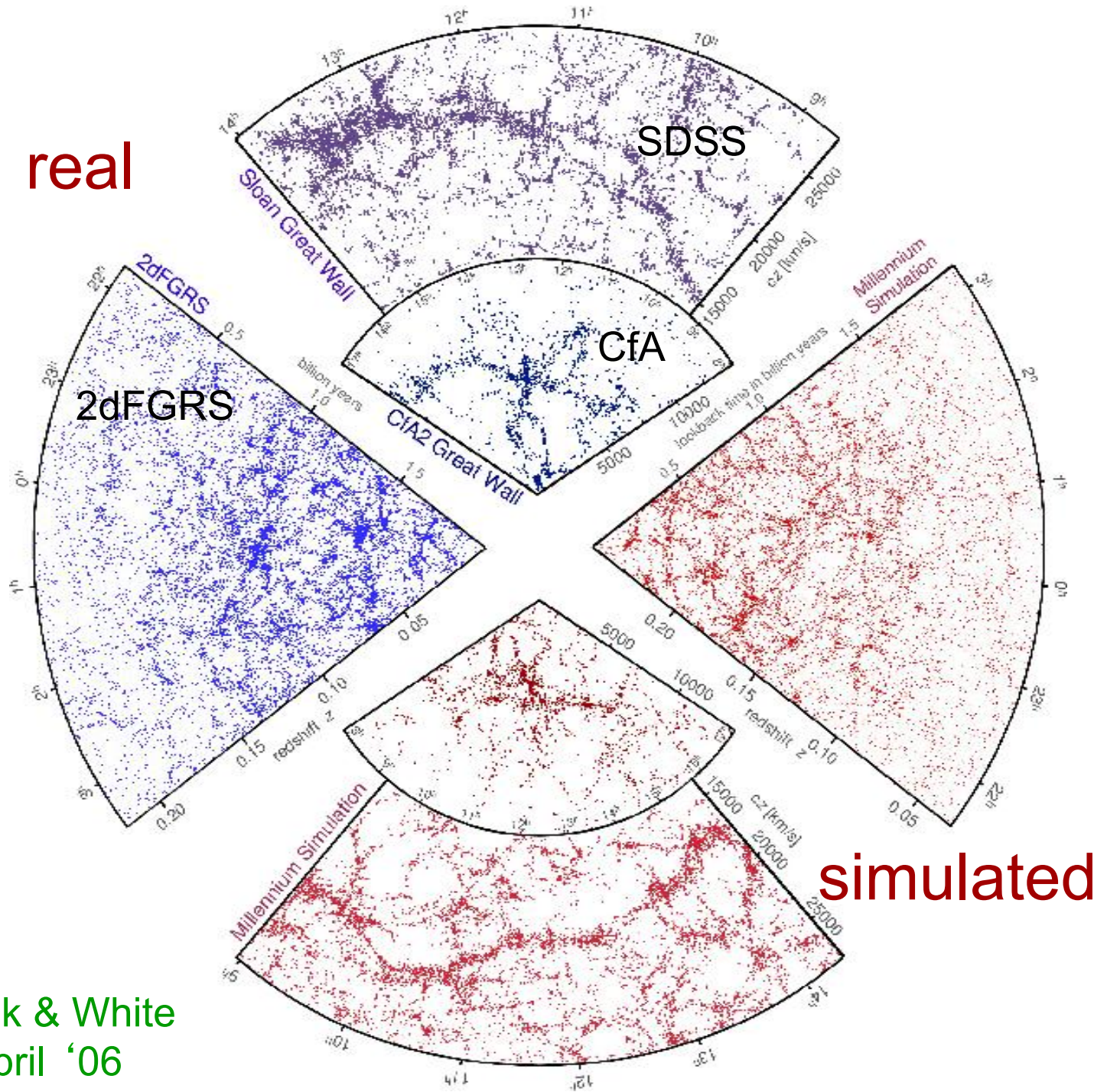
VIRGO

The Millennium/Aquarius/Phoenix simulation series



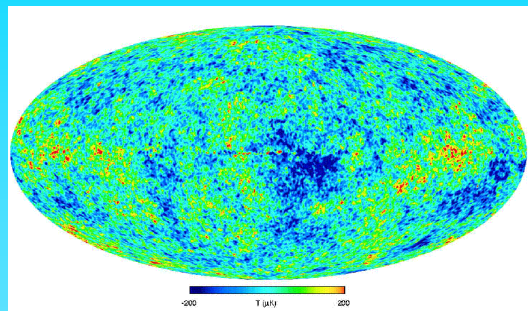
Springel et al '05, '06,
Gao et al '11

real

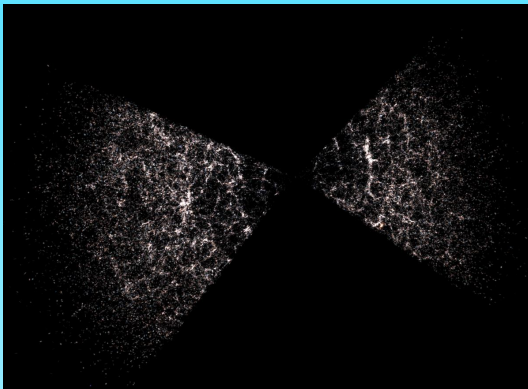


simulated

The cosmic power spectrum: from the CMB to the 2dFGRS



$z \sim 1000$



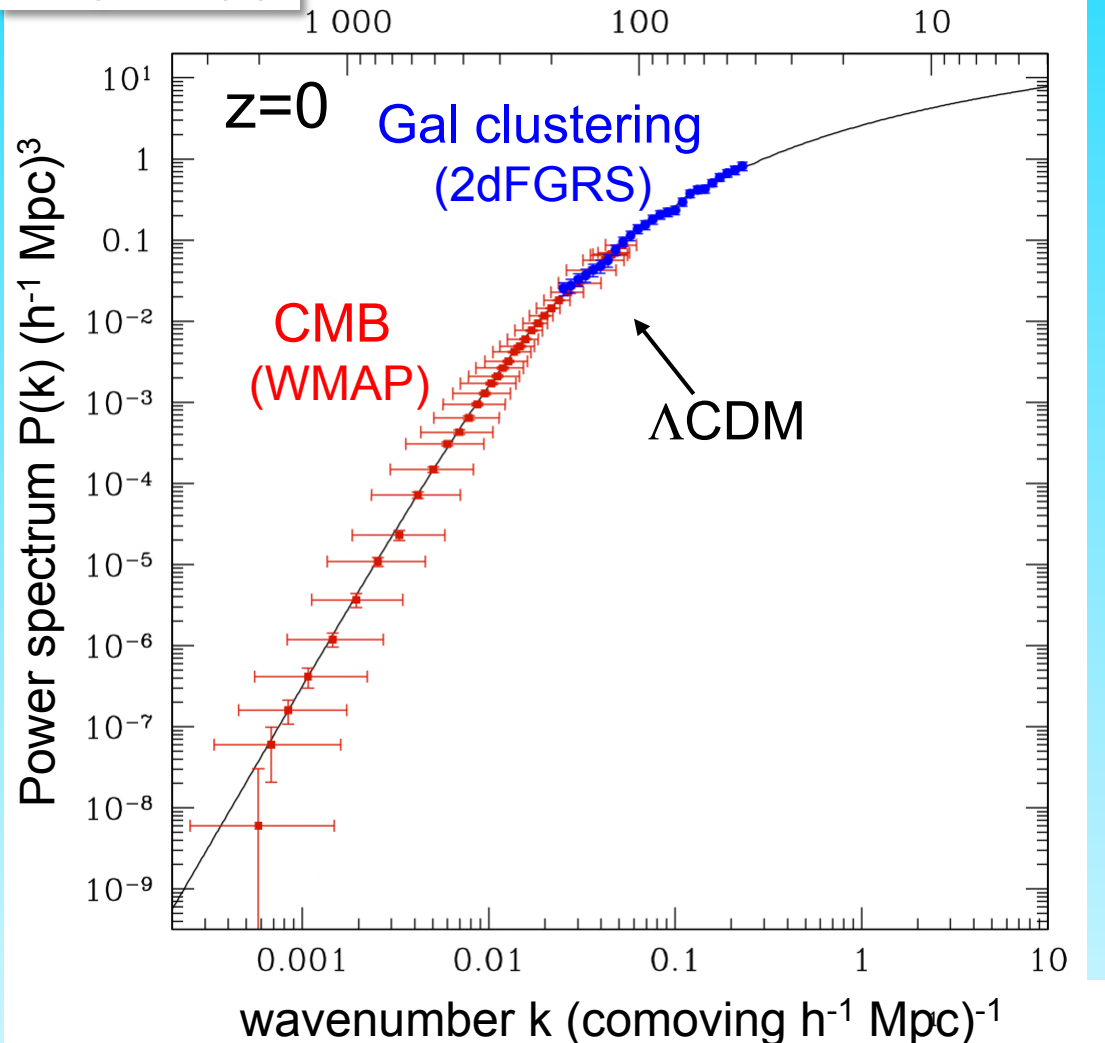
$z \sim 0$

⇒ Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06

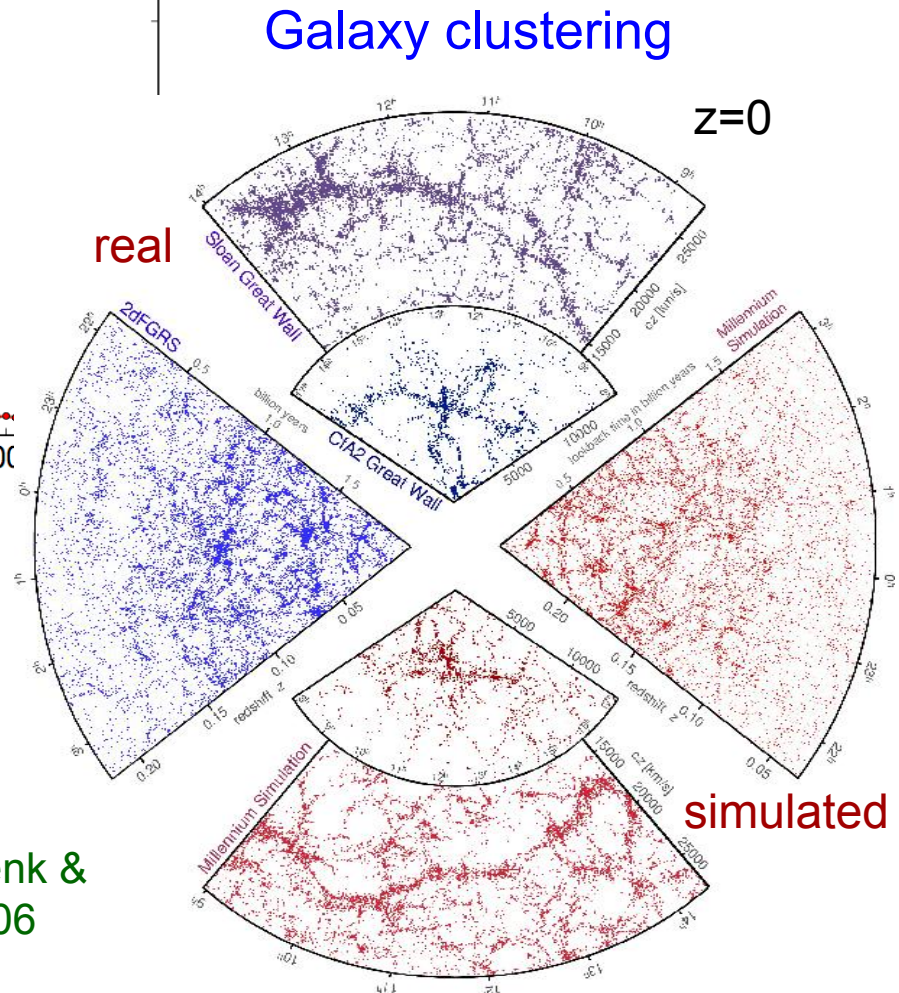
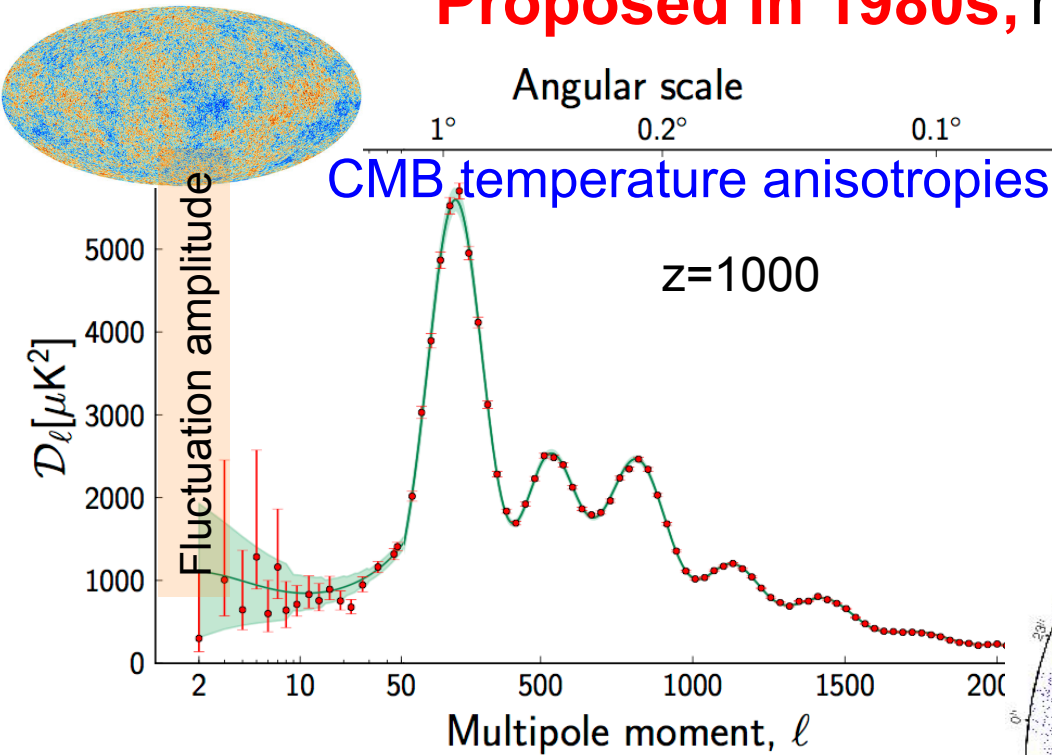
Log $k^3 P(k)$

wavelength k^{-1} (comoving h^{-1} Mpc)



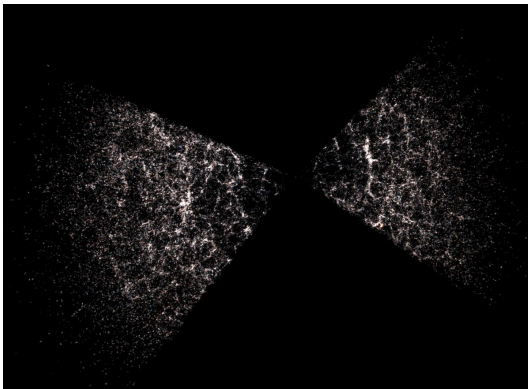
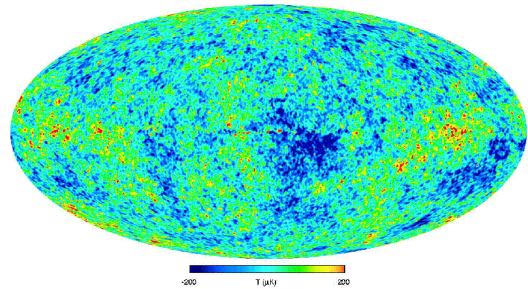
The Λ CDM model of cosmogony

Proposed in 1980s; now empirically supported by:



Springel, Frenk &
White 2006

The cosmic power spectrum: from the CMB to the 2dFGRS

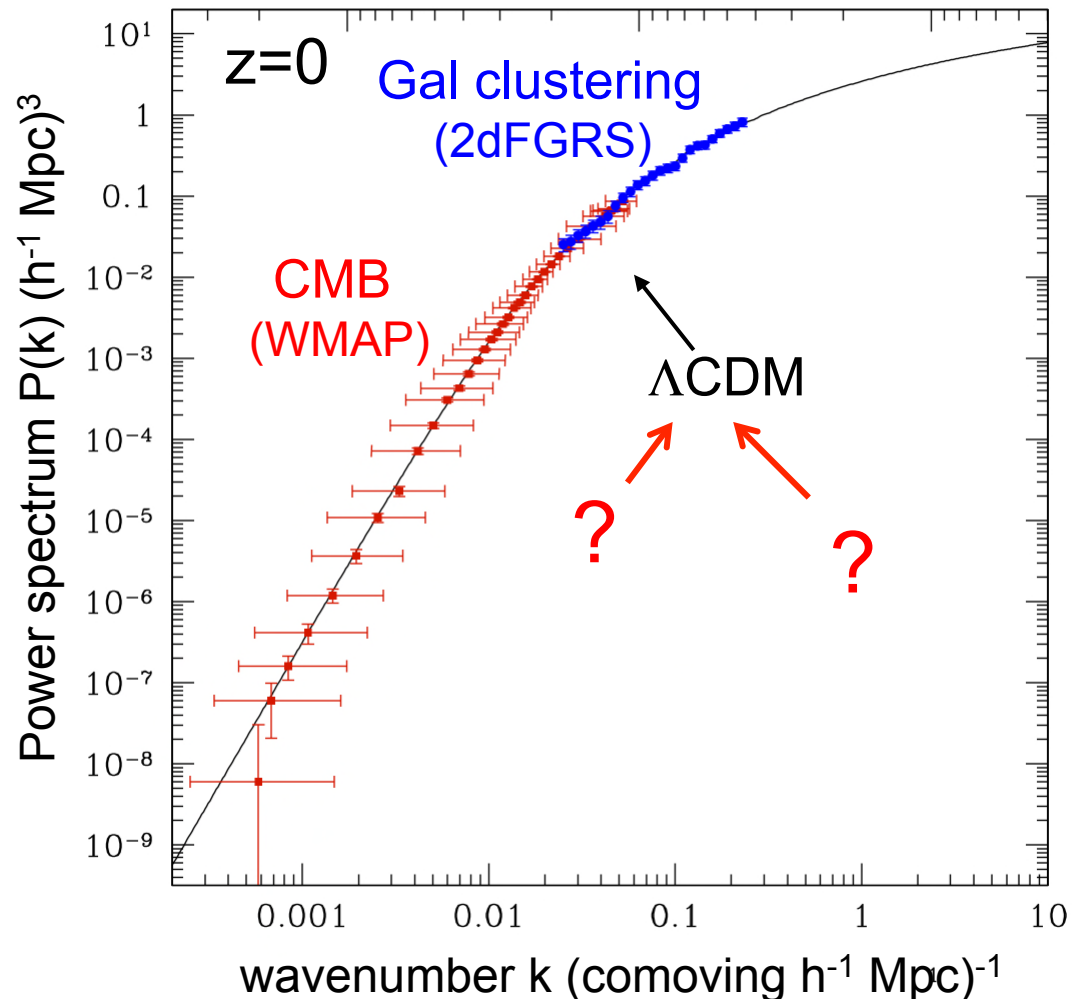


$z \sim 1000$

$\text{Log } k^3 P(k)$

wavelength k^{-1} (comoving h^{-1} Mpc)

1 000 100 10



$\Rightarrow \Lambda\text{CDM}$ provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06

The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

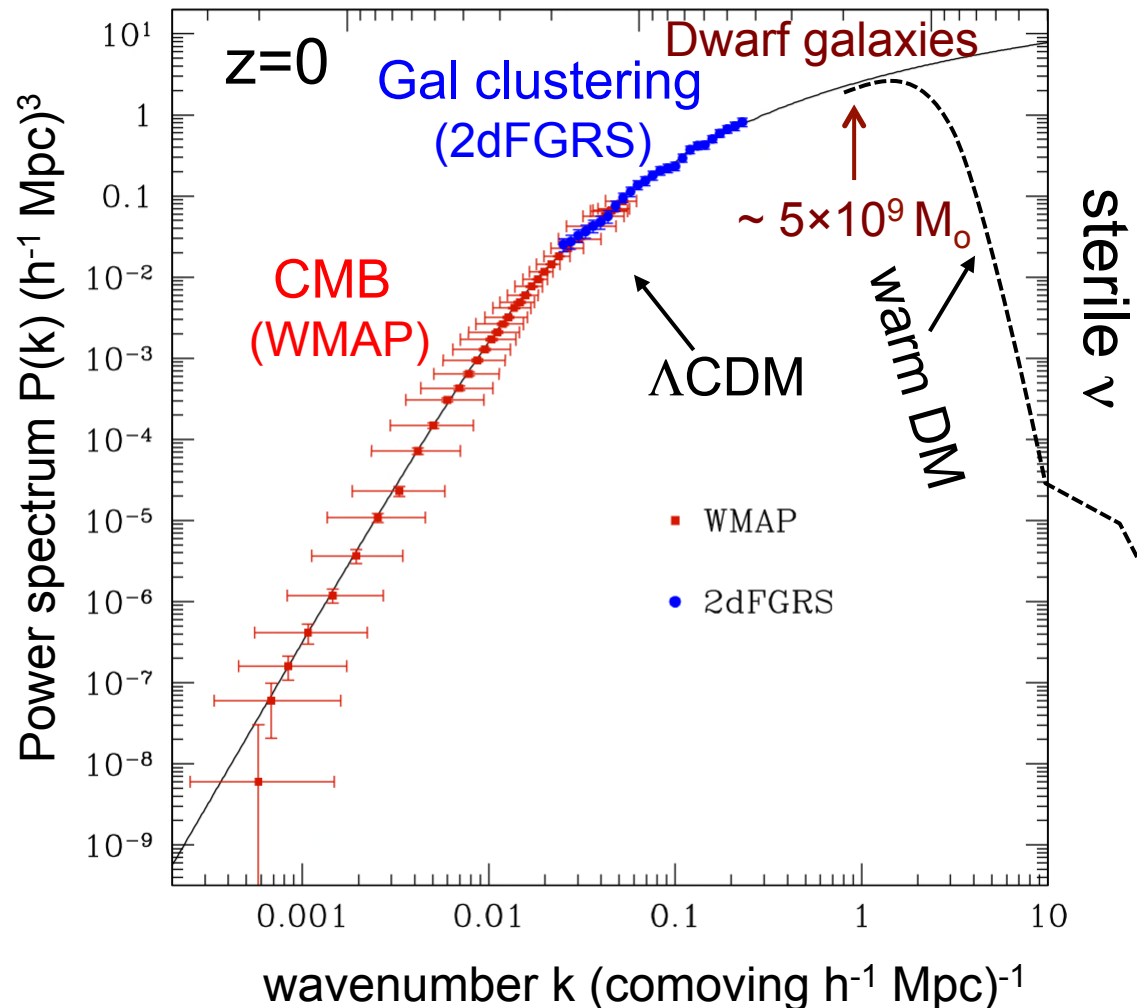
$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

Log $k^3 P(k)$ wavelength k^{-1} (comoving h^{-1} Mpc)



Sterile neutrinos

Explain:

- Neutrino oscillations and masses
- Baryogenesis
- Absence of right-handed neutrinos in standard model
- Dark matter

Sterile neutrino minimal standard model (ν MSM; Boyarski+ 09):

- Extension of SM w. 3 sterile neutrinos: 2 of GeV; 1 of keV mass
- If $\Omega_N = \Omega_{DM}$, 2 parameters: mass, lepton asymmetry/mixing angle
- GeV particles may be detected at CERN (SHiP)
- Dark matter candidate can be detected by X-ray decay



Both CDM & WDM compatible with CMB & galaxy clustering

Claims that both types of DM have been discovered:

- ◆ CDM: γ -ray excess from Galactic Center
- ◆ WDM (sterile ν): 3.5 X-ray keV line in galaxies and clusters

Cold dark matter

Annihilation radiation from the Galactic Centre?

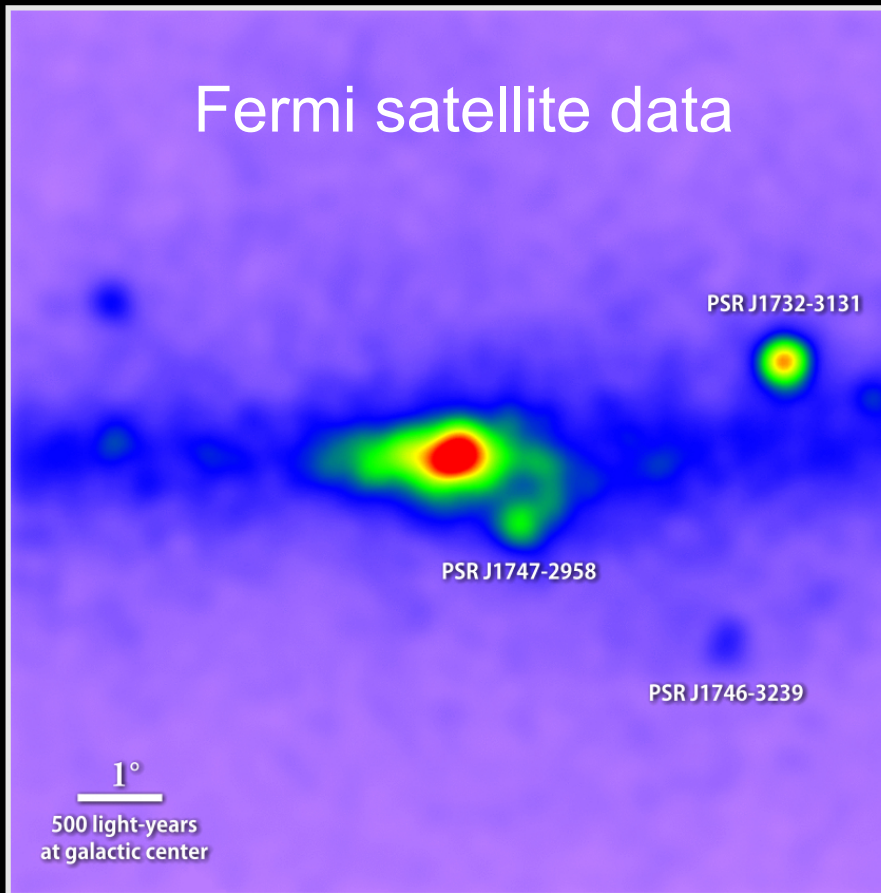
Cold dark matter

The Characterization of the Gamma-Ray Signal from the Central Milky Way: A Compelling Case for Annihilating Dark Matter

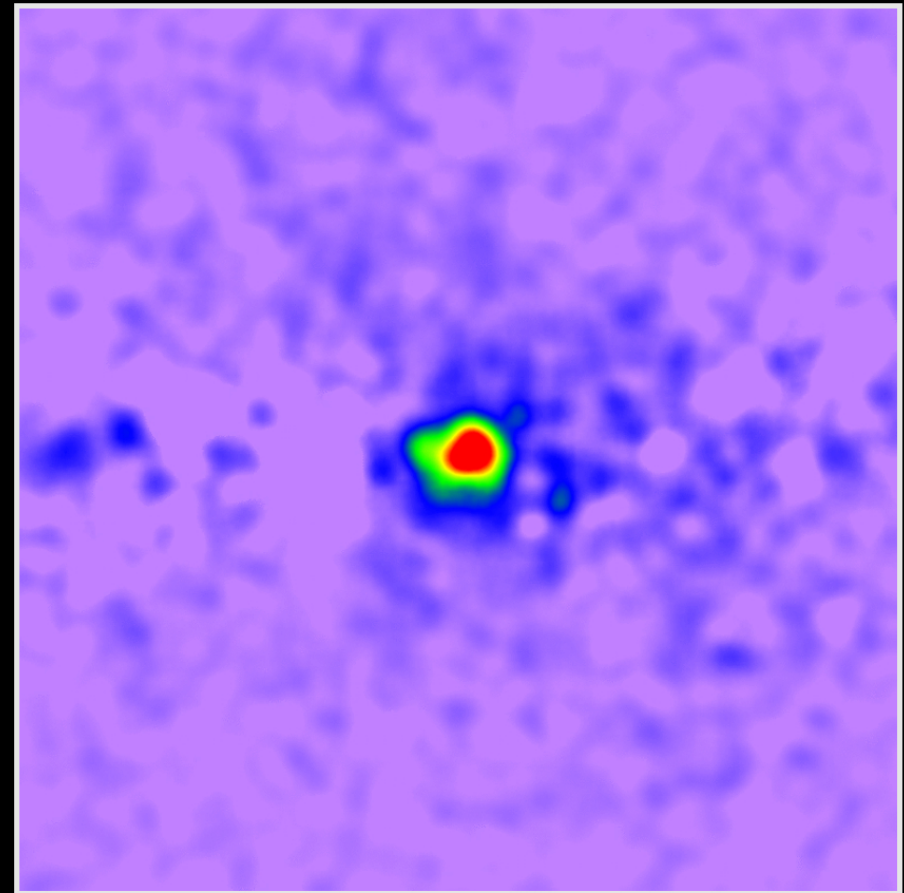
Tansu Daylan,¹ Douglas P. Finkbeiner,^{1,2} Dan Hooper,^{3,4} Tim Linden,⁵
Stephen K. N. Portillo,² Nicholas L. Rodd,⁶ and Tracy R. Slatyer^{6,7}

Uncovering a gamma-ray excess at the galactic center

Fermi satellite data



Unprocessed map of 1.0 to 3.16 GeV gamma rays



Known sources removed

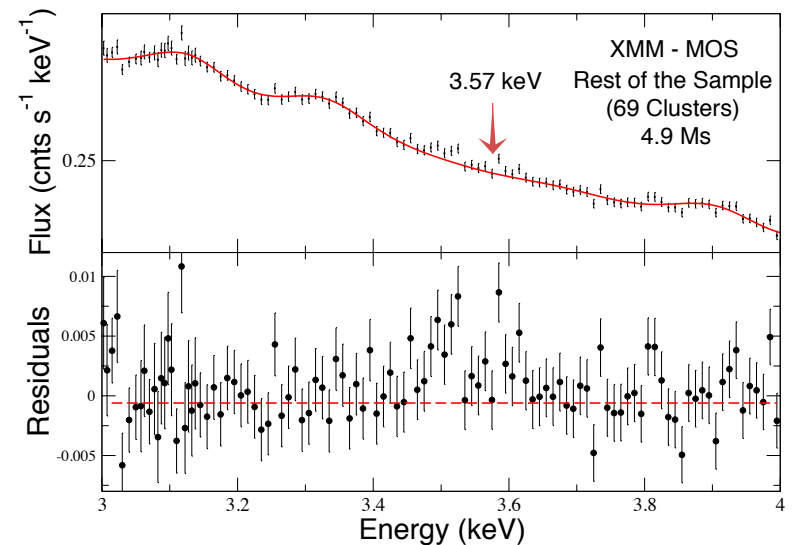
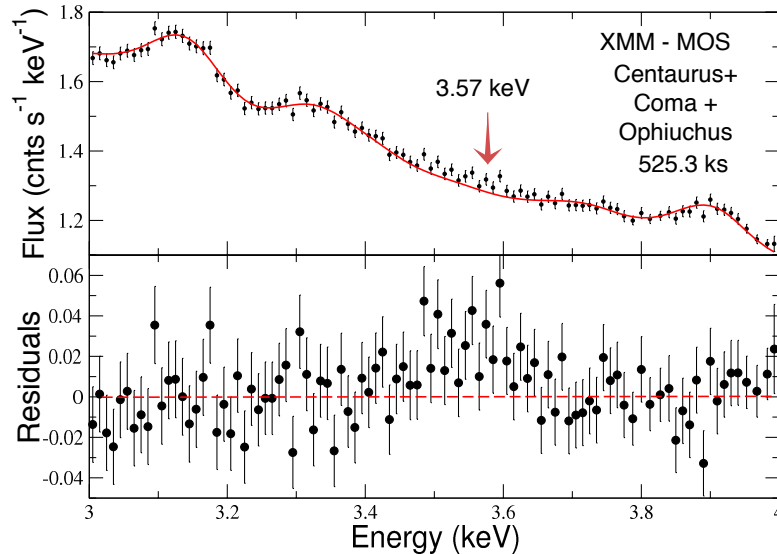
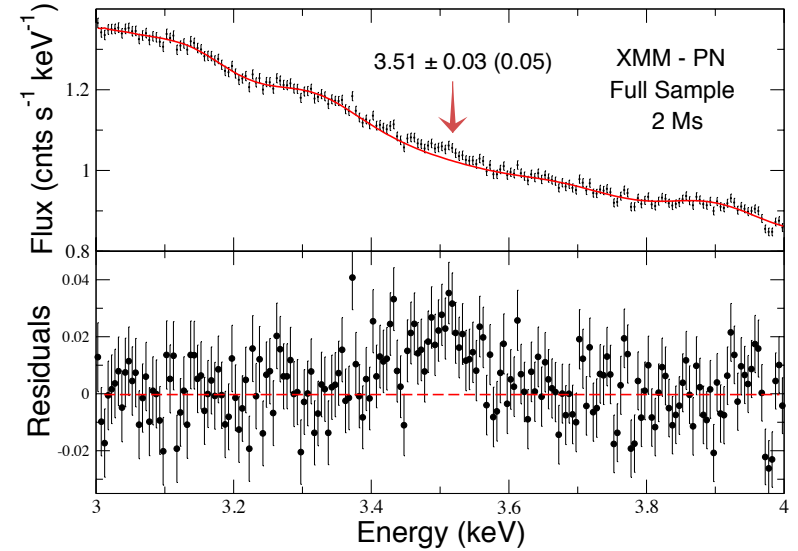
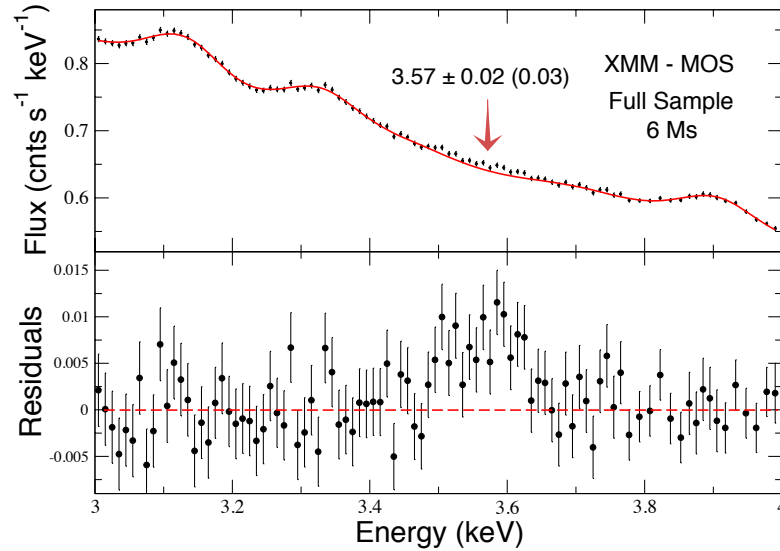
Warm dark matter

Decay line at 3.51 keV in galaxies and clusters

Warm dark matter WDM decay line in 69 stacked clusters?

$E=3.57$ keV

Bulbul et al. '14 See also Boyarsky et al. '14





Both CDM & WDM compatible with CMB & galaxy clustering

Claims that both types of DM have been discovered:

- ◆ CDM: γ -ray excess from Galactic Center
- ◆ WDM (sterile ν): 3.5 X-ray keV line in galaxies and clusters

Very unlikely that both are right!



The identity of the dark matter is encoded
in dwarf galaxies and in the halo of the MW
(strongly non-linear regime)

$z = 48.4$

$T = 0.05 \text{ Gyr}$

500 kpc

The image is a dark purple, noisy astronomical visualization. It features a horizontal scale bar at the bottom center, consisting of a white line with vertical end caps, labeled "500 kpc". The background is a mottled dark purple with some lighter, brownish-purple patches and significant pixel-level noise.



Cold Dark Matter

Warm Dark Matter

13.4 billion years ago

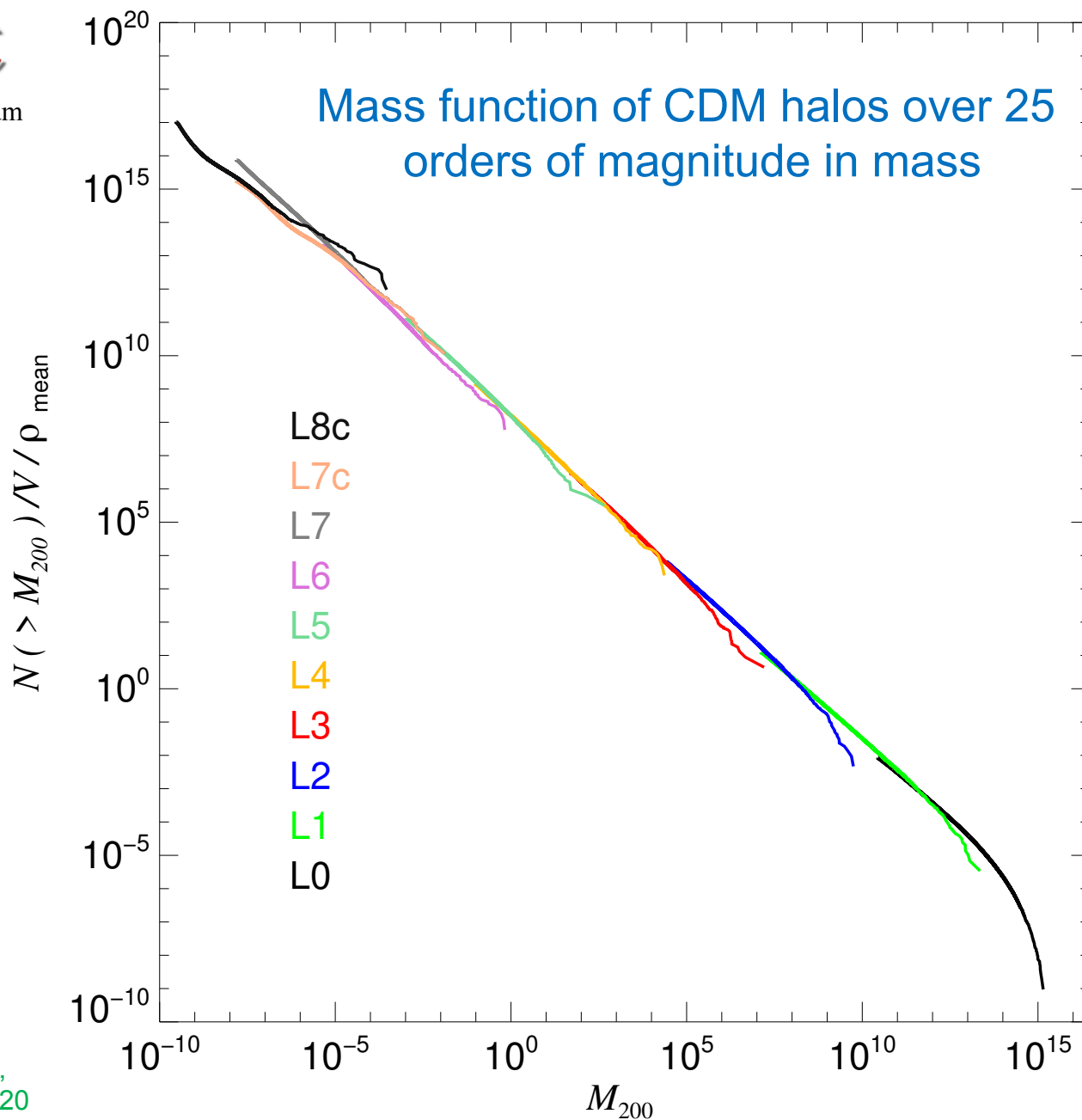
cold dark matter



warm dark matter



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12



The subhalo mass function

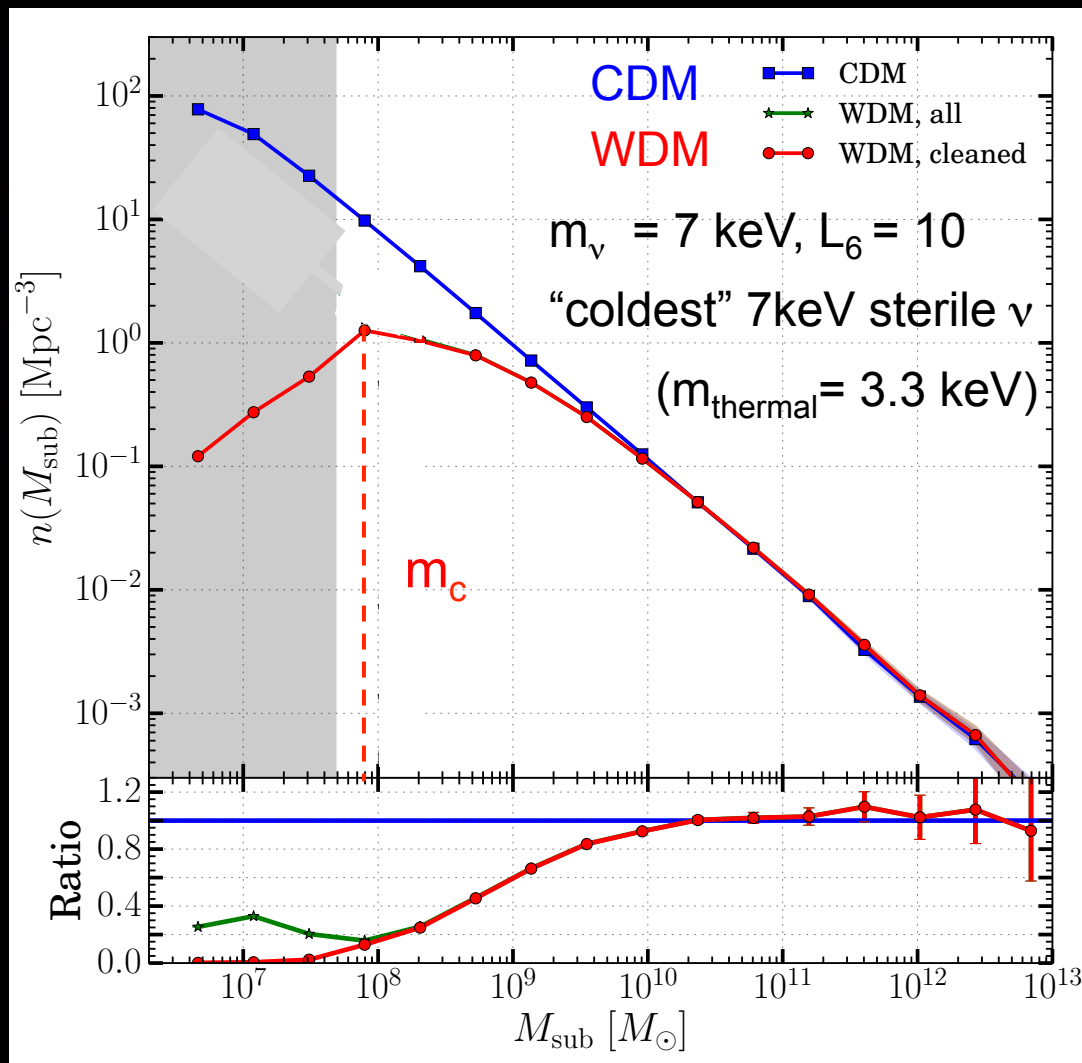


CDM

WDM

3 x fewer WDM subhalos at $3 \times 10^9 M_\odot$

10 x fewer at $10^8 M_\odot$



How can we distinguish the two?

Astrophysical tests of dark matter

Count the number of small-mass halos

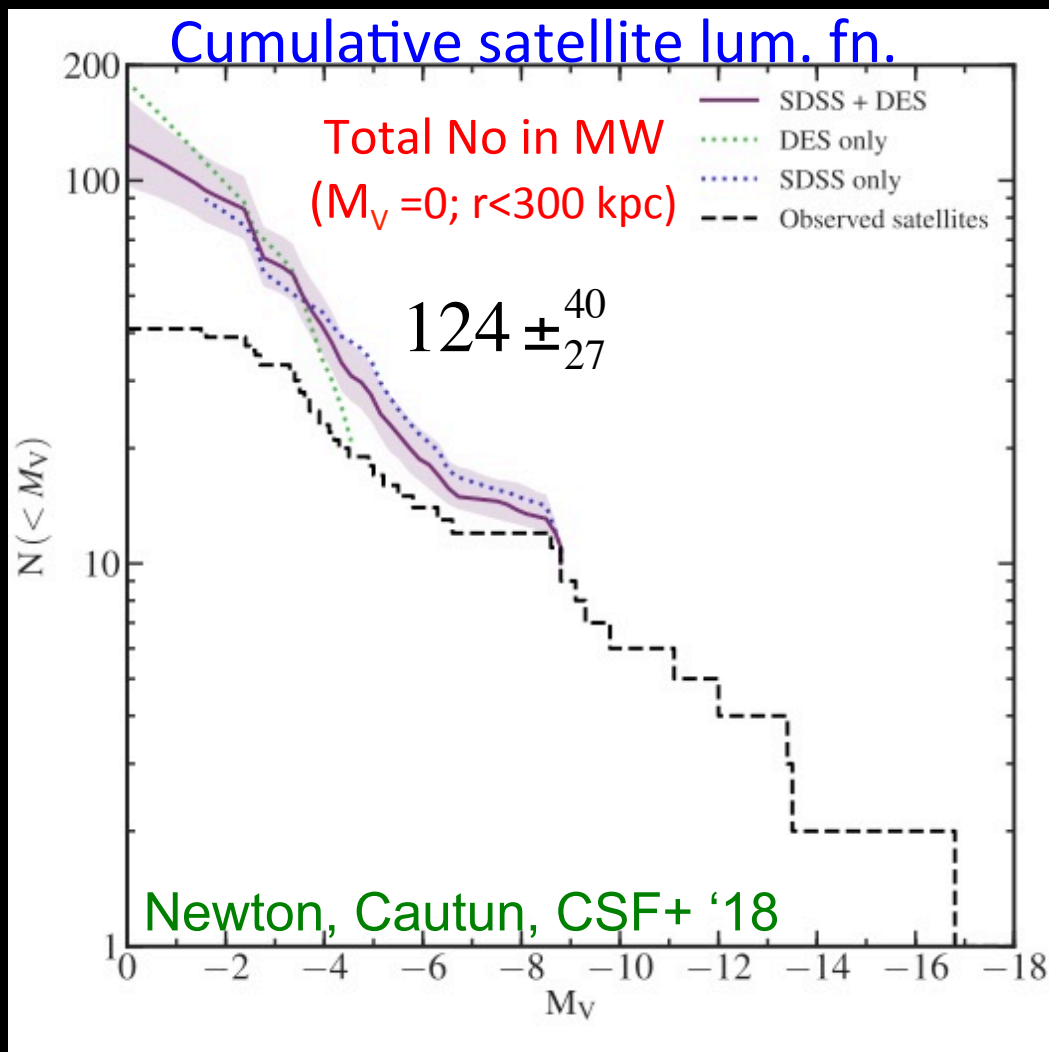
1. Number of dark matter halos (the halos mass fn.)
(the ``missing satellites problem)
2. Annihilation/decay radiation

Let's begin by counting what we can see



The satellites of the Milky Way

In the MW: ~ 55 satellites discovered so far

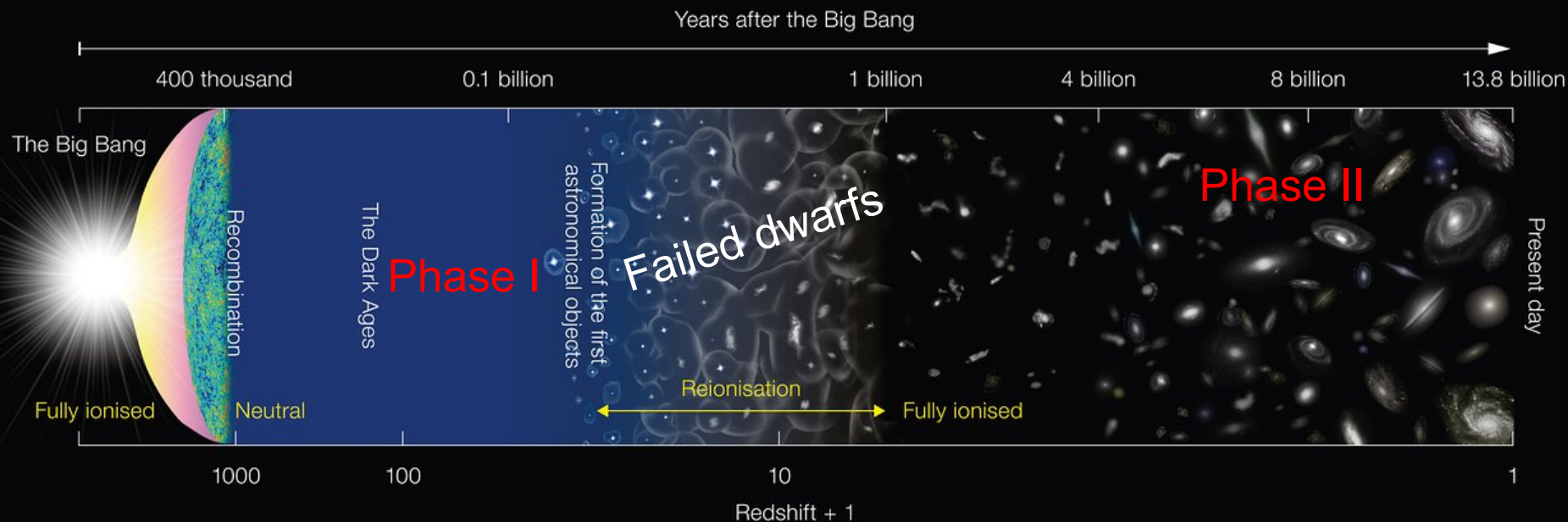


Most subhalos never make a galaxy!

“Missing satellites” problem:

CDM predicts many more subhalos in the Milky Way than there are observed satellites

The two phases of galaxy formation



Phase I: During the “dark ages” H gas is neutral
First stars reionize H and heat it up to 10^4K

Phase II: H Gas is ionized ($T_{\text{vir}} > 10^4\text{K}$ form)

A galaxy formation primer

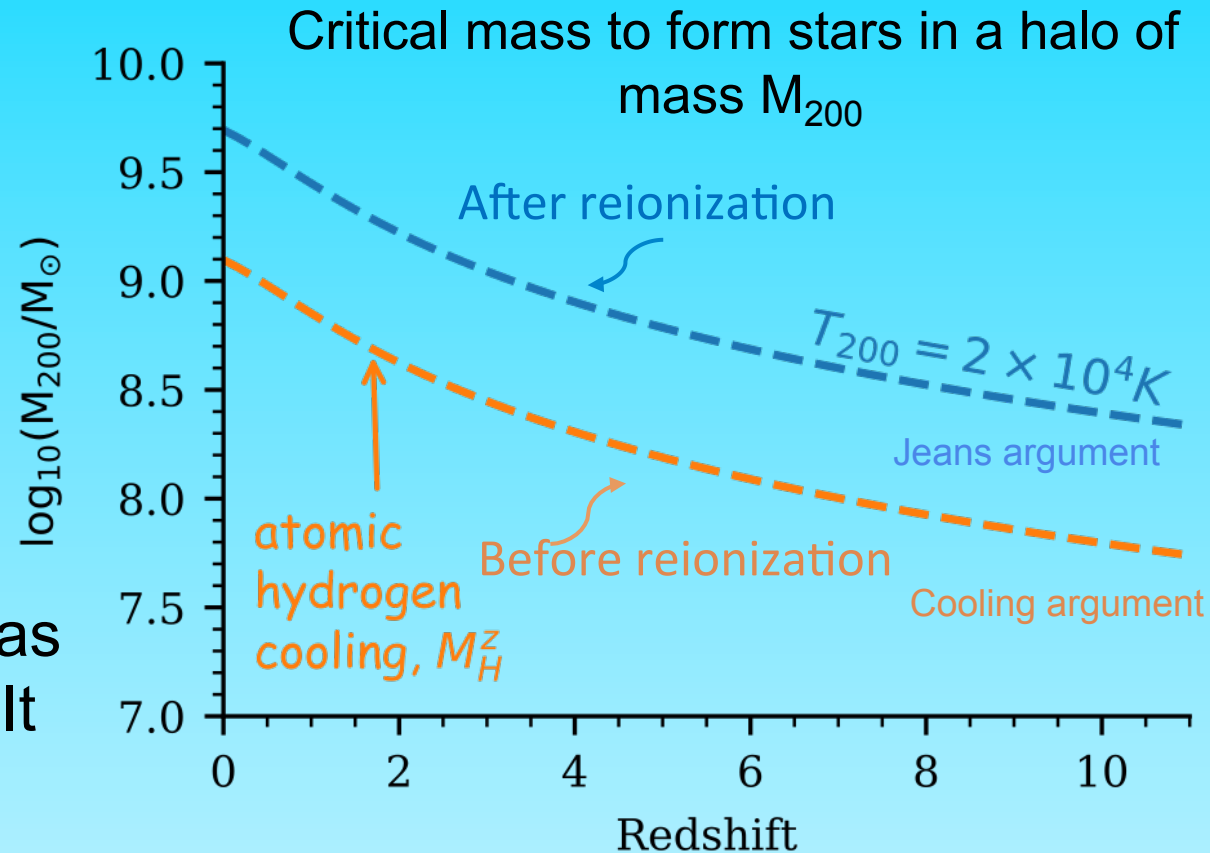
1. Before reionization, stars can only form if gas can cool for which

→ $T > 7000 \text{ K}$

$$M_H^z \sim (4 \times 10^7 M_\odot) \left(\frac{1+z}{11} \right)^{-3/2}$$

2. After H reionization, gas is heated to $T = 2 \times 10^4 \text{ K}$. It can only cool and form stars in halos with:

$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$



Benitez-Llambay & CSF '20

A galaxy formation primer

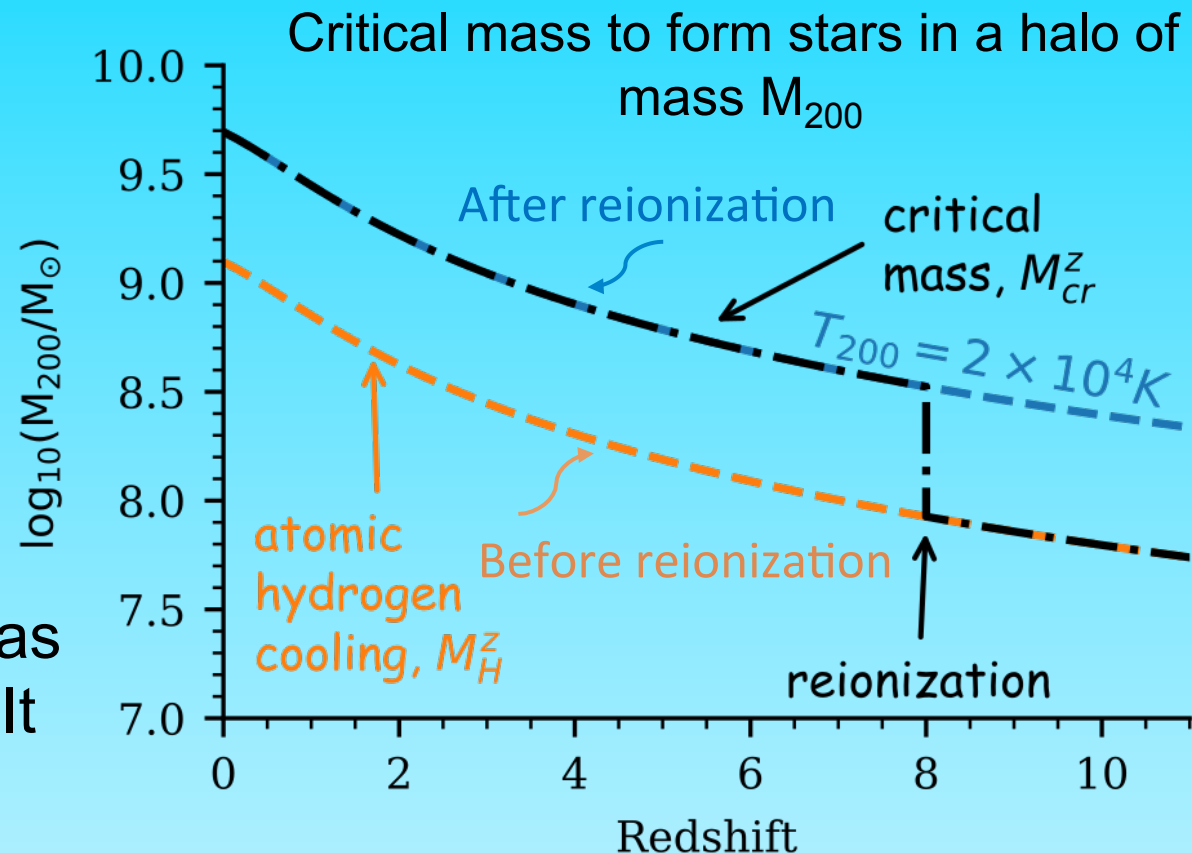
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$$\rightarrow T > 7000 \text{ K}$$

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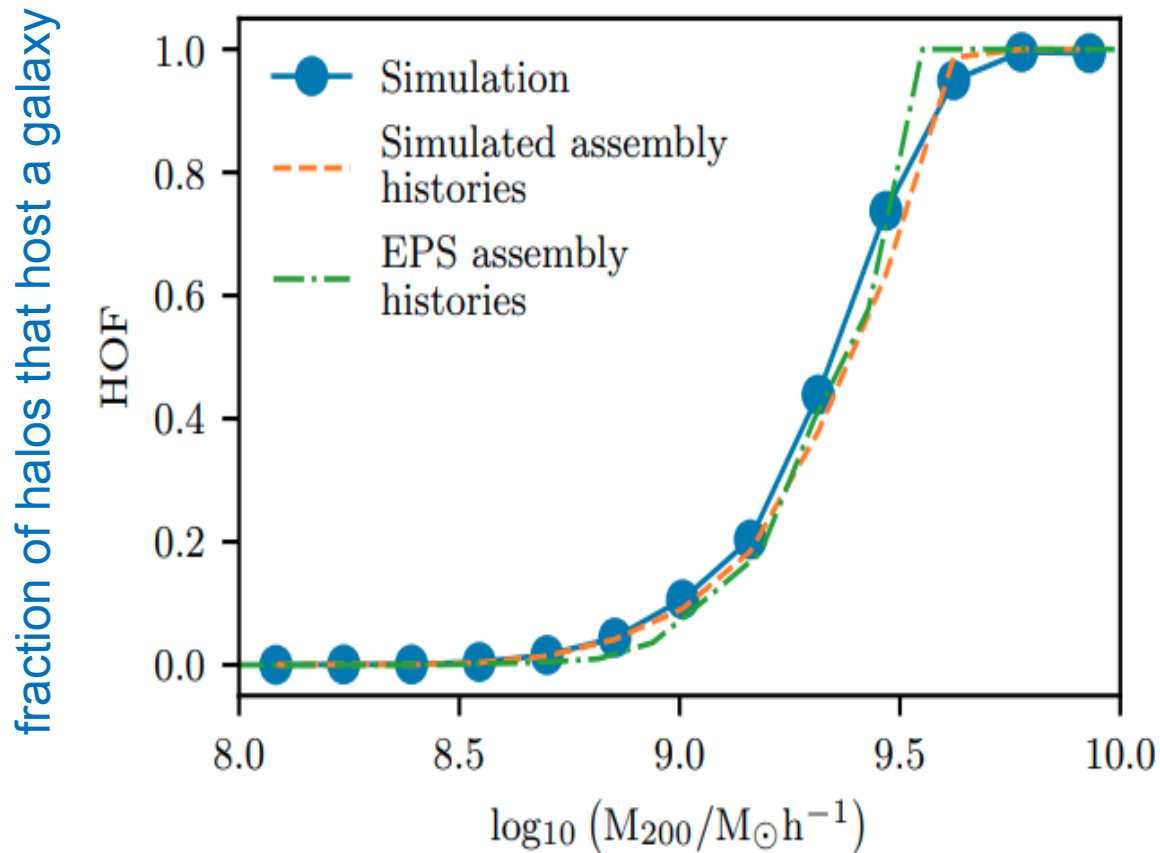
$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$

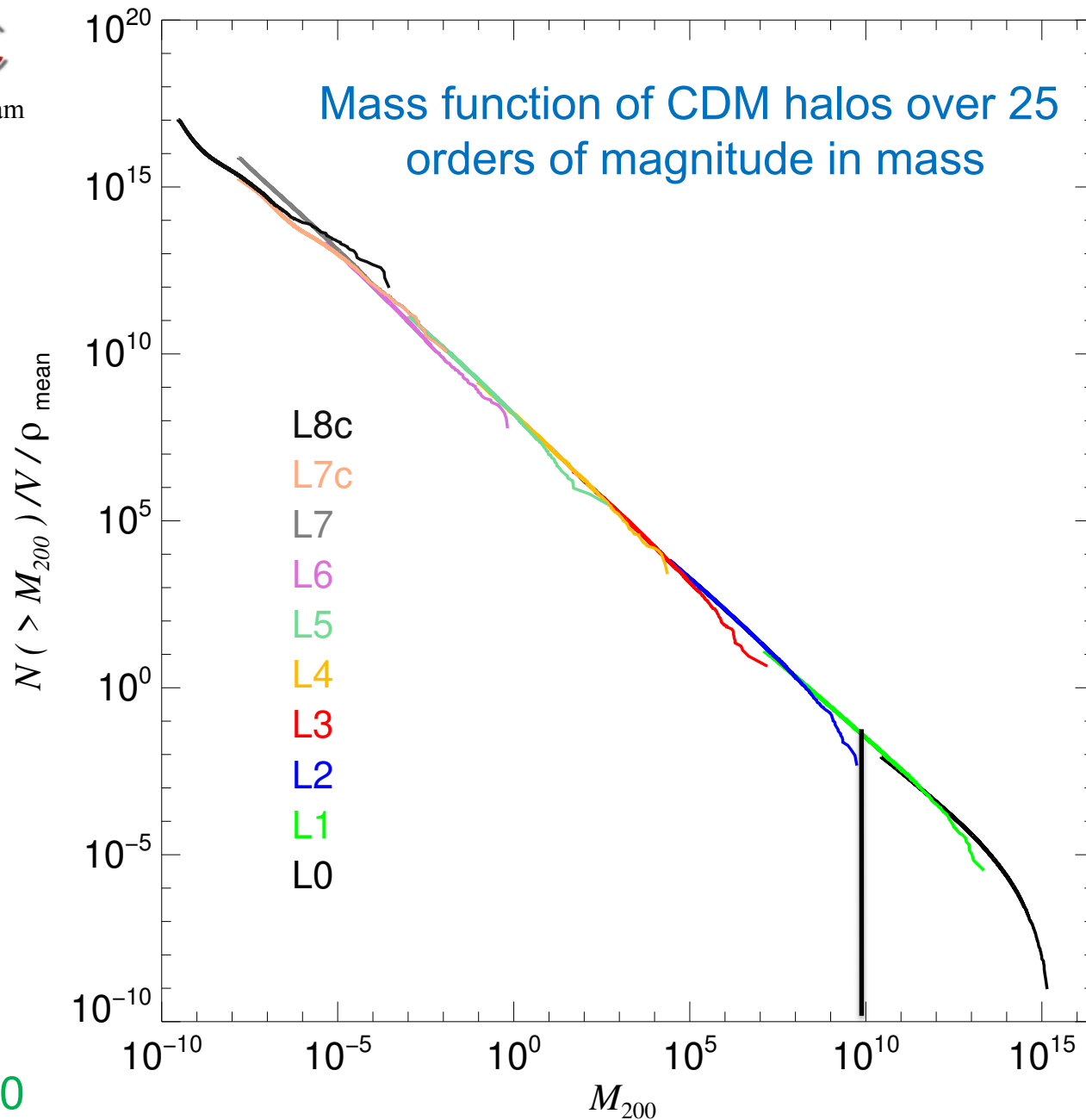


Benitez-Llambay & CSF '20

A galaxy formation primer

Halo Occupation Fraction (HOF): fraction of halos of a given mass that host a galaxy



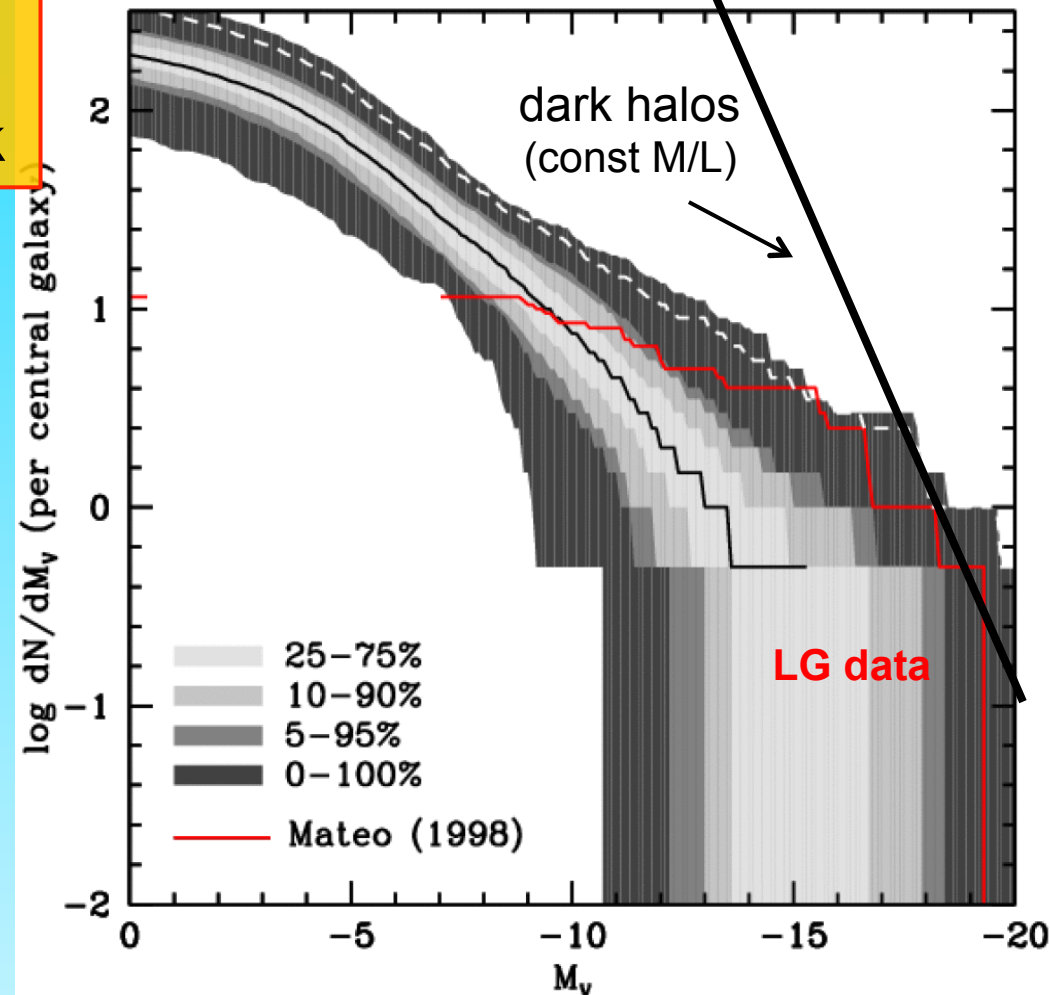


Wang et al '20

Luminosity Function of Local Group Satellites

Semi-analytic model of galaxy formation including effects of reionization and SN feedback

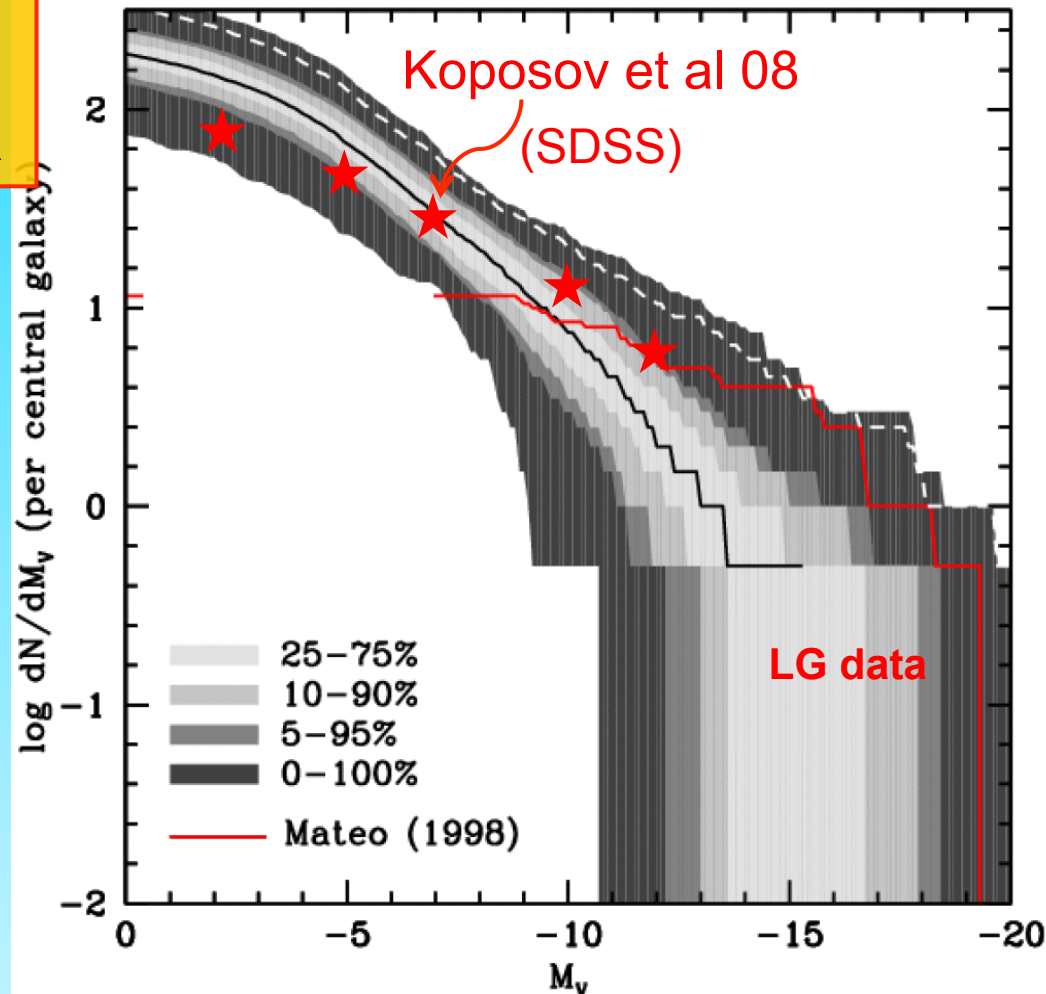
- Median model → correct abundance of sats brighter than $M_V = -9$ ($V_{\text{cir}} > 12$ km/s)
- Model predicts many, as yet undiscovered, faint satellites



Luminosity Function of Local Group Satellites

Semi-analytic model of galaxy formation including effects of reionization and SN feedback

- Median model → correct abundance of sats brighter than $M_V = -9$ ($V_{\text{cir}} > 12$ km/s)
- Model predicts many, as yet undiscovered, faint satellites



VIRGO

icc.dur.ac.uk/Eagle

“Evolution and assembly of galaxies and
their environment”

THE EAGLE PROJECT

Virgo Consortium

Durham: Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

Leiden: Rob Crain, Joop Schaye.

Other: Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...

VIRG

Dark matter

APOSTLE
EAGLE full
hydro
simulations

Local Group

CDM

Sawala, CSF
et al '16



Stars

VIRG

APOSTLE
EAGLE full
hydro
simulations

Local Group

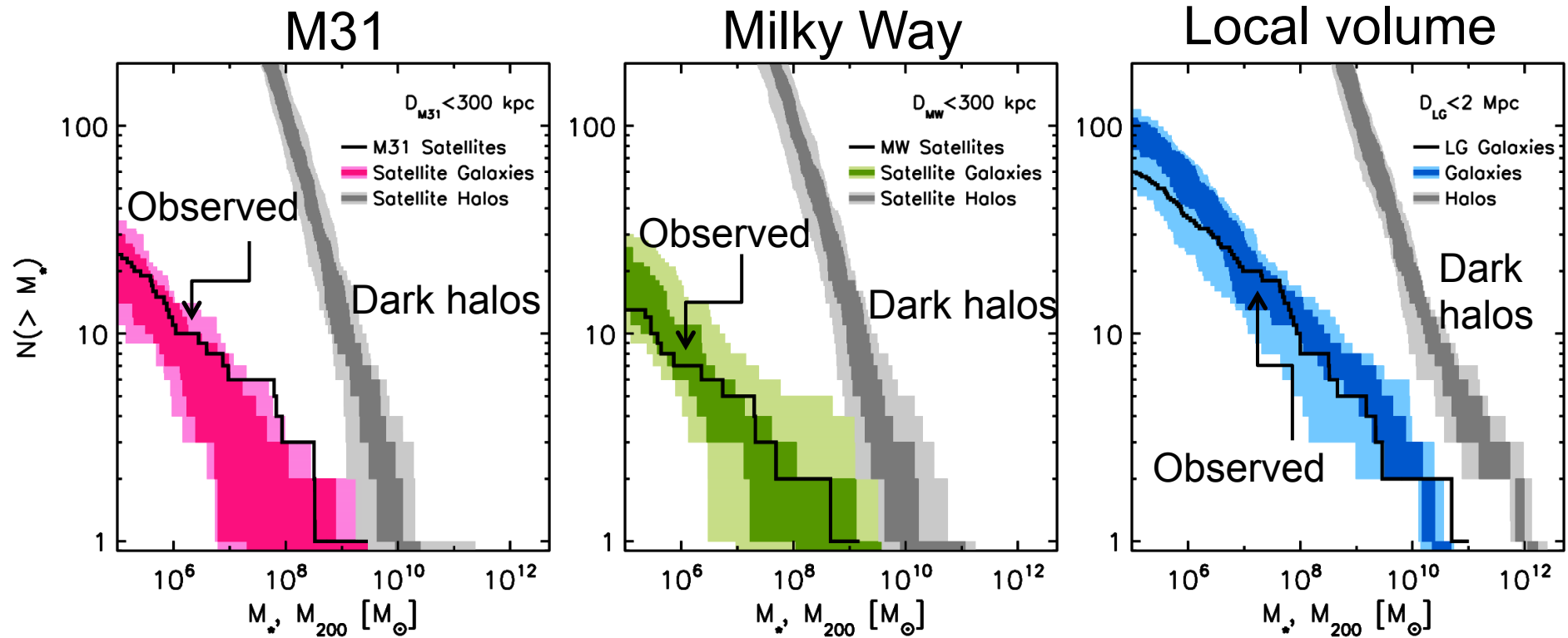
Stars

Far fewer satellite galaxies than CDM halos

Sawala, CSF
et al '16



EAGLE Local Group simulation



When galaxy formation is taken
into account



CDM predicts the observed
abundance of satellites

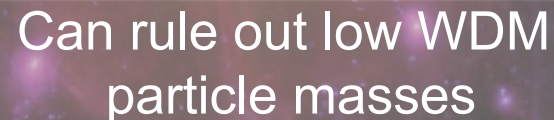
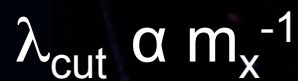


There is **no** such thing as a “**missing
satellite problem**” in CDM!



Dark matter subhalos in WDM

(a few tens)

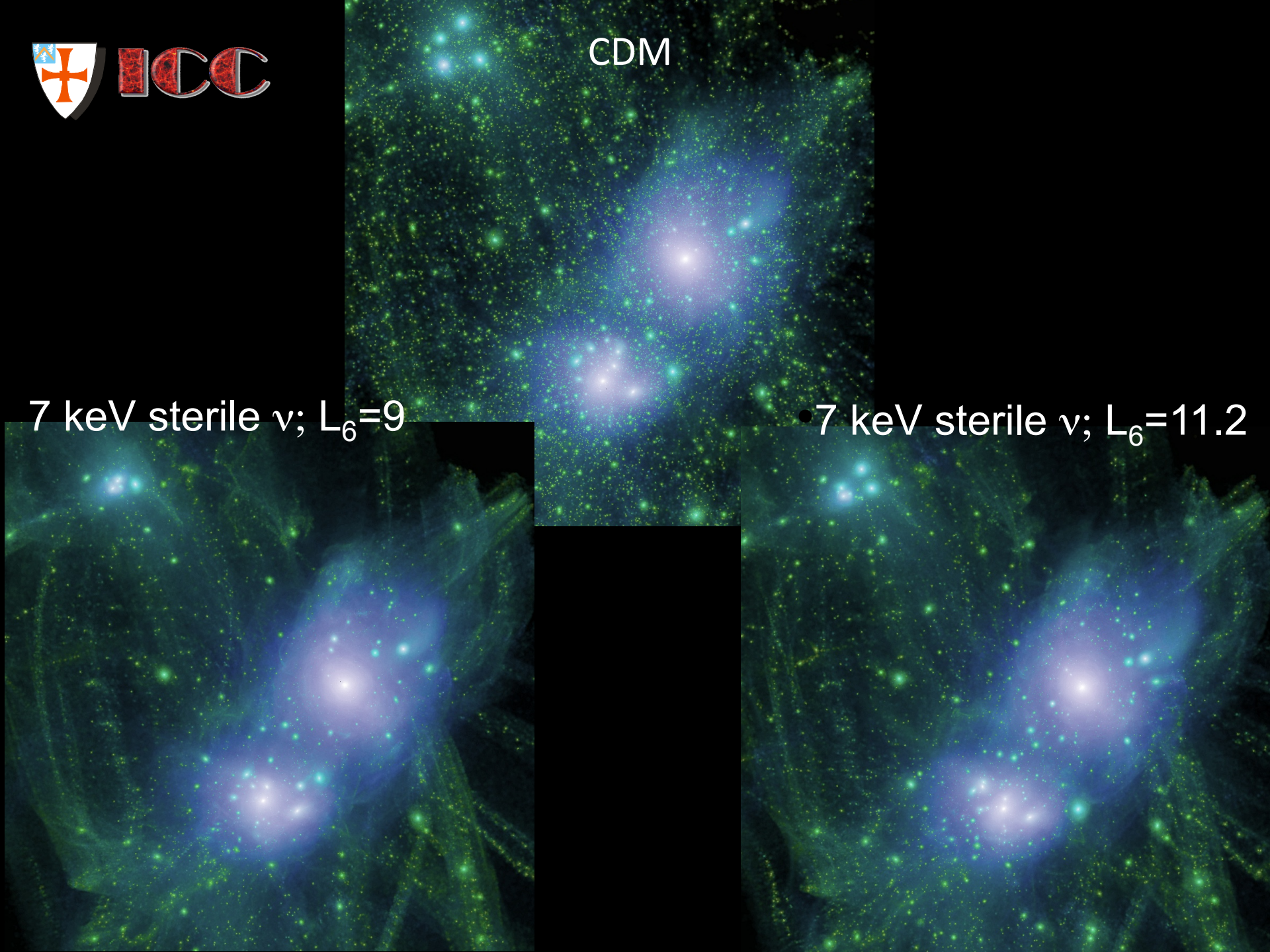




CDM

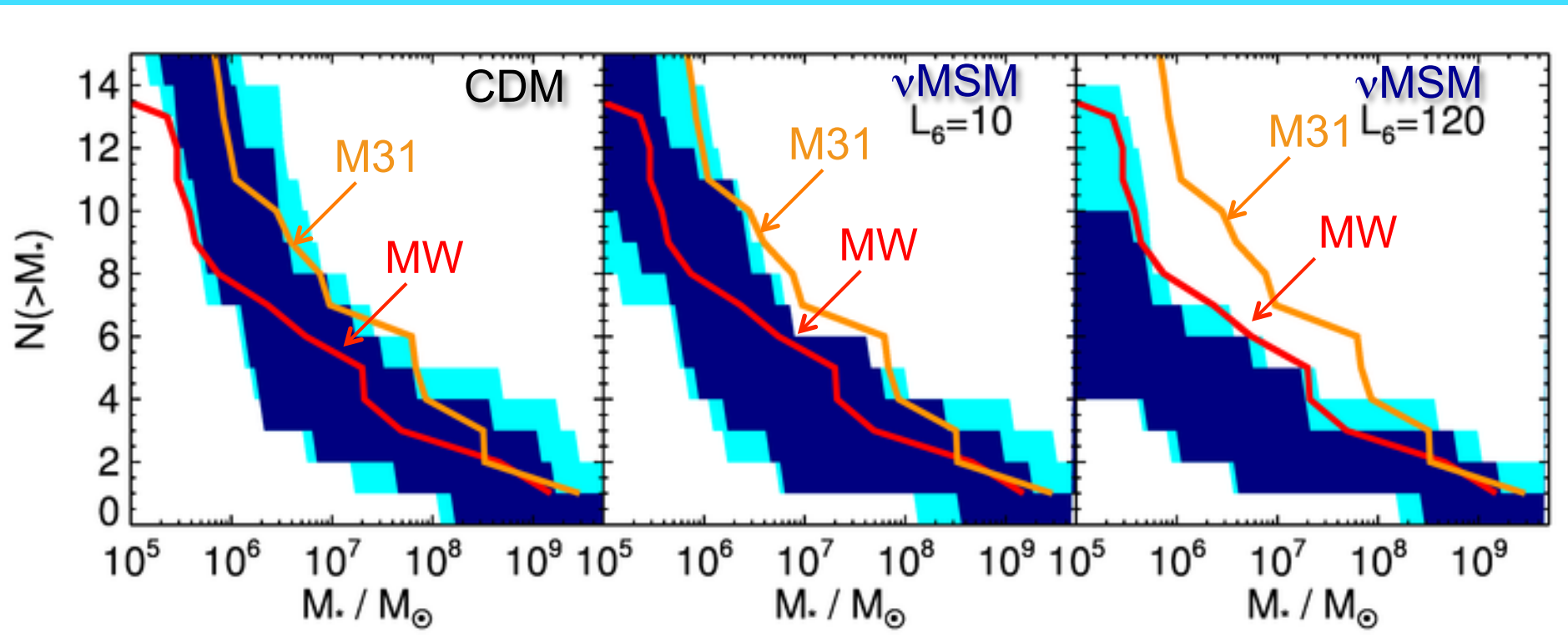
7 keV sterile ν ; $L_6=9$

• 7 keV sterile ν ; $L_6=11.2$



Luminosity Function of Local Group Satellites in WDM

From “Warm Apostle:” 7keV sterile ν $M_h \sim 10^{12} M_\odot$



Lovell et al. '16



Can we distinguish CDM/WDM?

cold dark matter

warm dark matter

Rather than counting faint galaxies,
count the number of dark halos
("failed dwarfs")



Can we count dark haloes?

cold dark matter

warm dark matter

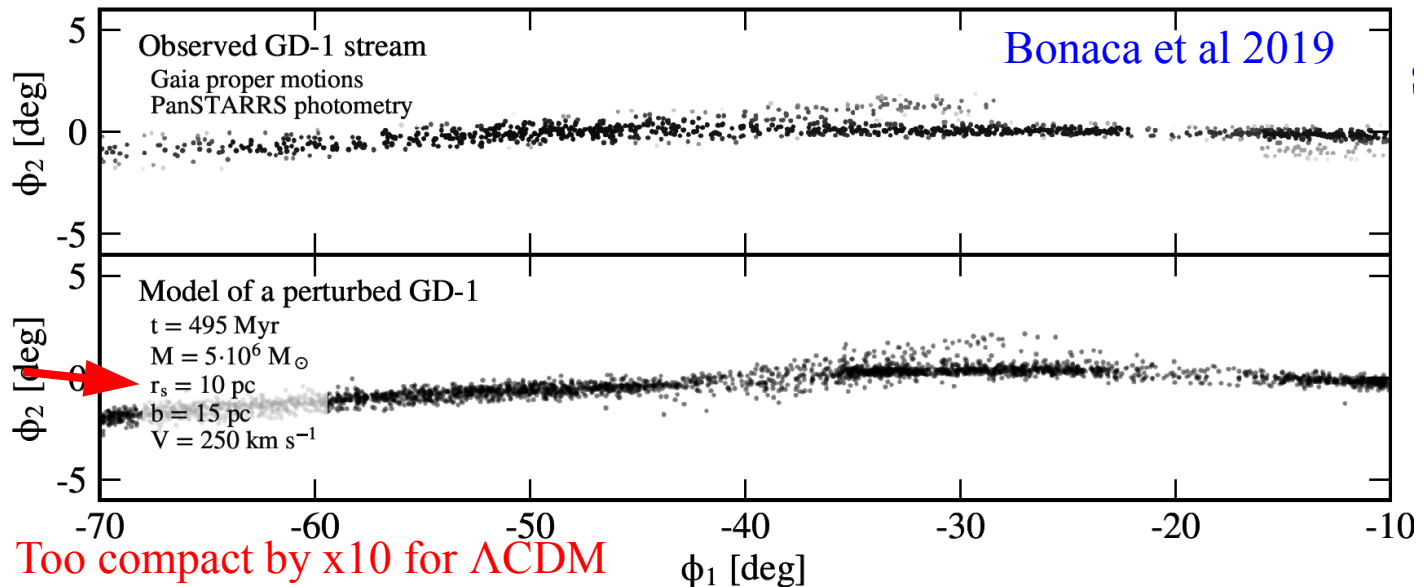
Three ways to detect small CDM halos

1. Gaps in streams
2. Gravitational lensing
3. Annihilation radiation

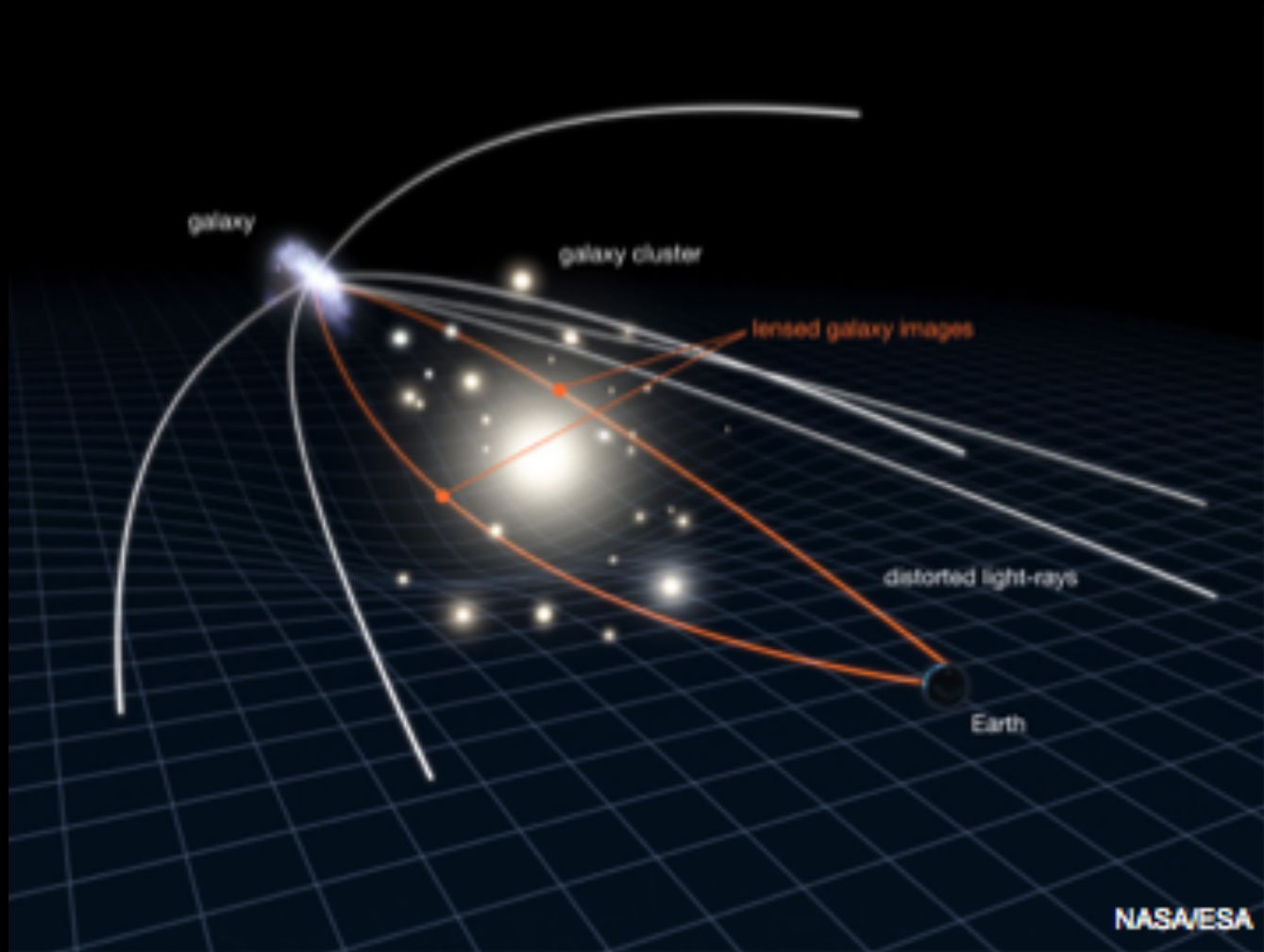
Gaps in tidal streams

Cold tidal streams (e.g. from globular clusters) in the MW halo can be perturbed by passing subhalos

Perturbations are significant and could be created by encounter with object of mass $\sim 10^7 M_\odot$ object



Gravitational lensing: Einstein rings

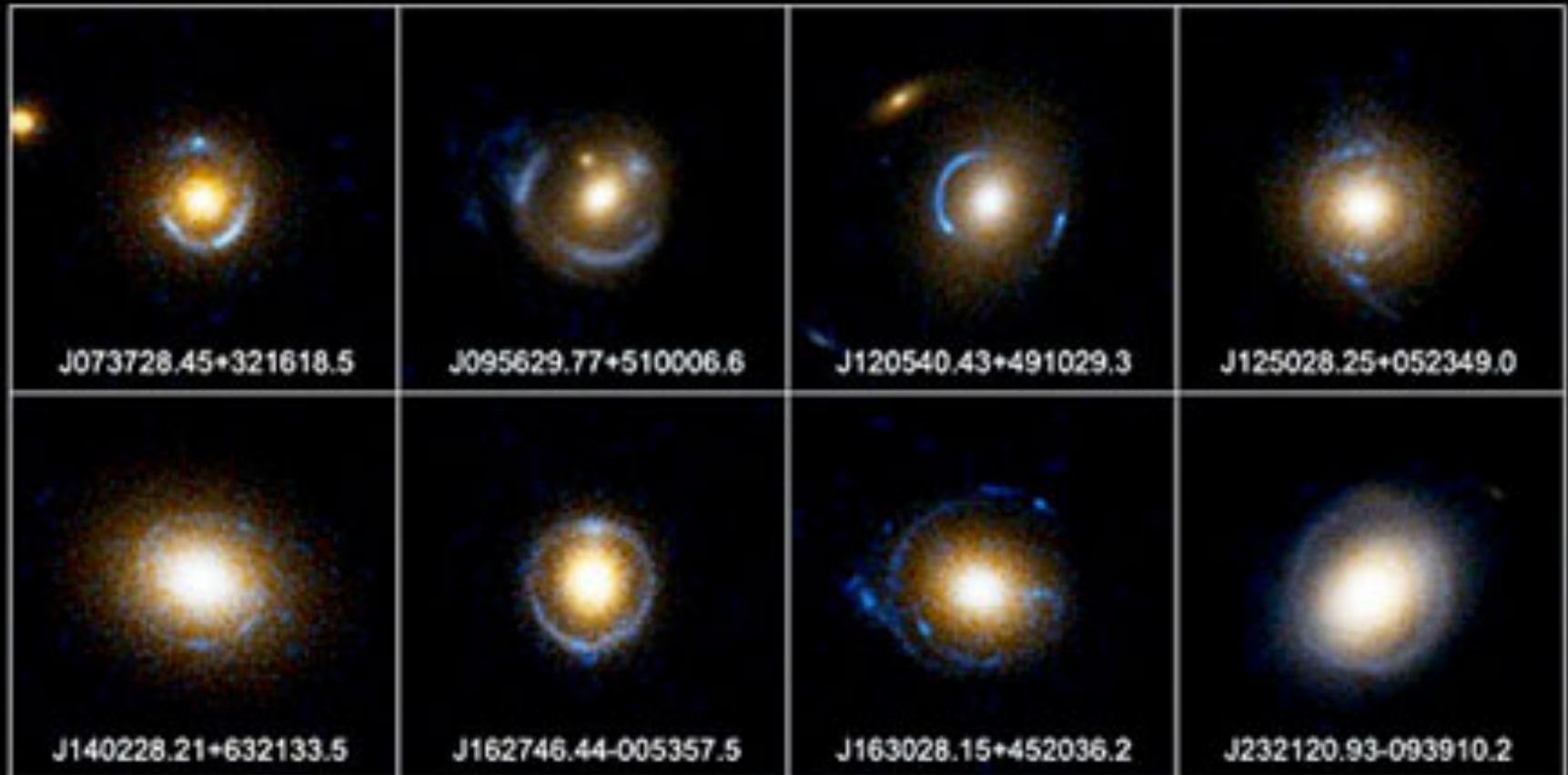


When the source and the lens are well aligned → strong arc or an Einstein ring

SLAC sample of strong lenses

Einstein Ring Gravitational Lenses

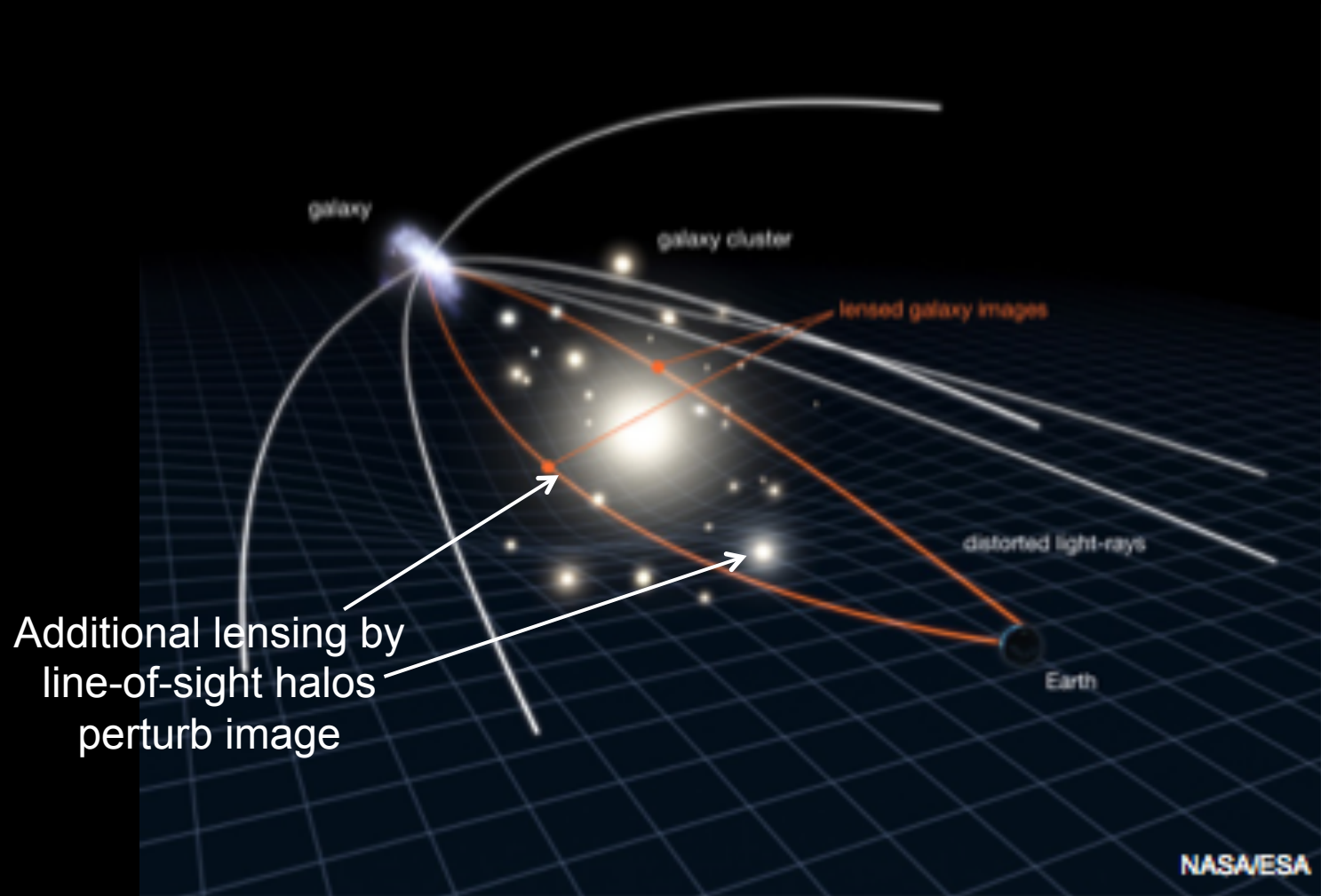
Hubble Space Telescope • ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

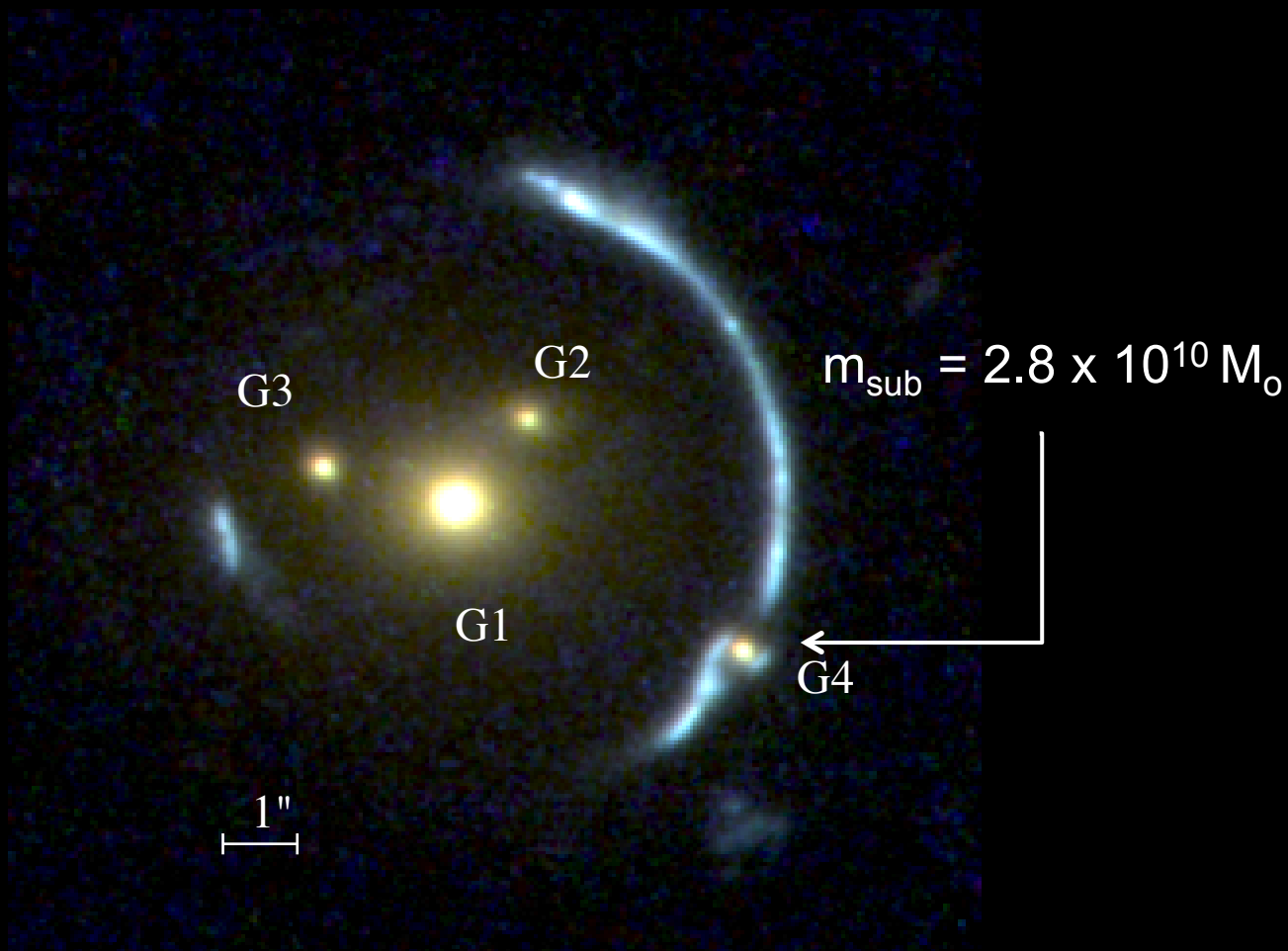
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image

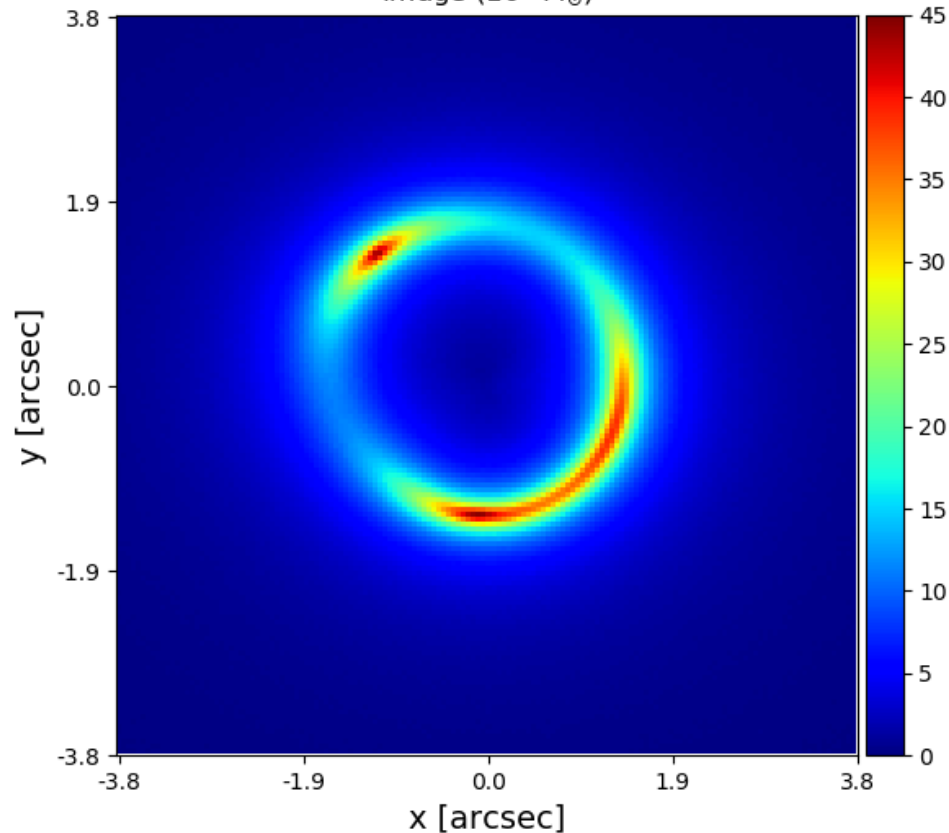


Strong lensing: detecting small halos

HST “data”: $z_{\text{source}}=1$; $z_{\text{lens}}=0.2$ $10^7 M_{\odot}$ halo – **NOT** so easy to spot

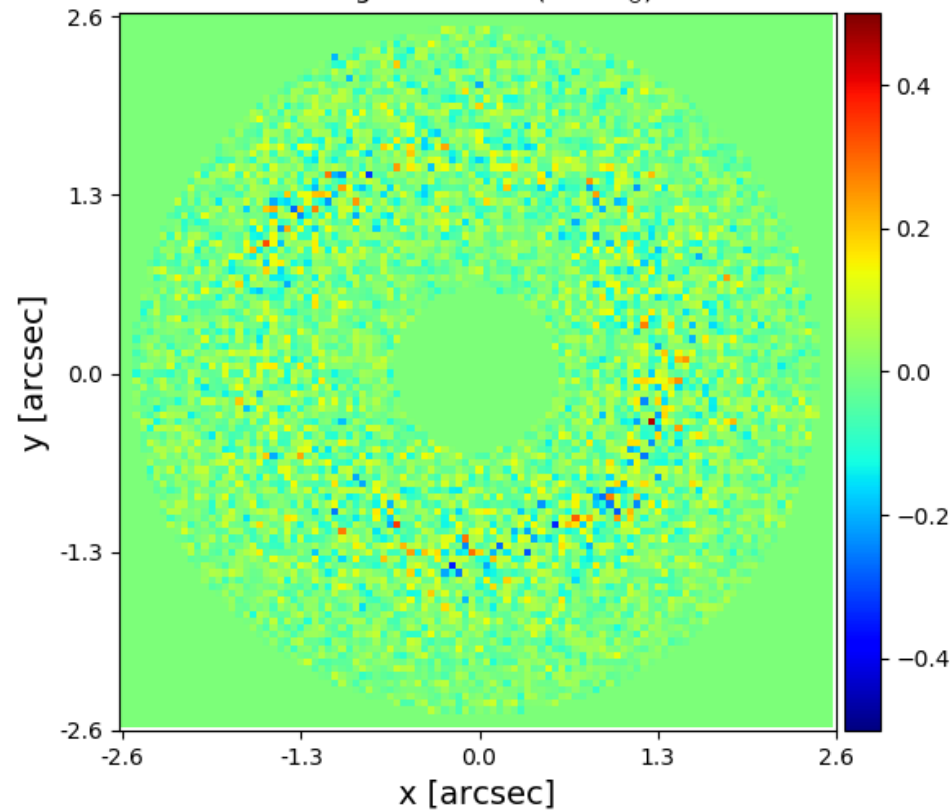
Image

Image ($10^7 M_{\odot}$)

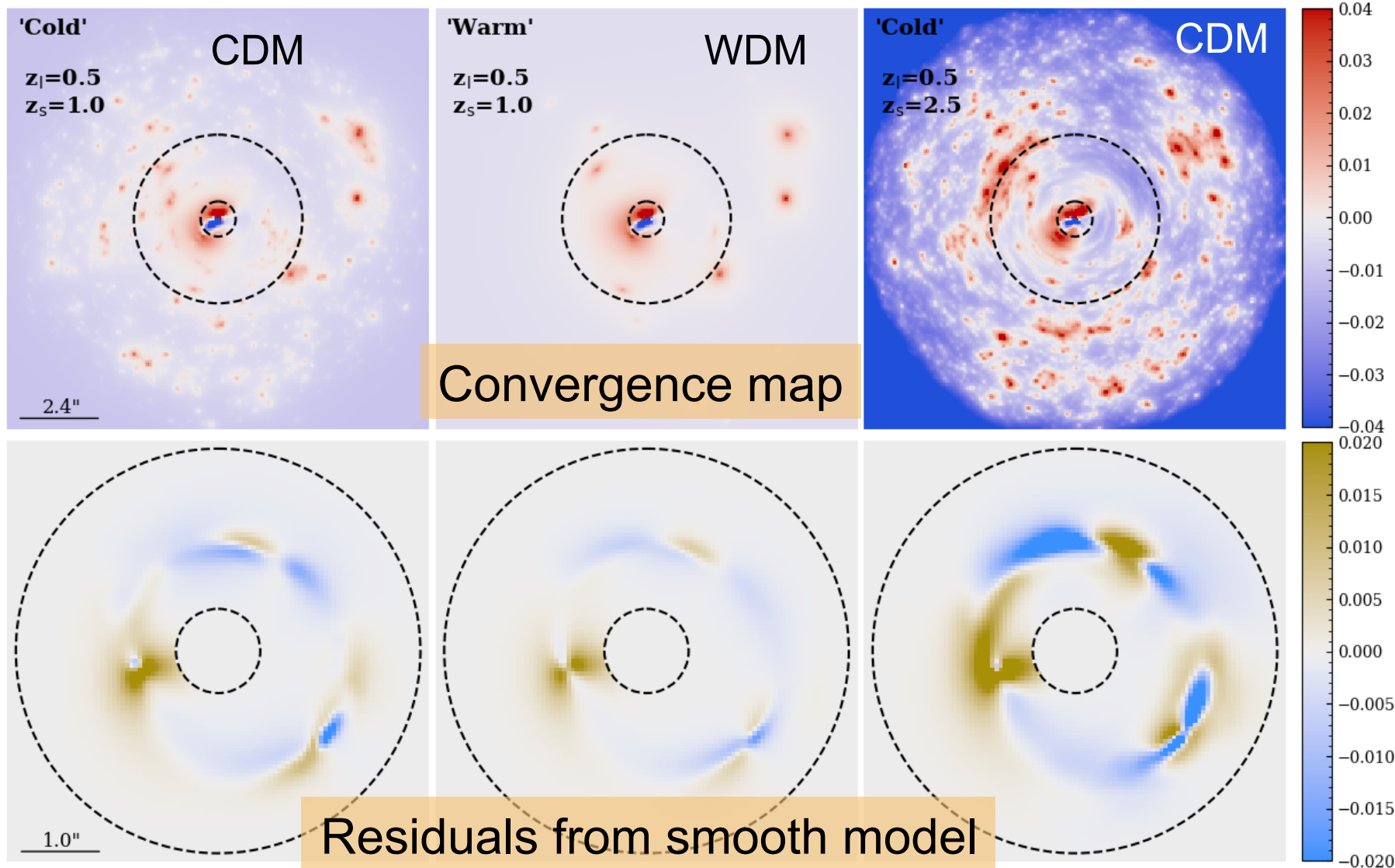


Residuals

Image Residuals ($10^7 M_{\odot}$)

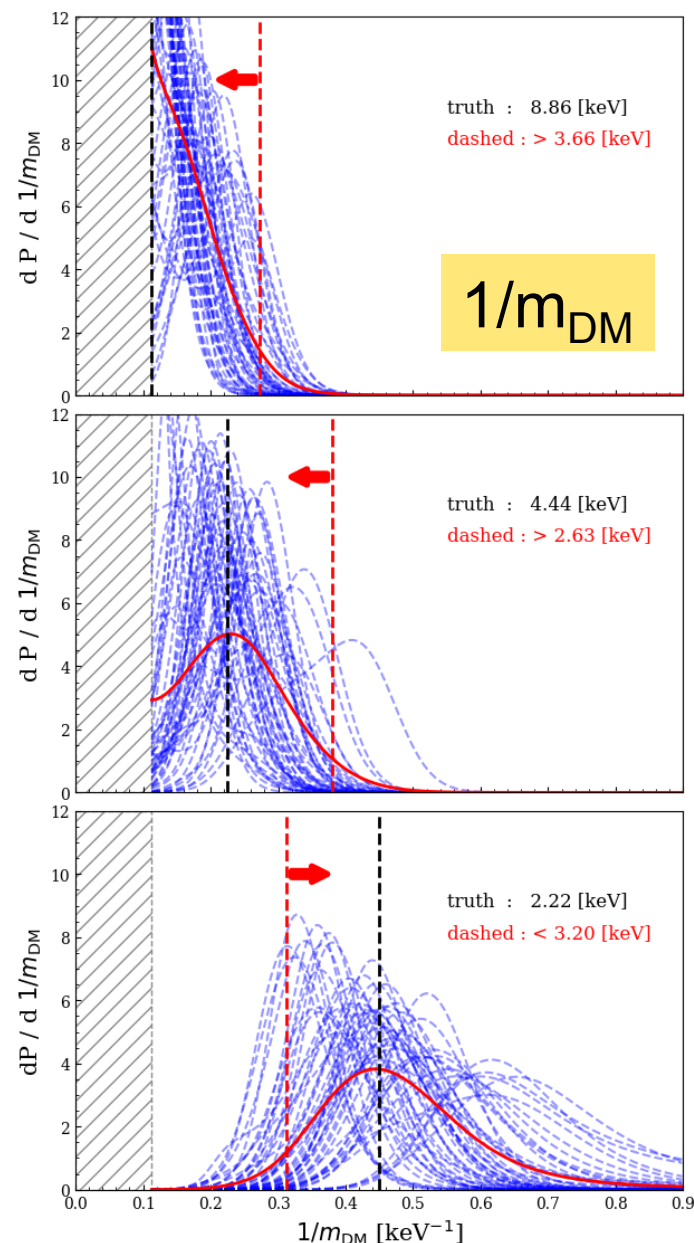
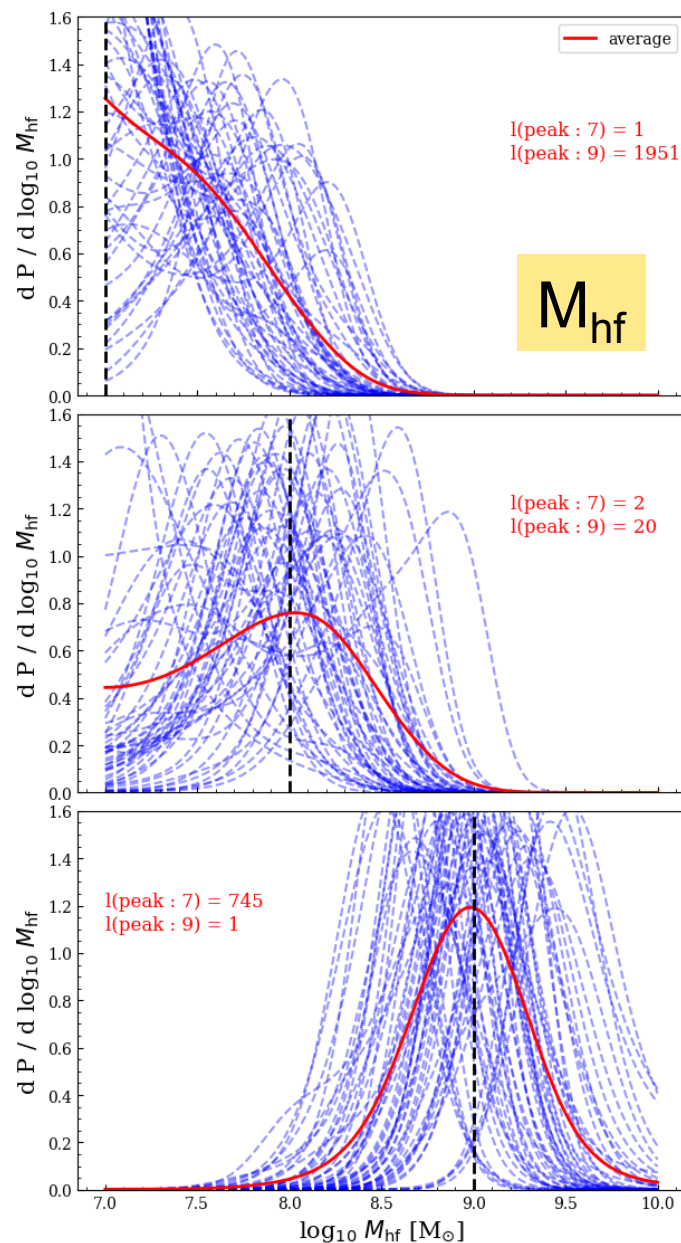


Strong lensing: detecting small halos



Strong lensing: detecting small halos

Posterior distributions (mock observations) for power spectrum of residuals

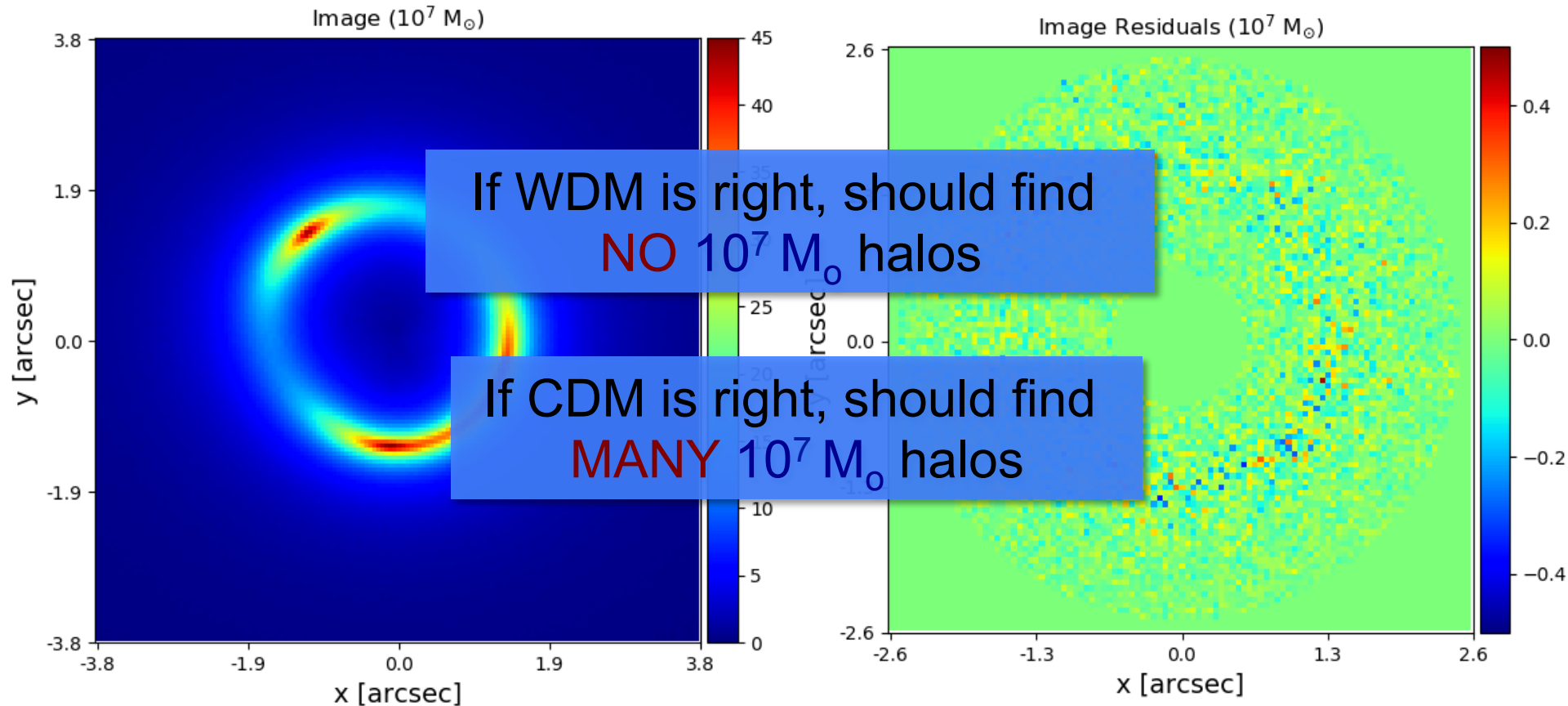


Constraints from forward modelling of 50 systems

He et al. '20

Detecting halos w. strong lensing

Can detect halos as small as $10^7 - 10^8 M_\odot$



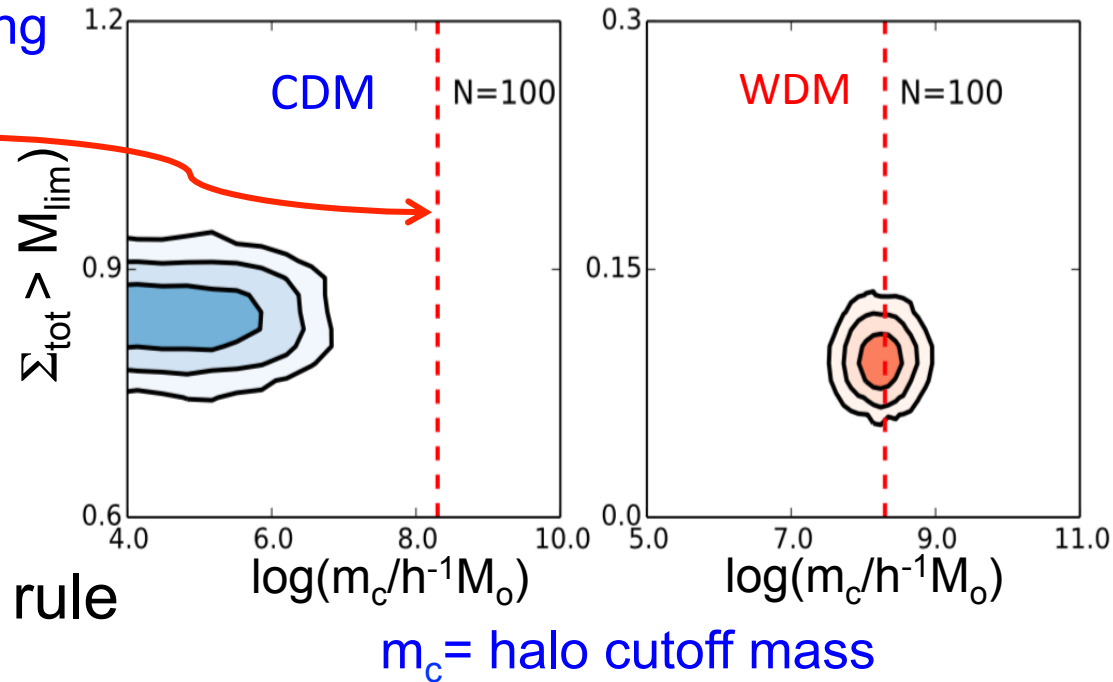
Detecting substructures with strong lensing

Σ_{tot} = projected halo number density within Einstein ring

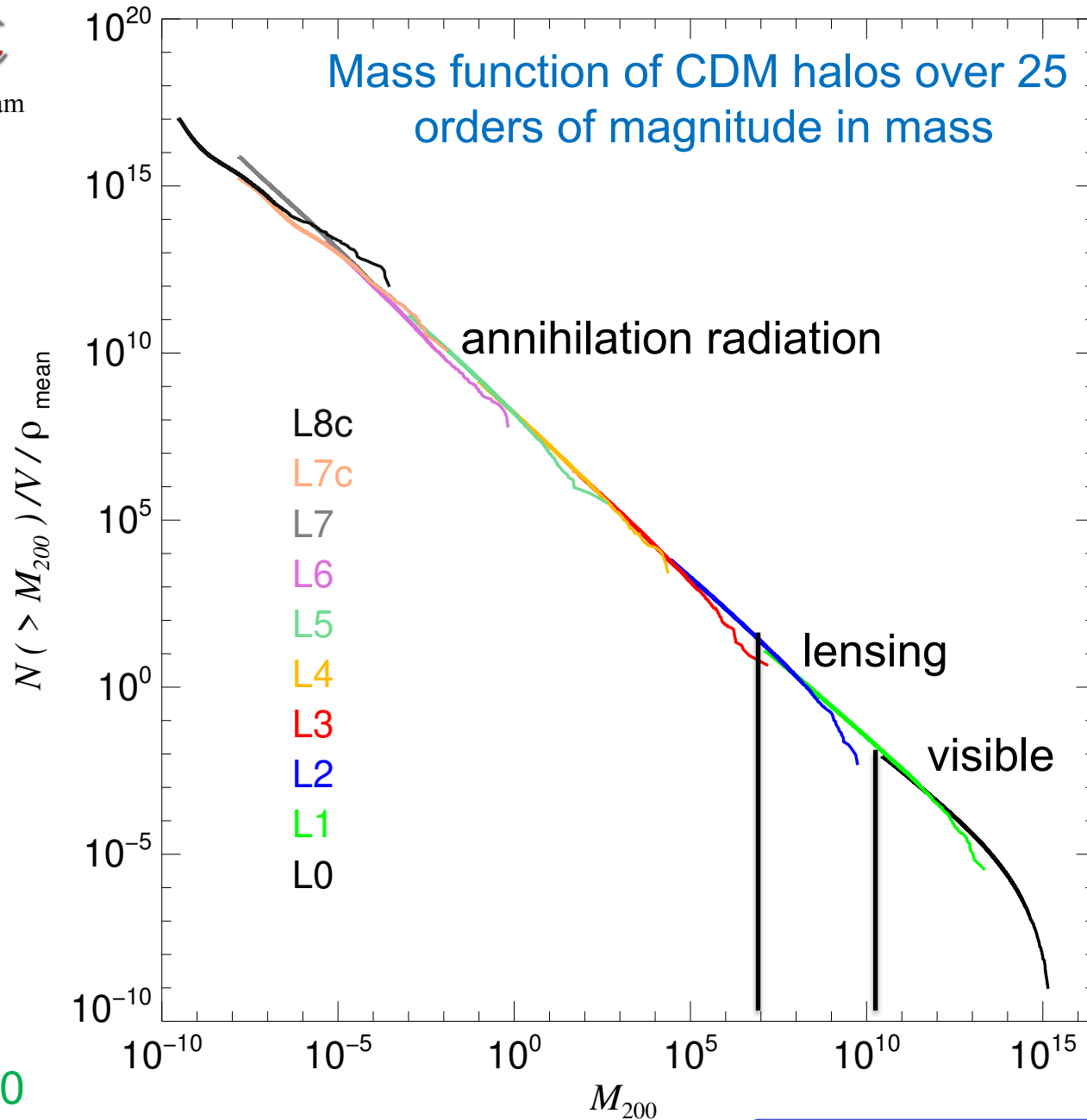
Detection limit = $10^7 h^{-1} M_{\odot}$

$m_c = 1.3 \times 10^8 h^{-1} M_{\odot}$ for coldest 7 keV sterile neutrino

100 Einstein ring systems and detection limit: $m_{\text{low}} = 10^7 h^{-1} M_{\odot}$



- If DM is 7 keV sterile $\nu \rightarrow$ rule out **CDM** at $>3\sigma$!
- If DM is CDM \rightarrow rule out 7 keV **sterile ν** at many σ





Can we count dark haloes?

cold dark matter

warm dark matter

Three ways to detect small CDM halos

1. Gaps in streams
2. Gravitational lensing
3. Annihilation radiation

Indirect CDM detection through annihilation radiation

Supersymmetric particles are Majorana particles → **annihilate** into Standard Model particles (including **γ -rays**)

Intensity of annihilation radiation at x is:

$$I(x) = \frac{1}{8\pi} \sum_f \frac{dN_f}{dE} \langle \sigma_f v \rangle \int_{los} \left(\frac{\rho_\chi}{M_\chi} \right)^2 dl$$

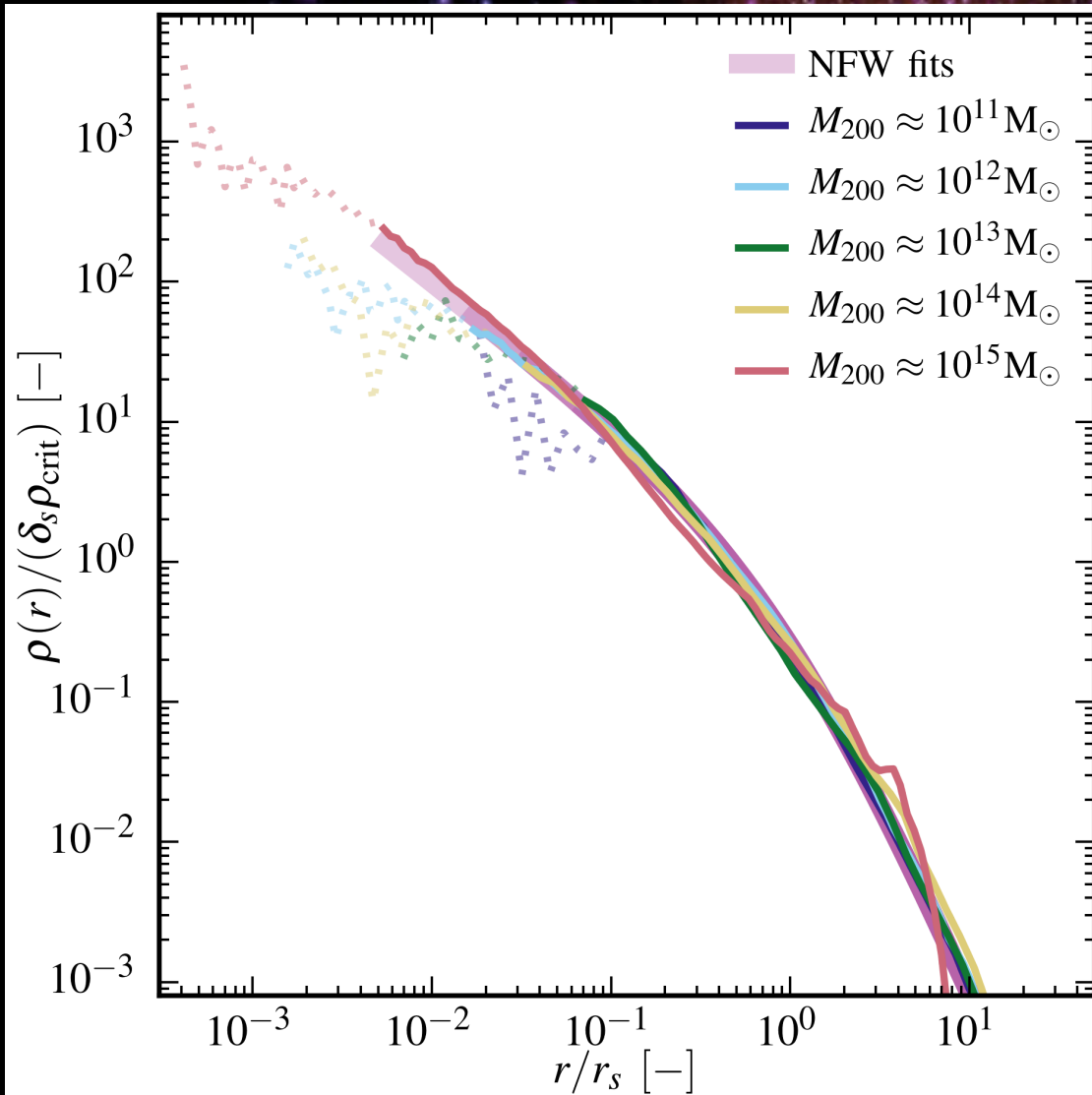
↑ cross-section (particle physics)
↓ halo density at x (astrophysics)

$\langle \sigma v \rangle = 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ → relic abundance in simple SUSY models

⇒ Theoretical expectation requires knowing $\rho(x)$

⇒ Accurate high resolution **N-body** simulations of **halo** formation from **CDM initial conditions**

The Density Profile of Cold Dark Matter Halos



Shape of halo profiles
~independent of halo mass &
cosmological parameters

Density profiles are “cuspy” -
no ‘core’ near the centre

Fitted by simple formula:

$$\frac{\rho(r)}{\rho_{\text{crit}}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

(Navarro, Frenk & White '97)

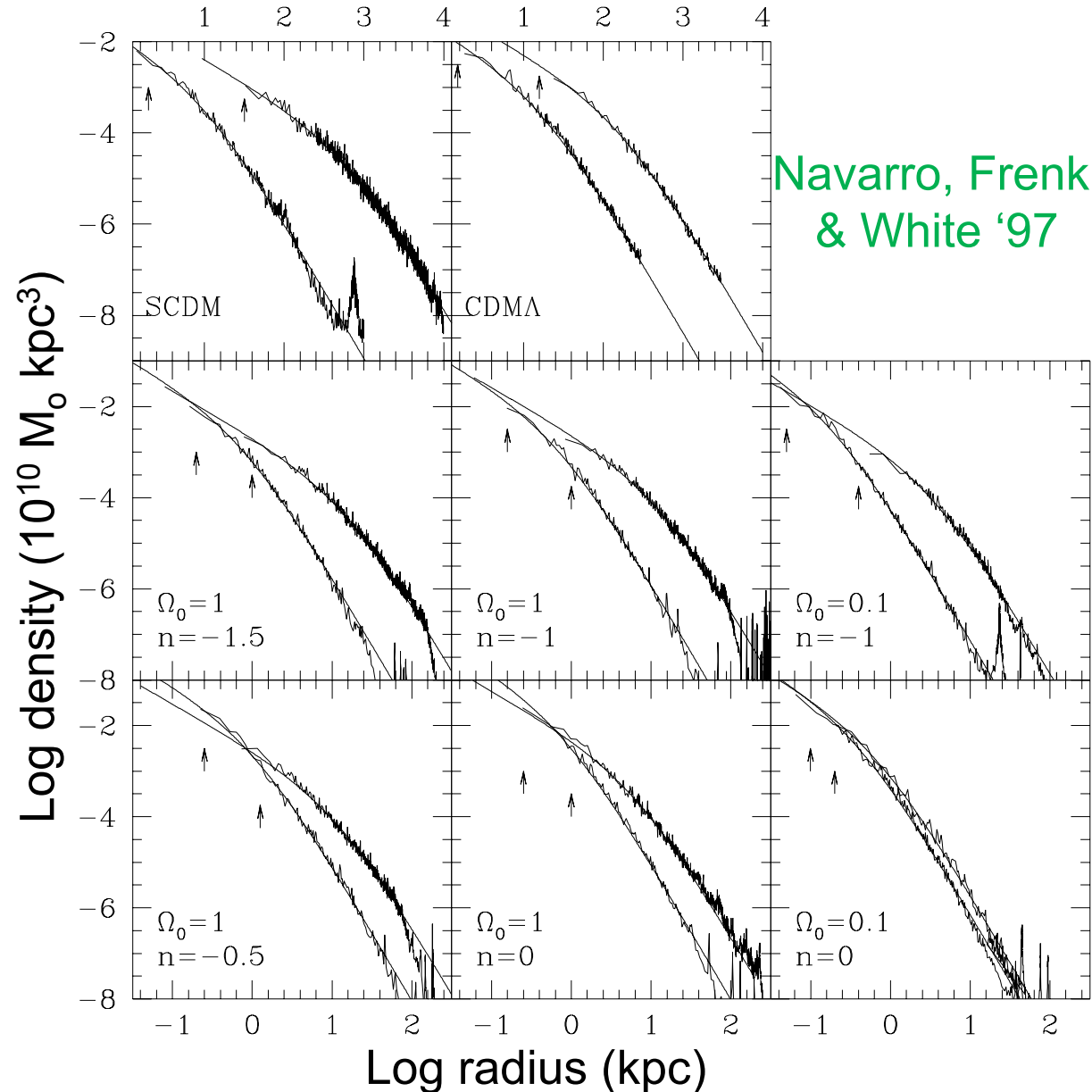
More massive halos and
halos that form earlier have
higher densities (bigger δ)

Universal halo density profiles

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

Fits the spherically averaged density profiles of halos over a wide mass range.

2 parameters:
 Characteristic density δ_c
 radius: r_s



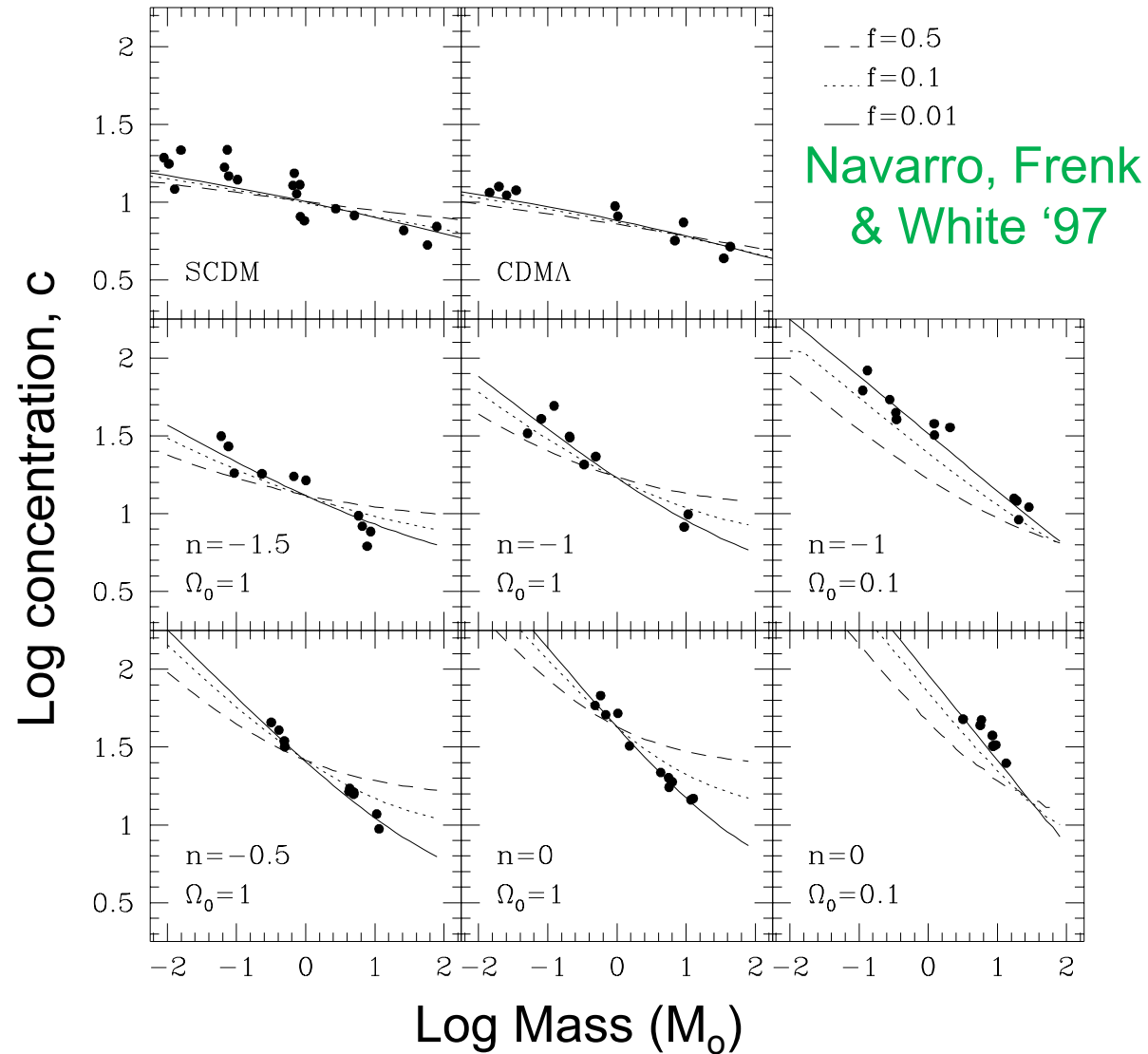
Universal halo density profiles

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

2 parameters:
 Characteristic
 density, δ_c
 radius, r_s

The two parameters
 are related to halo
 mass in a way that is
 cosmology dependent:

$c \searrow$ as $M \nearrow$



Universal halo density profiles

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

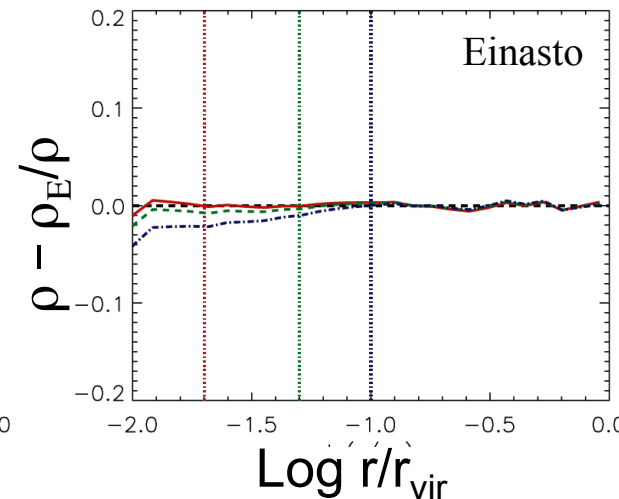
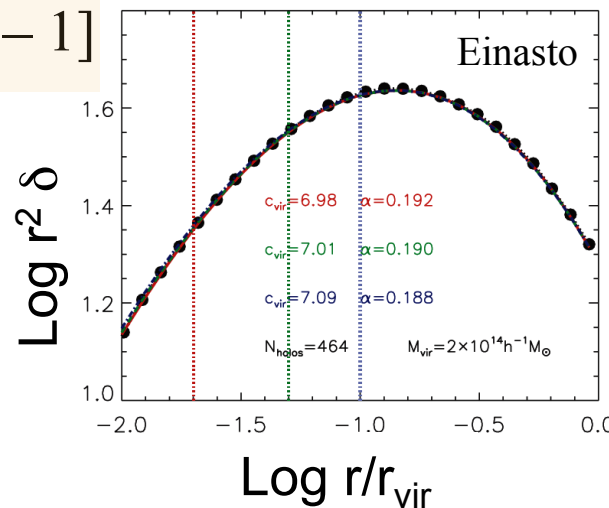
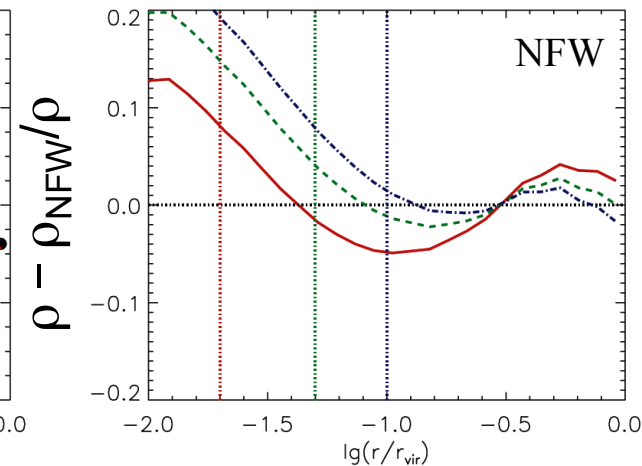
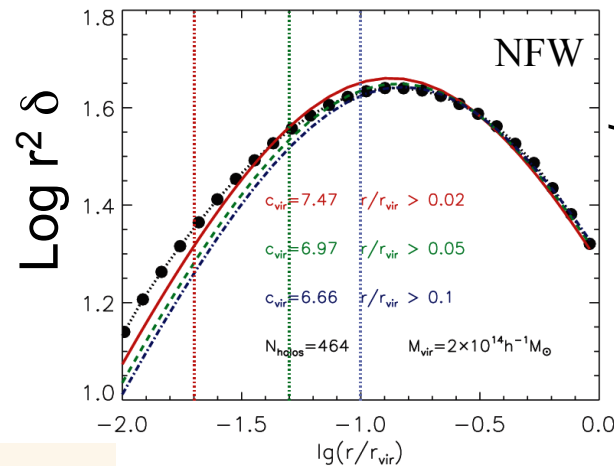
The “Einasto” formula

$$\ln(\rho(r)/\rho_{-2}) = (-2/\alpha) [(r/r_{-2})^\alpha - 1]$$

Fits mean profiles
even better

Gao et al 2008

Averaged cluster mass halos fit with NFW and Einasto





Cores or cusps in nature?



↓
Cores

↓
Cusps

No convincing evidence for cores in observed galaxies



But, if it turns out that
cores exist is this end
of CDM?



The physics of core formation

Cusps → cores

Perturb central halo region
by growing a galaxy
adiabatically and removing
it suddenly (Navarro, Eke
& Frenk '96)

Cores may also form by
repeated fluctuations in
central potential (e.g. by
SN explosions) (Read &
Gilmore '05; Pontzen &
Governato '12,'14; Bullock &
Boylan-Kolchin '17)

Navarro, Eke & Frenk (1996)

The cores of dwarf galaxy haloes L75

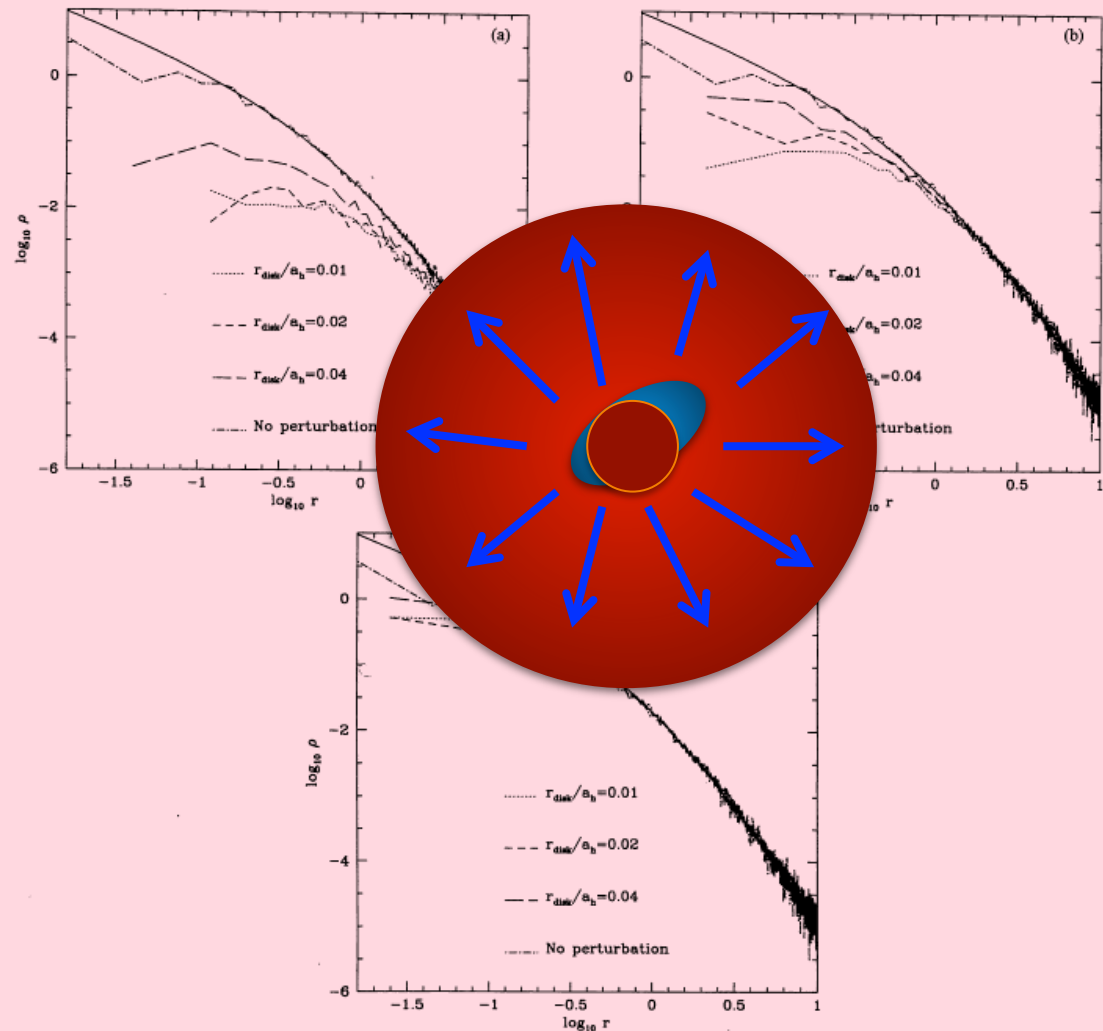
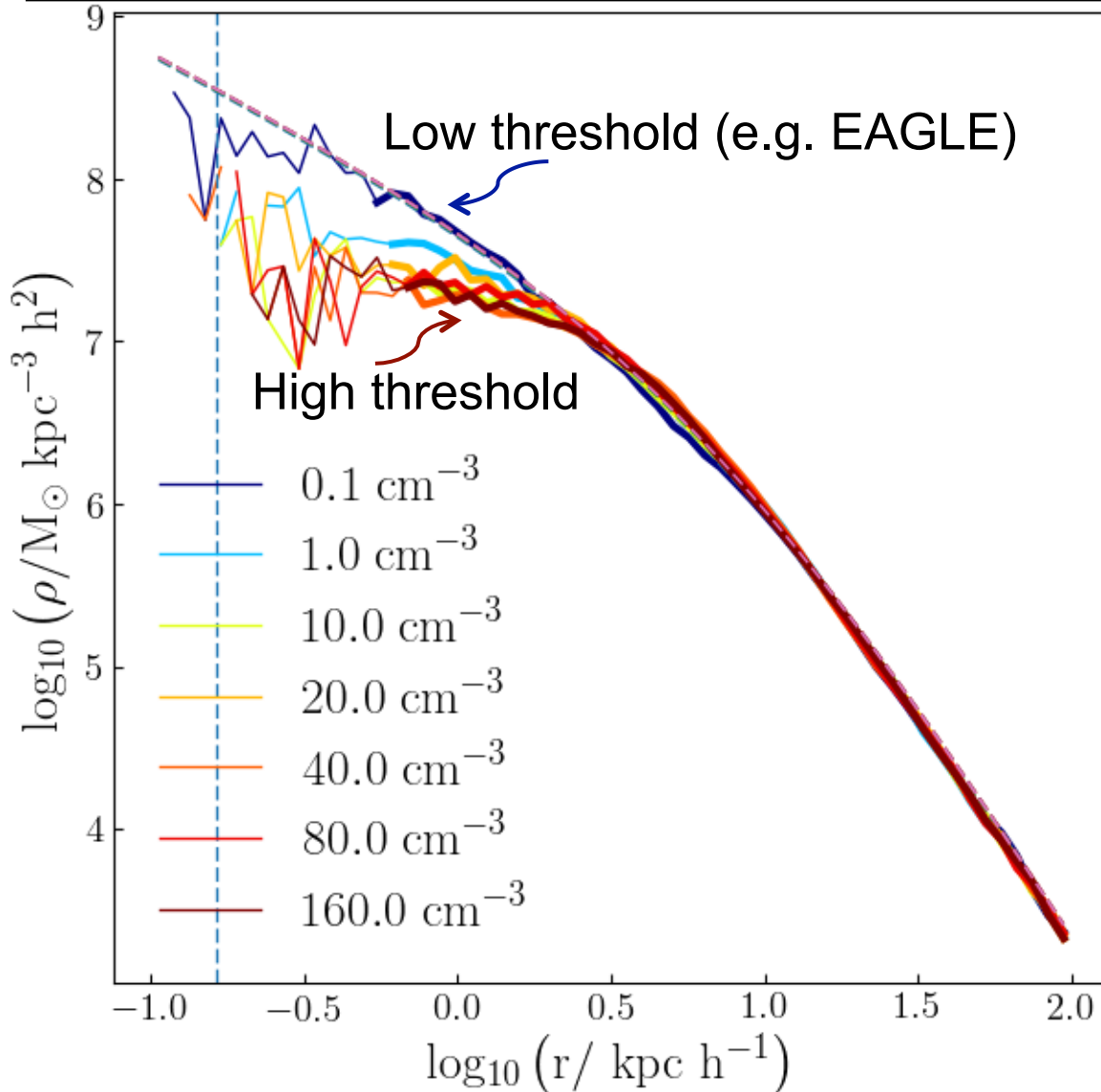
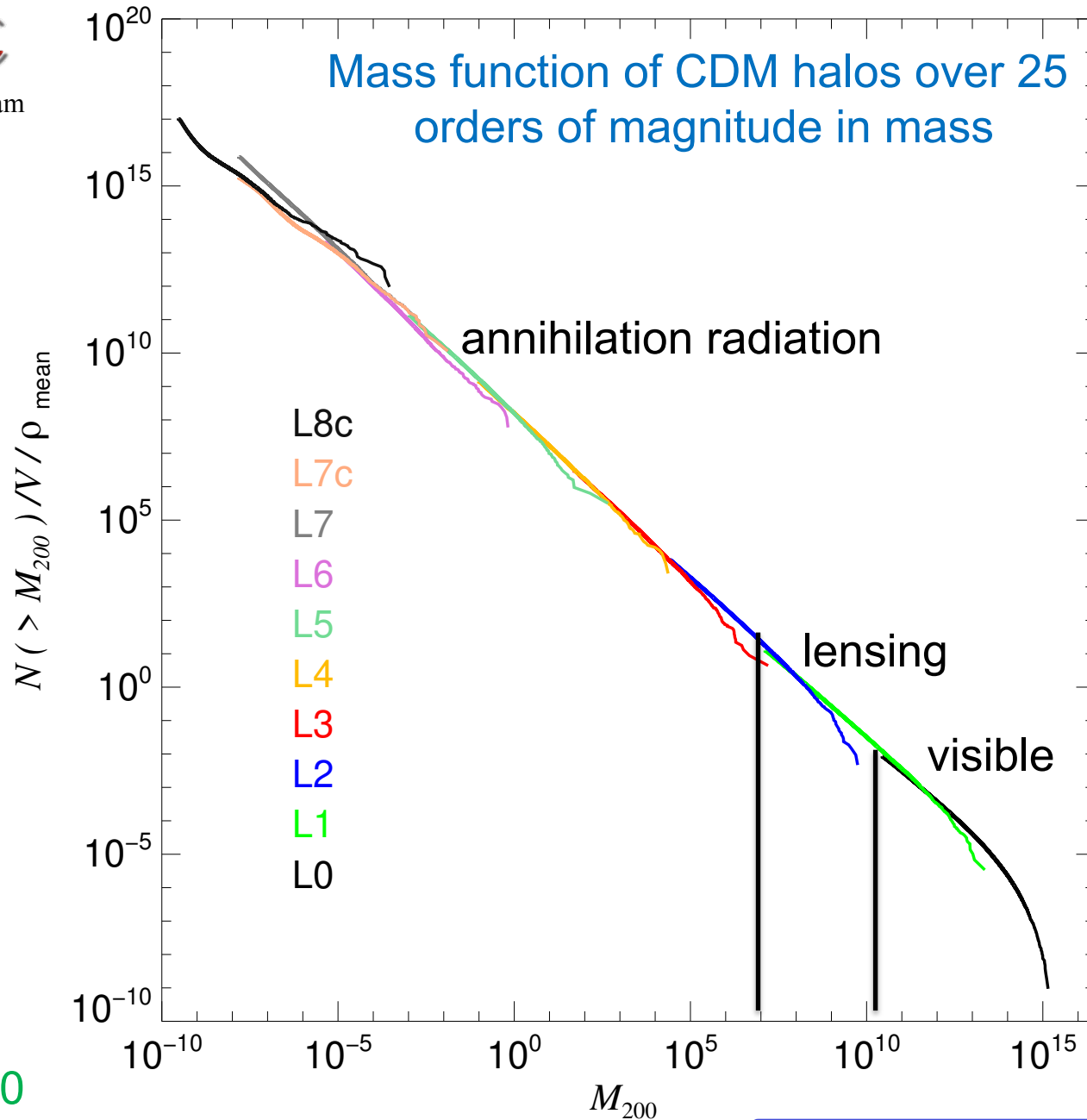


Figure 3. Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at $t=200$. (a) $M_{\text{disc}}=0.2$. (b) $M_{\text{disc}}=0.1$. (c) $M_{\text{disc}}=0.05$.

Cores or cusps in simulations?

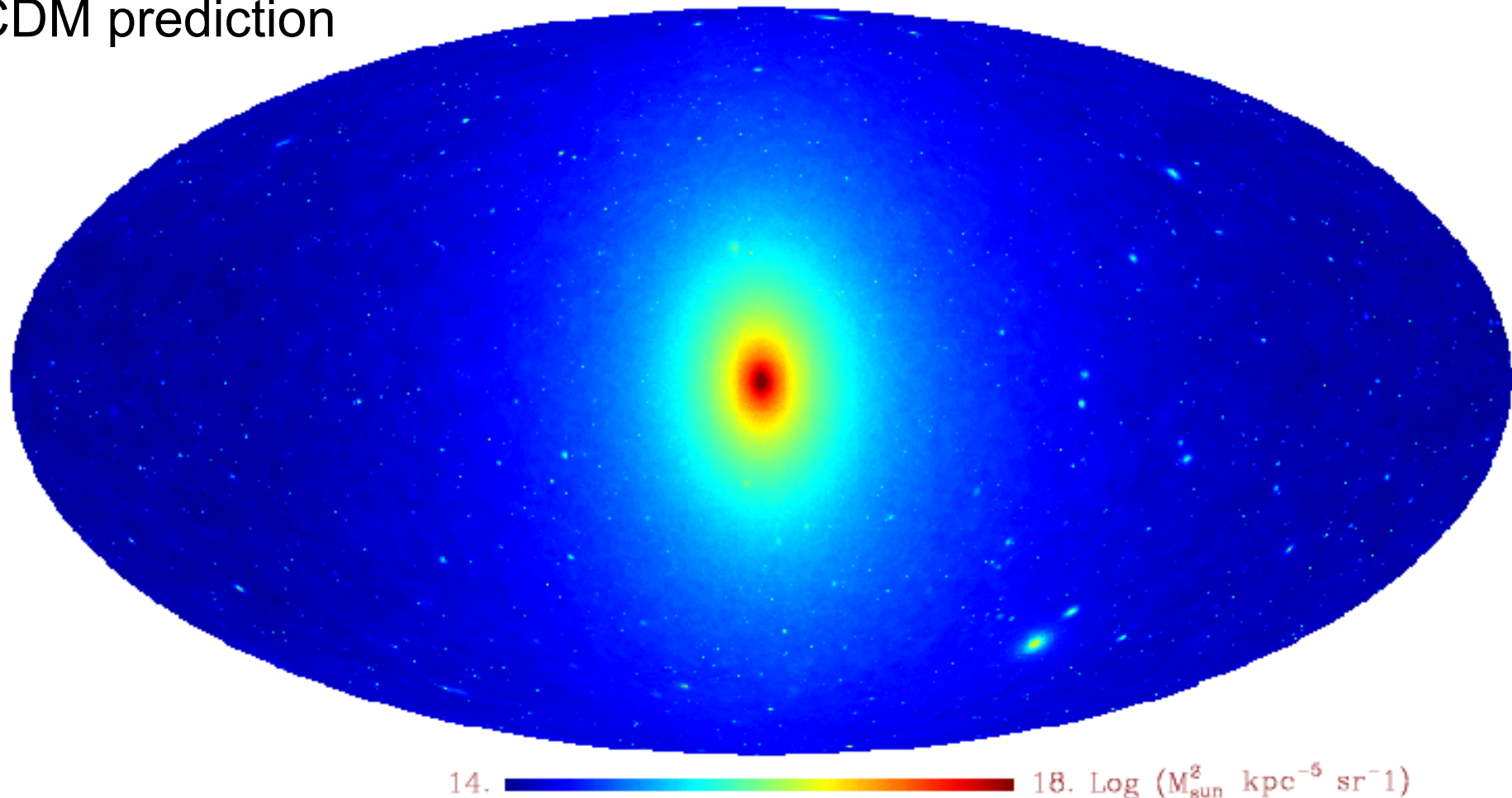




The Milky Way seen in annihilation radiation

Aquarius simulation: $N_{200} = 1.1 \times 10^9$

CDM prediction



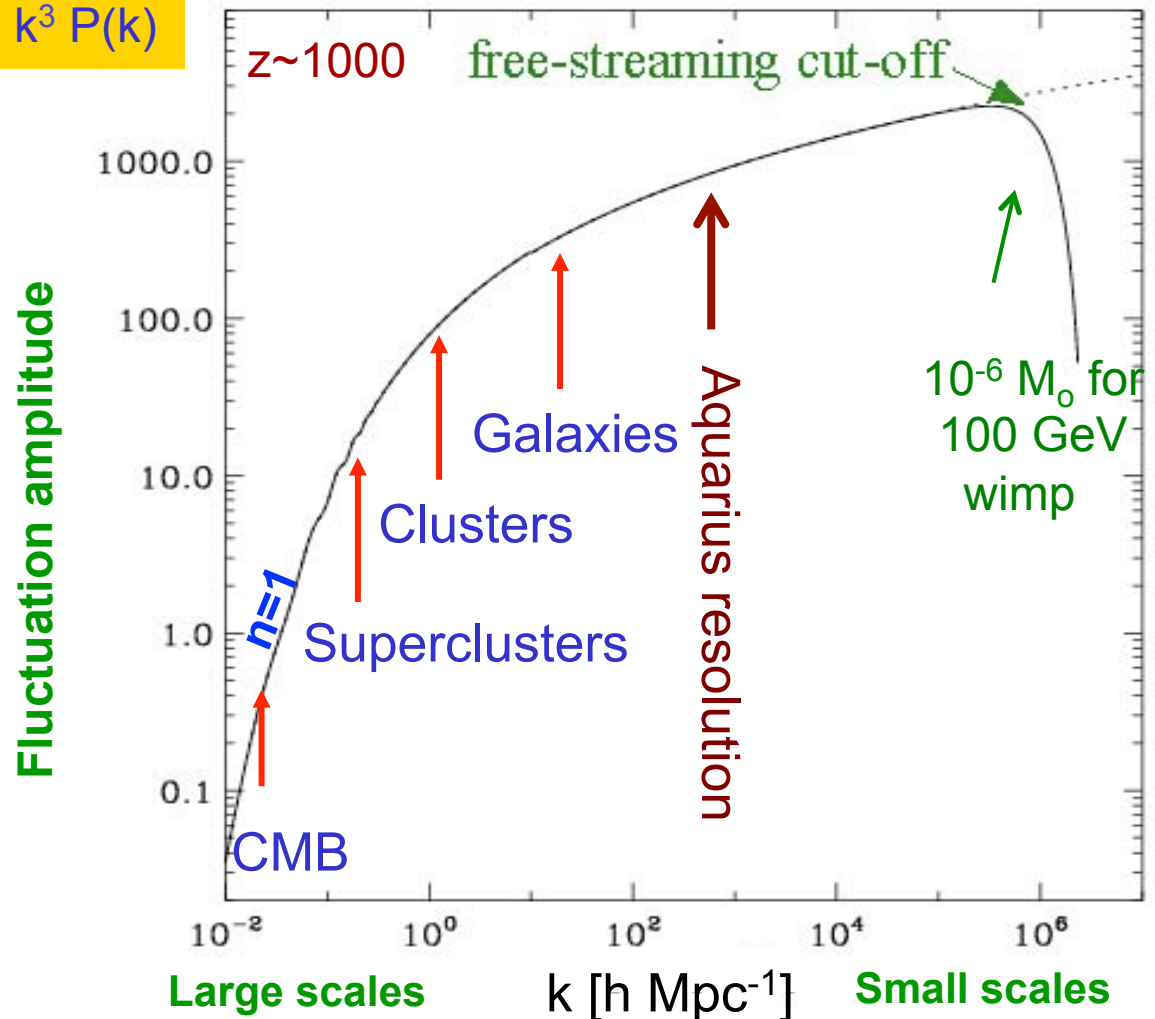
The cold dark matter linear power spectrum

The linear power spectrum
 (“power per octave”)

$$\lambda_{\text{cut}} \propto m_{\chi}^{-1}$$

Assumes a 100GeV wimp
 Green et al '04

$k^3 P(k)$



Wang, Bose, Frenk, Gao, Jenkins, Springel & White 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{14} M_{\odot}$$

Base Level

L0

150 Mpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{12} M_{\odot}$$

Zoom Level 1

L1

15 Mpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^9 M_{\odot}$$

Zoom Level 2

L2

1 Mpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^6 M_{\odot}$$

Zoom Level 3

L3

150 kpc

Wang, Bose et al 2020

The VVV simulation

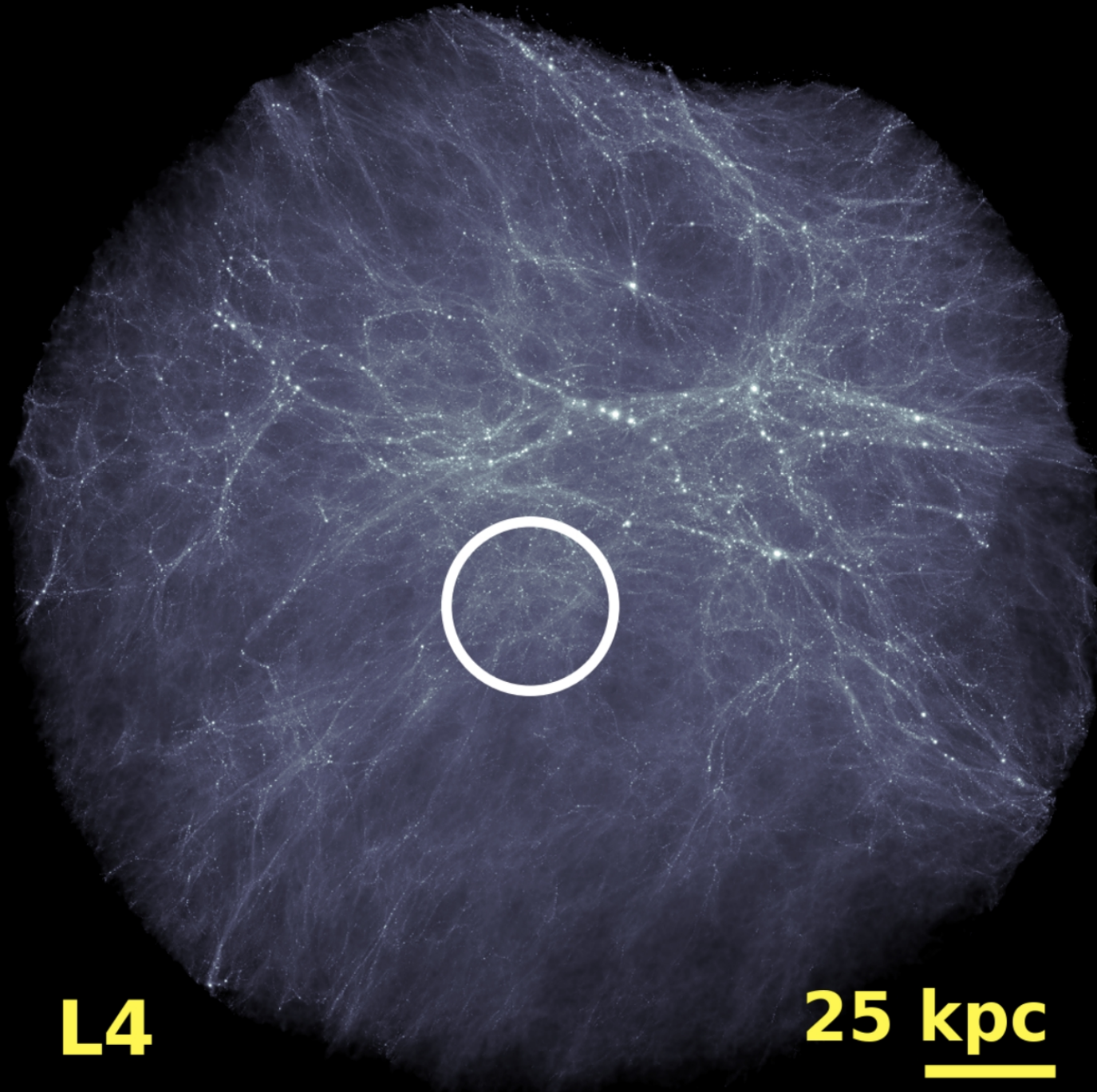
Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^3 M_{\odot}$$

Zoom Level 4



L4

25 kpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

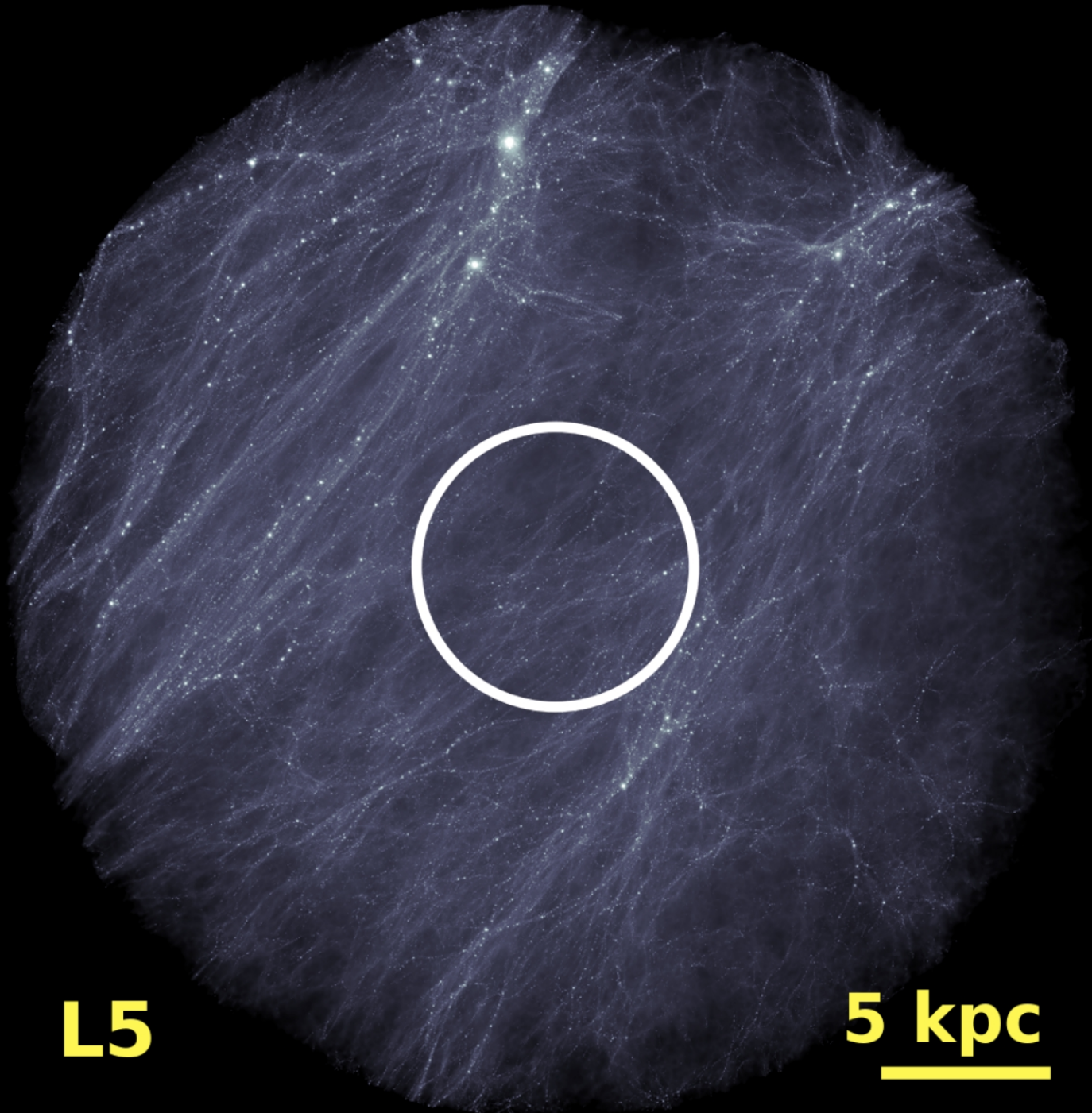
$$M_{\text{char}} = 10 M_{\odot}$$

Zoom Level 5

L5

5 kpc

Wang, Bose et al 2020



The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{-1} M_{\odot}$$

Zoom Level 6

L6

1 kpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

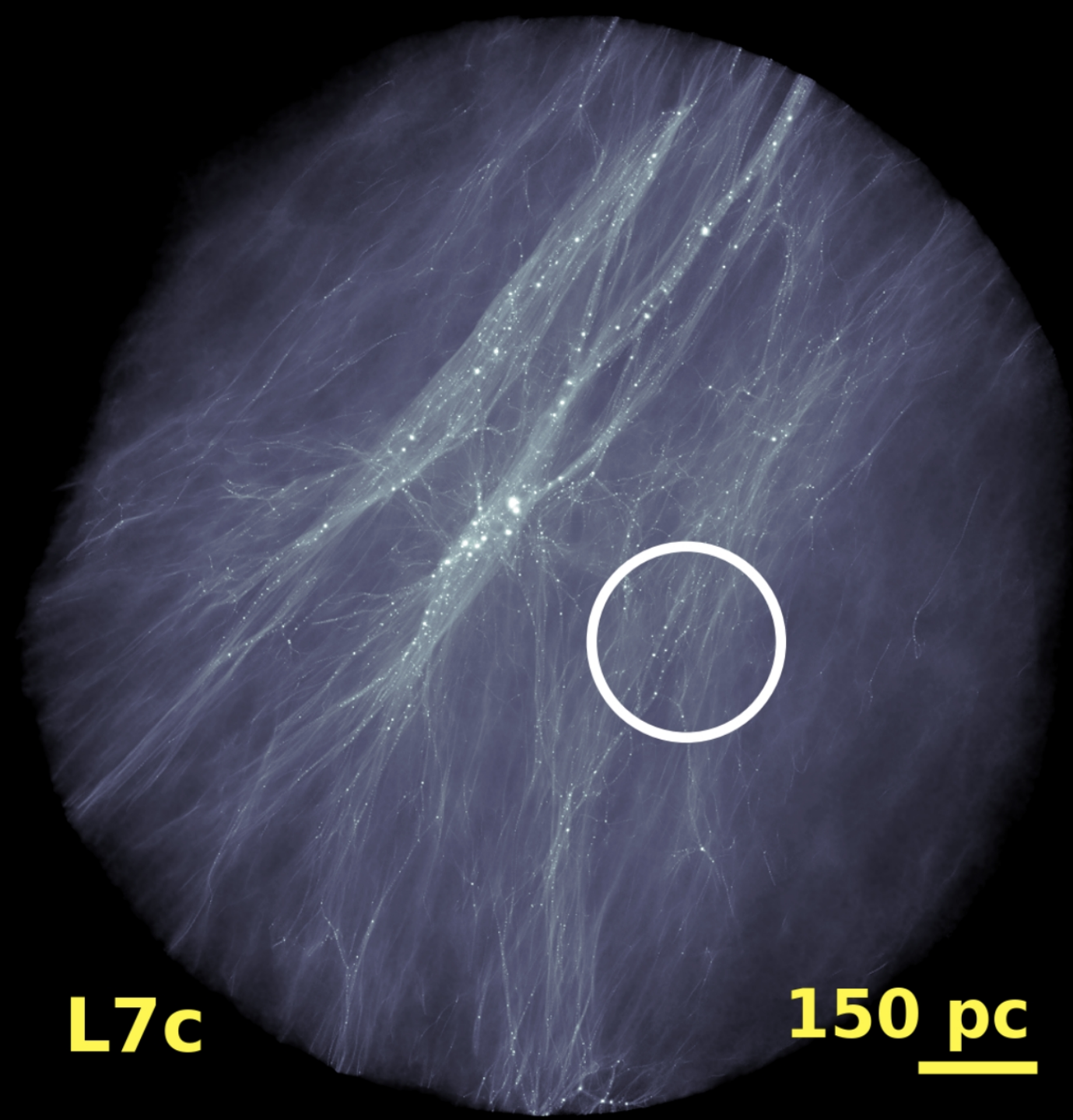
$$M_{\text{char}} = 10^{-4} M_{\odot}$$

Zoom Level 7

L7c

150 pc

Wang, Bose et al 2020



The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{-6} M_{\odot}$$

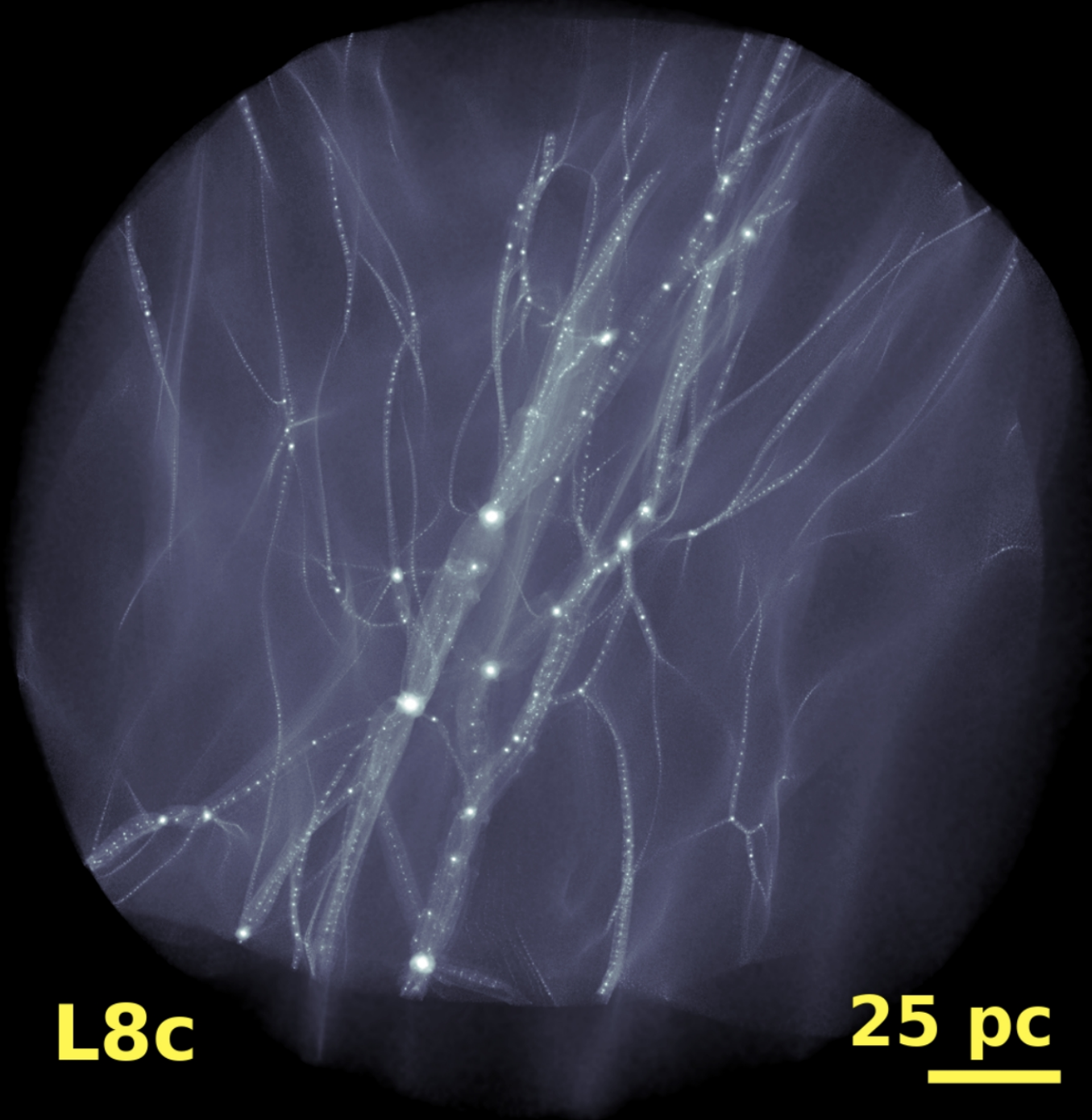
Zoom Level 8

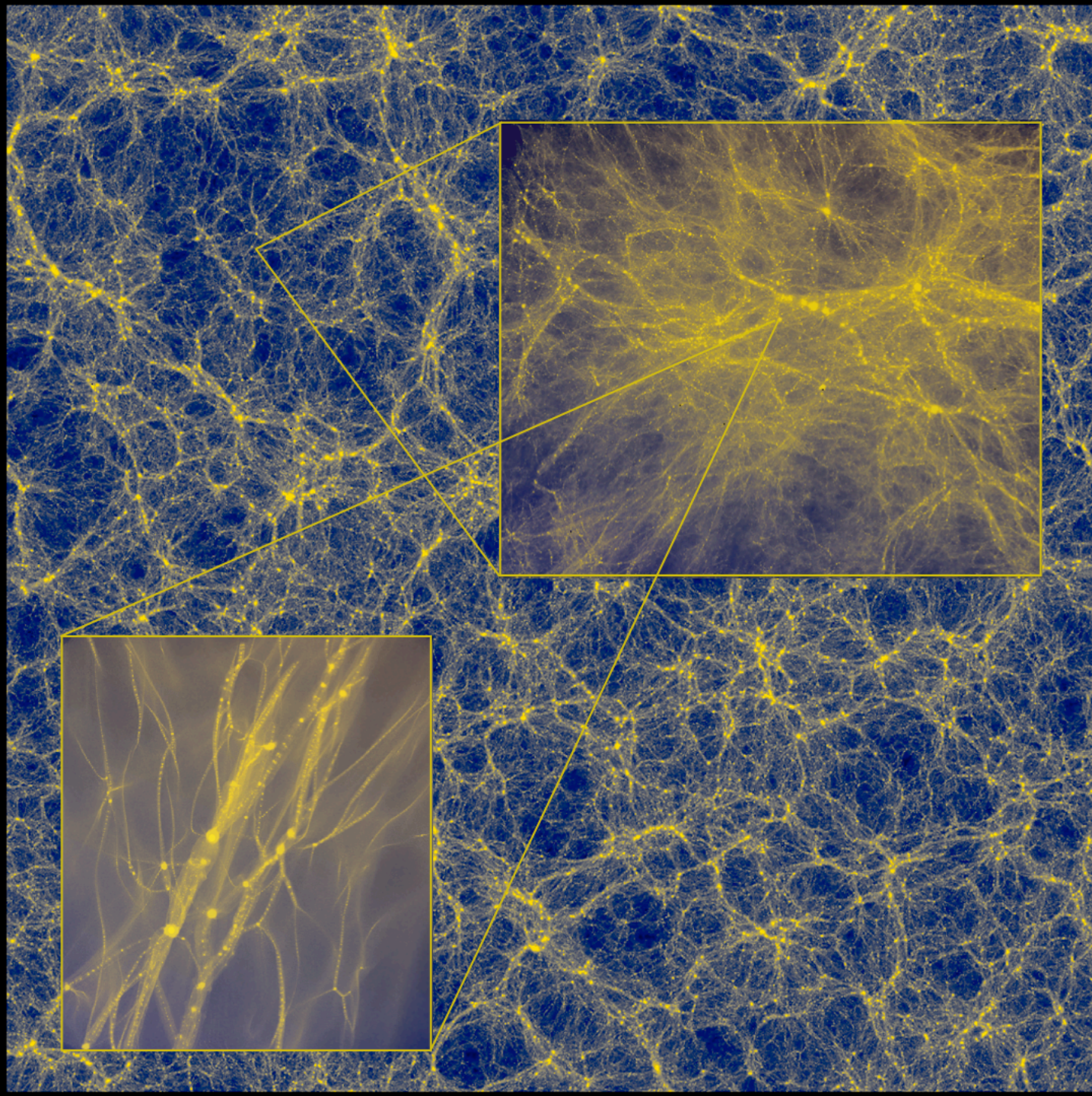
The density of
this region is
only $\sim 3\%$ of the
cosmic mean

Wang, Bose et al 2020

L8c

25 pc

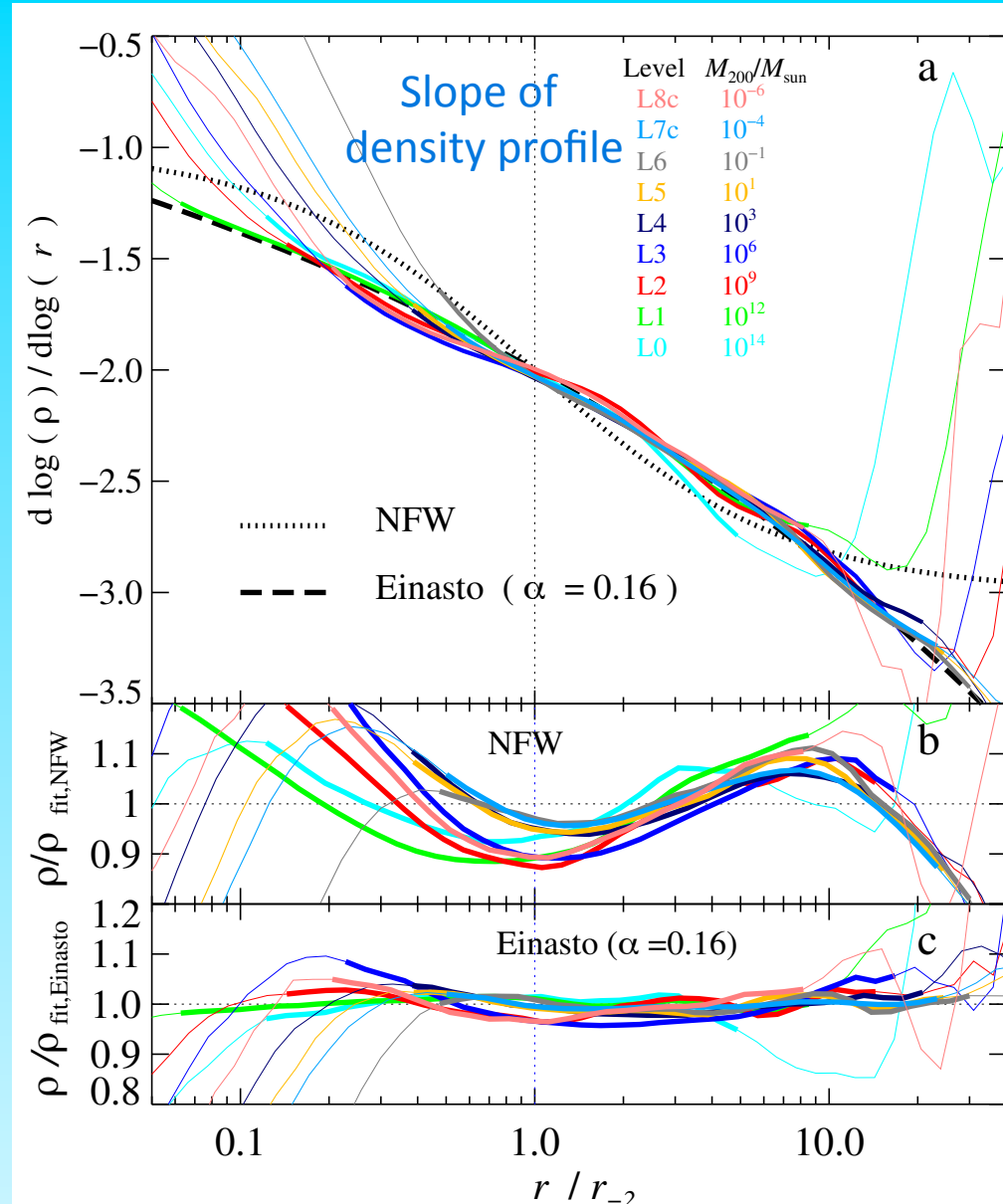




Wang et al '20

Density profile shapes

Over **19 orders** of magnitude in halo **mass** and 4 orders of magnitude in density, the mean density **profiles** of halos are **fit** by **NFW** to within **20%** and by **Einasto** ($\alpha = 0.16$) to within **7%**



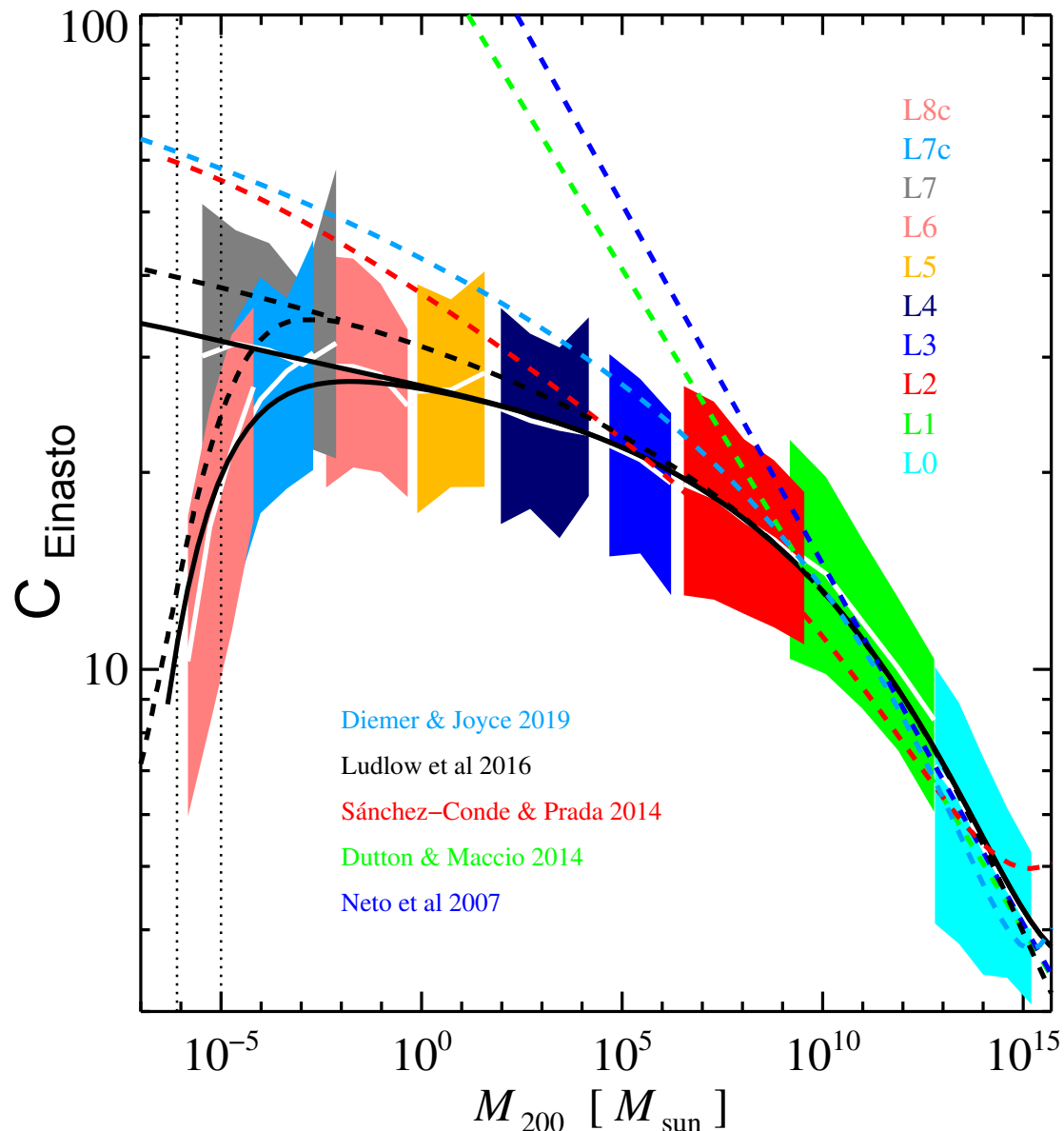
Concentration-mass relation

Concentrations at small mass are **lower** than all previous extrapolations by up to factors of tens.

A **turndown** at 10^3 Earth masses is due to the **free-streaming limit**.

The **scatter** depends only weakly on halo mass

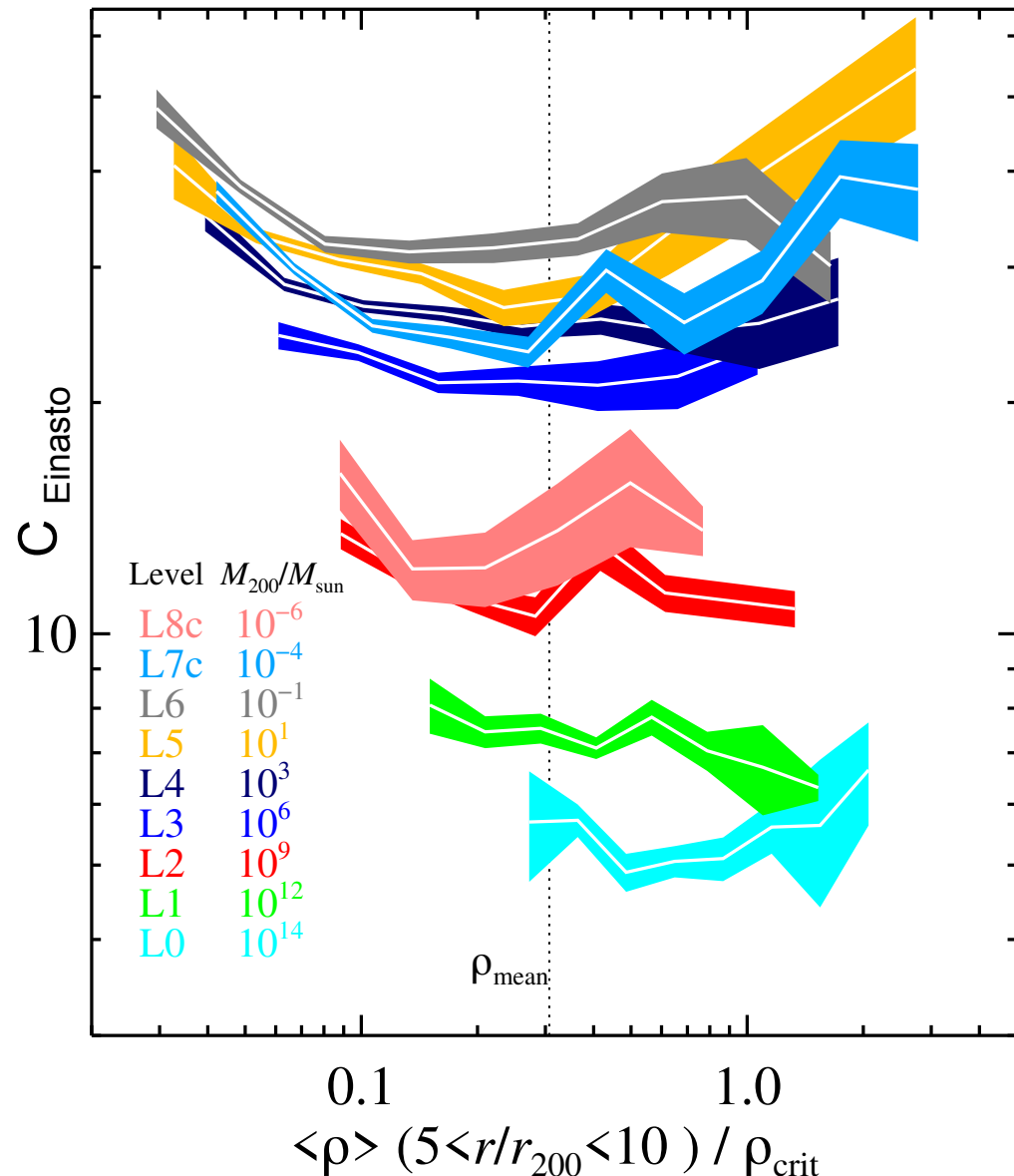
Wang, Bose, CSF + '20



Concentration-density relation

At given halo mass,
concentration does not
depend on local
environment density

The range of local
environment density does
not depend strongly on halo
mass



Annihilation luminosity

The contribution of halos to the mean $z = 0$ **luminosity density** of the Universe is almost **independent** of their **mass** over the mass range

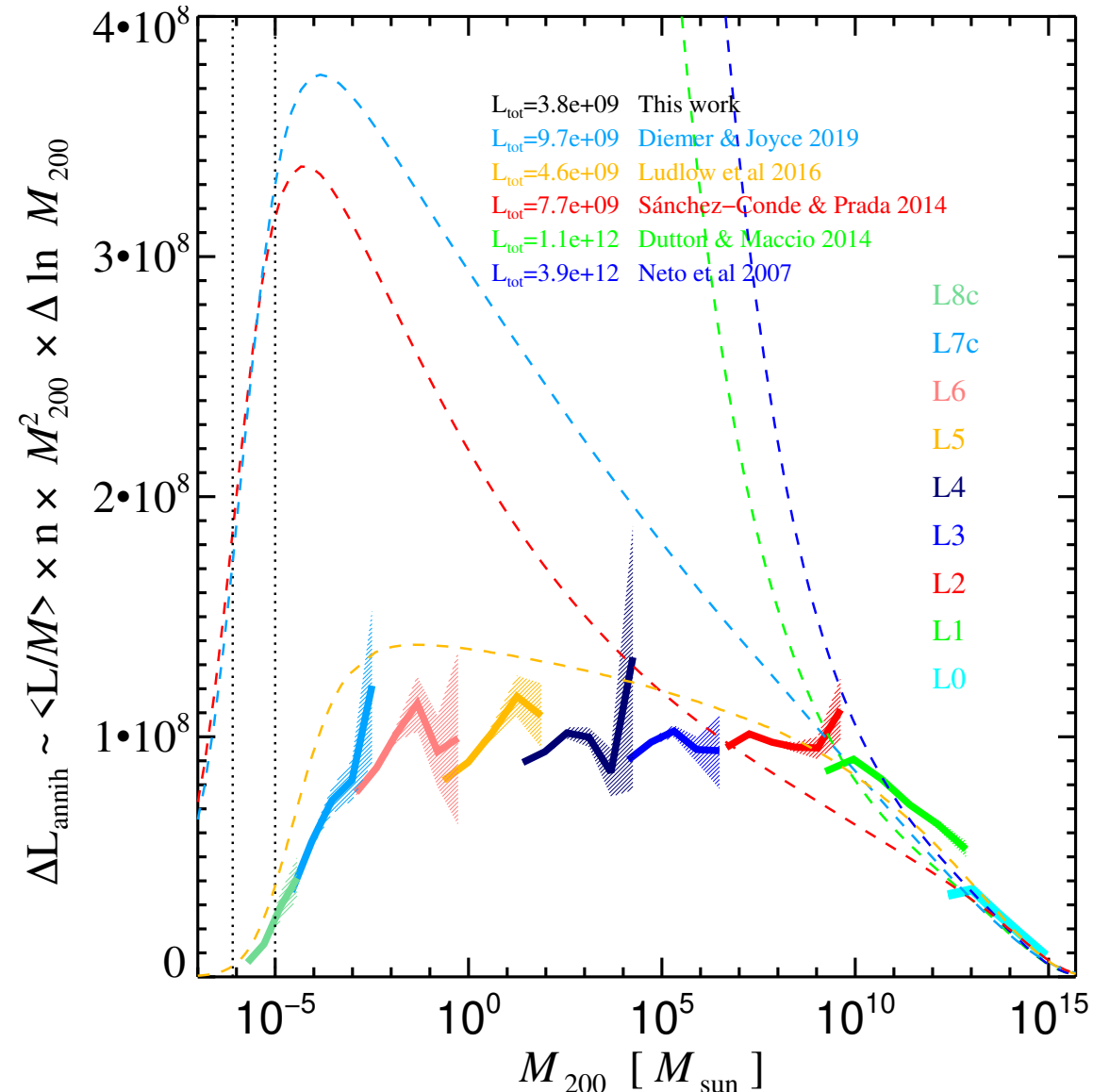
$$10^{-4} M_{\odot} < M_{\text{halo}} < 10^{12} M_{\odot}$$

It is **lower** than **previously** estimated by factors between 3 and **1000**

This still neglects the substructure contribution to halo luminosity

Wang, Bose, CSF + '20

Annihilation luminosity per unit cosmological volume





Conclusions

- Λ CDM: great **success** on scales $> 1\text{Mpc}$: CMB, LSS, gal evolution
 - But on these scales **Λ CDM** cannot be distinguished from **WDM**
 - The **identity** of the DM makes a big difference on **small scales**
1. CDM makes many small subhalos but most ($\sim 5 \cdot 10^8 M_0$) are dark \rightarrow **No satellite problem** in CDM or WDM
 2. No evidence for cores; **baryon effects** can make them \rightarrow **No “core/cusp” problem** in CDM or WDM
 3. Distortions of **strong** gravitational **lenses** offer a **clean test** of CDM vs WDM \rightarrow and can potentially **rule out CDM!**
 4. Halos of **all masses** have **NFW** profiles \rightarrow annihiln radn



Conclusions II

- **Smallest** halos: in **CDM** → Earth mass
- Halos of collisionless dark matter have **universal NFW density profiles** at low redshift on **all mass scales** (21 orders of magnitude)
- Near the **cutoff** free-streaming reduces halo concentration
- **Mass-concentration** relation **independent** of local **environment**
- Very **small (sub)halos** can **dominate** the **annihilation** luminosity