

Hints of New Physics in $b \rightarrow s$ transitions

(or)

Looking for New Physics in Flavour Physics in quark sector

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DESY-Zeuthen



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www.utfit.org

Flavour Physics in the *Standard Model* (SM) in the quark sector:

~ half of the
Standard Model

10 free parameters

6 quarks masses

4 CKM parameters

Wolfenstein parametrization : $\lambda, A, \bar{\rho}, \bar{\eta}$
 η responsible of CP violation in SM

In the Standard Model, charged weak interactions among quarks are codified in a 3 X 3 unitarity matrix : the **CKM Matrix**.

The existence of this matrix conveys the fact that the quarks which participate to weak processes are a linear combination of mass eigenstates

*The fermion sector is poorly constrained by SM + Higgs Mechanism
mass hierarchy and CKM parameters*

The Unitarity Triangle

The CKM is unitary

CKM matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Wolfenstein parameterization:

$$\simeq \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

$$\overline{AB} = \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = \sqrt{(1 - \bar{\rho})^2 + \bar{\eta}^2} = \frac{1}{\lambda} \left| \frac{V_{td}}{V_{cb}} \right| \sim \frac{1}{\lambda} \left| \frac{V_{td}}{V_{ts}} \right|$$

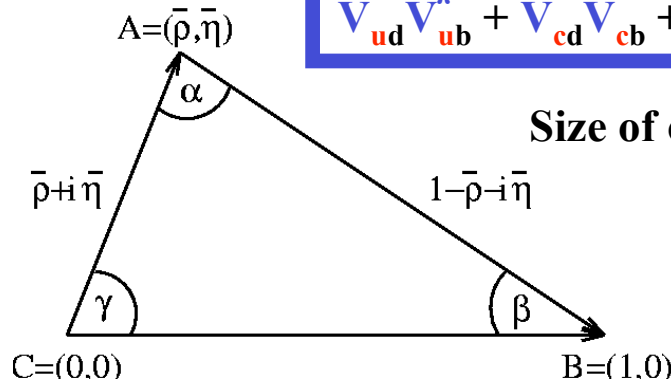
$$\overline{AC} = \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} = \sqrt{\bar{\rho}^2 + \bar{\eta}^2} = \left(1 - \frac{\lambda^2}{2}\right) \frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right|$$

$$\beta = \arg\left(\frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*}\right) = \text{atan}\left(\frac{\bar{\eta}}{(1 - \bar{\rho})}\right)$$

$$\gamma = \arg\left(\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right) = \text{atan}\left(\frac{\bar{\eta}}{\bar{\rho}}\right)$$

$$\alpha + \beta + \gamma = \pi$$

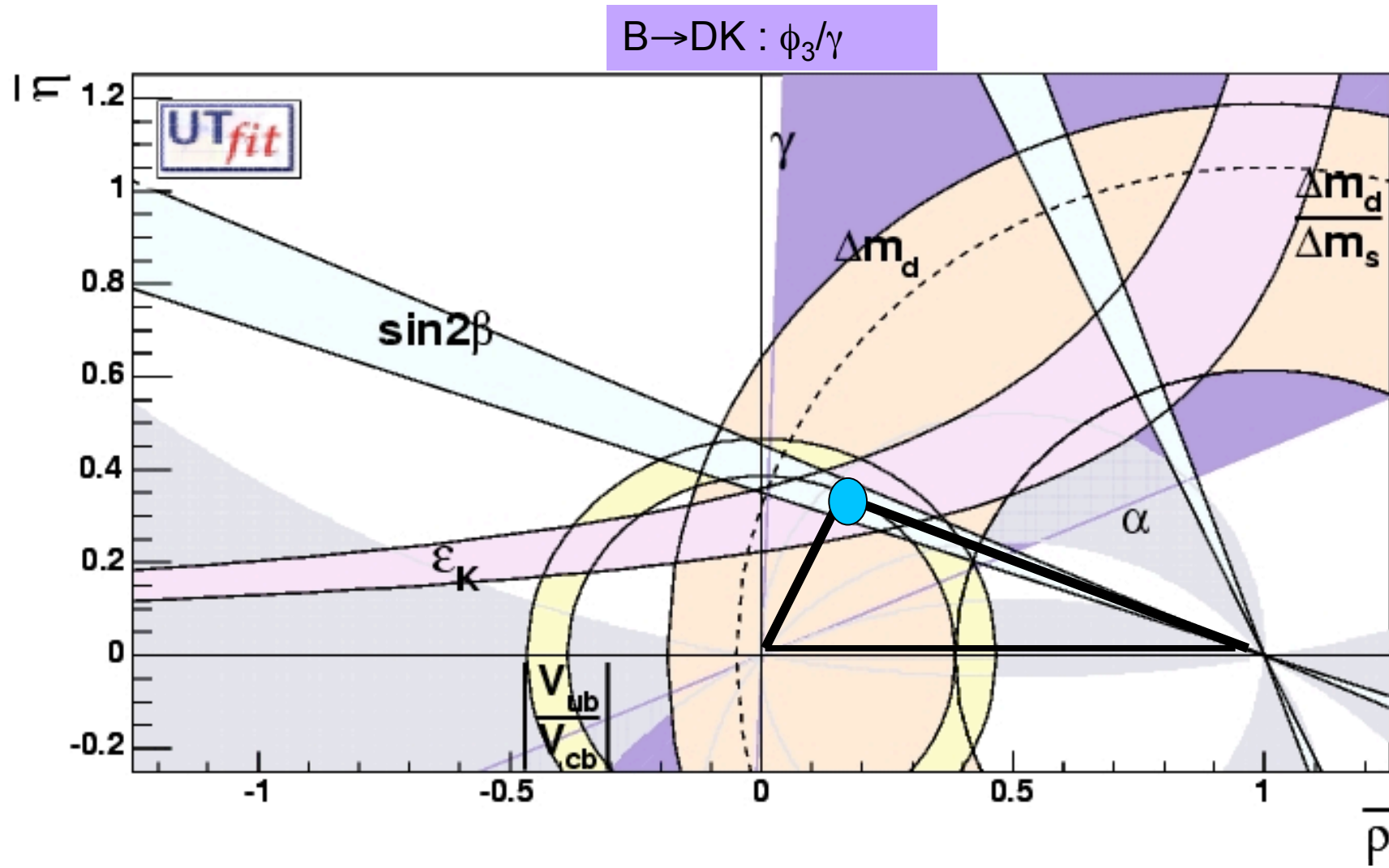
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



Size of order λ^3 : λ^3 : λ^3

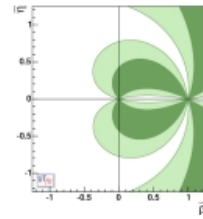
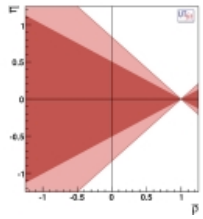
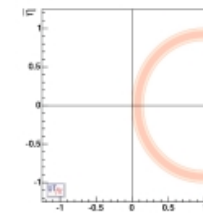
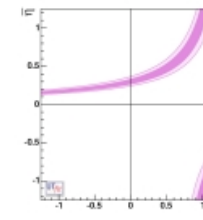
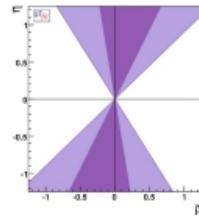
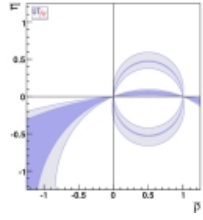
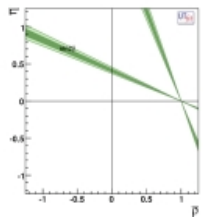
$(b \rightarrow u)/(b \rightarrow c)$	$\bar{\rho}^2 + \bar{\eta}^2$	$f_+, F(1), \dots$
Δm_d	$(1 - \bar{\rho})^2 + \bar{\eta}^2$	$f_{B_d}^2 \mathbf{B}_{B_d}$
$\Delta m_d / \Delta m_s$	$(1 - \bar{\rho})^2 + \bar{\eta}^2$	ξ
ϵ_K	$\bar{\eta} [(1 - \bar{\rho}) + P]$	\mathbf{B}_K
β	$\text{atan}(\bar{\eta} / (1 - \bar{\rho}))$	-
γ	$\text{atan}(\bar{\eta} / \bar{\rho})$	-

An example on how to fit the UT parameters and fit new physics

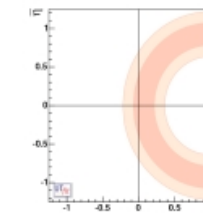
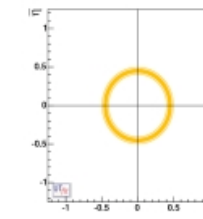




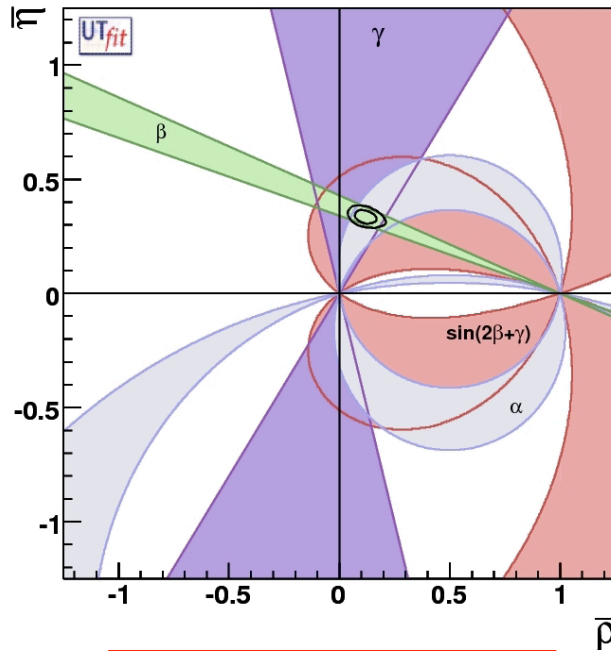
Fit with the Standard Model (SM)



function(ρ, η, \dots)



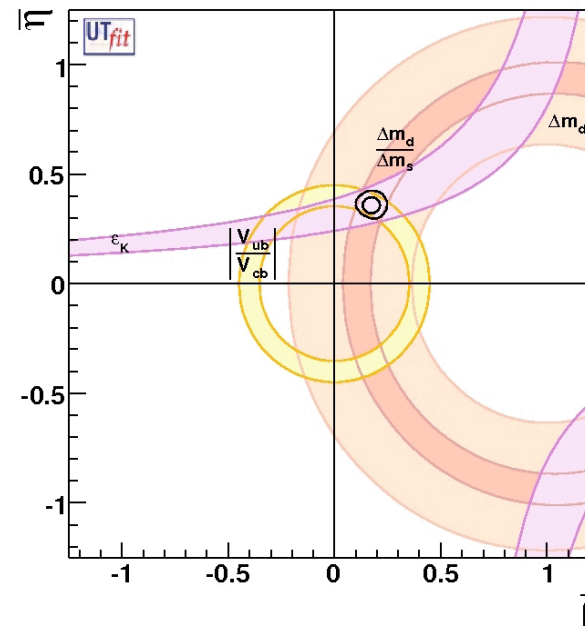
Angles



$$\rho = 0.120 \pm 0.034$$

$$\eta = 0.335 \pm 0.020$$

Sides + ϵ_K

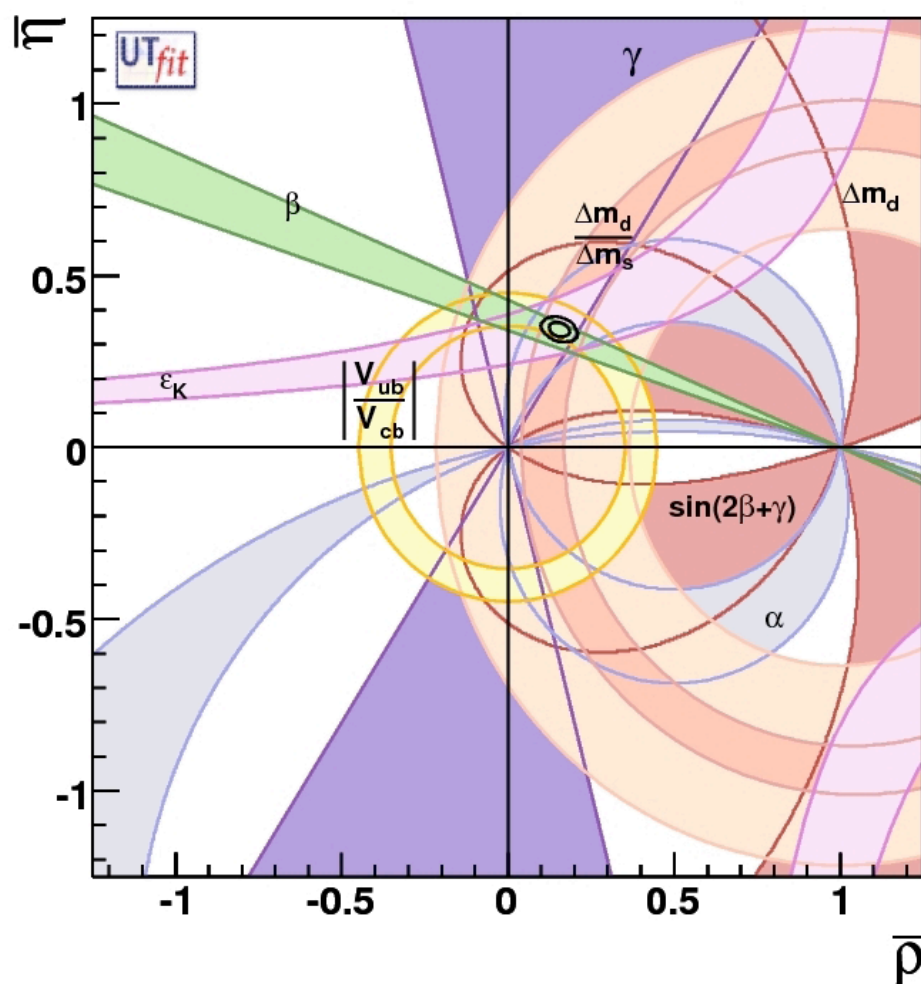


$$\rho = 0.175 \pm 0.027$$

$$\eta = 0.360 \pm 0.023$$

Global Fit

$$\Delta m_d, \Delta m_s, V_{ub}, V_{cb}, \epsilon_K + \cos 2\beta + \beta + \alpha + \gamma + 2\beta + \gamma$$



Tremendous success of the CKM picture

$$\bar{\rho} = 0.155 \pm 0.022$$

$$\bar{\eta} = 0.342 \pm 0.014$$

Should we stop here ?

How to look for NP ?
And in case of no observation to
establish how much room is left
for NP effects...?

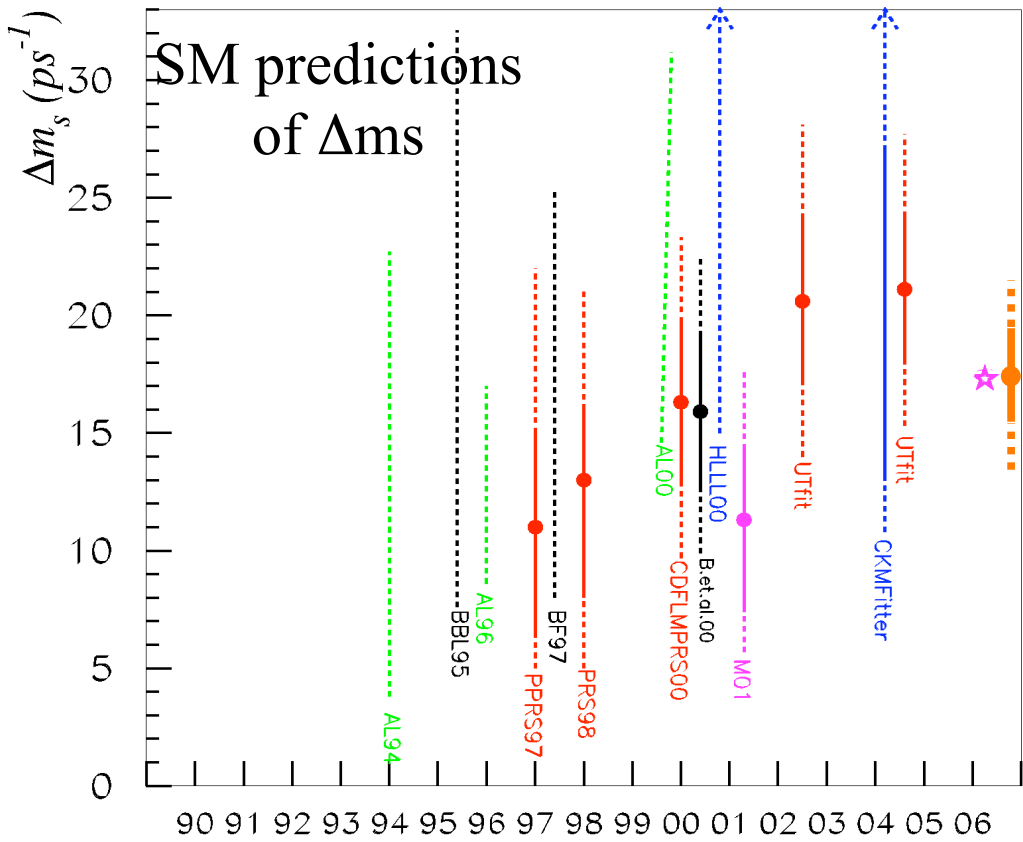
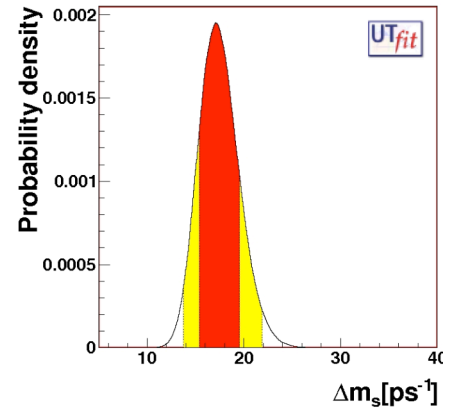
Long story...

Some example in next 4 transparencies..

some specific example of NP tests..

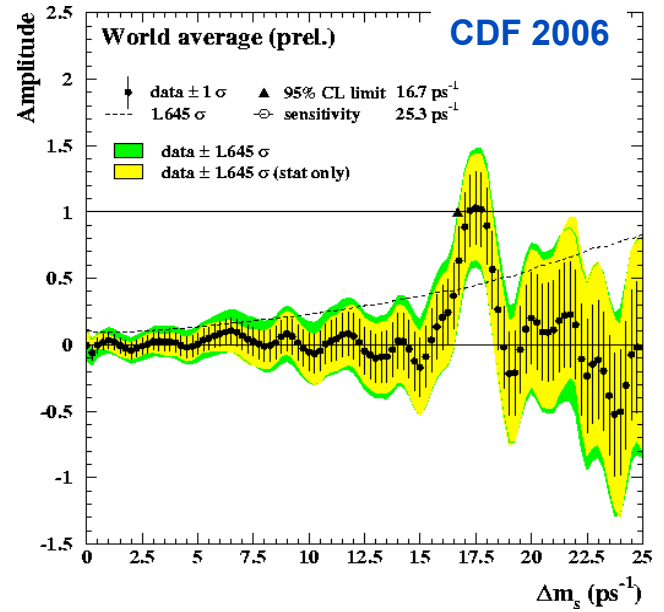
Δm_s

SM expectation
 $\Delta m_s = (17.5 \pm 2.1) \text{ ps}^{-1}$



CDF only : signal at 5σ

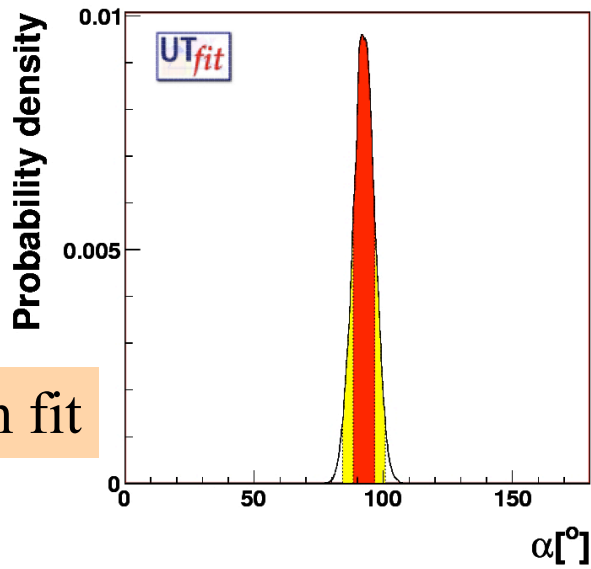
$\Delta m_s = (17.77 \pm 0.12) \text{ ps}^{-1}$



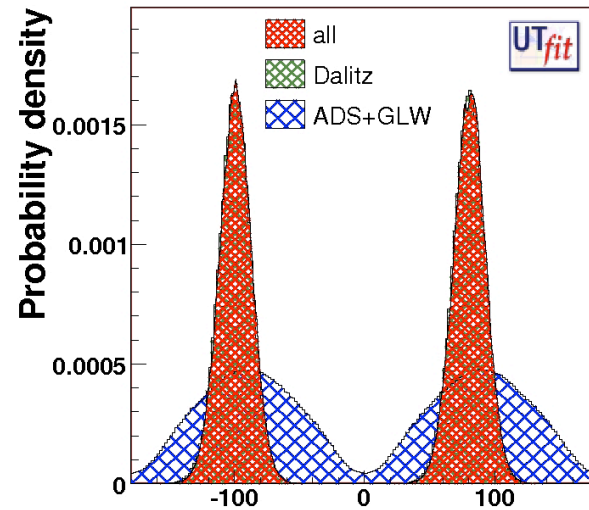
Tevatron results
Limited by Lattice calculations



From fit



$$\gamma = (64.0 \pm 3.0)^\circ$$



$$\gamma = (81 \pm 13)^\circ \quad \gamma [^\circ]$$

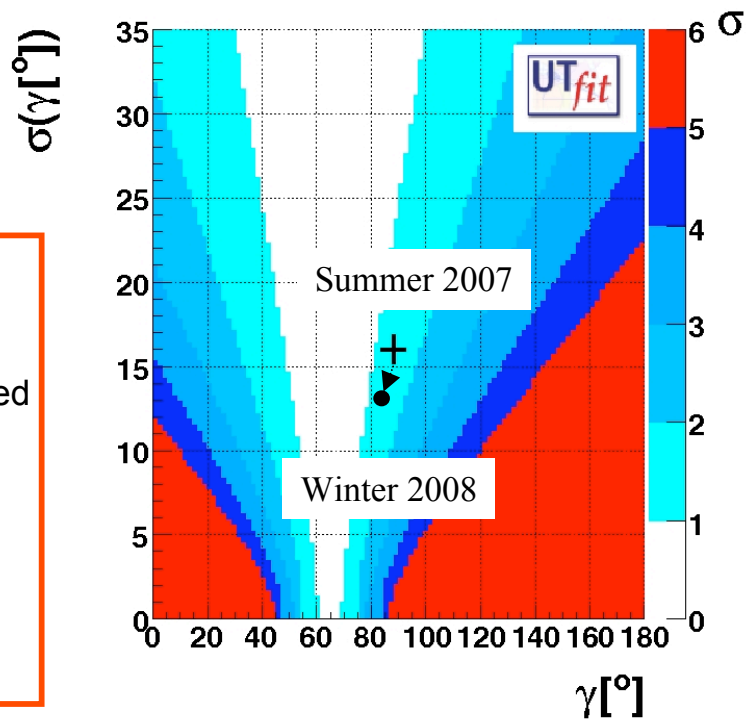
(up to π ambiguity)

Direct measurement

Legenda

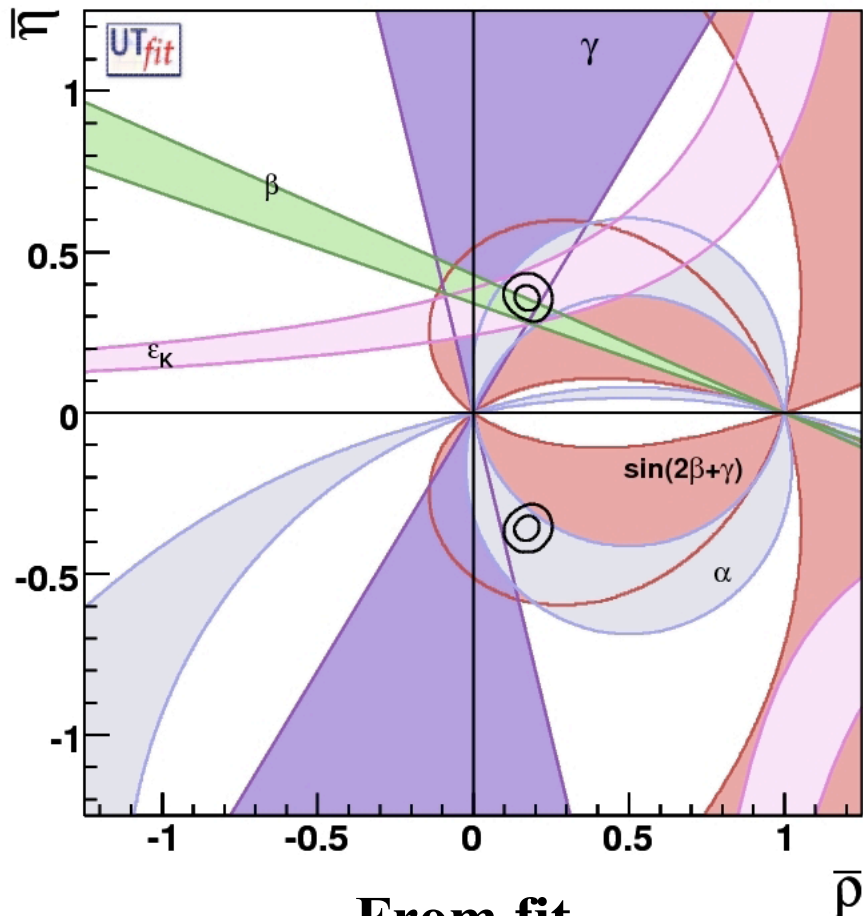
agreement between the predicted values and the measurements at better than :

- | | | |
|------|------|------|
| □ 1σ | ■ 3σ | ■ 5σ |
| ■ 2σ | ■ 4σ | ■ 6σ |



B factories results
LHCb expected to contribute

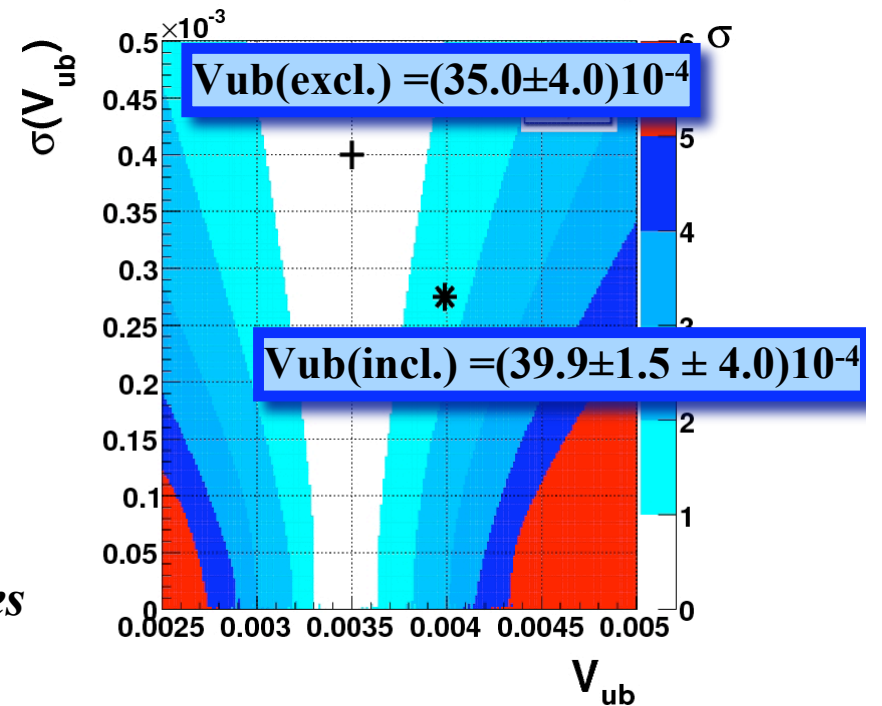
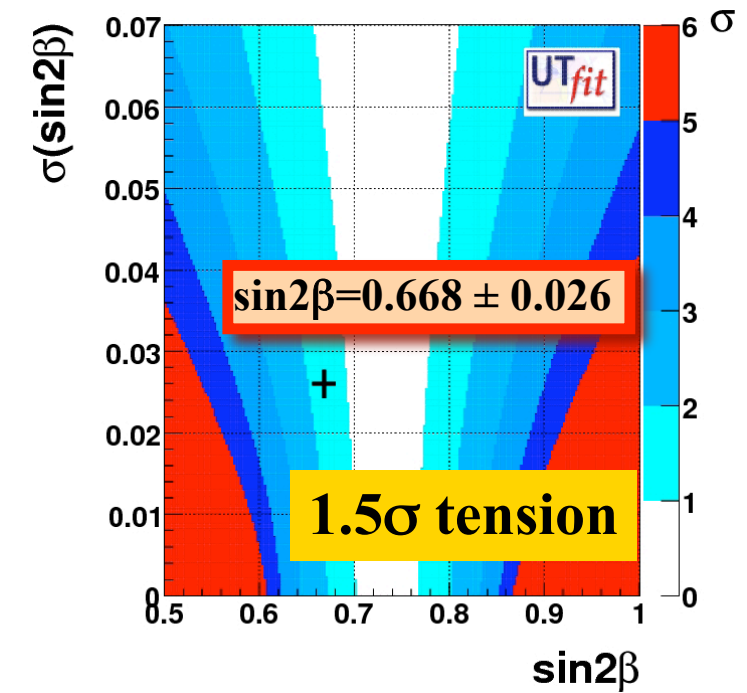
$\sin 2\beta$ vs V_{ub}



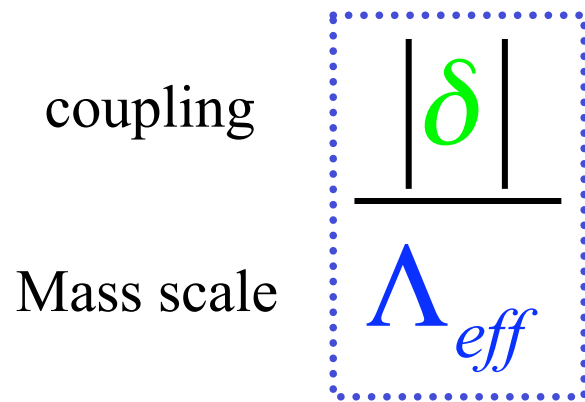
$$\sin 2\beta = 0.736 \pm 0.034$$

$$V_{ub} = (34.8 \pm 1.6) 10^{-4}$$

B factories results



Flavour Physics measure



NP physics could be always around the corner

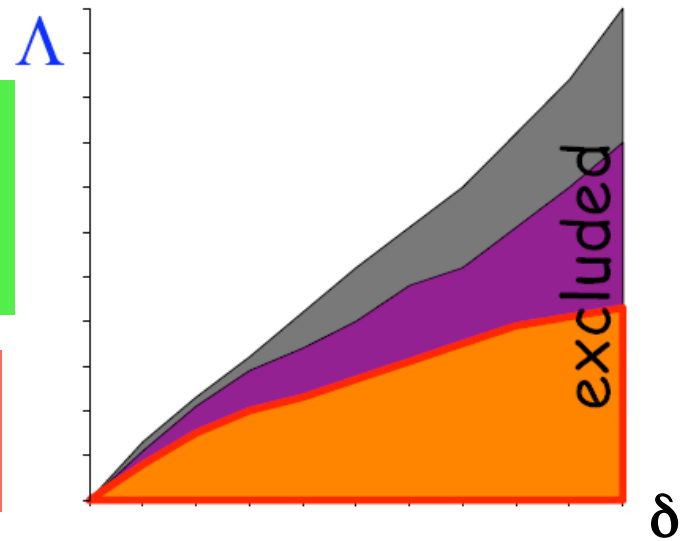
WHAT IS REALLY STRANGE IS THAT WE DID NOT SEE ANYTHING....

With masses of New Particles at few hundred GeV effects on measurable quantities should be important

Problem known as the FLAVOUR PROBLEM

$\Lambda_{\text{eff}} \lesssim 1\text{TeV}$ + flavour-mixing
protected by additional symmetries (as MFV)

Couplings can be still large if
 $\Lambda_{\text{eff}} > 1..10..\text{TeV}$



If there is NP at scale Λ , it will generate new operator of dimension D with coefficients proportional to Λ^{4-D}

only operator of $D=6$ contribute. So that in fact you have a dependence on $1/\Lambda^2$

Today we concentrate on a
Model Independent fit to $\Delta F=2$ observable
which show a 2.5σ evidence of NP
in the $b \rightarrow s$ transitions

Fit in a NP model independent approach

$\Delta F=2$

Parametrizing NP physics in $\Delta F=2$ processes

$$C_q e^{i\delta_d} = \frac{Q_{\Delta B=2}^{NP} + Q_{\Delta B=2}^{SM}}{Q_{\Delta B=2}^{SM}}$$

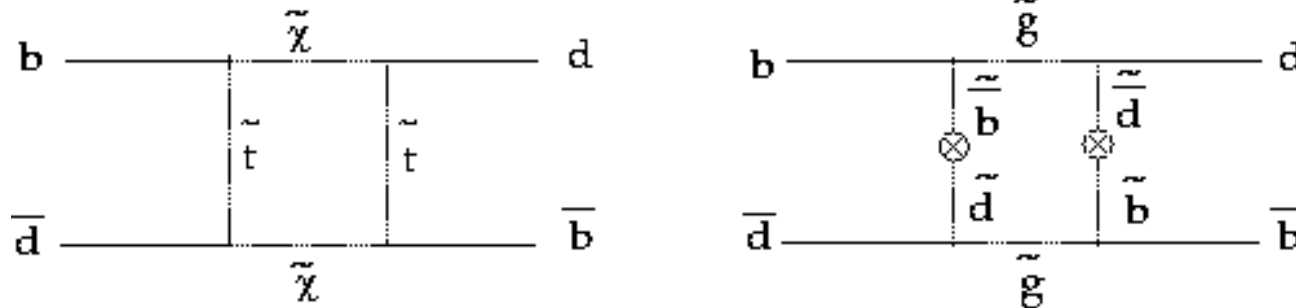
Soares, Wolfenstein PRD47;
 Deshpande, Dutta, Oh PRL77;
 Silva, Wolfenstein PRD55;
 Cohen et al. PRL78;
 Grossman, Nir, Worah PLB407;
 Ciuchini et al. @ CKM Durham

$\Delta m_d^{EXP} = C_{B_d} \Delta m_d^{SM}$	$f(\rho, \eta, C_{B_d}, QCD..)$
$A_{CP}(J/\Psi, K^0) = \sin(2\beta + 2\phi_{B_d})$	$f(\rho, \eta, \phi_{B_d})$
$\alpha^{EXP} = \alpha^{SM} - \phi_{B_d}$	$f(\rho, \eta, \phi_{B_d})$
$ \epsilon_K ^{EXP} = C_\epsilon \epsilon_K ^{SM}$	$f(\rho, \eta, C_\epsilon, QCD..)$
$\Delta m_s^{EXP} = C_{B_s} \Delta m_s^{SM}$	$f(\rho, \eta, C_{B_s}, QCD..)$
$A_{CP}(J/\Psi, \phi) = \sin(2\beta_s - 2\phi_{B_s})$	$f(\rho, \eta, \phi_{B_s})$
...	

Using the example of the Supersymmetry

To help with a more specific example :

Example for B oscillations (FCNC- $\Delta B=2$) :



$$\left| \frac{Q_{\Delta B=2}^{NP}}{Q_{\Delta B=2}^{SM}} \right| \leq p_r \quad \rightarrow \quad \frac{|\delta_{bq}|}{\Lambda_{eff}} \leq \sqrt{p_r} \frac{|V_{tb}^* V_{tq}|}{M_W}$$

p_r upper limit of the relative contribution of NP
 δ_{bd} NP physics coupling
 Λ_{eff} NP scale (masses of new particles)

If couplings ~ 1

$$\delta_{bq} \sim 1 \quad \Lambda_{eff} \sim 10/\sqrt{p_r} \text{ TeV}$$

$$\delta_{bs} \sim 1 \quad \Lambda_{eff} \sim 2/\sqrt{p_r} \text{ TeV}$$

all possible intermediate possibilities

$$\delta_{bq} \sim 0.1 \quad \Lambda_{eff} \sim 1/\sqrt{p_r} \text{ TeV}$$

$$\delta_{bs} \sim 0.1 \quad \Lambda_{eff} \sim 0.2/\sqrt{p_r} \text{ TeV}$$

Minimal Flavour Violation

$$\delta_{q'd} \approx V_{tq'}^* V_{td}$$

(couplings small as CKM elements)

$$\Lambda_{eff} \sim 0.08/\sqrt{p_r} \text{ TeV}$$

Oversimplified picture : for a quantitative analysis see for instance

UTfit collaboration

JHEP 0803:049,2008 *arXiv:0707.0636*

Constraints

		ρ, η	C_d	φ_d	C_s	φ_s	$C_{\varepsilon K}$
Tree processes	γ (DK)	X					
	V_{ub}/V_{cb}	X					
	Δm_d	X	X				
1 \leftrightarrow 3 family	ACP (J/ Ψ K)	X		X			
	ACP (D π (ρ),DK π)	X		X			
	A_{SL}		X	X			
	α ($\rho\rho, \rho\pi, \pi\pi$)	X		X			
2 \leftrightarrow 3 family	A_{CH}		X	X	X	X	
	$\Delta\Gamma_s/\Gamma_s$				X	X	
	Δm_s				X		
	ASL(Bs)				X	X	
1 \leftrightarrow 2 family	ACP (J/ Ψ ϕ)	$\sim X$				X	
	ε_K	X					X

5 new free parameters

C_s, φ_s B_s mixing

C_d, φ_d B_d mixing

$C_{\varepsilon K}$ K mixing

Today :

fit possible with 10 constraints

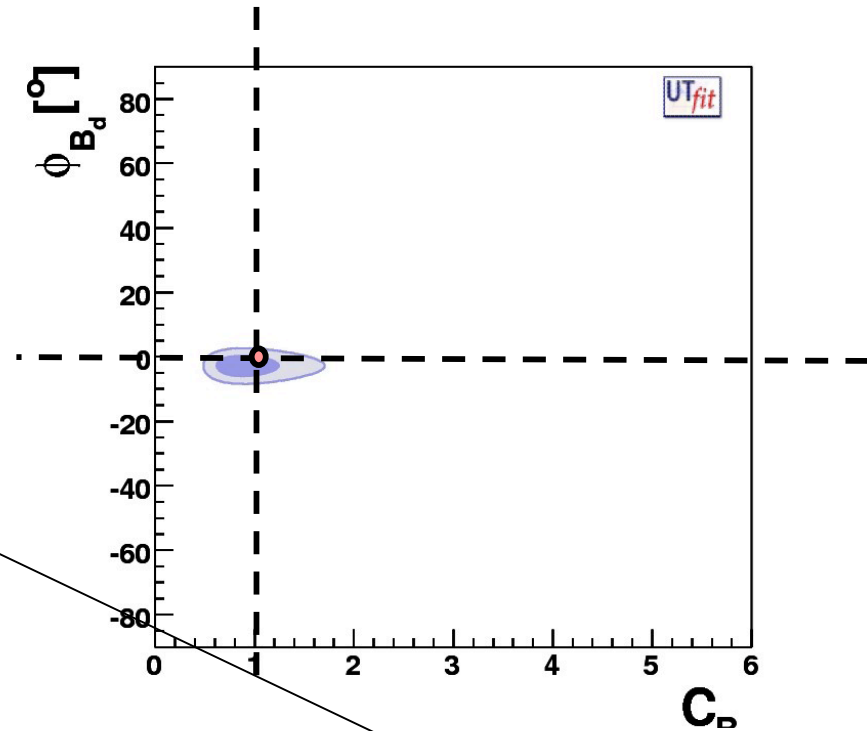
and 7 free parameters

$(\rho, \eta, C_d, \varphi_d, C_s, \varphi_s, C_{\varepsilon K})$

B_d

$$C_{B_d} = 0.96 \pm 0.23$$

$$\phi_{B_d} = -(2.9 \pm 1.9)^\circ$$

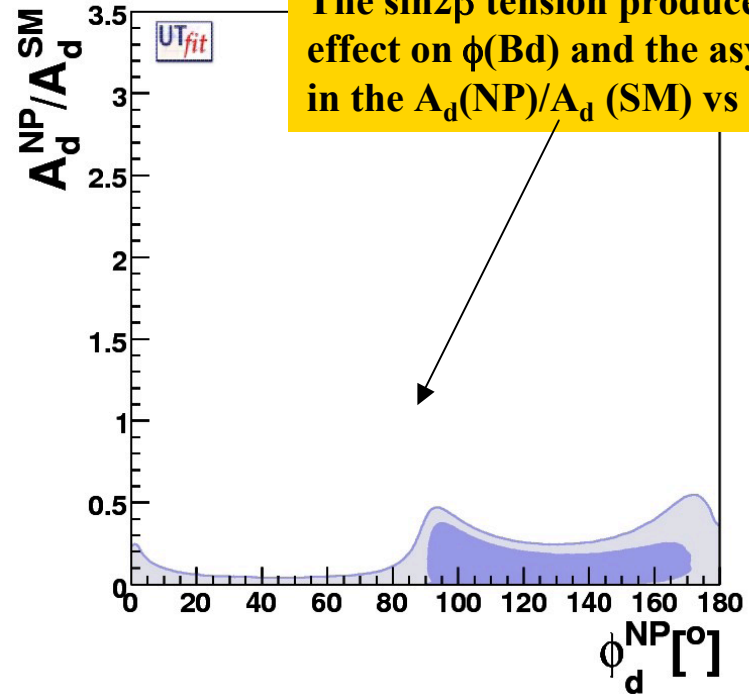


A_{NP}/A_{SM} vs ϕ_{NP}

$$C_{B_d} e^{2i\phi_{B_d}} = \frac{A_{SM} e^{2i\beta} + A_{NP} e^{2i(\beta + \phi_{NP})}}{A_{SM} e^{2i\beta}}$$

With present data $A_{NP}/A_{SM} = 0 @ 1.5\sigma$

$A_{NP}/A_{SM} \sim 1$ only if $\phi_{NP} \sim 0$
 $A_{NP}/A_{SM} \sim 0-30\%$ @95% prob.



The $\sin 2\beta$ tension produces a 1.5σ effect on $\phi(B_d)$ and the asymmetry in the $A_d(NP)/A_d(SM)$ vs $\phi(NP)$ plot

Actual sensitivity
for a generic NP phase
in the B_d sector
 $r = A_{NP}/A_{SM} \sim 10-15\%$

This is not yet a prove that if NP should be MFV violating

Just for showing the link between precision and mass scale



$$\left| \frac{Q_{\Delta B=2}^{NP}}{Q_{\Delta B=2}^{SM}} \right| \leq r \quad \rightarrow \quad \frac{|\delta_{bq}|}{\Lambda_{eff}} \leq \sqrt{r} \frac{|V_{tb}^* V_{tq}|}{M_W}$$

r upper limit of the relative contribution of NP
δ_{bd} NP physics coupling
Λ_{eff} NP scale (masses of new particles)

Take a case where $\delta_{q'd} \approx V_{tq}^* V_{td} \longrightarrow \Lambda_{eff} \sim 80/\sqrt{r} \text{ GeV} \longrightarrow \Lambda_{eff} \sim (200-250) \text{ GeV}$

MORE PRECISION IS NEEDED

B_s sector : very recent results

	ρ, η	C_d	φ_d	C_s	φ_s
A_{CH}		X	X	X	X
$\tau(B_s), \Delta\Gamma_s/\Gamma_s$				X	X
Δm_s				X	
ASL(B _s)				X	X
ACP (J/Ψ φ)	~X				X

D0, CDF (2006-2007)

CDF, D0, LEP

CDF (~2006), D0, LEP

D0 (2007)

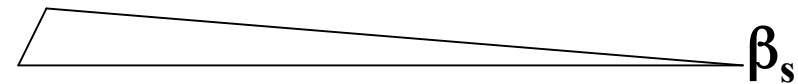
D0, CDF (2007-2008)



The realm of Tevatron

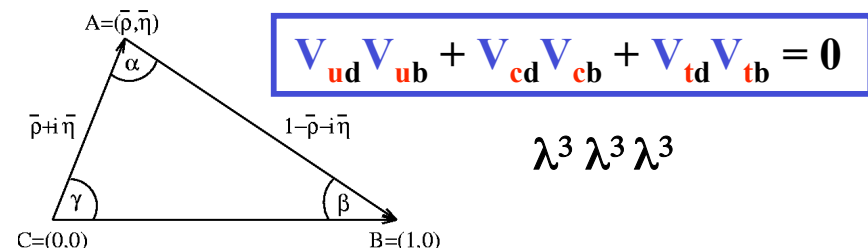
$$\beta_s = \arg\left(\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right) = (1.03 \pm 0.06)^\circ$$

$$V_{td}V_{cd} + V_{ts}V_{cs} + V_{tb}V_{cb} = 0 \quad \lambda^2 \lambda^4 \lambda^4$$



Recall that in B_d sector

$$\beta = \arg\left(\frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*}\right) = (21.8 \pm 0.7)^\circ$$



ϕ_s vs of $\Delta\Gamma_s$ using $B_s \rightarrow J/\psi\phi$

Nota bene
for the experimental result
 $\phi_s = -2\beta_s$

Angular (θ, φ, ψ) analysis as a function of the **proper time**.

Similar to measurement of β in $B_d \rightarrow J/\psi K^*$.

Respect to the B_d case, there is additional sensitivity because of $\Delta\Gamma_s$ term

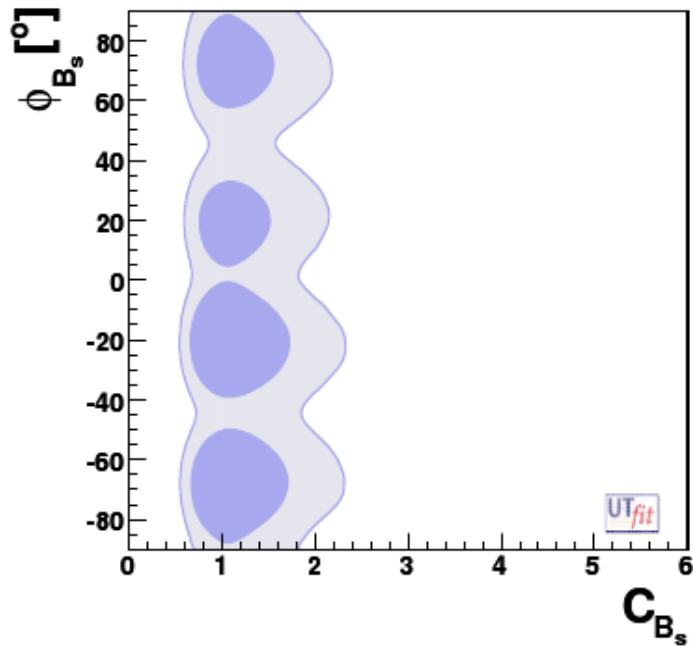
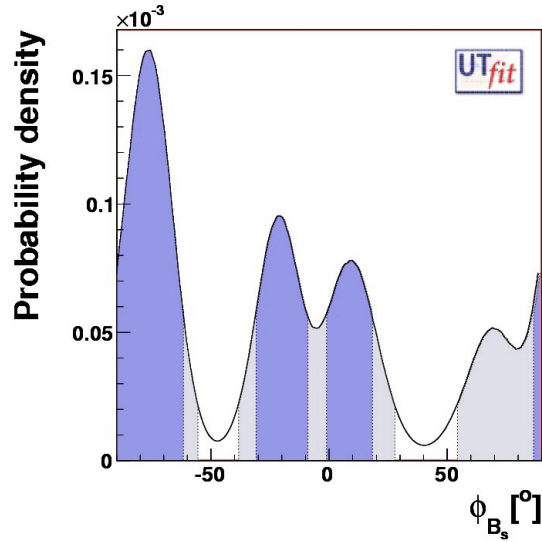
$$\frac{d^4\Gamma}{dt d\cos\theta d\varphi d\cos\psi} \propto$$

$$\begin{aligned} & 2 \cos^2 \psi (1 - \sin^2 \theta \cos^2 \varphi) |A_0(t)|^2 \\ & + \sin^2 \psi (1 - \sin^2 \theta \sin^2 \varphi) |A_{\parallel}(t)|^2 \\ & + \sin^2 \psi \sin^2 \theta |A_{\perp}(t)|^2 \\ & + (1/\sqrt{2}) \sin 2\psi \sin^2 \theta \sin 2\varphi \operatorname{Re}(A_0^*(t) A_{\parallel}(t)) \\ & + (1/\sqrt{2}) \sin 2\psi \sin 2\theta \cos \varphi \operatorname{Im}(A_0^*(t) A_{\perp}(t)) \\ & - \sin^2 \psi \sin 2\theta \sin \varphi \operatorname{Im}(A_{\parallel}^*(t) A_{\perp}(t)). \end{aligned}$$

Dunietz, Fleisher and Nierste
Phys.Rev D63:114015,2001

Experimentally θ and φ are well determined from the μ from J/ψ
 ψ is the decay plane between the J/ψ and the ϕ .

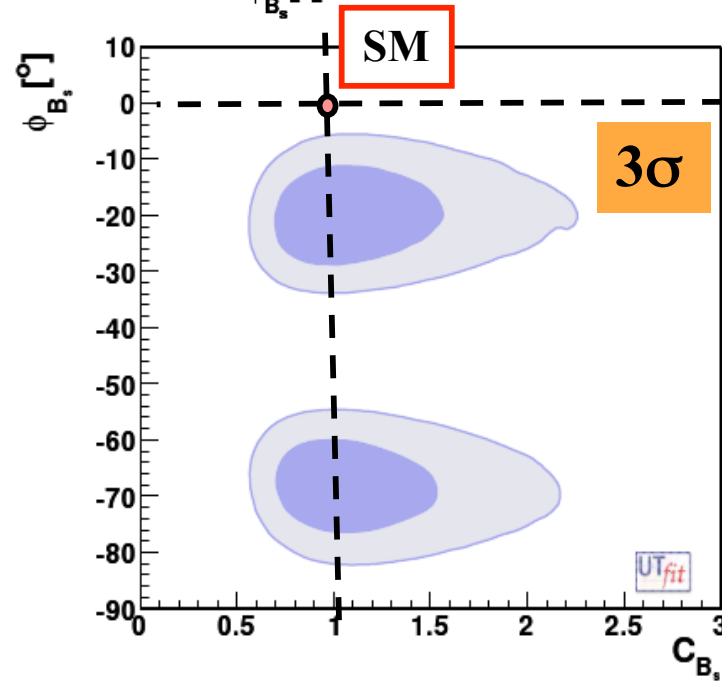
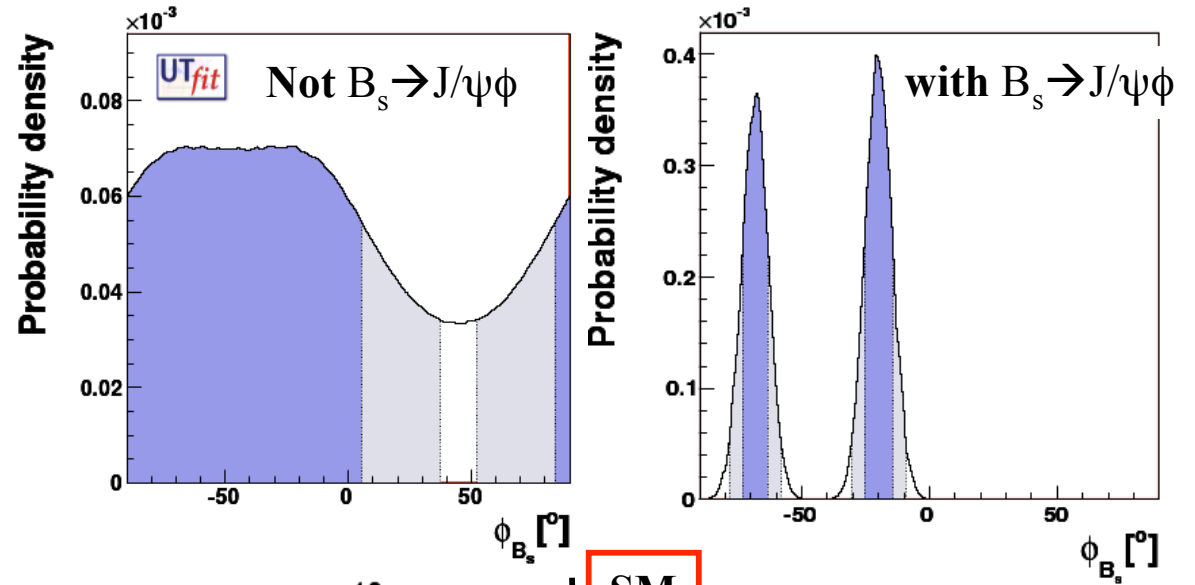
Winter 2007



$$C(B_s) = 1.11 \pm 0.32$$

$$\phi(B_s) = (-69 \pm 14)^\circ \cup (-20 \pm 14)^\circ \cup (20 \pm 5)^\circ \cup (72 \pm 8)^\circ$$

Before ICHEP 2008



$$C(B_s) = 1.07 \pm 0.29$$

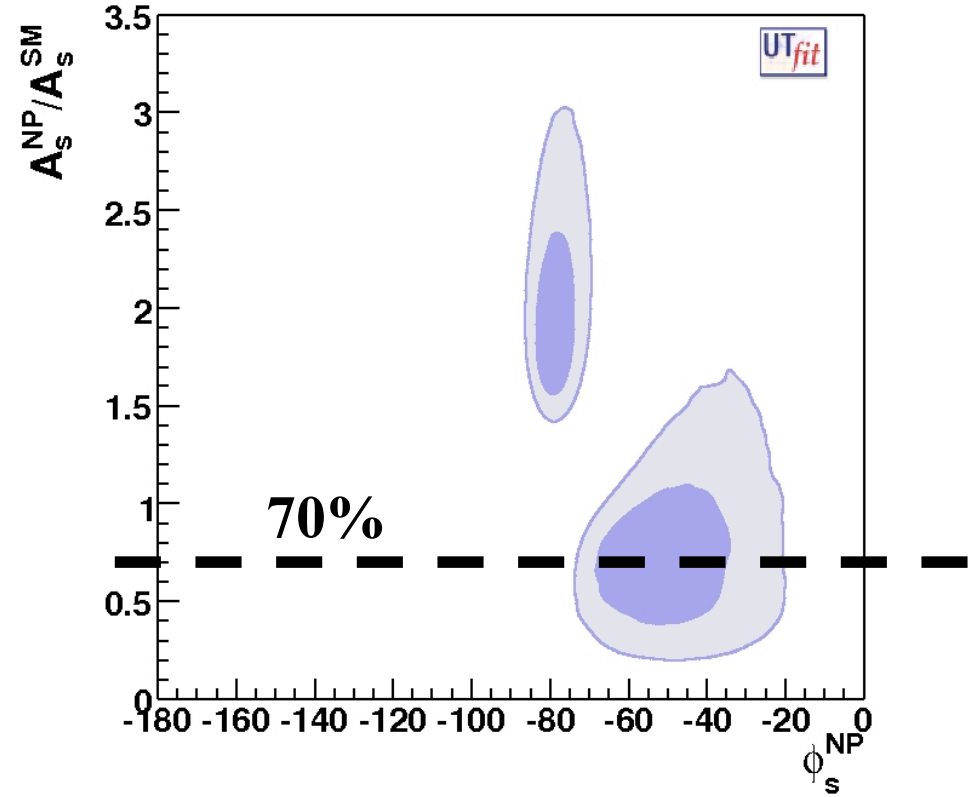
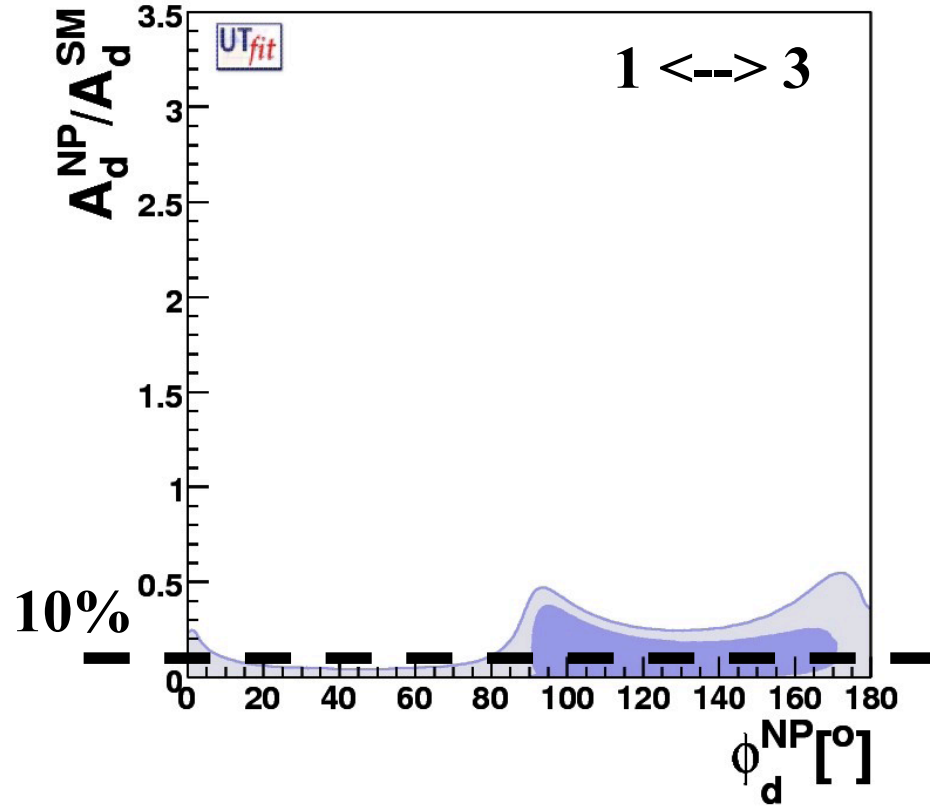
$$\phi(B_s) = (-19.9 \pm 5.6)^\circ \cup (-68.2 \pm 4.9)^\circ$$

arXiv:0803.0659v1 [hep-ph] 5 Mar 2008

B_d 1 \leftrightarrow 3

vs

B_s 2 \leftrightarrow 3

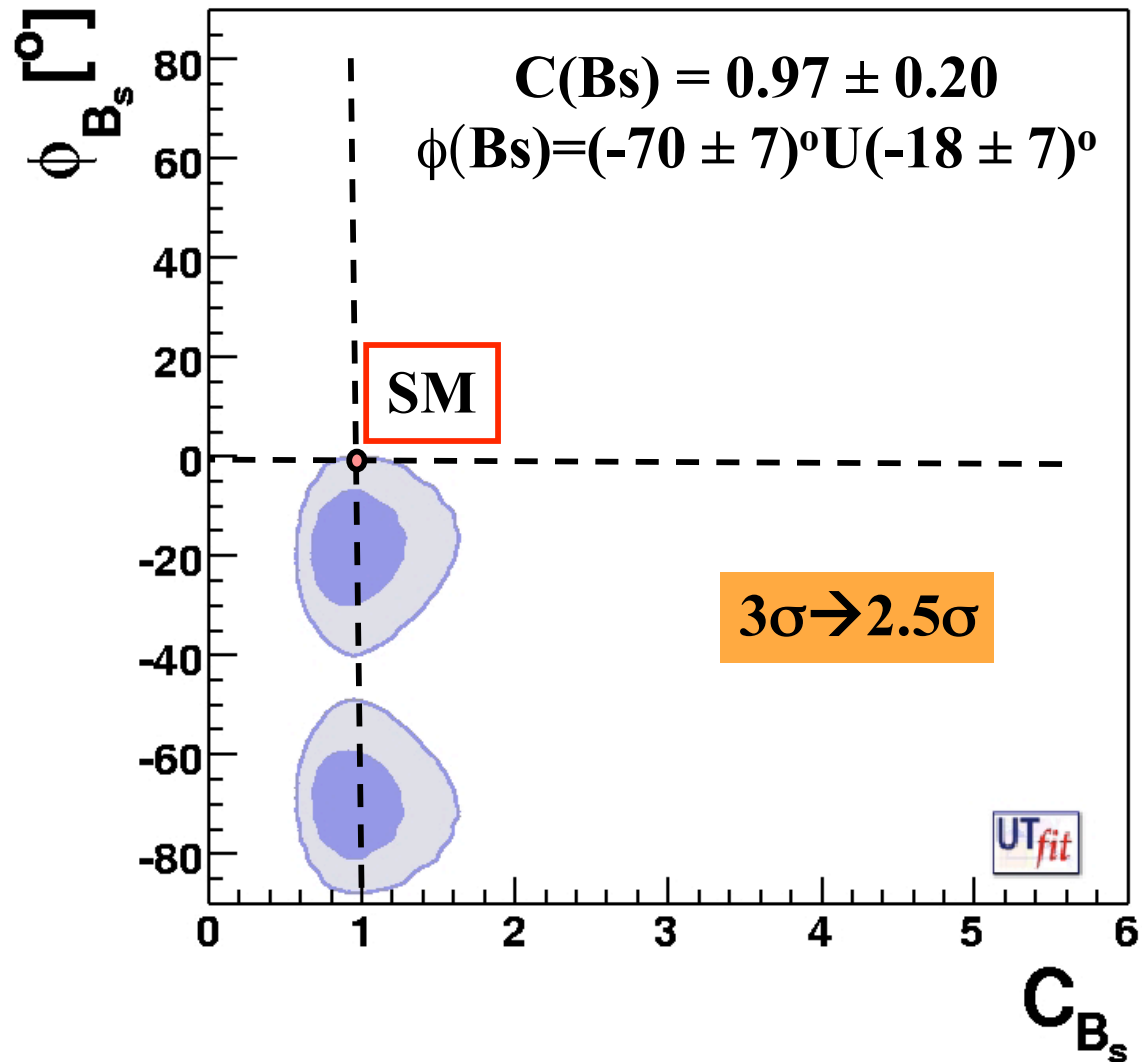
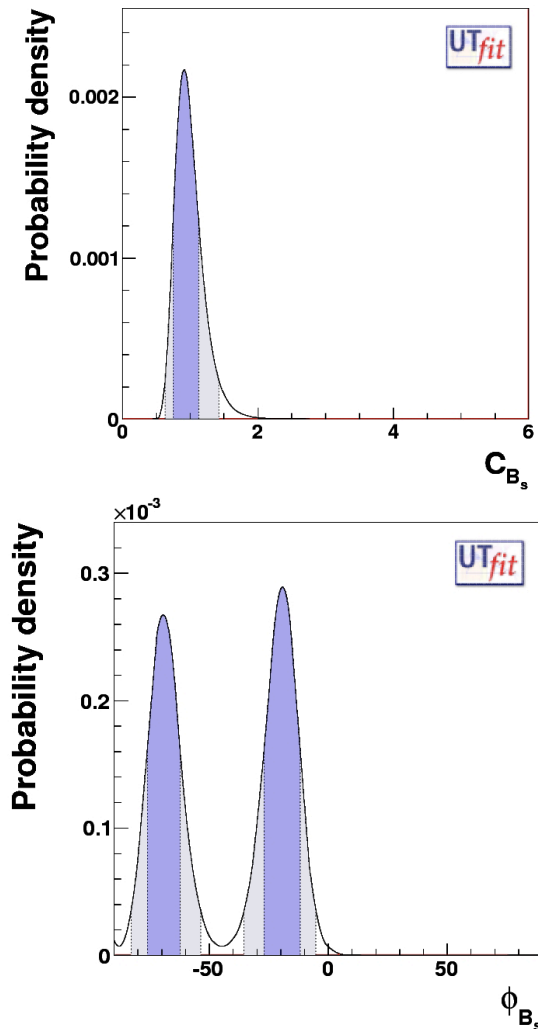


$$A_{NPd}/A_{SMd} \sim 0.1 \text{ and } A_{NPs}/A_{SMs} \sim 0.7$$

correspond to $A_{NPd}/A_{NPs} \sim \lambda^2$ i.e. to an additional λ suppression.

After ICHEP 2008-CKM2008

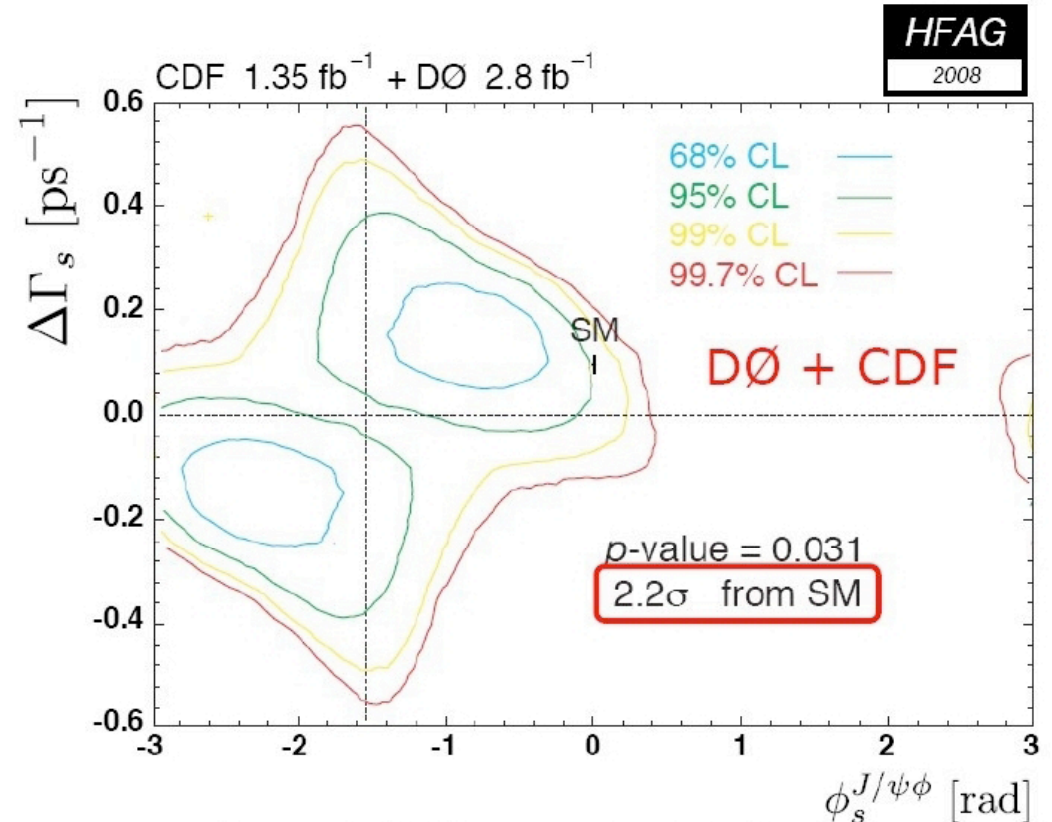
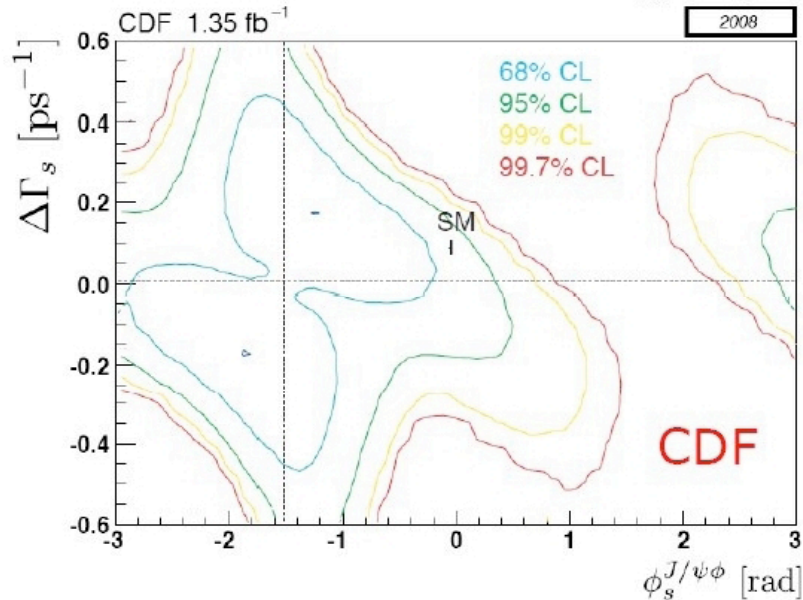
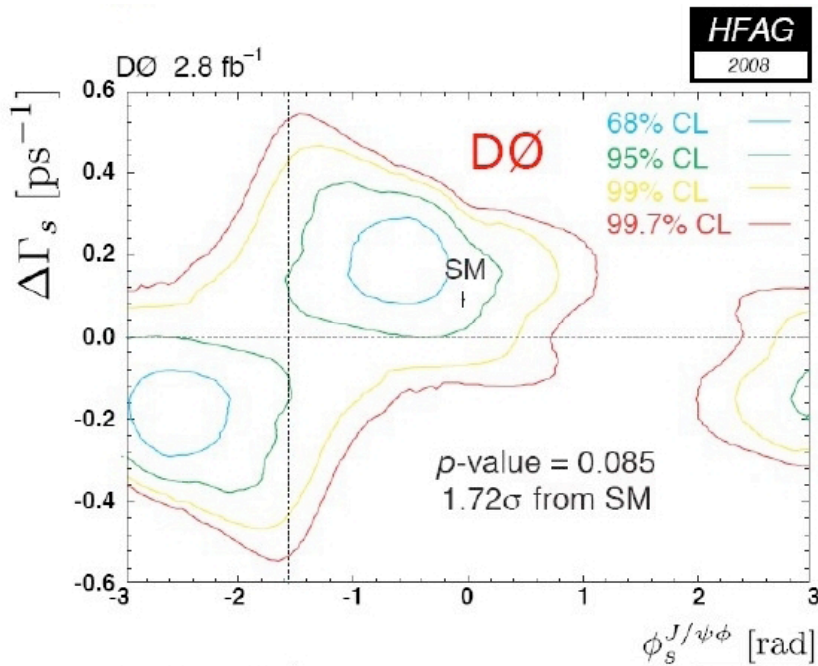
ICHEP 2008. D0 released the likelihood without assumptions on the strong phases



New CDF data not included:

new CDF likelihood “not ready yet” SM compatibility decreased in the CDF analysis

Here the results from HFAG. Without additional constraints



$$\phi_s = -2.37^{+0.38}_{-0.27} \text{ rad}, \quad -0.75^{+0.27}_{-0.38} \text{ rad}$$

$$\Delta\Gamma_s = -0.150^{+0.066}_{-0.059} \text{ ps}^{-1}, \quad 0.150^{+0.059}_{-0.066} \text{ ps}^{-1}$$

90% C.L. 1-d regions:

$$\phi_s \in [-2.85, -1.65], \quad [-1.47, -0.29]$$

$$\Delta\Gamma_s \in [-0.265, -0.036], \quad [0.036, 0.265]$$

July 31, 2008

See Diego Tonello (CDF), Lars Sonnenschein (D0) CKM08 Rome

This result, if confirmed, will imply

:

- of course \rightarrow NP physics

- NP not Minimal Flavour Violation

(large couplings..new particles not necessary below the TeV scale)

- NP model must explain why effects on B_d (which can still be as large as 20%) and K systems are smaller

1 \leftrightarrow 2: strong suppression

1 \leftrightarrow 3: $\leq O(10\%)$

2 \leftrightarrow 3: $O(1)$

this pattern is not unexpected in flavour models and in SUSY-GUTs

\rightarrow Flavour physics central

- B_d sector, for $\Delta F=2$ but also $\Delta F=1$ $b \rightarrow s$ transitions

- K sector

- of course B_s sector

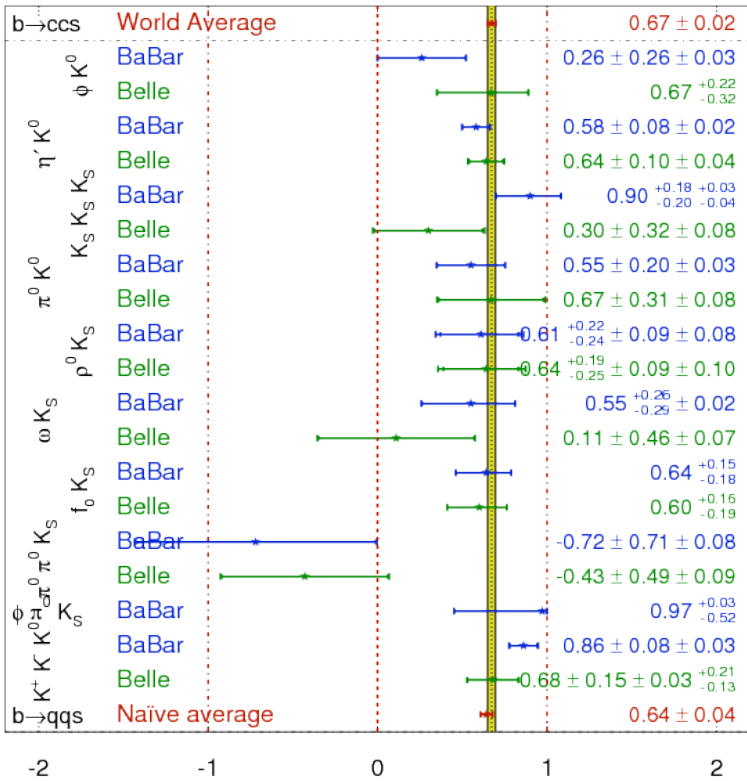
See next page 

**PRECISION
IS NEEDED**

$\Delta F=1$

$b \rightarrow s$ transitions are very sensitive to NP contributions ($\Delta F=1$)

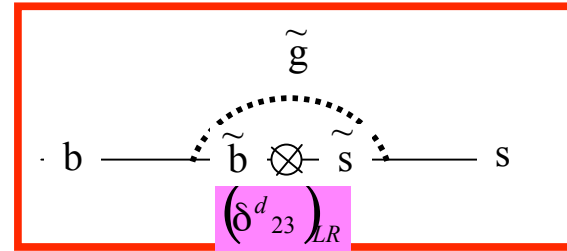
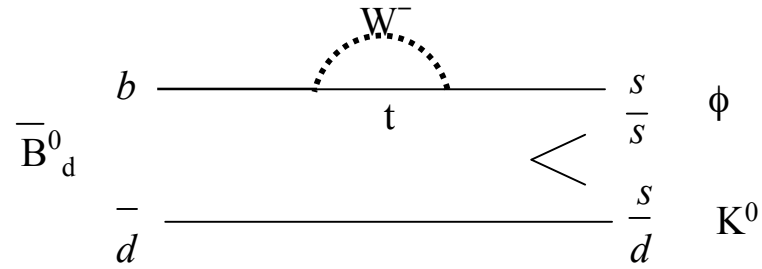
$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$ **HFAG**
CKM2008 PRELIMINARY



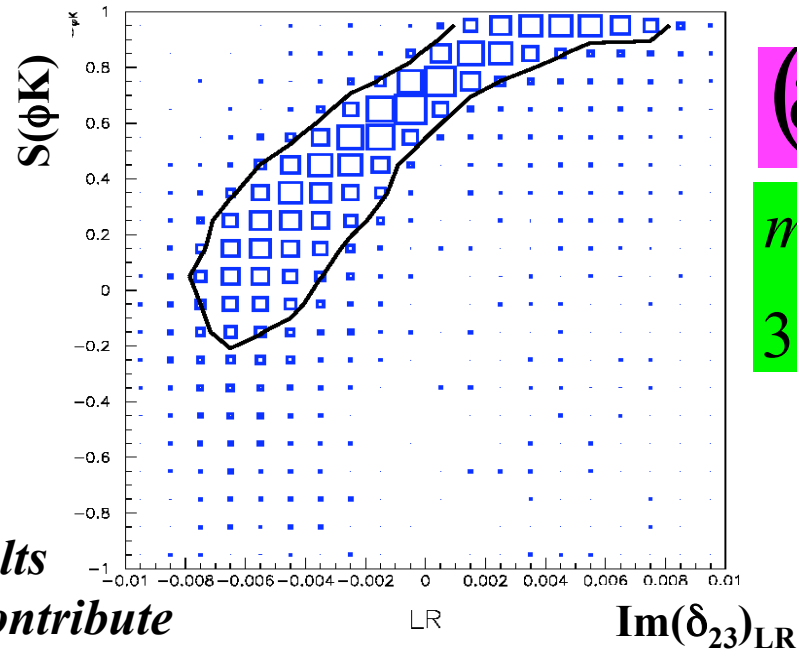
The disagreement is much reduced

PRECISION IS NEEDED

B factories results
SuperB expected to contribute



New Physics contribution (2-3 families)



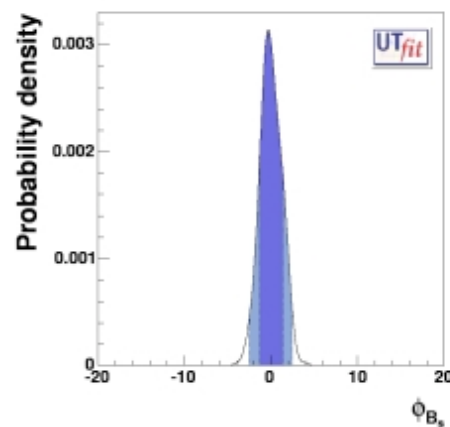
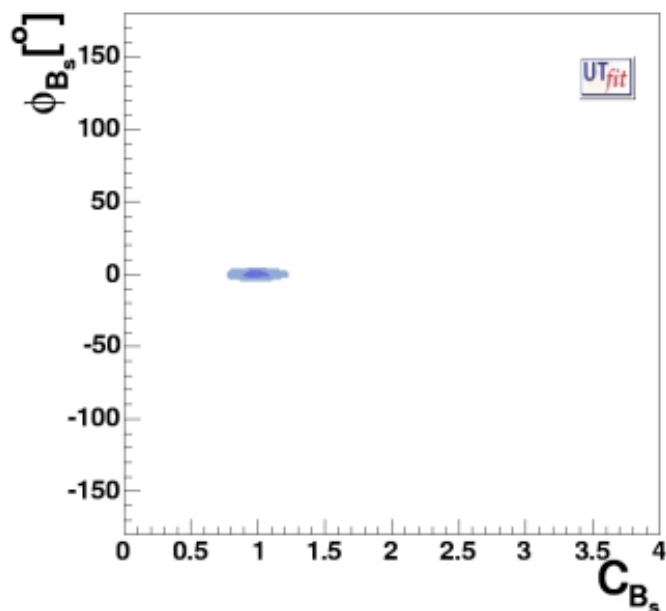
$(\delta^d_{23})_{LR}$

$m_{\tilde{q}} = m_{\tilde{g}}$
350 GeV

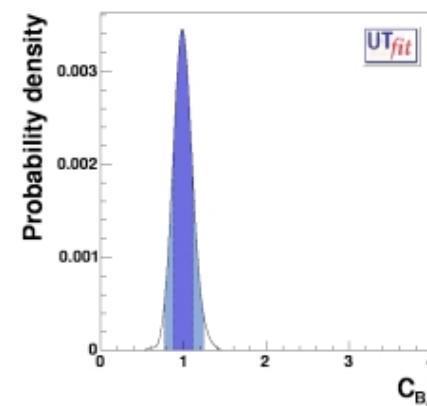
CFMS

- **D0 and CDF will update their results. They have not used entire dataset.**
If the NP phase stay so large they could observe it with the full/final dataset
- φ_s is a golden measurement for LHCb

Simulation done with 4fb^{-1} .



$$\varphi_{B_s} = (0.0 \pm 1.3)^\circ$$



$$C_{B_s} = 0.99 \pm 0.12$$

But also with much less data, LHCb can observe the effect if will stay so large

New studies show that (end 2009 ?)

LHCb with $0.5\text{fb}^{-1} \rightarrow \sigma(\phi_{B_s}) = 0.06$

ATLAS with $2.5\text{fb}^{-1} \rightarrow \sigma(\phi_{B_s}) = 0.16$

See Gaia Lanfranchi CKM08/Rome

Flavour physics in the quark sector is in his mature age

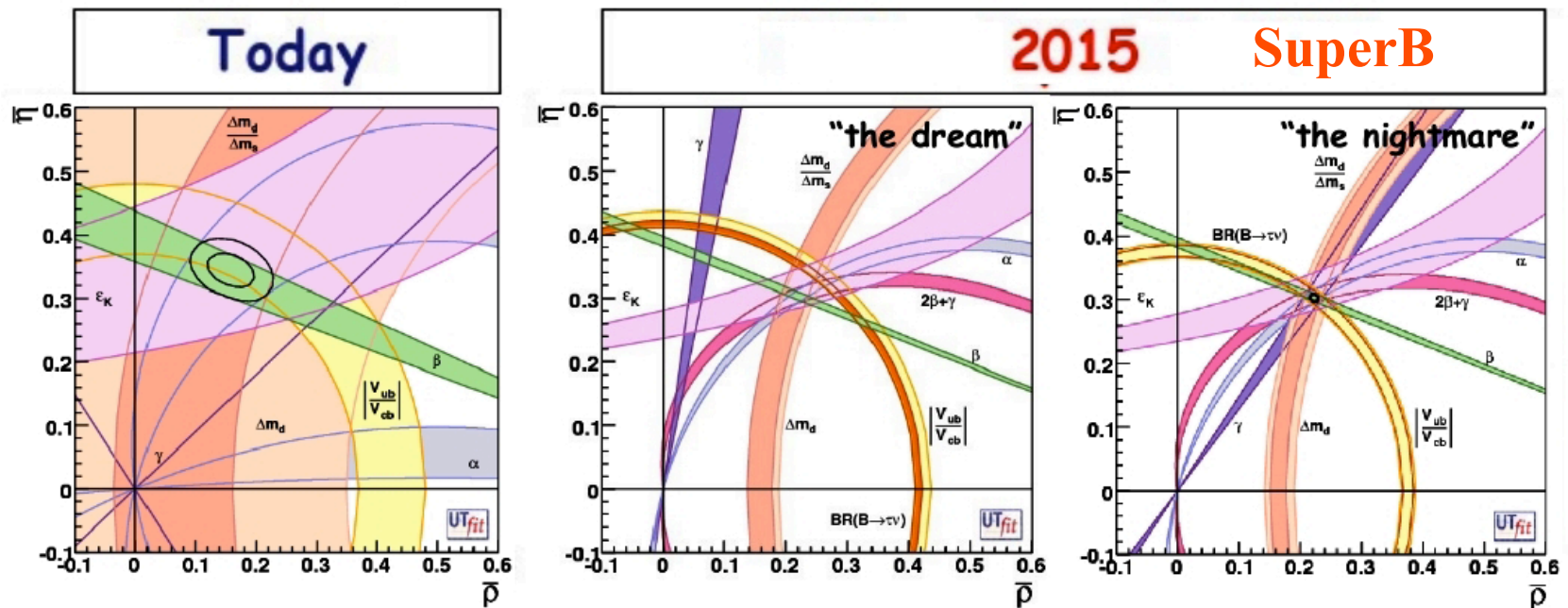
In $b \rightarrow d$ transitions NP effects are “confined” to be at order less $\sim 10\text{-}15\%$!

New data from Tevatron show $\sim 2.5\sigma$ discrepancy from SM in $b \rightarrow s$ transitions

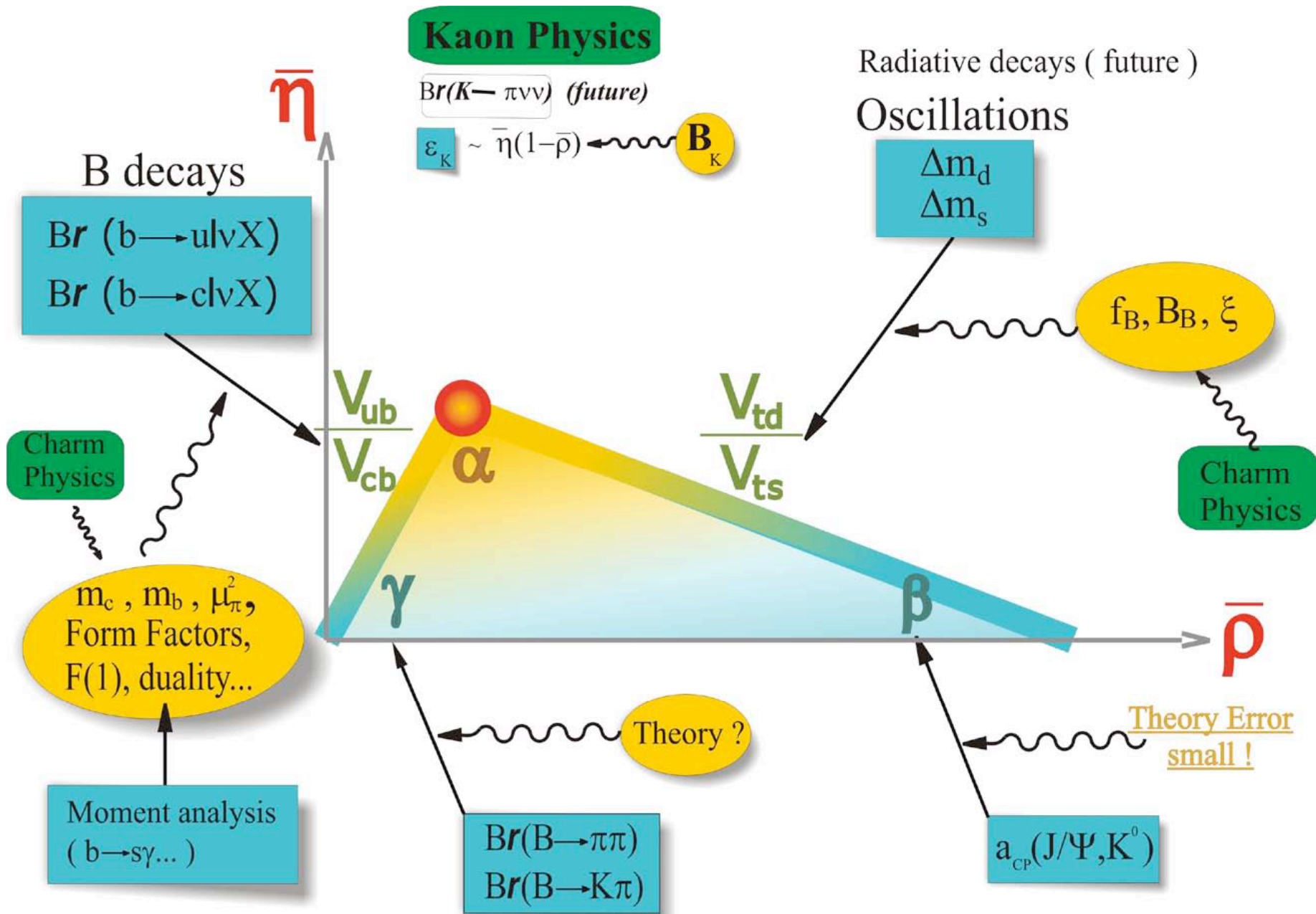
If confirmed would imply NP and not Minimal Flavour Violation

Tevatron (with full statistics) and LHCb will clarify the discrepancy

Flavour Physics is alive more than ever to look for NP beyond SM

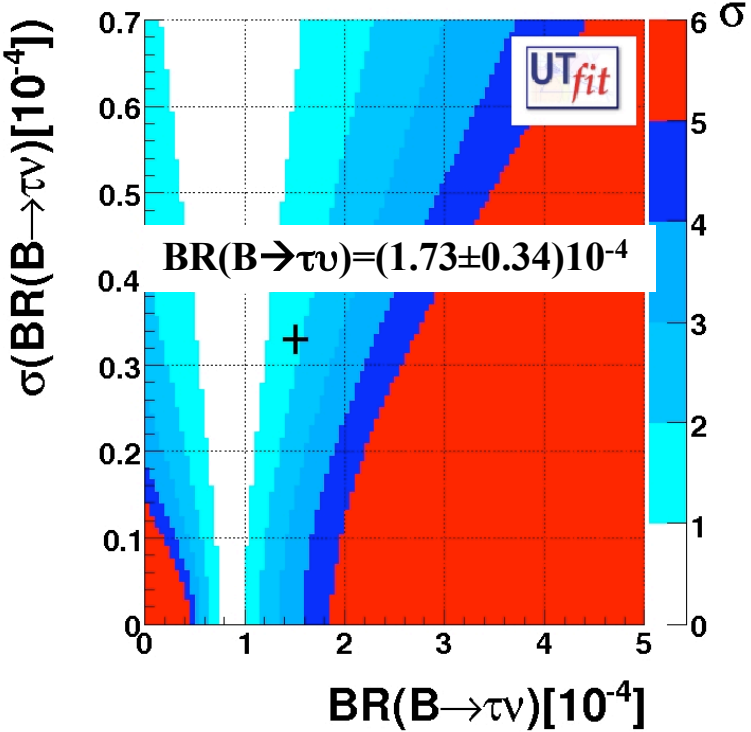
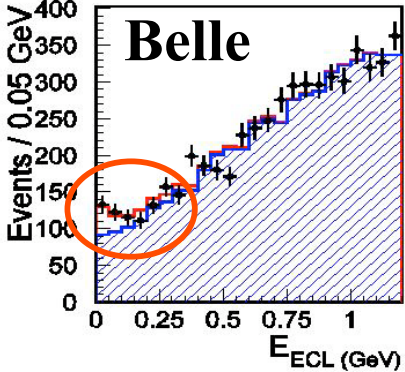
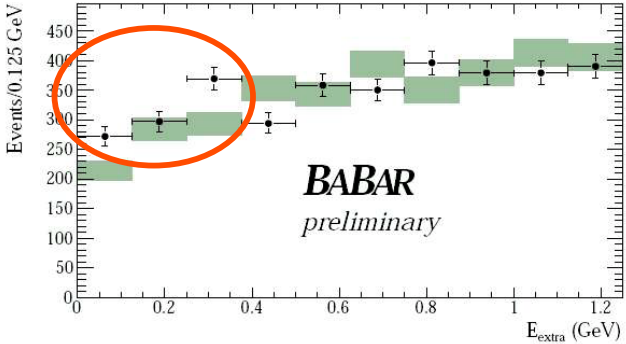
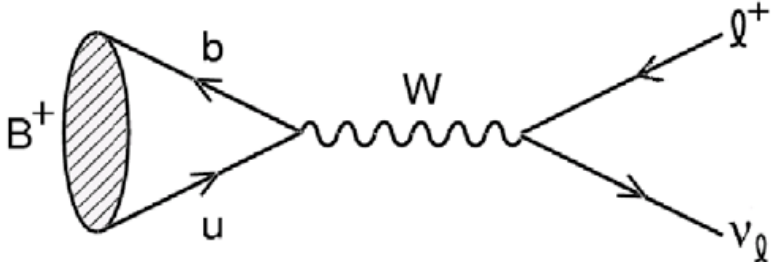


***BACKUP
MATERIAL***



B → τν

$$\mathcal{B}(B \rightarrow l\nu) = \frac{G_F^2 m_B m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$



B factories results
SuperB expected to contribute

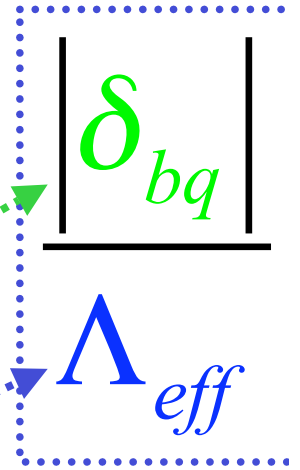
The problem of particle physics today is :
where is the NP scale $\Lambda \sim 0.5, 1 \dots 10^{16}$ TeV

The quantum stabilization of the Electroweak Scale
suggest that $\Lambda \sim 1$ TeV
LHC will search on this range

What happens if the NP scale is at 2-3..10 TeV
...naturalness is not at loss yet...

Flavour Physics explore also this range

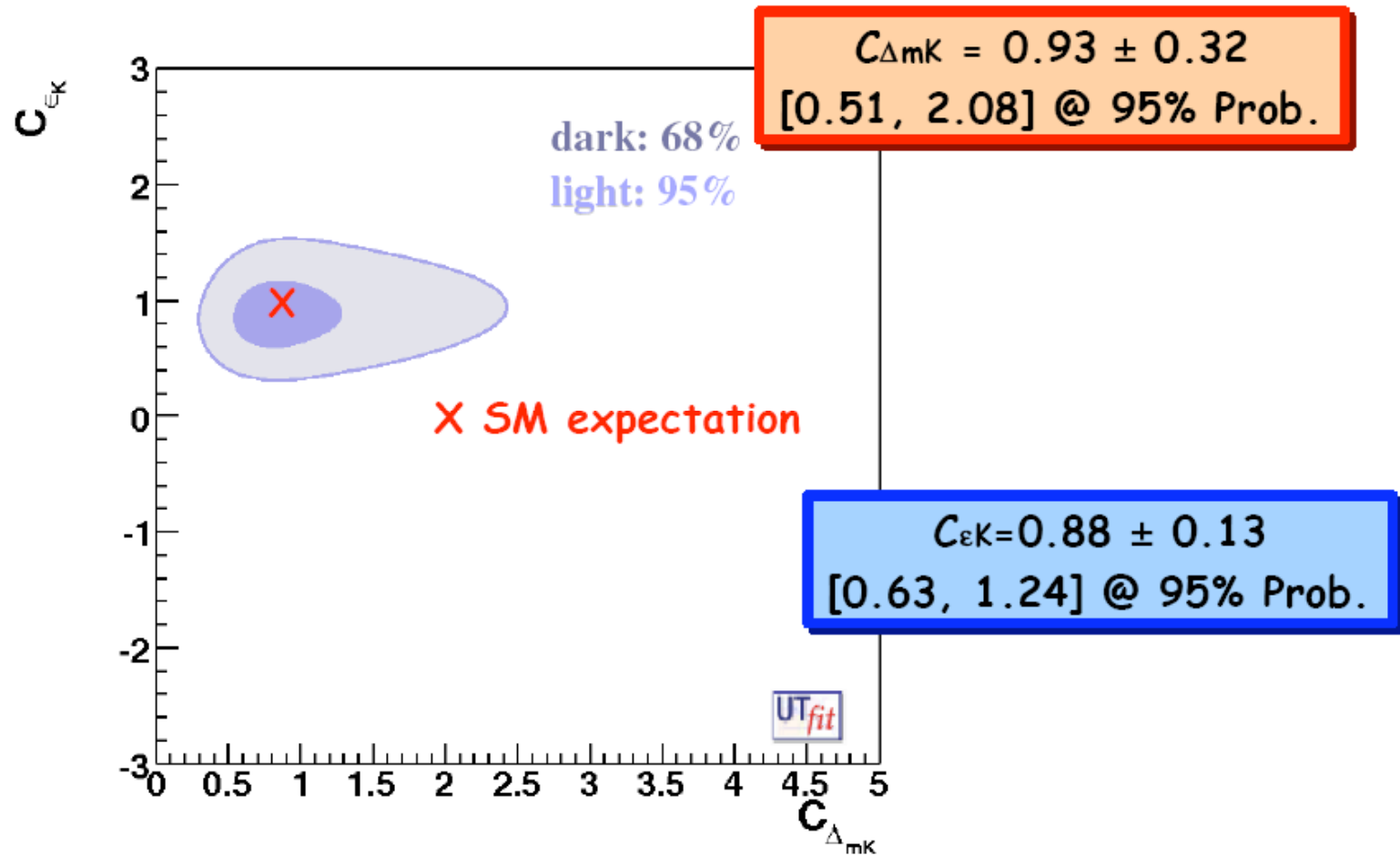
We want to perform flavour measurements such that :
- if NP particles are discovered at LHC we able
study the **flavour structure of the NP**
- we can explore **NP scale** beyond the LHC reach



If there is NP at scale Λ , it will generate new operator of
dimension D with coefficients proportional to Λ^{4-D}

You could demonstrate that only operator of $D=6$ contribute
So that in fact you have a dependence on $1/\Lambda^2$

Kaon sector



$$A_{SL} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \ell^+ X) - \Gamma(B^0 \rightarrow \ell^- X)}{\Gamma(\bar{B}^0 \rightarrow \ell^+ X) + \Gamma(B^0 \rightarrow \ell^- X)}$$

$$= -\text{Re} \left(\frac{\Gamma_{12}}{M_{12}} \right)^{\text{SM}} \frac{\sin 2\phi_{B_d}}{C_{B_d}} + \text{Im} \left(\frac{\Gamma_{12}}{M_{12}} \right)^{\text{SM}} \frac{\cos 2\phi_{B_d}}{C_{B_d}}$$

$$\tau_{B_s}^{FS} = \frac{1}{\Gamma_s} \frac{1 - \left(\frac{\Delta\Gamma_s}{2\Gamma_s} \right)^2}{1 + \left(\frac{\Delta\Gamma_s}{2\Gamma_s} \right)^2}$$

Flavour specific final states

$$A_{CH} = \frac{1}{4} \left(A_{SL}^d + \frac{f_s}{f_d} \frac{\chi_{s0}}{\chi_{d0}} A_{SL}^s \right)$$

$$\chi_q^{(-)} = \frac{\frac{\Delta\Gamma_q}{\Gamma_q} + 4 \frac{\Delta m_q}{\Gamma_q}}{\frac{\Delta\Gamma_q}{\Gamma_q} (z_q^{(-)} - 1) + 4 \left(2 z_q^{(-)} + \frac{\Delta m_q}{\Gamma_q} (1 + z_q^{(-)}) \right)}$$

With $z = |q/p|^2$ and $\bar{z} = |p/q|^2$

$$\frac{\Delta\Gamma_q}{\Delta m_q} = -2 \frac{\kappa}{C_{B_q}} \left\{ \cos(2\phi_{B_q}) \left(n_1 + \frac{n_6 B_2 + n_{11}}{B_1} \right) - \frac{\cos(\phi_q^{\text{SM}} + 2\phi_{B_q})}{R_t^q} \left(n_2 + \frac{n_7 B_2 + n_{12}}{B_1} \right) + \frac{\cos(2(\phi_q^{\text{SM}} + \phi_{B_q}))}{R_t^{q^2}} \right.$$

$$\left. \left(n_3 + \frac{n_8 B_2 + n_{13}}{B_1} \right) + \cos(\phi_q^{\text{Pen}} + 2\phi_{B_q}) C_q^{\text{Pen}} \left(n_4 + n_9 \frac{B_2}{B_1} \right) - \cos(\phi_q^{\text{SM}} + \phi_q^{\text{Pen}} + 2\phi_{B_q}) \frac{C_q^{\text{Pen}}}{R_t^q} \left(n_5 + n_{10} \frac{B_2}{B_1} \right) \right\}$$

NLO calculation of the matrix element of B meson mixing

Ciuchini et al. JHEP 0308:031,2003.

$$|A_{0,\parallel}(t)|^2 = |A_{0,\parallel}(0)|^2 \left[\mathcal{T}_+ \pm e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right],$$

$$|A_{\perp}(t)|^2 = |A_{\perp}(0)|^2 \left[\mathcal{T}_- \mp e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right],$$

$$\begin{aligned} \text{Re}(A_0^*(t)A_{\parallel}(t)) &= |A_0(0)||A_{\parallel}(0)| \cos(\delta_2 - \delta_1) \\ &\times \left[\mathcal{T}_+ \pm e^{-\bar{\Gamma}t} \sin \phi_s \sin(\Delta M_s t) \right], \end{aligned}$$

Tagging is important to separate the time evolution of mesons produced as Bs or anti-Bs. In this way we obtain direct sensitivity to CP-violating phase. This phase enters with terms proportional to **cos(2β_s)** and **sin(2β_s)**. Analyses which do not use flavour tagging are sensitive to |cos(2β_s)| and |sin(2β_s)|, leading to a four-fold ambiguities in the determination of φ_s.

$$\text{Im}(A_0^*(t)A_{\perp}(t)) = |A_0(0)||A_{\perp}(0)|$$

$$\begin{aligned} &\times [e^{-\bar{\Gamma}t} (\pm \sin \delta_2 \cos(\Delta M_s t) \mp \cos \delta_2 \sin(\Delta M_s t) \cos \phi_s) - \\ &(1/2)(e^{-\Gamma_H t} - e^{-\Gamma_L t}) \sin \phi_s \cos \delta_2], \end{aligned}$$

Only two-fold ambiguity

Ambiguity for
 $\phi_s \rightarrow \pi - \phi_s, \Delta\Gamma_s \rightarrow -\Delta\Gamma_s,$
 $\cos(\delta_1 - \delta_2) \rightarrow -\cos(\delta_1 - \delta_2)$

$$\text{Im}(A_{\parallel}^*(t)A_{\perp}(t)) = |A_{\parallel}(0)||A_{\perp}(0)|$$

$$\begin{aligned} &\times [e^{-\bar{\Gamma}t} (\pm \sin \delta_1 \cos(\Delta M_s t) \mp \cos \delta_1 \sin(\Delta M_s t) \cos \phi_s) - \\ &(1/2)(e^{-\Gamma_H t} - e^{-\Gamma_L t}) \sin \phi_s \cos \delta_1], \end{aligned}$$

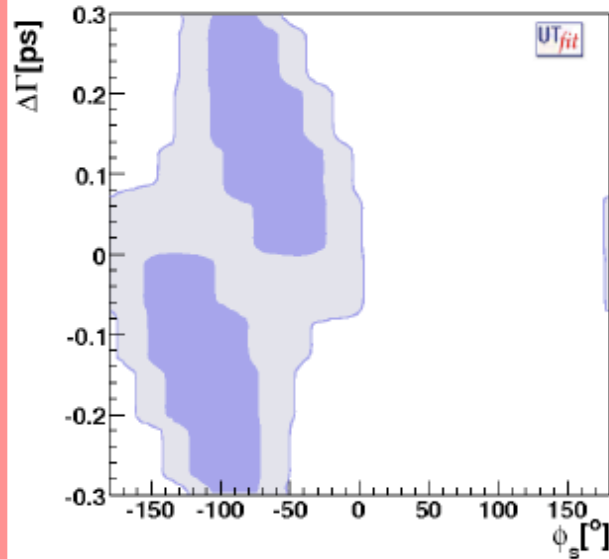
$$\text{where } \mathcal{T}_{\pm} = (1/2) \left[(1 \pm \cos \phi_s) e^{-\Gamma_L t} + (1 \mp \cos \phi_s) e^{-\Gamma_H t} \right].$$

TeVatron results
LHCb expected to contribute

Before ICHEP2008

1.35 fb⁻¹

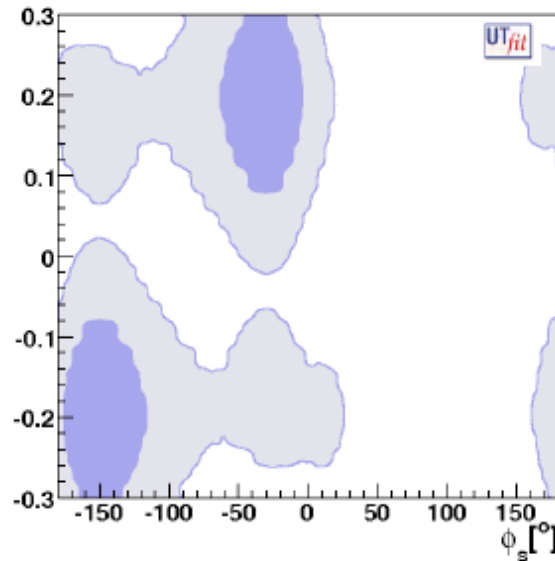
CDF tagged
measurement



*directly from the
Likelihood given by CDF*

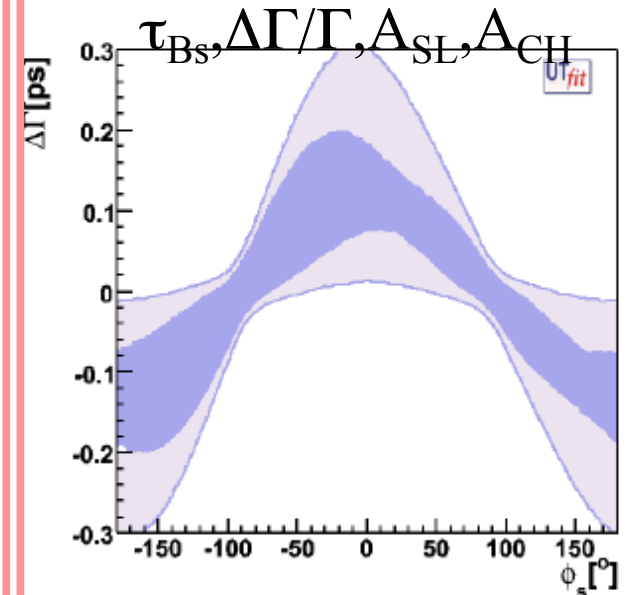
2.8 fb⁻¹

D0 tagged
measurement



*No likelihood available from D0
Conservative approach used
(for details see appendix)*

Other
measurements

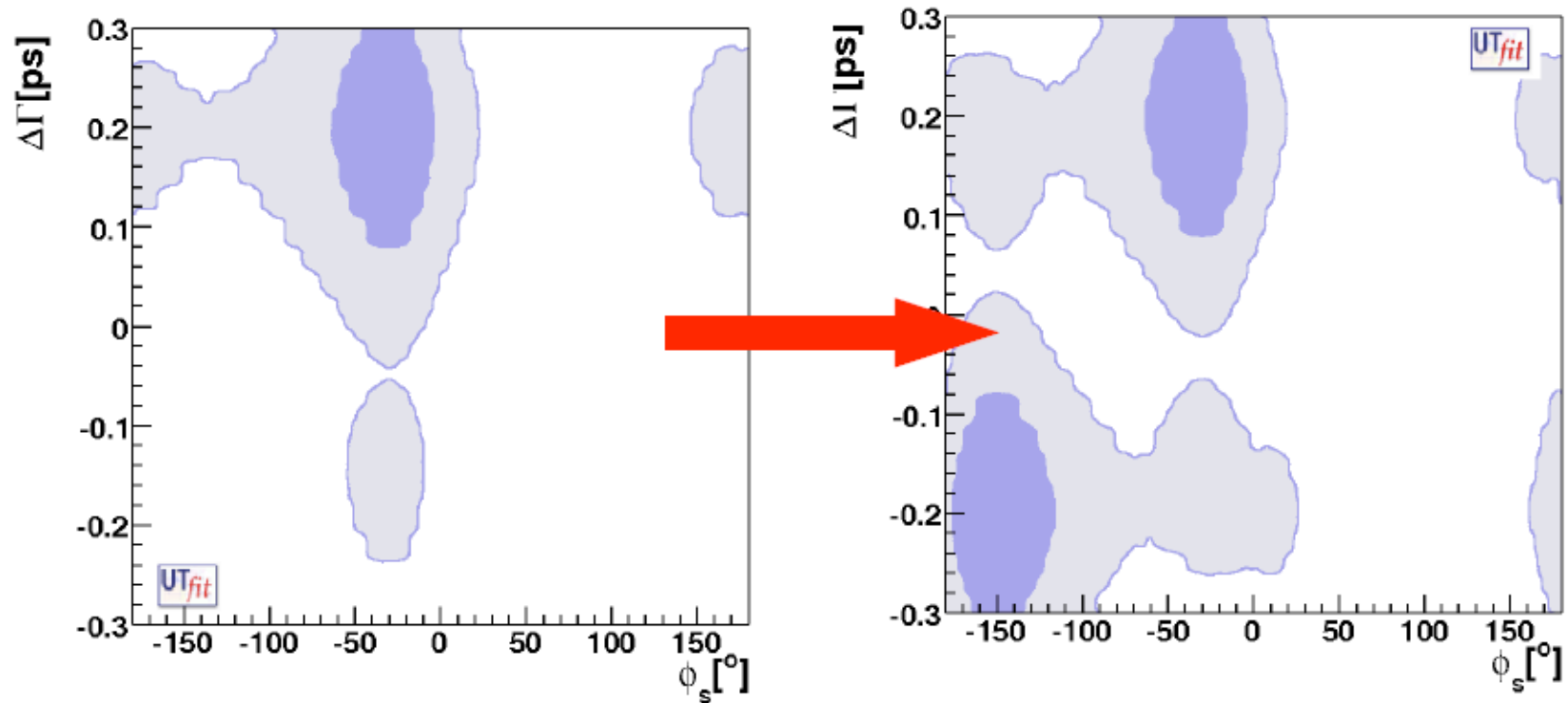


*All available measured used
with and up-to-date
hadronic parameters*

**Notice that the two measurements
are in agreement**

**Other measurements are
also important**

Modeling D0 data (I)



D0 data

Used by UTfit

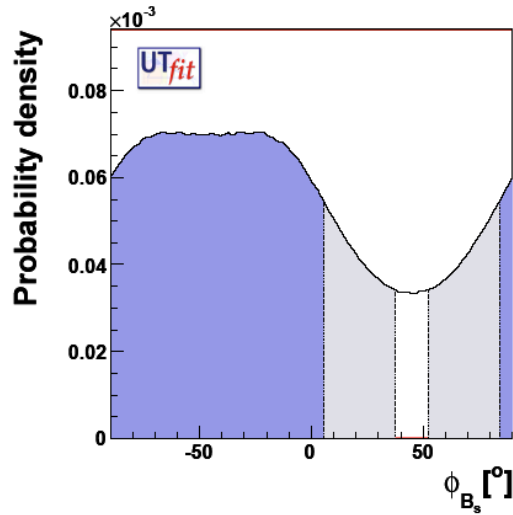
**Strong phase taken also
From $B_d \rightarrow J/\psi K^* + \text{SU}(3)$**

NO AMBIGUITY

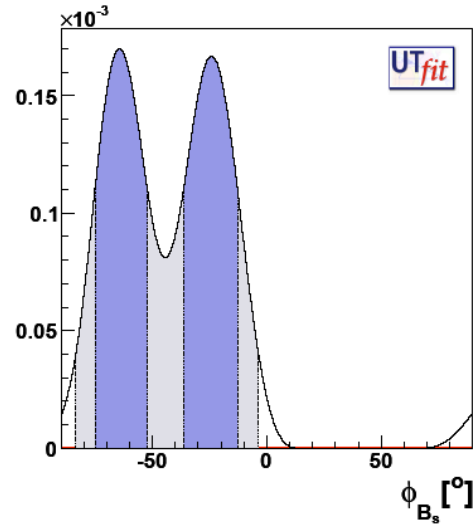
**The problem is that the singlet
Component of the f is ignored.**

**WE REINTRODUCE THE
AMBIGUITY (mirroring the likelihood)**

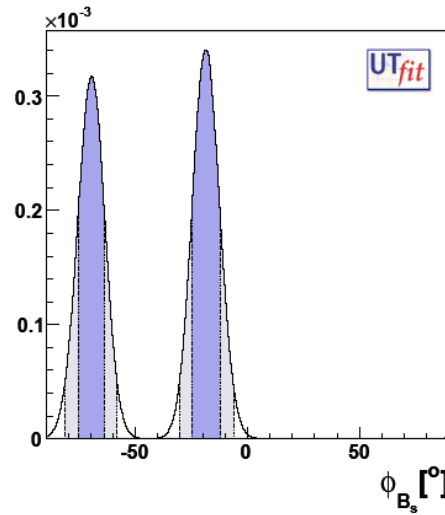
- Stability of the result, who is contributing more ?
- Is an evidence....How many sigmas ?



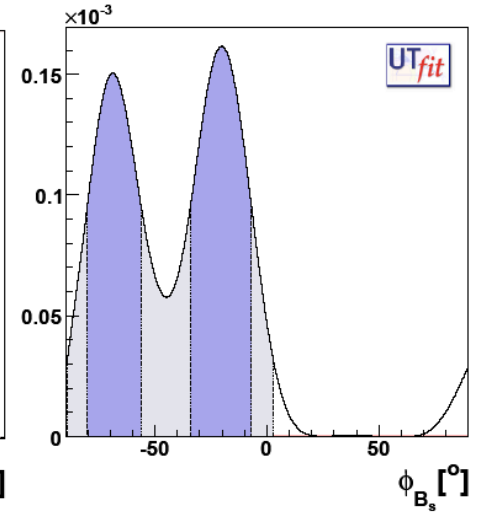
Without tagged analyses D0 and CDF



Including only CDF



Including only D0 Gaussian



Including only D0 likelihood profile

**Depending of the approach used (for treating D0 data)
 φ_s is away from zero from 3σ up to 3.7σ .**

Modeling D0 data (II)

DEFAULT METHOD

We have the results with 7x7 correlation matrix. Fit at 7 parameters \rightarrow we extract 2 parameters ($\Delta\Gamma_s$ and φ_s).

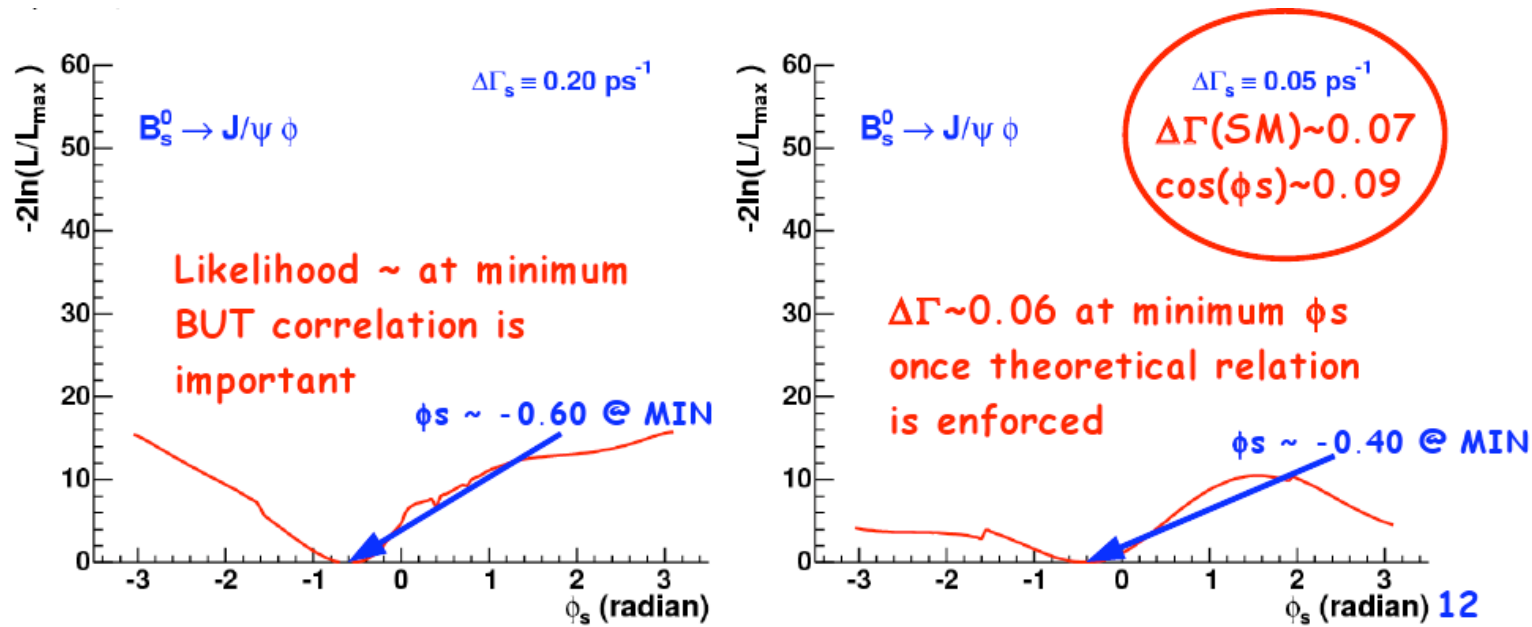
TABLE I: Summary of the likelihood fit results for three cases: free ϕ_s , ϕ_s constrained to the SM value, and $\Delta\Gamma_s$ constrained by the expected relation $\Delta\Gamma_s^{SM} \cdot |\cos(\phi_s)|$.

	free ϕ_s	$\phi_s \equiv \phi_s^{SM}$	$\Delta\Gamma_s^{sh}$
$\bar{\tau}_s$ (ps)	1.52 ± 0.06	1.53 ± 0.06	1.49 ± 0.05
$\Delta\Gamma_s$ (ps ⁻¹)	0.19 ± 0.07	0.14 ± 0.07	0.083 ± 0.018
$A_{\perp}(0)$	0.41 ± 0.04	0.44 ± 0.04	0.45 ± 0.03
$ A_{\perp}(0) ^2 - A_{\parallel}(0) ^2$	0.34 ± 0.05	0.35 ± 0.04	0.33 ± 0.04
δ_1	-0.52 ± 0.42	-0.48 ± 0.45	-0.47 ± 0.42
δ_2	3.17 ± 0.39	3.19 ± 0.43	3.21 ± 0.40
ϕ_s	$-0.57^{+0.24}_{-0.30}$	$\equiv -0.04$	-0.46 ± 0.28
ΔM_s (ps ⁻¹)	$\equiv 17.77$	$\equiv 17.77$	$\equiv 17.77$

Two others approach used to include non-Gaussian tails:

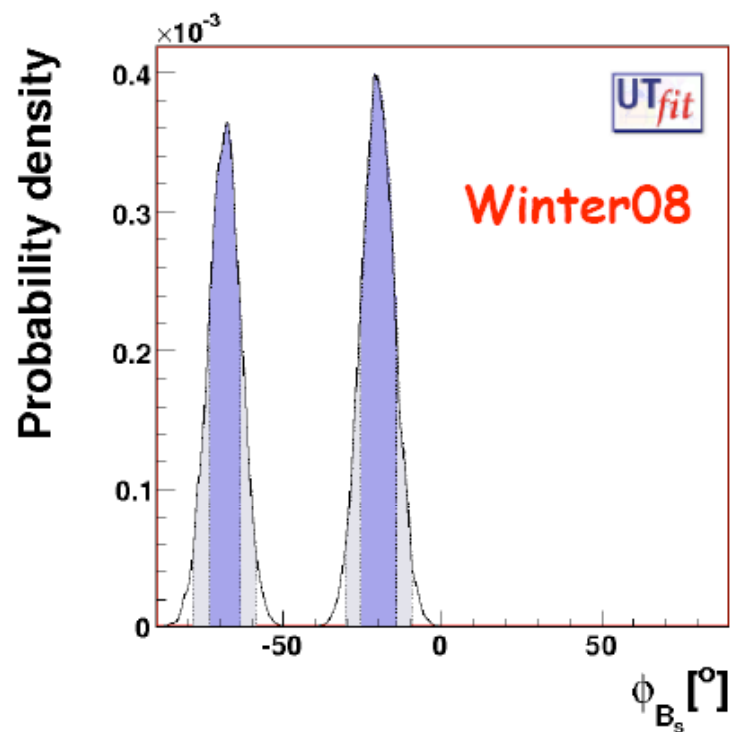
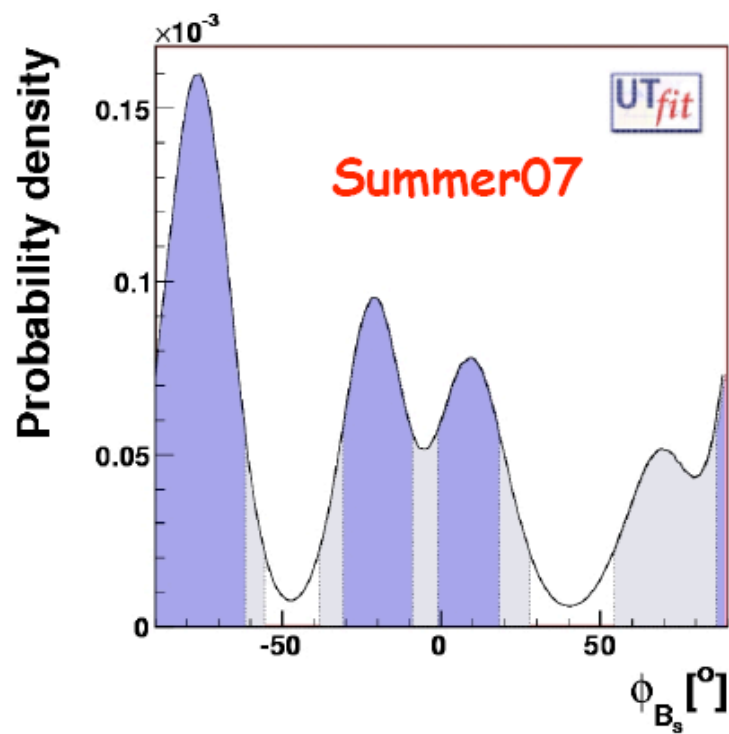
- Scale errors such they agree with the quoted “ 2σ ” ranges
- Use the 1D profile likelihood given by D0 (fig 2).

ICHEP 2008. D0 released the likelihood without assumption on the strong phases



Move from $1.35\text{fb}^{-1} \rightarrow 2.8\text{fb}^{-1}$

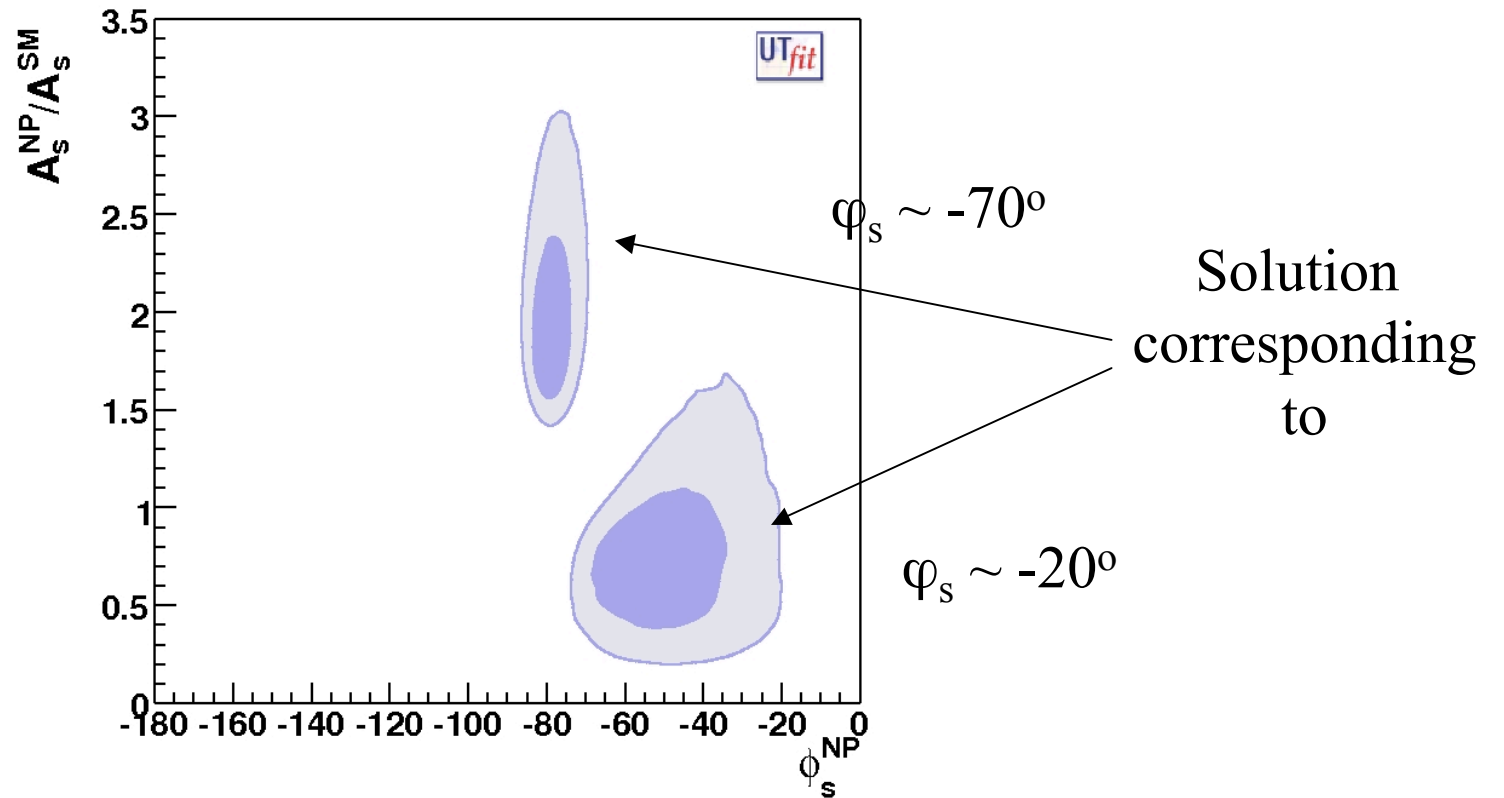
Evolution of this result



The two most probable peaks of last summer are now enhanced

Looking at the result with a different parametrization

$$C_{B_s} e^{2i\varphi_{B_s}} = \frac{A_{SM} e^{-2i\beta_s} + A_{NP} e^{-2i(\varphi_s^{NP} - \beta_s)}}{A_{SM} e^{-2i\beta_s}}$$



$$A_s^{NP} / A_s^{SM} = (0.73 \pm 0.35)$$

$$\varphi_s^{NP} = (-51 \pm 11)^\circ$$

$$\begin{aligned}
\hat{B}_K &= 0.75 \pm 0.07 , \\
f_{B_s} &= 245 \pm 25 \text{ MeV} \quad , \quad f_B = 200 \pm 20 \text{ MeV} \quad , \quad f_{B_s}/f_B = 1.21 \pm 0.04 , \\
f_{B_s}\sqrt{\hat{B}_{B_s}} &= 270 \pm 30 \text{ MeV} \quad , \quad f_B\sqrt{\hat{B}_{B_d}} = 225 \pm 25 \text{ MeV} \quad , \quad \xi = 1.21 \pm 0.04 , \\
\hat{B}_{B_d} &= \hat{B}_{B_s} = 1.22 \pm 0.12 \quad , \quad \hat{B}_{B_s}/\hat{B}_{B_d} = 1.00 \pm 0.03 , \\
|V_{cb}| \text{ (excl.)} &= (39.2 \pm 1.1) \cdot 10^{-3} \quad , \quad |V_{ub}| \text{ (excl.)} = (35.0 \pm 4.0) \cdot 10^{-4} .
\end{aligned}$$

These averages can be compared with the previous ones used by UTfit

$$\begin{aligned}
\hat{B}_K &= 0.79 \pm 0.04 \pm 0.08 , \\
f_{B_s} &= 230 \pm 30 \text{ MeV} \quad , \quad f_B = 189 \pm 27 \text{ MeV} \quad , \quad f_{B_s}/f_B = 1.22_{-0.06}^{+0.05} , \\
f_{B_s}\sqrt{\hat{B}_{B_s}} &= 262 \pm 35 \text{ MeV} \quad , \quad f_B\sqrt{\hat{B}_{B_d}} = 214 \pm 38 \text{ MeV} \quad , \quad \xi = 1.23 \pm 0.06 , \\
\hat{B}_{B_d} &= 1.28 \pm 0.05 \pm 0.09 \quad , \quad \hat{B}_{B_s}/\hat{B}_{B_d} = 1.02 \pm 0.02_{-0.02}^{+0.06} , \\
|V_{cb}| \text{ (excl.)} &= (39.1 \pm 0.6 \pm 1.7) \cdot 10^{-3} \quad , \quad |V_{ub}| \text{ (excl.)} = (34.0 \pm 4.0) \cdot 10^{-4} .
\end{aligned}$$