# Ultimate precision Standard Model tests: the muon magnetic anomaly



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## Magnetic moment

The magnetic dipole moment of a particle can be observed from its motion in a magnetic field

Intrinsic magnetic moment discovered in Stern-Gerlach experiment, 1922:



 $\rightarrow$  atoms have intrinsic and quantised angular momentum

Uhlenbeck & Goudsmit postulated in 1925 that electrons have spin angular momentum with magnetic dipole moment:  $e/2m_e$  (Bohr magneton)

Dirac's relativistic theory of the electron (1928) naturally accounted for quantized particle spin, and described elementary spin-1/2 particles

In the classical limit, one finds the Pauli equation with magnetic moment:

 $\vec{\mu} = -g_e \frac{e}{2m_e} \vec{S}$ , with  $|g_e| = 2$  the gyromagnetic factor (and radius  $R_e = 0$ , ie, elementary !)

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Today, everyone knows that the proton is composite, and the electron is a point-like particle ...

But – is it really ?

 $\rightarrow$  Precise  $g_e$  measurement is key !



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Dirac's prediction was confirmed to 0.1% by Kinsler & Houston in 1934 through studying the Zeeman effect in neon [Phys. Rev. 46, 533 (1934)]

A deviation from  $g_e = 2$  was established by Nafe, Nels & Rabi only in 1947 by comparing the hyperfine structure of hydrogen and deuterium spectra [Phys. Rev. 71, 914 (1947)]

A first precision measurement of  $g_e = 2.00344 \pm 0.00012$  (*wrong: 2.00232...*!) was made by Kusch & Foley in 1947 using Rabi's atomic beam magnetic resonance technique [Phys. Rev. 72, 1256 (1947)]







Ever since experimentalists & theorists are racing for  $g_e$  precision to test QED

A series of (Nobel prize winning) experiments was performed using single electron capture in a cylindrical Penning trap and measuring the spin ( $\omega_s$ ) to cyclotron ( $\omega_c = eB/m_e$ ) frequency ratio, giving:  $g_e/2 = \omega_s/\omega_c$ 





#### Anomalous magnetic moment:

$$a_e = \frac{g_e - 2}{2} = 1\ 159\ 652\ 180.73(28)\ \cdot\ 10^{-12}$$
(24 ppb precision, 1.8 below 1987 value)

Hanneke, Fogwell, Gabrielse (Harvard), 0801.1134, 1009.4831 ]

Cylindrical Penning trap cavity used to confine a single electron and inhibit spontaneous emission



Hans G. Dehmelt Nobel 1989

## Quantum fluctuations

+ ...

е

coupling to virtual fields:

 $(g-2)_{\rho} \neq 0$  (1<sup>st</sup> order QED)

Dirac's gyromagnetic factor is lowest order QED graph, but there are quantum corrections...

+

Quantum fluctuations slightly increase gyromagnetic factor, so that:

е

 $(g-2)_e \neq 0$  (full Standard Model)

$$a_e^{\text{QED}} = \frac{\alpha}{2\pi} + \dots = 0.001\ 161\ \dots$$

е

 $(g-2)_e = 0$  (Dirac)

Schwinger 1948 (Nobel price 1965) First QFT loop calculation! [ Phys. Rev. 73, 416 (1948) ]



Julian Schwinger

# Theory and comparison with experiment

In a tour de force five QED loops have been computed [Kinoshita et al, 1412.8284 (2014)]

$$a_e^{\text{QED}} = \frac{\alpha}{2\pi} - 0.328478444 \left(\frac{\alpha}{\pi}\right)^2 + 1.181234 \left(\frac{\alpha}{\pi}\right)^3 - 1.912(1) \left(\frac{\alpha}{\pi}\right)^4 - 7.8(3) \left(\frac{\alpha}{\pi}\right)^5$$

adding to these small contributions from hadronic and weak loops, and using the best value  $\alpha^{-1} = 137.035\ 999\ 049\ (90)$ , from a measurement of  $h/m_{\rm Rb}$  via the recoil velocity of Rubidium atoms when absorbing photon [Bouchendira et al, 1012.3627 (2010),  $\alpha^2 = 2R_{\infty}m_{\rm Rb}h/(cm_em_{\rm Rb})$ ], one finds:

 $a_e^{\text{SM}} = 1\ 159\ 652\ 181.64\ (4)(76)\cdot 10^{-12}$  $a_e^{\text{Exp}} = 1\ 159\ 652\ 180.73(28)\ \cdot 10^{-12}$ 

In agreement with experiment
 (errors are from loop terms and α respectively)

Measurement and SM prediction can be used to derive most precise value of  $\alpha$ 

 $\alpha^{-1}(a_e) = 137.035\,999\,157\,(4)(33)$ 

(errors are from theory and experiment, respectively)

(0.25 ppb precision, 3 times better than Rb based value) [Kinoshita et al, 1412.8284 (2014)]

## Theoretical properties

The anomalous magnetic moment of an elementary particle corresponds to an effective Lagrangian interaction of mass dimension 5. It is finite and calculable

At lowest order in QED, the anomalous magnetic moment is universal:

$$a_e^{\text{QED,LO}} = a_\mu^{\text{QED,LO}} = a_\tau^{\text{QED,LO}} = \frac{\alpha}{2\pi}$$

Differences, ie, lepton mass dependence are introduced at loop level:  $(\alpha/\pi)^2$ 

SM contribution to  $a_e$  dominated by mass-independent Feynman diagrams in QED with electrons in internal lines

Lepton mass effects become significant for  $a_{\mu}$  !



The measurement of the muon g-2 is harder as the muon is instable (2.2 µs)  $\rightarrow$  why bother ?

- $\rightarrow$  All sectors of SM physics contribute measurably to muon g-2
- → At lowest order where mass effects appear, contributions from heavy virtual "new physics" (NP) particles of mass  $\Lambda_{\rm NP}$  scale as  $m_\ell^2$

Muon g-2 looses "only" about factor 23 (4) in experimental (theoretical) precision, so  $a_{\mu}$  expected to be significantly more sensitive to NP than  $a_{e}$ 

*Example*: weak + Higgs boson contribution is  $1536 \cdot 10^{-12} (\mu)$  and  $0.030 \cdot 10^{-12} (e) \rightarrow$  ratio of ~ 51,000

## Measuring the muon g-2

?

 $\sim \sim \sim$ 



The BNL muon g–2 experiment (E821), 1997–2001

# Measuring the muon g-2

Analogous approach as for electron: search for discrepancy between the frequencies of cyclotron motion and spin precession

For polarised muons moving in a uniform *B* field (perp. to muon spin and orbit plane), and focused in an electric quadrupole field, the observed difference between spin precession and cyclotron frequency (= "anomalous frequency"), ignoring  $\mu$ EDM, is:

$$\vec{\omega}_{a} \equiv \vec{\omega}_{s} - \vec{\omega}_{c} = \frac{e}{m_{\mu}c} \left[ a_{\mu}\vec{B} - \left( a_{\mu} - \frac{1}{\gamma^{2} - 1} \right) \vec{\beta} \times \vec{E} \right]$$
Motional magnetic field

With electrostatic focusing, no gradient *B* field focusing needed so that *B* can be made as uniform as possible !

 $\vec{\omega}_a$  Independent of muon momentum

The *E* field dependence is eliminated at the "magic  $\gamma$ ":  $\gamma = 29.3 \rightarrow p_{\mu} = 3.09 \text{ GeV}$ 

The experiment measures  $(g_{\mu} - 2)/2$  directly

[J. Bailey et al., NP B150, 1 (1979)]

Exploit muon properties in experiment

1. Parity violation polarizes muons in pion decay Pions from proton-nucleon collision (AGS)

2. Anomalous frequency proportional to  $a_{\mu}$ 

- 3. Magic  $\gamma$ :  $\vec{\omega}_a = \frac{e}{m_{\mu}c} \left[ a_{\mu} \vec{B} - \left( a_{\mu} - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right] \approx \frac{e}{m_{\mu}c} a_{\mu} \vec{B}$
- 4. Again parity violation in muon decay

 $\mu_{\text{polarised}}^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$ 

fast electron emitted in direction opposite to muon spin





 $\rightarrow e + \nu_e + \nu_\mu$ 

## BNL E821: muon g-2 experiment

- A 24 GeV proton beam (AGS) incident on a target produces large number of pions that decay to muons
- The 3.1 GeV muon beam (relativistically enhanced lifetime of 64 μs) is injected into a 7.1 m radius ring with 1.4 T vertical magnetic field, which produces cyclotron motion matching the ring radius
- Electrostatic focusing of the beam is provided by a series of quadrupole lenses around the ring.



- Decay electrons (correlated with  $\mu$  spin precession) counted vs. time in calorimeters inside ring ( $\rightarrow \omega_a$ )
- Precise measurement of  $\omega_a$  and *B* allows to extract  $a_\mu$

### BNL E821: muon g-2 experiment



Observed positron rate in successive 100 µs periods ~150 polarisation rotations during measurement period

Anomalous frequency:

$$\omega_a \approx \frac{e}{m_\mu c} \frac{a_\mu B}{a_\mu B}$$

obtained from time-dependent fit to electron counts (for given energy *E*)

$$N(t) = N_0 e^{-t/\gamma \tau} [1 - A \cdot \sin(\omega_a t - \phi)]$$

In blue: fit parameters

Total systematic uncertainty on  $\omega_a$ : 0.2–0.3 ppm, with largest contributors:

- *pileup* (~in-time arrival of two low-*E* electrons)
- muon losses
- coherent betatron oscillation (muon loss and CBO amplitude [frequency: 0.48 MHz, compared to ω<sub>a</sub>: 0.23 MHz] are part of fit)
- calorimeter gain changes

The B-field is mapped with 17 NMR probes mounted on a trolley pulled through the beampipe



Azimuthal average for one trolley run. Contours are 0.5 ppm field differences.

*B*-field is proportional to free proton precession frequency  $\omega_p$ ( $B = \omega_p / \mu_p$ ) measured by NMR probes so one can write:

$$a_{\mu} = \frac{\frac{e}{m_{\mu}c} a_{\mu}B}{\frac{e}{m_{\mu}c} \frac{g}{2}B - \frac{e}{m_{\mu}c} a_{\mu}B} = \frac{\omega_{a}}{\omega_{L} - \omega_{a}}$$
$$= \frac{\frac{\omega_{a}}{\omega_{L}}}{\frac{\omega_{L}}{\omega_{p}} - \frac{\omega_{a}}{\omega_{p}}} = \frac{\mathcal{R}}{\lambda - \mathcal{R}}$$

where:  $\omega_L$  is Larmor frequency of muon,  $\mathcal{R}$  measured by E821, and the  $\mu$ -to-p magnetic moment ratio is:  $\lambda = 3.183$  345 107(84) ( $\lambda$  is determined from muonium ( $\mu^+e^-$ ) hyperfine level structure measurements)

 $\rightarrow$  Systematic uncertainty on  $\omega_p$  between 0.2 and 0.4 ppm

 $\omega_a$  and  $\omega_p$  measured independently in blind analyses  $\rightarrow$  doubly blind experiment!

### Result, and comparison with earlier experiments

E821 final result (1997–2001 data):

 $a_{\mu} = 11\,659\,209.1\,(5.4)(3.3)\,\cdot 10^{-10}$ 

(0.54 ppm precision, assumes CPT invariance) [ Muon g–2, E821, hep-ex/0602035 with updated value for  $\lambda$  ]

Agreement between  $\mu^{\scriptscriptstyle +}$  and  $\mu^{\scriptscriptstyle -}$  results



### Evolution of experimental sensitivity:

#### [See, eg, Miller, de Rafael, Roberts, hep-ph/0703049]

Experiment	Beam	Measurement	$\delta a_{\mu}/a_{\mu}$	Required theor. terms	
Columbia-Nevis ('57)	$\mu^+$	$g = 2.00 \ (\sigma = 0.10)$		<i>g</i> = 2	Muon behaves like heavy electron
Columbia-Nevis ('60)	$\mu^+$	0.001 13 (+16)(-12)	12 %	$\alpha/2\pi$	
CERN 1 (SC, 1961)	$\mu^+$	0.001 145 (22)	1.9 %	α/2π	
CERN 1 (SC, 1962)	$\mu^+$	0.001 162 (5)	0.43 %	$(\alpha/\pi)^2$	
CERN 2 (PS, 1968)	$\mu^+$	0.001 166 16 (31)	266 ppm	$(\alpha/\pi)^3$	
CERN 3 (PS, 1979)	$\mu^{\pm}$	0.001 165 923 0 (84)	7.2 ppm	$(\alpha/\pi)^3$ + had (60 ppm)	Electrostatic
BNL E821 (1997-2001)	$\mu^{\pm}$	0.001 165 920 91 (63)	0.54 ppm	$(\alpha/\pi)^4$ + had + weak + ?	focusing, magic γ

# Confronting Experiment with Theory

The Standard Model prediction of  $a_{\mu}$  is decomposed in its main contributions:

$$a_{\mu}^{\text{SM}} = \frac{g_{\mu} - 2}{2} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Had}}$$

of which the hadronic contribution has the largest uncertainty

## Confronting Experiment with Theory



## QED contribution

Known to 5 loops, good convergence, diagrams with internal electron loops enhanced:

[5-loop: Aoyama, Hayakawa, Kinoshita, Nio, 1205.5370 (2012)]

Using  $\alpha = 137.035999049(90)$  from Rubidium recoil measurement, gives:

 $a_{\mu}^{\text{QED}} = 11\,658\,471.895(0.008)\cdot 10^{-10}$ 

with negligible uncertainty compared to experimental error of  $6.3 \cdot 10^{-10}$ 

Evidence for  $\gamma\gamma \rightarrow \gamma\gamma$ light-by-light scattering (LBLS) seen by ATLAS in 5.02 TeV ultraperipheral Pb+Pb collisions

Picture shows LBLS candidate: two  $E_T = 4.9$  GeV back-toback photons with no additional activity

[ 1702.01625 ]



Field strength of up to 10<sup>25</sup> V/m reached





# Electroweak contribution

EW contribution involving *W*, *Z* or Higgs is suppressed at least by a factor:  $\frac{\alpha}{\pi} \frac{m_{\mu}^2}{m_W^2} \approx 4 \cdot 10^{-9}$ 

The first loop gives: [Jackiw, Weinberg and others 1972]

$$a_{\mu}^{\text{EW},1-\text{loop}} = \frac{G_F m_{\mu}^2}{8\sqrt{2}\pi^2} \left[ \frac{5}{3} + \frac{1}{3} (1 - 4\sin^2\theta_W)^2 + \mathcal{O}\left(\frac{m_{\mu}^2}{m_W^2}\right) + \mathcal{O}\left(\frac{m_{\mu}^2}{m_H^2}\right) \right] = 19.48 \cdot 10^{-10}$$



1-loop diagrams (some cancellation between *W/Z* graphs)



2-loop diagrams (+ Higgs exchange)

Three-loop leading logarithms are found to be small (~ $10^{-12}$ ) [Degrassi, Giudice, hep-ph/9803384, and others ]

Two-loop contribution surprisingly large due to large  $\ln(m_Z/m_\mu)$ : [Czarnecki, Krause, Marciano, 1995, and others]

$$a_{\mu}^{\text{EW},2-\text{loop}} = -4.12(0.10) \cdot 10^{-10}$$
  
 $\Rightarrow a_{\mu}^{\text{EW},1+2-\text{loop}} = 15.36(0.10) \cdot 10^{-10}$ 

# Hadronic contribution

The dominant hadronic contribution and uncertainty stems from the lowest order contribution,  $a_{\mu}^{\text{Had,LO}}$ , which cannot be calculated from perturbative QCD as it is in the nonperturbative regime

Tools to approach low-energy QCD:

- 1. Lattice QCD (encouraging results, but precision is challenging; prediction of broad range of dispersion relations prior to  $a_{\mu}^{Had,LO}$ needed to build confidence)
- 2. Effective QFT with hadrons such as chiral perturbation theory (limited validity range)
- 3. Hadronic models (hard to estimate robust uncertainties)
- 4. Dispersion relations and experimental data ...



## Digression: Running of $\alpha_{QED}(M_z)$

Photon vacuum polarisation function  $\Pi_{\gamma}(q^2)$ 

$$i\int d^4x \ e^{iqx} \left\langle 0 \left| T J^{\mu}_{\text{em}}(x) \left( J^{\nu}_{\text{em}}(0) \right)^{\dagger} \right| 0 \right\rangle = - \left( g^{\mu\nu} q^2 - q^{\mu} q^{\nu} \right) \prod_{\gamma} (q^2)$$

Only vacuum polarisation "screens" electron charge  $\alpha(s) = \frac{\alpha(0)}{1 - \Delta \alpha(s)}$ 

with: 
$$\Delta e$$

$$\Delta \alpha(s) = -4\pi \alpha \operatorname{Re}\left[\prod_{\gamma}(s) - \prod_{\gamma}(0)\right]$$

split into leptonic and hadronic contribution

Born:  $\sigma^{(0)}(s) = \sigma(s)(\alpha/\alpha(s))^2$ 

Leptonic  $\Delta \alpha_{lep}(s)$  calculable in QED (known to 3-loops). However, quark loops are modified by longdistance hadronic physics, cannot be calculated with perturbative QCD

### Precise knowledge $\alpha(m_{z})$ important ingredient to global electroweak fit

 $\Delta \alpha_{had}(s)$  uncertainty contributes 1.8 MeV to  $m_W$  SM prediction (total error of SM: 8 MeV), but dominant uncertainty to  $\sin^2 \theta_{eff}$  (SM)



# Hadronic contribution

Akin to  $\Delta \alpha_{had}(s)$ , the lowest-order hadronic contribution to  $a_{\mu}$  can be obtained from a dispersion relation: [Bouchiat, Michel, 1961]



 $\Rightarrow a_{\mu}^{\text{Had,LO}} = 692.6(3.3) \cdot 10^{-10}$ 

[DHMZ, Davier 1612.02743 (2016)]



The hadronic contribution to  $a_{\mu}^{SM}$  has the largest uncertainty, dominated by the lowest-order term, but a significant uncertainty also stems from hadronic light-by-light scattering (see later)

Most recent SM estimates: [Davier 1612.02743]

$$a_{\mu}^{\rm SM} = 11\,659\,181.7(4.2)\cdot 10^{-10}$$

compared to experiment:

$$a_{\mu}^{\text{Exp}} = 11\ 659\ 209.1(6.3)\cdot 10^{-10}$$

with difference:

$$\Delta a_{\mu} = a_{\mu}^{\text{Exp}} - a_{\mu}^{\text{SM}} = (27.4 \pm 7.6) \cdot 10^{-10}$$

$$\rightarrow 3.6\sigma \text{ level}$$

Need to scrutinise hadronic contributions:

 $\sigma(a_{\mu}^{\text{SM}})[10^{-10}] = 4.2 = 0.0^{\text{QED}} \oplus 0.1^{\text{EW}} \oplus 3.3^{\text{Had,LO}} \oplus 0.1^{\text{Had,N(N)LO}} \oplus 2.6^{\text{Had,LBL}}$ 



# The hadronic contribution to the muon g-2

All hadronic contributions (LO, NLO, NNLO), except for light-by-light scattering (LBLS), can be obtained via dispersion relations using a mix of experimental data and perturbative QCD

The LBLS contribution is a four-point function that is currently estimated using meson models







## The hadronic contribution to the muon g-2

In the following, all  $a_{\mu}$  numbers are given in units of  $10^{-10}$ 

### Introduction

Long history of  $a_{\mu}^{\text{Had,LO}}$  determinations involving theorists and experimentalists

$$a_{\mu}^{\text{Had,LO}} = \frac{1}{3} \left(\frac{\alpha}{\pi}\right)^2 \int_{m_{\pi}^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

- Improvement mostly driven by better
   e<sup>+</sup>e<sup>-</sup> → hadrons data (intermittently also hadronic tau decays used to improve over insufficient-quality low-mass e<sup>+</sup>e<sup>-</sup> data)
- The understanding of the data and the treatment of their uncertainties improved over time
- Sum-rule tests allowed to expand the use of perturbative QCD to predict *R*(*s*)
- Fairly consistent picture reached



### The challenge

The dispersion relation is solved using a mix of  $e^+e^- \rightarrow$  had data and QCD, depending on s



- [π<sup>0</sup>γ 1.8 GeV]: sum of 34 exclusive channels; few unmeasured channels are estimated using isospin symmetry
- [1.8 3.7 GeV]: agreement between data and QCD for *uds* continuum  $\rightarrow$  more precise QCD NNNLO used; J/ $\psi$  &  $\psi$ (2S) resonances from Breit-Wigners
- [ 3.7 5.0 GeV ]: open charm pair production: use of data
- [ 5.0 GeV ∞ ]: NNNLO QCD (assuming global quark-hadron duality to hold across *bb* threshold)

 $e^+e^- \rightarrow \pi^+\pi^-$  contributes 73% to  $a_\mu^{\rm Had,LO}$  and 59% to total uncertainty-squared

Many of the efforts in the last twenty years concentrated on that channel. Recent experiments dominated by systematic uncertainties

Three types of input data: Compilation and combination: DHMZ, Davier 1612.02743 (2016) [qu]  $\rho(770)$ TOF KLOE12 **Energy scans**: CMD-2 ( $\delta_{syst} \sim 0.8\%$ ),  $\rho - \omega$  mixing **Cross section** 10<sup>3</sup> OLYA \* BES SND ( $\delta_{syst} \sim 1.5\%$ ), + DM1, DM2, OLYA, CMD ◊ SND TOF CMD2 DM1 10<sup>2</sup> KLOE08 • DM2 **ISR-based measurements: BABAR** KLOE10 • BABAR ( $\delta_{syst} \sim 0.5\%$ ), BES-III ( $\delta_{syst} \sim 0.9\%$ ), KLOE 10 Average  $(\delta_{svst} \sim 0.8 - 1.4\%)$  $\rho(1700)$  $e^+$ Data combination hadrons  $e^+e^- \rightarrow \pi^+\pi^-$ **10<sup>-1</sup>**  $e^{-}$ 1.5 0.5 2 2.5 √s [GeV] Hadronic tau decay data via isospin •

Relative to uncertainty<sup>2</sup> due to quadratic addition (neglecting inter-channel correlations here)

31

symmetry (CVC): ALEPH, OPAL, CLEO, Belle ( $\delta_{syst-combined} \sim 0.7\%$ ),

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- **ISR-based measurements**: BABAR  $(\delta_{syst} \sim 0.5\%)$ , BES-III  $(\delta_{syst} \sim 0.9\%)$ , KLOE  $(\delta_{syst} \sim 0.8-1.4\%)$



 Hadronic tau decay data via isospin symmetry (CVC): ALEPH, OPAL, CLEO, Belle (δ<sub>syst-combined</sub> ~ 0.7%),

Relative to uncertainty<sup>2</sup> due to quadratic addition (neglecting inter-channel correlations here)

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Monumental ISR analysis: BABAR, 1205.2228 50 뜨 45 40 35 30 25 20 15 Pion form factor fit 10 well behaved, but 5E complex structure 0<sup>t</sup> 0.72 0.74 0.76 0.78 0.8 0.82  $\sqrt{s'}$  (GeV)

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- Energy scan measurements (ex. CMD-2 / 0.8%): detection efficiency, radiative corrections (0.4%), beam energy (0.3%), ...
- **ISR-based measurements** (ex. BABAR / >0.5%): pion identification (0.3%),  $\mu^+\mu^-$  reference (0.4%), ...
- Tau data (see later, ALEPH, 0.3% on normalisation): π<sup>0</sup> and photon reconstruction (0.2%), hadronic interactions (0.2%), ...

Huge amount of precision data, but — with a close look — one notices issues...

Three types of input data:

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Relative to uncertainty<sup>2</sup> due to quadratic addition (neglecting inter-channel correlations here)

## Digression: Combining data points for integration

The integration of data points belonging to different experiments, with different within-experiment, inter-experiment and inter-channel correlated systematic uncertainties, and with different data densities requires a careful treatment

It is thereby mandatory to test the accurateness of the integration procedure in terms of central value and uncertainty using representative models with known truth

#### DHMZ approach for a given channel:

- Quadratic interpolation of the data points for each experiment
- Local weighted average between interpolations performed in infinitesimal bins (1 MeV); local PDG error rescaling in case of incompatibility
- Full covariance matrices: correlations between data points of an experiment (systematic errors), between experiments and channels
- Error propagation (up to dispersion integrals) using pseudo experiments
- Possible bias tested in  $2\pi$  channel using a GS model (closure test): negligible for quadratic interpolation, but not for linear model (trapezoidal rule)


### The dominant $e^+e^- \rightarrow \pi^+\pi^-$ contribution





#### The dominant $e^+e^- \rightarrow \pi^+\pi^-$ contribution — impact on $a_\mu$

2003: dominated by VEPP-2M data:	$a_{\mu}^{\text{Had,LO}}[\pi^{+}\pi^{-}] = 508.2 \pm 5.2 \pm 2.7 (5.9_{\text{total}})$
2010: incl. ISR KLOE 2008 & BABAR:	$= 508.4 \pm 1.3 \pm 2.6$ (2.9)
2010: incl. also KLOE 2010:	$= 507.8 \pm 1.2 \pm 2.6 (2.9)$
2016: incl. also KLOE 2012 and BES-III:	$= 506.9 \pm 1.1 \pm 2.3 (2.5)$
Using all data except KLOE (BABAR):	= 510.11 ± 2.8 (502.15 ± 3.5)

[DHMZ numbers]

It is possible to also use precise  $\tau \rightarrow \pi^+ \pi^0 \nu$  data via isospin symmetry (CVC):



But it requires to correct for isospin breaking effects. Last estimate:  $516.2 \pm 2.9 \pm 2.0_{\text{IB}}$  (3.5) [2.1 $\sigma$  above  $e^+e^-$ ]

Some IB effects still under debate (eg,  $\gamma - \rho$  mixing). While the use of tau data helped significantly in the 1990-ies when the quality of the  $e^+e^-$  data was insufficient, with the much improved  $e^+e^-$  precision we consider the tau data less appealing for the  $a_{\mu}$  estimate

# The $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ contribution

 $e^+e^- \rightarrow \pi^+\pi^-\pi^0$  contributes with 6.6% to  $a_\mu^{\text{Had,LO}}$  and 19% to its uncertainty-squared

Good agreement among precision data (no BABAR data yet below 1.04 GeV)



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# The $e^+e^- \rightarrow \phi(1020) \rightarrow K_S K_L$ , $K^+K^-$ contributions

 $e^+e^- \rightarrow K_S K_L$ ,  $K^+K^-$  contribute to 5.1% to  $a_\mu^{\text{Had,LO}}$  and 2.3% to its uncertainty-squared

Good consistency in  $K_S K_L$  final state, new data from CMD-3 and BABAR BABAR reconstructed  $K_L$  directly via their nuclear interactions in the electromagnetic calorimeter



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Problems in  $K^+K^-$  channel, discrepancy between BABAR and CMD-2/SND (VEPP-2000)  $K^+K^-$  final state with low kaons at threshold hard to reconstruct for energy-scan experiments. Easier in BABAR due to ISR boost



BABAR ( $\sigma_{syst} = 0.7\%$ ) higher by 5.1% compared to CMD-2 ( $\sigma_{syst} = 2.2\%$ ) and by 9.6% compared to SND ( $\sigma_{syst} = 7.1\%$ ). Rise of  $a_{\mu}^{Had,LO}$  by ~1 (absolute) when including BABAR into average

Preliminary data from CMD-3 seem to indicate significantly larger cross section than earlier results. Waiting for publication

### The $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$ , $\pi^+\pi^-\pi^0\pi^0$ contributions

The four pion channels contribute with 4.5% to  $a_{\mu}^{\text{Had,LO}}$  and 3.7% to its uncertainty-squared

 $\pi^+\pi^-\pi^+\pi^-$  channel pretty well known since long, but  $\pi^+\pi^-\pi^0\pi^0$  challenging. Discrepancies in earlier data, but recent precise (~3.1% systematic) measurement from BABAR much improving



 $\geq 5\pi$  channels (incl.  $\eta\pi\pi$ ) contribute with 0.5% to  $a_{\mu}^{\text{Had,LO}}$  and 1.5% to its uncertainty-squared

Also here, large improvement from BABAR ISR data, problems in older datasets



#### The $e^+e^- \rightarrow KK \pi(\pi\pi)$ contributions (many charge combinations)

Past analyses suffered from missing final states that were estimated by symmetry arguments

Systematic measurement of exclusive processes by BABAR completes the  $KK\pi$  and (almost) all  $KK\pi\pi$  final states. Their sum contributes 0.5% to  $a_{\mu}^{\text{Had,LO}}$  and 0.2% to uncertainty-squared



Selection of measurements by BABAR and others

# Full combination of all exclusive modes: R(s) [ $\sqrt{s} \le 2 \text{ GeV}$ ]



# Full combination of all exclusive modes: R(s) [ $\sqrt{s} \le 2$ GeV]



# The charm resonance region (above $D\overline{D}$ threshold)

3.7–5.0 GeV region contributes with 1.1% to  $a_{\mu}^{\text{Had,LO}}$  and 0.8% to its uncertainty-squared

Good agreement between measurements. Precision dominated by BES ( $\sigma_{syst}$  ~ 3.5%)



# Data, QCD and the big picture (2016)



# Full compilation in numbers

#### **Legend**: First error statistical, second channel-specific systematic, third common systematic (correlated) For $R_{QCD}$ , uncertainties are due to: $\alpha_s$ , NNNLO truncation, resummation (FOPT vs. CIPT), quark masses

Channel	$a_{\mu}^{\text{had,LO}} \ [10^{-10}]$	Channel	$a_{\mu}^{\text{had,LO}} \ [10^{-10}]$
$\overline{\pi^0\gamma}$	$4.29 \pm 0.06 \pm 0.04 \pm 0.07$	$\overline{K^+K^-}$	$22.67 \pm 0.25 \pm 0.32 \pm 0.15$
$\eta\gamma$	$0.65 \pm 0.02 \pm 0.01 \pm 0.01$	$K_S K_L$	$12.82\pm 0.06\pm 0.18\pm 0.15$
$\pi^+\pi^-$	$506.93 \pm 1.09 \pm 2.17 \pm 0.75$	$\phi$ (non: $K\overline{K}, 3\pi, \pi\gamma, \eta\gamma$ )	$0.05\pm 0.00\pm 0.00\pm 0.00$
$\pi^+\pi^-\pi^0$	$46.00 \pm 0.40 \pm 1.09 \pm 0.86$	$K\overline{K}\pi$	$2.45 \pm 0.06 \pm 0.12 \pm 0.07$
$2\pi^{+}2\pi^{-}$	$13.70 \pm 0.03 \pm 0.28 \pm 0.13$	$K\overline{K}2\pi$	$1.35 \pm 0.09 \pm 0.38 \pm 0.03$
$\pi^+\pi^-2\pi^0$	$18.03 \pm 0.06 \pm 0.49 \pm 0.26$	$K\overline{K}3\pi$ (estimate)	$-0.03\pm0.01\pm0.02\pm0.00$
$2\pi^+ 2\pi^- \pi^0 \ (\eta \text{ excl.})$	$0.69 \pm 0.04 \pm 0.06 \pm 0.03$	$\phi\eta$	$0.36 \pm 0.02 \pm 0.02 \pm 0.01$
$\pi^+\pi^-3\pi^0$ ( $\eta$ excl., from isospin)	$0.35 \pm 0.02 \pm 0.03 \pm 0.01$	$\omega K \overline{K} \; (\omega  o \pi^0 \gamma)$	$0.00\pm 0.00\pm 0.00\pm 0.00$
$3\pi^{+}3\pi^{-}$	$0.11\pm 0.00\pm 0.01\pm 0.00$	$\omega\eta\pi^0$	$0.06 \pm 0.04 \pm 0.00 \pm 0.00$
$2\pi^+ 2\pi^- 2\pi^0 \ (\eta \text{ excl.})$	$0.72\pm 0.06\pm 0.07\pm 0.14$	$R$ data $3.7-5.0~{\rm GeV}$	$7.29 \pm 0.05 \pm 0.30 \pm 0.00$
$\pi^+\pi^-4\pi^0$ ( $\eta$ excl., from isospin)	$0.11\pm 0.01\pm 0.11\pm 0.00$	$J/\psi$	$6.28\pm0.07$
$\eta \pi^+ \pi^-$	$1.18\pm 0.03\pm 0.06\pm 0.02$	$\psi(2S)$	$1.57\pm0.03$
$\eta\omega$	$0.30 \pm 0.03 \pm 0.03 \pm 0.01$	$R_{\rm QCD} \ [1.8 – 3.7 \ { m GeV}] \ (uds)$	$33.45 \pm 0.14 \pm 0.12 \pm 0.21 \pm 0.04$
$\eta 2\pi^+ 2\pi^-$	$0.02\pm 0.01\pm 0.00\pm 0.00$	$R_{\rm QCD} \ [5.0-9.3 \ { m GeV}] \ (udsc)$	$6.86 \pm 0.02 \pm 0.00 \pm 0.01 \pm 0.03$
$\eta \pi^+ \pi^- 2 \pi^0$	$0.02\pm 0.01\pm 0.01\pm 0.00$	$R_{\rm QCD} \ [9.3-12.0 \ {\rm GeV}] \ (udscb)$	$1.21 \pm 0.00 \pm 0.00 \pm 0.00 \pm 0.01$
$\omega \pi^0 \ (\omega \to \pi^0 \gamma)$	$0.89 \pm 0.01 \pm 0.02 \pm 0.02$	$R_{\rm QCD} \ [12.0-40.0 \ {\rm GeV}] \ (udscb)$	$1.64 \pm 0.00 \pm 0.00 \pm 0.00 \pm 0.00$
$\omega(\pi\pi)^0 \ (\omega \to \pi^0 \gamma)$	$0.08\pm 0.00\pm 0.01\pm 0.00$	$R_{\rm QCD} [> 40.0 \text{ GeV}] (udscb)$	$0.16 \pm 0.00 \pm 0.00 \pm 0.00 \pm 0.00$
$\omega$ (non: $3\pi, \pi\gamma, \eta\gamma$ )	$0.36 \pm 0.00 \pm 0.01 \pm 0.00$	$R_{\rm QCD} \ [> 40.0 \ {\rm GeV}] \ (t)$	$0.00\pm 0.00\pm 0.00\pm 0.00\pm 0.00$
		Sum	$692.6 \pm 1.2 \pm 2.6 \pm 1.6 \pm 0.1_{\psi} \pm 0.3_{\rm QCD}$

 $a_{\mu}^{\text{Had,LO}} = (692.6 \pm 3.3) \cdot 10^{-10}$ 

NLO two-point correlation contributions to  $a_{\mu}^{\text{Had,NLO}}$  can be computed akin to the LO part via (a sum of) dispersion relations

$$a_{\mu}^{\text{Had,NLO}(i)} = \frac{1}{3} \left(\frac{\alpha}{\pi}\right)^2 \int_{m_{\pi}^2}^{\infty} ds \, \frac{K^{(i)}(s)}{s} R(s)$$



Each diagram corresponds to specific kernel function  $K^{(i)}$ 

 $\Rightarrow a_{\mu}^{\text{Had,NLO}} = (-9.87 \pm 0.09) \cdot 10^{-10}$ 

AKurz et al, 1511.08222.

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NNLO two-point function corrections have also been computed:  $a_{\mu}^{\text{Had,NNLO}} = (1.24 \pm 0.01) \cdot 10^{-10}$ 

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$$\Rightarrow a_{\mu}^{\text{Had,NLO}} = (-9.87 \pm 0.09) \cdot 10^{-10}$$

 $\Rightarrow a_u^{\text{Had,LBL}} = (10.5 \pm 2.6) \cdot 10^{-10}$ 

AKurz et al, 1511.08222.



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The four-point hadronic LBL scattering contribution, however, cannot be obtained this way and models are used instead

Calculation uses hadronic models with  $\pi^0$ ,  $\eta^{(\prime)}$ , ... pole in  $\pi^{(\prime)}$ ,  $\pi^{(\prime)}$  and  $\pi^{\pm}$  loops in the large- $N_C$  limit (*Lattice QCD offers promising alternative*)

Prades, de Rafael, Vainshtein, 0901.0306

· Educated guess (other groups find smaller / larger uncertainty)



# Muon g-2 summary

Summing all contributions [ · 10<sup>-10</sup>]:

 $a_{\mu}^{\text{QED}} = 11\ 658\ 471.895 \pm 0.008$  $a_{\mu}^{\text{EW}} = 15.36 \pm 0.10$  $a_{\mu}^{\text{Had,LO}} = 692.6 \pm 3.3$  $a_{\mu}^{\text{Had,NLO}} = -9.87 \pm 0.09$  $a_{\mu}^{\text{Had,NLO}} = 1.24 \pm 0.01$  $a_{\mu}^{\text{Had,LBL}} = 10.5 \pm 2.6$  $a_{\mu}^{\text{SM}} = (11\ 659\ 181.7 \pm 4.2) \cdot 10^{-10}$ 



 $\Delta a_{\mu} = a_{\mu}^{\text{Exp}} - a_{\mu}^{\text{SM}} = 27.4 \pm 6.3_{\text{exp}} \pm 4.2_{\text{SM}} \ (\pm 7.6_{\text{tot}}) \quad \rightarrow 3.6\sigma \text{ level}$ 

# Digression: Can it be real ?

The absolute size of the effect  $\Delta a_{\mu} = 27.4 \pm 7.6$  is large compared to EW contribution of 15.4 (but some cancellation among bosons in latter contribution)

• Generic decoupling new physics predicts:  $a_{\mu}^{\text{NP}} \sim \text{C} \cdot \left(\frac{m_{\mu}}{m_{\text{NP}}}\right)^2$  [Jegerlehner, Nyffeler, 0902.3360]

Here:  $m_{\rm NP} \sim 2$  TeV for C = 1,  $m_{\rm NP} \sim 100$  GeV for  $C = \frac{\alpha}{\pi}$  (natural strength),  $m_{\rm NP} \sim 5$  GeV for  $C = \left(\frac{\alpha}{\pi}\right)^2$ 

- Generic **SUSY** predicts:  $a_{\mu}^{\text{SUSY}} \sim \text{sign}(\mu) \cdot (13 \cdot 10^{-10}) \cdot \left(\frac{100 \text{ GeV}}{m_{\text{SUSY}}}\right)^2 \cdot \tan\beta$ 
  - In constrained SUSY models,  $\Delta a_{\mu}$  cannot be reconciled with the non-observation of strongly produced sparticles at the LHC [de Vries et al, MasterCode, 1504.03260]
  - However, general models such as the pMSSM can still accommodate  $\Delta a_{\mu}$  with light neutralinos, charginos and sleptons, not yet excluded by the LHC
- A "dark photon" ( $\gamma'$ ) coupling to SM via mixing with photon may give:  $a_{\mu}^{\gamma'} \sim \frac{\alpha}{2\pi} \varepsilon F(m_{\gamma'})$ 
  - $\Delta a_{\mu}$  is accommodated for coupling strength  $\varepsilon \sim 0.1$  0.2% and mass  $m_{\gamma \prime} \sim 10-100~{
    m MeV}$
  - Searches for a dark photon have been performed (so far negative) or are planned at colliders (LHC, *B*-factories, KLOE, ...) and fixed target experiments (Jefferson Lab, MAMI, ...)



# SM perspectives $(\Delta a_{\mu} = 27.4)$

Long standing 3-ish sigma discrepancy between data and SM on  $a_{\mu}$ . On the SM side:

- BABAR-KLOE discrepancy in  $\pi^+\pi^-$  channel unresolved. New data from CMD-3 expected, and a new BABAR analysis with the full data sample (0.3% systematic uncertainty may be reachable, current BABAR: 0.5% on peak)
- The  $\pi^+\pi^-\pi^0$  channel should be further improved (need BABAR data at and below  $\phi(1020)$ )
- The  $K^+K^-$  data from CMD-2/3/SND must be scrutinized and understood
- Need to compare BABAR and forthcoming CMD-3/SND results in the 1–2 GeV range (so far they agree)
- More results will come from BES-III and Belle-2
- Alternative  $a_{\mu}^{\text{Had,LO}}$  determinations: (1) Lattice calculations; (2) proposal via a dispersion integral in the spacelike region by an ultra-precise  $\mu e \rightarrow \mu e$  differential cross section measurement [Abbiendi et al, 1609.08987]



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Uncertainty on  $a_{\mu}^{\text{Had,LO}}$  improved by factor of 2 during the last 13 years. Now twice smaller than exp. uncertainty. LBL scattering, estimated from hadronic models, has an uncertainty of similar size that currently appears irreducible. Lattice QCD calculations may provide the way forward.

The recent & future SM improvements pave the road of a full exploitation of the next generation g-2 experiments at Fermilab and J-PARC

# New muon g-2 experiments



E989 aims at overall factor 4 improvement ( $\sigma_{tot} \sim 1.5$ ), following measurement principle of E821 (reusing E821 magnet) [1501.06858]

- Statistics: increased  $\mu$  injection efficiency, higher repetition rate
- Reduction of systematic uncertainty on  $\omega_a$  and *B*-field by factor 3 by improved instrumentation, shimming, stability, monitoring

Start of commissioning of E989 in 2017, final results expected by 2020!



E34 follows entirely new, compact "zero *E*-field" approach (off magic  $\gamma$ ) using low-emittance, low-momentum ("cold muon") beam

- μ<sup>+</sup> stopped to form muonium (e<sup>-</sup>μ<sup>+</sup>) atoms → laser ionisation leaves ~3 keV μ<sup>+</sup> → reacceleration to 300 MeV → injection into compact 3 T storage magnet with 66 cm orbit diameter → measure decay e<sup>+</sup> in silicon tracker
- Target  $a_{\mu}$  precision: 4.5 at stage-one, 1.2 final

E34 approved among future priority projects by KEK. Detector partially funded, moving ahead with construction. Fascinating project!

Both exps. also aim at improving  $\mu$ EDM sensitivity by 2 orders of magnitude to < 10<sup>-21</sup> e cm (E821: < 1.9 10<sup>-19</sup> e cm ) EDM tilts spin precession plane radially  $\rightarrow \mu$  polarisation acquires vertical component which oscillates with horizontal precession frequency

# Conclusions

Davier & DHMZ, 1612.02743 (Dec 2016)

Non-conclusive 3.6 $\sigma$  discrepancy between experiment and SM prediction in muon g-2

The "effect" is large, too large for new physics in light of the negative LHC results?

Fortunately, we do not need to speculate at this stage as new experiments and improved SM predictions are forthcoming!

JN 2009 (e<sup>+</sup>e<sup>-</sup>-based)  $-301 \pm 65$ DHMZ 2010 (r-based)  $-197 \pm 54$ DHMZ 2010 (e<sup>+</sup>e<sup>-</sup>)  $-289 \pm 49$ HLMNT 2011 (e<sup>+</sup>e<sup>-</sup>)  $-263 \pm 49$ DHMZ 2016 (e<sup>+</sup>e<sup>-</sup>)  $-274 \pm 42$ BNL-E821 (world average)  $0 \pm 63$ -500 -400 -300 -200 -100 0 -700 -600 × 10<sup>-11</sup>  $a_{\mu} - a_{\mu}^{exp}$ 

# Conclusions

Accurate, minute measurement seems to the non-scientific imagination, a less lofty and dignified work than looking for something new.

But [many of] the grandest discoveries of science have been but the rewards of accurate measurement and patient long-continued labour in the minute sifting of numerical results.

Said to originate from: William Thomson Kelvin

2 Aug 1871 in a speech to the British Association for the Advancement of Science



Lord Kelvin

Additional slides



# New experiments Fermilab E989

E821 result had larger statistical uncertainty (5.4<sub>stat</sub> vs. 3.3<sub>syst</sub>) [· 10<sup>-10</sup>]

New experiment E989 at Fermilab aims at overall factor 4 improvement ( $\sigma_{tot} \sim 1.5$ ) with equal statistical and systematic uncertainty, following measurement principle of E821: [1501.06858]

- Reuse of E821 magnet, radial magnetic and vertical electric focusing of muons in storage ring, magic γ
- Reduction of statistical uncertainty by factor  $\sim \sqrt{21}$  ( $\sim 200B$  detected positrons) with less intense proton beam (ie, 84 times larger integrated luminosity needed): increased  $\mu$  injection efficiency, higher repetition rate
- Reduction of systematic uncertainty on  $\omega_a$  by factor 3: segmented calorimeters and waveform digitisation to separate pileup positrons; also improved timing measurement, energy resolution, gain stability
- Three tracker stations in front of calorimeters: monitor muon loss, muon momentum spread (deviation from magic γ), and coherent betatron oscillation motion (via positron trajectory),
- Improved magnetic field (aka  $\omega_p$ ) uniformity by passive shimming (mechanical adjustments), better mechanical and thermal stability, better monitoring, frequent field mapping under running conditions

#### Start of commissioning of E989 in 2017, final results expected by 2020!

E989 also aims at improving  $\mu$ EDM sensitivity by 2 orders of magnitude to < 10<sup>-21</sup> e cm (E821: < 1.9 10<sup>-19</sup> e cm ) EDM tilts spin precession plane radially  $\rightarrow \mu$  polarisation acquires vertical component which oscillates with horizontal precession frequency



# New experiments J-PARC E34

Entirely new, compact "zero *E*-field" approach (off magic γ)

- Replace electric quadrupole field focusing in E821 by low-emittance, low-momentum ("cold muon") beam
- Positive muons from pion decays are stopped in aerogel target where they form muonium  $(e^{-\mu^{+}})$  atoms
- The muonium atoms are laser ionised, leaving cold muons of momentum 3 keV in average
- These are reaccelerated (to increase lifetime) in a linac to 300 MeV
- Muons are injected into a compact, ultra-precise (iron shimmed) 3 T storage magnet with 66 cm orbit diameter (14 m in E821 / E989)
- The decay positrons are measured in silicon strip tracking detector (not a calorimeter) needed because of dense muon decay environment
- Target: 4.5 at stage-one, and 1.2 final on  $a_{\mu}$  [· 10<sup>-10</sup>], and ~10<sup>-21</sup> e cm final µEDM sensitivity

E34 was approved among the future priority projects by KEK. Detector partially funded, moving ahead with construction. Fascinating project!

# Dark photon search summary



