



# Neutrinos: Results and Future

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DESY  
March 4, 2008

# Evidence For $\nu$ Flavor Change

## Neutrinos

## Evidence of Flavor Change

Solar

Compelling

Reactor

Compelling

( $L \sim 180$  km)

Atmospheric

Compelling

Accelerator

Compelling

( $L = 250$  and  $735$  km)

Stopped  $\mu^+$  Decay

( LSND )  
( $L \approx 30$  m)

Unconfirmed by

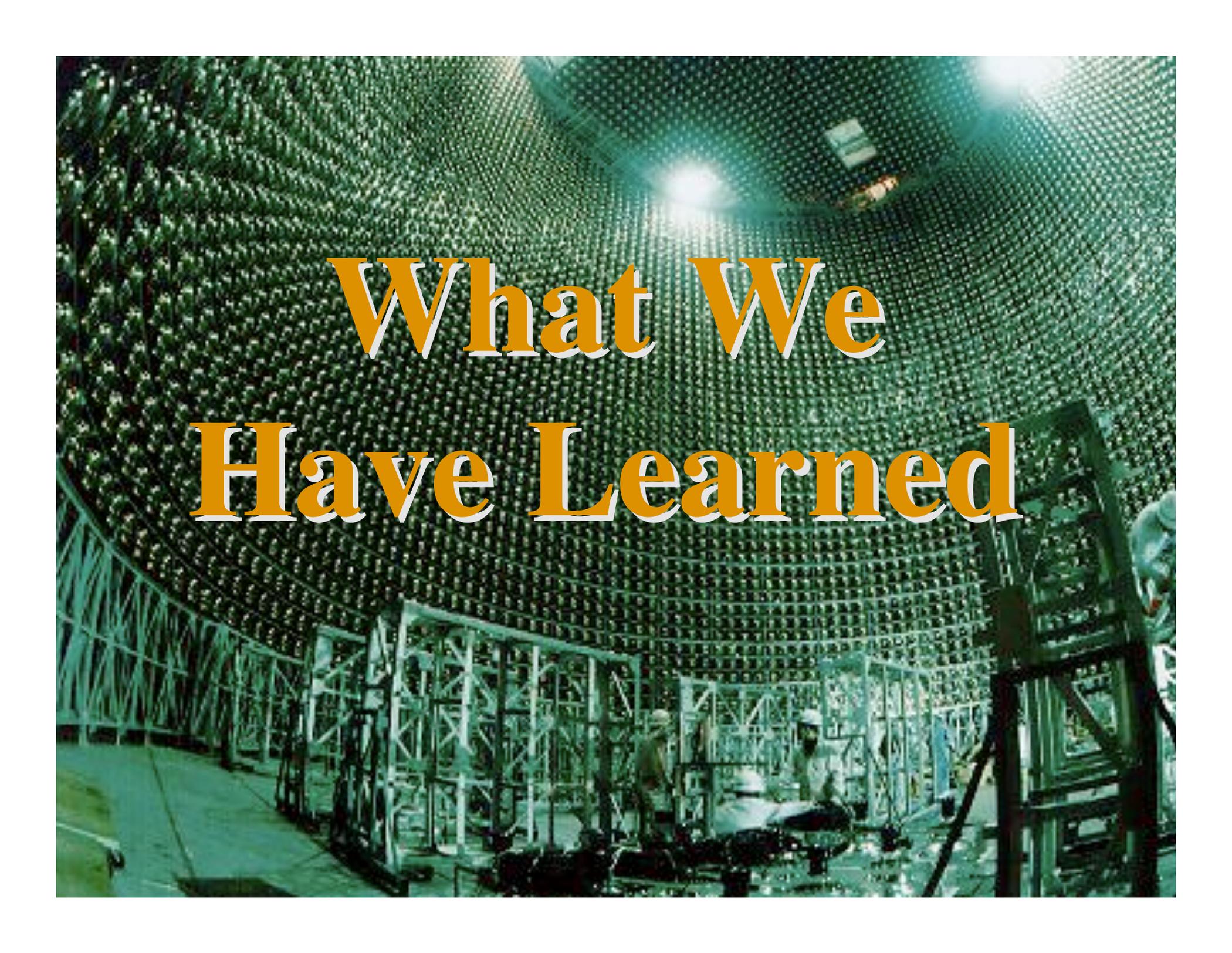
MiniBooNE

The neutrino flavor-change observations  
imply that —

Neutrinos have nonzero masses

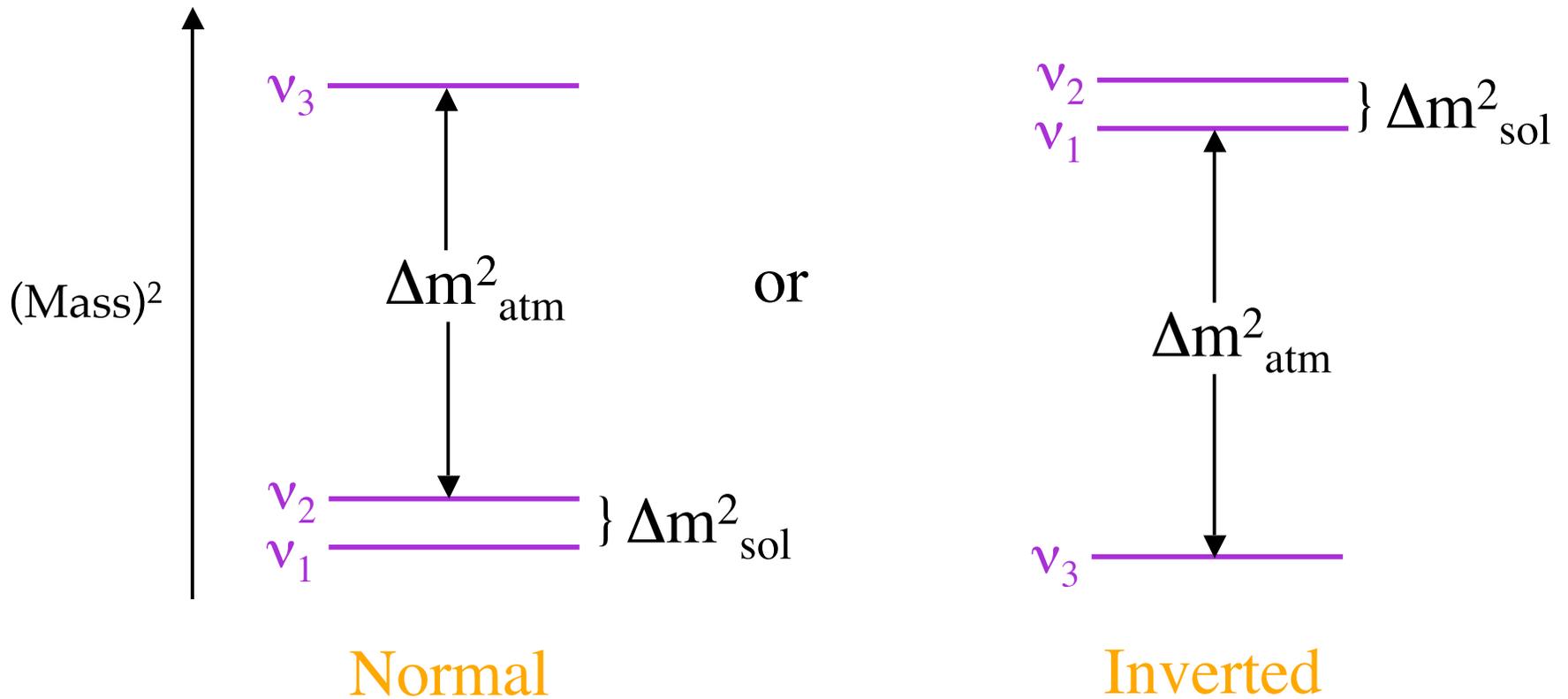
and that —

Leptons mix.



# What We Have Learned

# The (Mass)<sup>2</sup> Spectrum



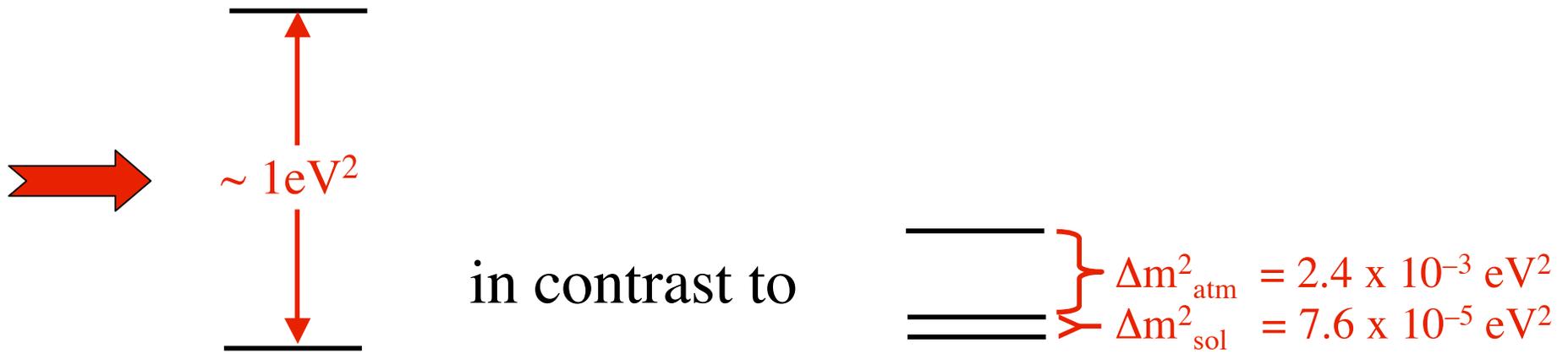
$$\Delta m^2_{sol} \cong 7.6 \times 10^{-5} \text{ eV}^2, \quad \Delta m^2_{atm} \cong 2.4 \times 10^{-3} \text{ eV}^2$$

# Are There *More* Than 3 Mass Eigenstates?

When only two neutrinos count,

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \sin^2 \left[ 1.27 \Delta m^2 (eV^2) \frac{L(km)}{E(GeV)} \right]$$

*Rapid*  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  oscillation reported by **LSND** —

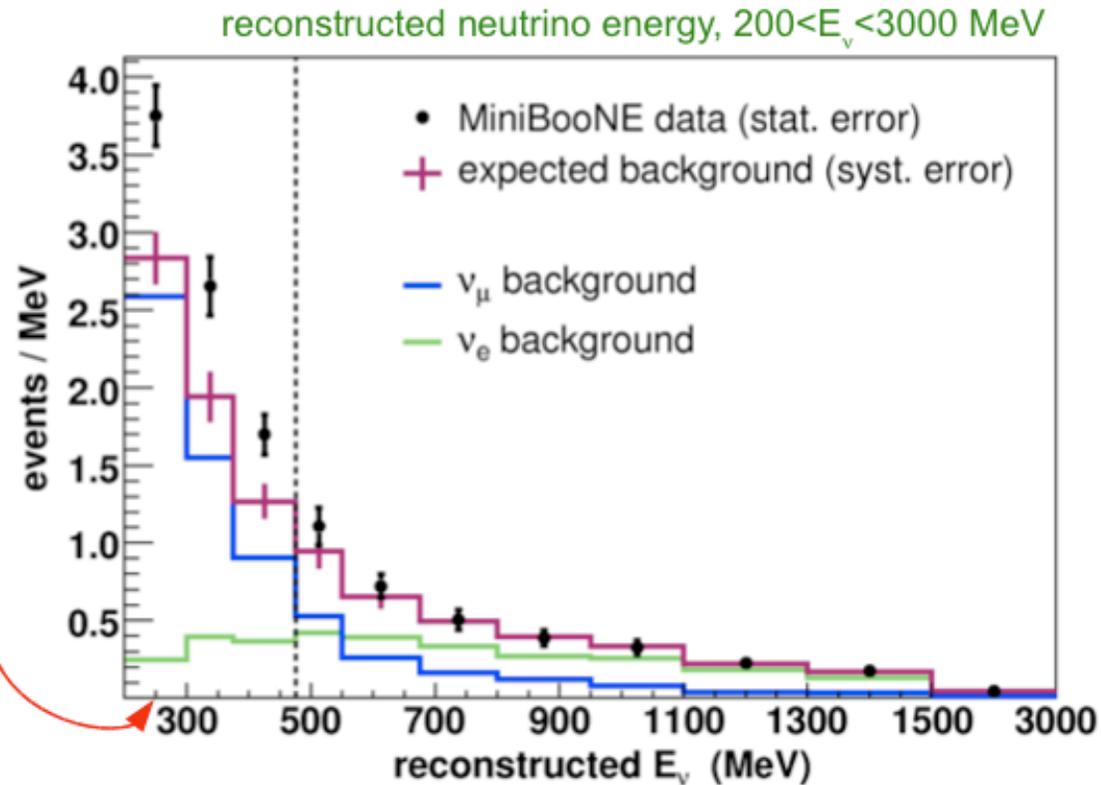


➔ At least **4** mass eigenstates.

# MiniBooNE Search for $\nu_{\mu} \rightarrow \nu_e$

R. Tayloe  
at LP07

- NEW:  
this energy bin



- No excess above background for energies  $E_{\nu} > 475$  MeV.
- Unexplained excess for  $E_{\nu} < 475$  MeV.
- Two-neutrino oscillation cannot fit LSND *and* MiniBooNE.
- More complicated fits are possible.

# MiniBooNE in the NuMI Beam

*The MiniBooNE detector is illuminated by **both** the MiniBooNE  $\nu_\mu$  beam, and the NuMI  $\nu_\mu$  beam pointed at MINOS.*

Distance to MiniBooNE —

$L$  (from NuMI source)  $\approx 1.4 L$  (from MiniBooNE source)

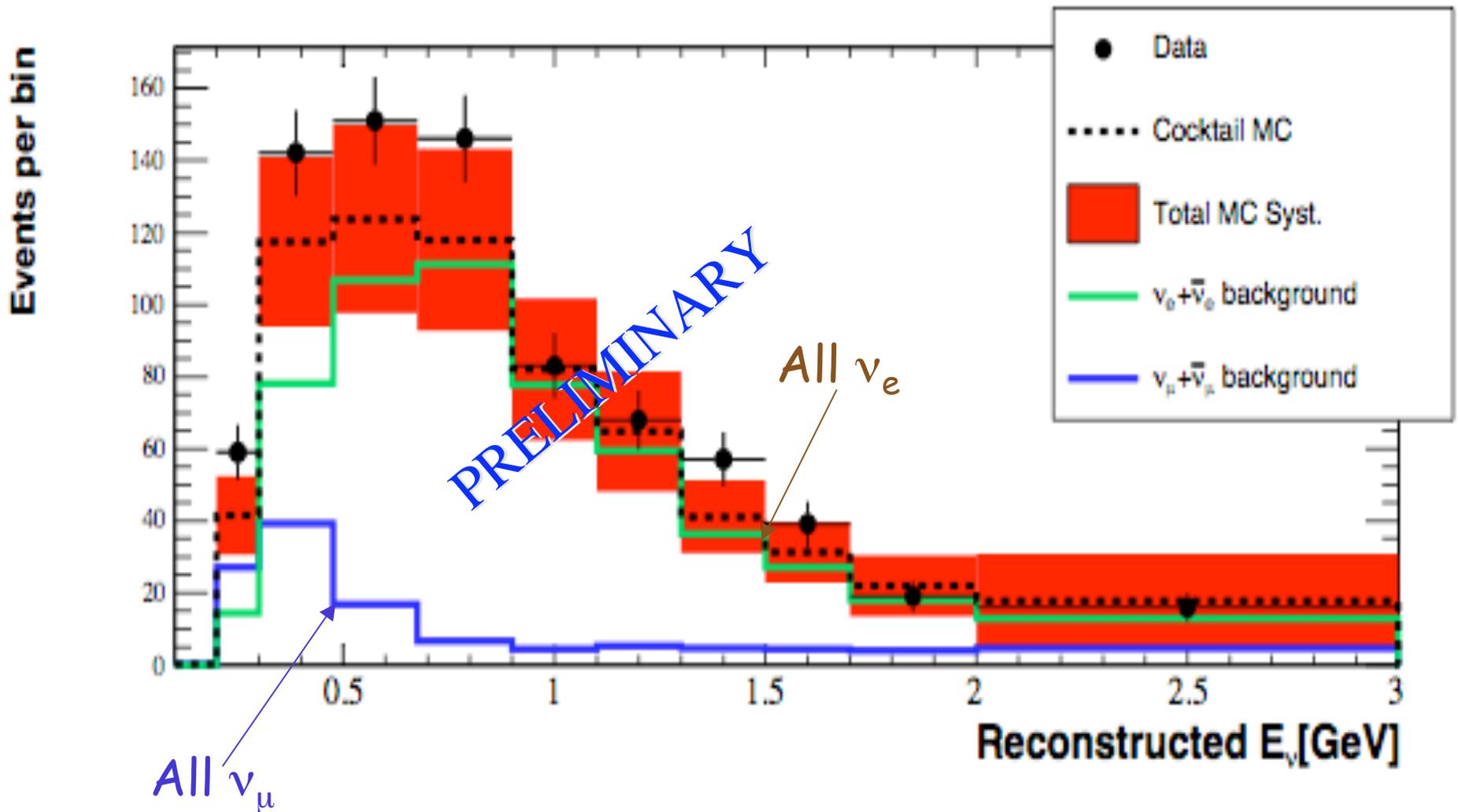
*Neutrino oscillation depends on  $L$  and  $E$  only through  $L/E$ .*

*Therefore, if an anomaly seen at some  $E$  in the MiniBooNE-beam data is due to oscillation, it should appear at  $1.4 E$  in the NuMI-beam data.*

# $\nu_e$ CCQE sample: Reconstructed energy $E_\nu$ of incoming $\nu$

(Z. Djurcic, Dec. 11, 2007)

$$E_\nu^{QE} = \frac{1}{2} \frac{2M_p E_\ell - m_\ell^2}{M_p - E_\ell + \sqrt{(E_\ell^2 - m_\ell^2) \cos \theta_\ell}}$$



To be continued ...

*Meanwhile, we will assume there are  
only 3 neutrino mass eigenstates.*

# Leptonic Mixing

This has the consequence that —

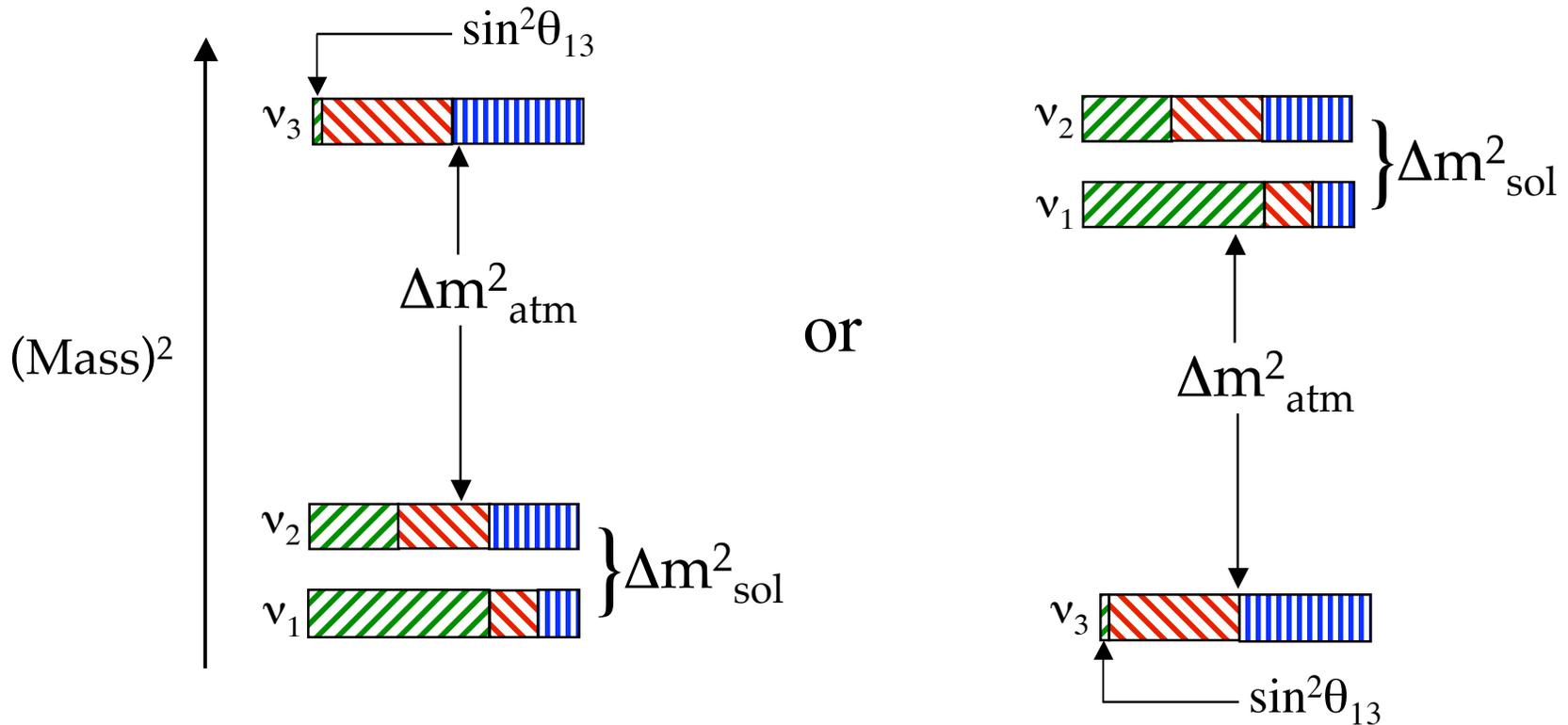
$$| \nu_i \rangle = \sum_{\alpha} U_{\alpha i} | \nu_{\alpha} \rangle .$$

Mass eigenstate  $\nu_i$  (where  $i = e, \mu, \text{ or } \tau$ ) is expressed as a sum of Flavor eigenstates  $\nu_{\alpha}$  (where  $\alpha = e, \mu, \tau$ ). The coefficients  $U_{\alpha i}$  are elements of the PMNS Leptonic Mixing Matrix.

Flavor- $\alpha$  fraction of  $\nu_i = |U_{\alpha i}|^2$ .

When a  $\nu_i$  interacts and produces a charged lepton, the probability that this charged lepton will be of flavor  $\alpha$  is  $|U_{\alpha i}|^2$ .

The spectrum, showing its approximate flavor content, is



Normal

Inverted

$\nu_e [ |U_{ei}|^2 ]$

$\nu_\mu [ |U_{\mu i}|^2 ]$

$\nu_\tau [ |U_{\tau i}|^2 ]$

# The Mixing Matrix

$$U = \begin{array}{c} \text{Atmospheric} \\ \left[ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{array} \right] \times \begin{array}{c} \text{Cross-Mixing} \\ \left[ \begin{array}{ccc} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{array} \right] \times \begin{array}{c} \text{Solar} \\ \left[ \begin{array}{ccc} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{array} \right] \\ \\ \left[ \begin{array}{ccc} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{array} \right] \end{array}
 \end{array}$$

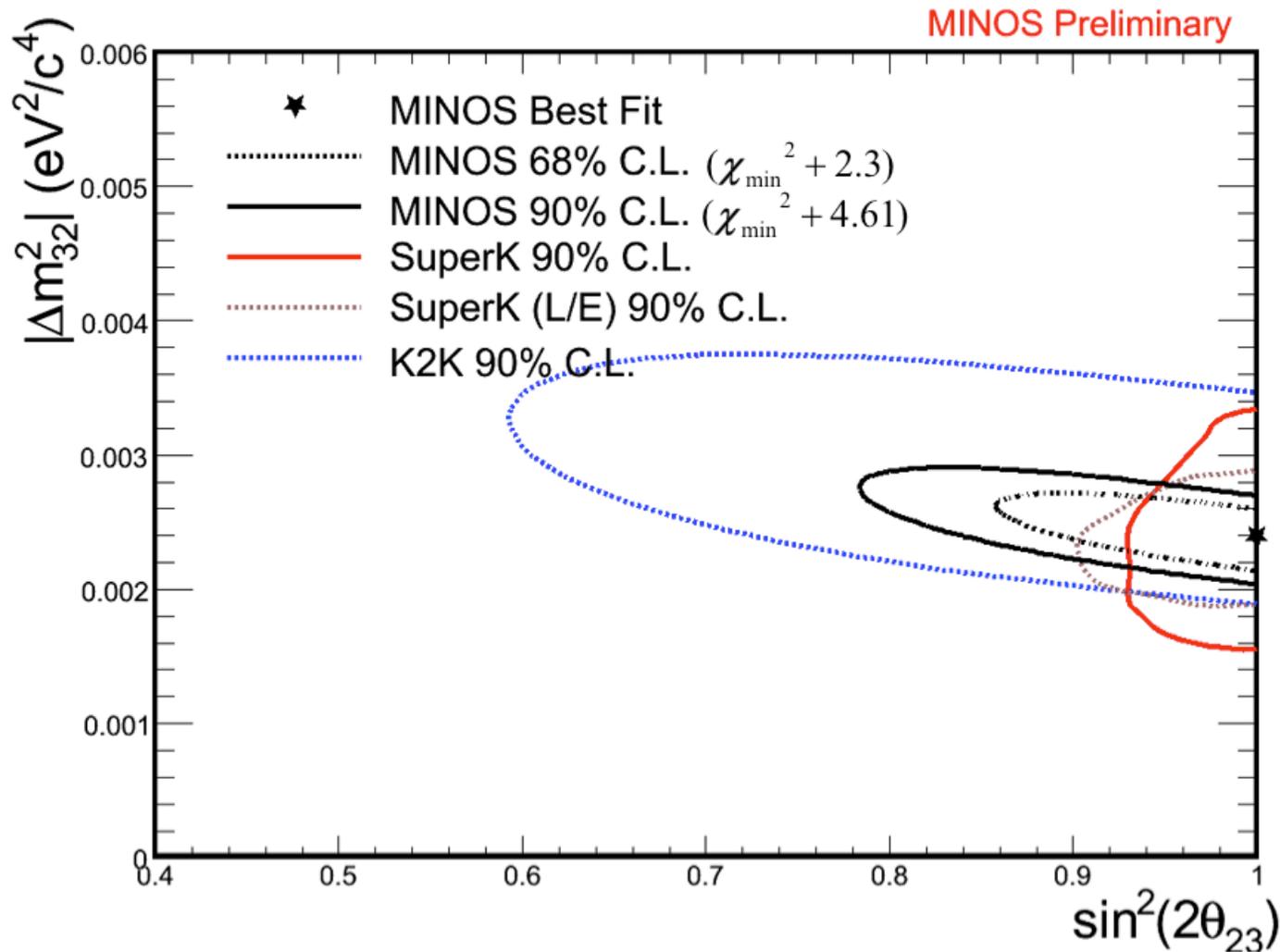
$$\begin{array}{l} c_{ij} \equiv \cos \theta_{ij} \\ s_{ij} \equiv \sin \theta_{ij} \end{array}$$

$$\theta_{12} \approx \theta_{\text{sol}} \approx 34^\circ, \quad \theta_{23} \approx \theta_{\text{atm}} \approx 37\text{-}53^\circ, \quad \theta_{13} \lesssim 10^\circ$$

Majorana ~~CP~~  
phases

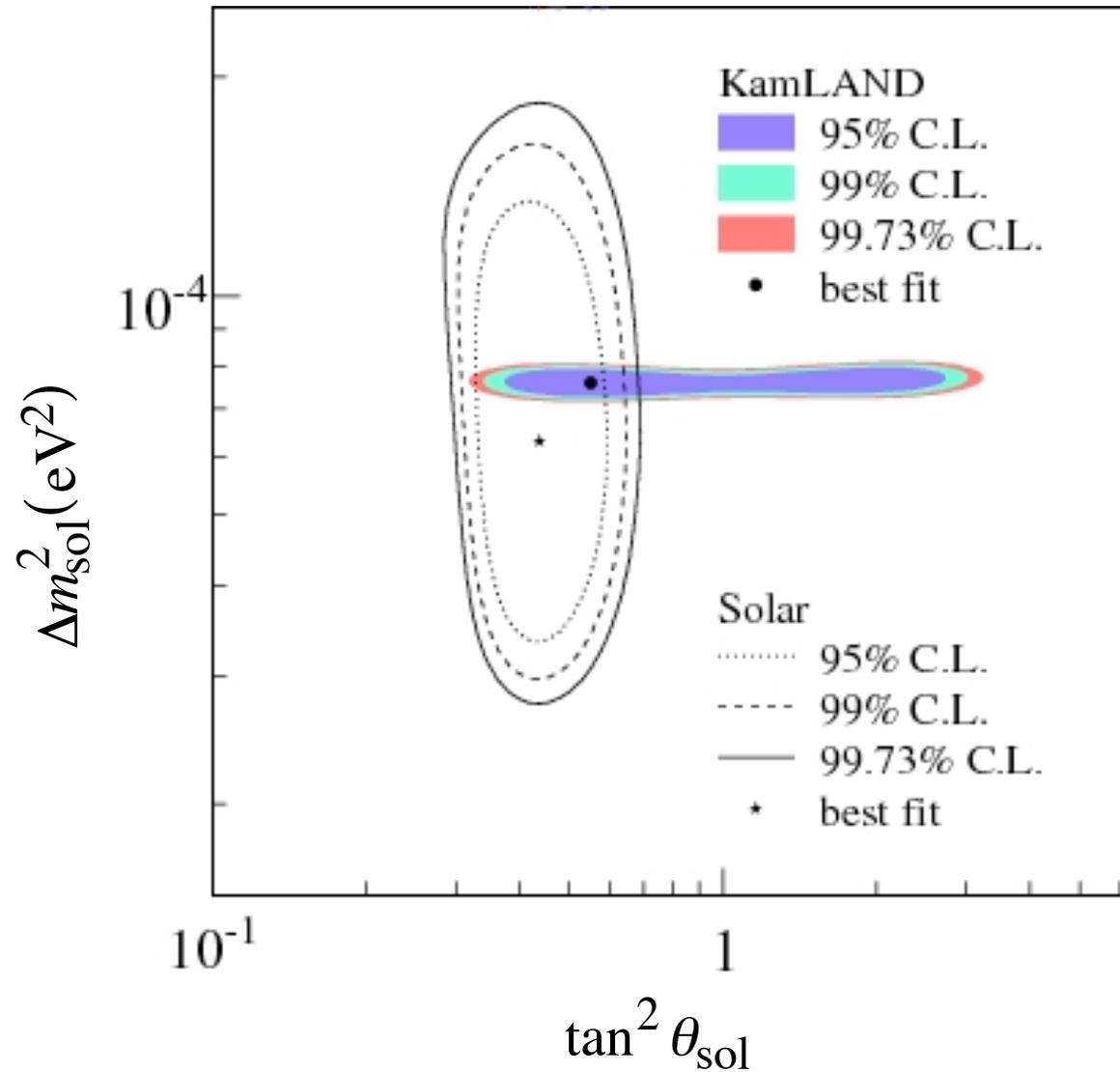
$\delta$  would lead to  $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \neq P(\nu_\alpha \rightarrow \nu_\beta)$ . ~~CP~~

But note the crucial role of  $s_{13} \equiv \sin \theta_{13}$ .



From talk  
by N.  
Saoulidou

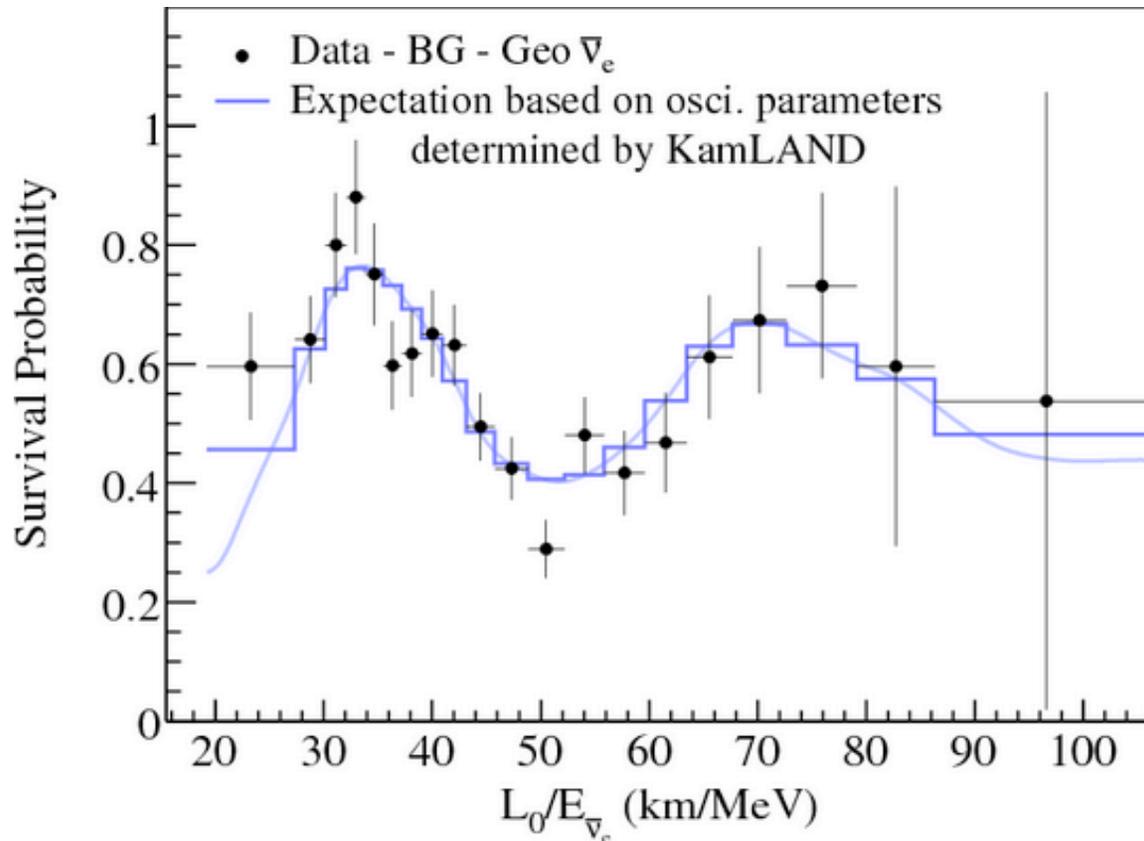
“Atmospheric”  $\Delta m^2$  and mixing angle  
from MINOS, Super-K, and K2K.



Presented by  
KamLAND,  
a reactor  $\bar{\nu}_e$   
experiment.

“Solar”  $\Delta m^2$  and mixing angle  
from KamLAND and solar experiments.

# KamLAND Evidence for Oscillation



$L_0 = 180$  km is a flux-weighted average travel distance.

*$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$  actually oscillates!*

# $^7\text{Be}$ Solar Neutrinos

Until recently, only the  $^8\text{B}$  solar neutrinos, with  $E \sim 7 \text{ MeV}$ , had been studied in detail.

The Large Mixing Angle MSW (*matter*) effect boosts the fraction of the  $^8\text{B}$  solar  $\nu_e$  that get transformed into neutrinos of other flavors to roughly 70%.

At the energy  $E = 0.862 \text{ MeV}$  of the  $^7\text{Be}$  solar neutrinos, the matter effect is expected to be very small. Only about 45% of the  $^7\text{Be}$  solar  $\nu_e$  are expected to change into neutrinos of other flavors.

# Borexino —

Detects the  ${}^7\text{Be}$  solar neutrinos  
via  $\nu_e \rightarrow \nu_e$  elastic scattering.

## Event rate (Counts/day/100 tons)

Observed:	$47 \pm 7(\text{stat}) \pm 12(\text{syst})$
Expected (No Osc):	$75 \pm 4$
Expected (With 45% Osc):	$49 \pm 4$
Expected (With 70% Osc):	$\sim 31$



# The Open Questions

- What is the absolute scale of neutrino mass?
- Are neutrinos their own antiparticles?
- Are there “sterile” neutrinos?

**We must be alert to surprises!**

- What is the pattern of mixing among the different types of neutrinos?

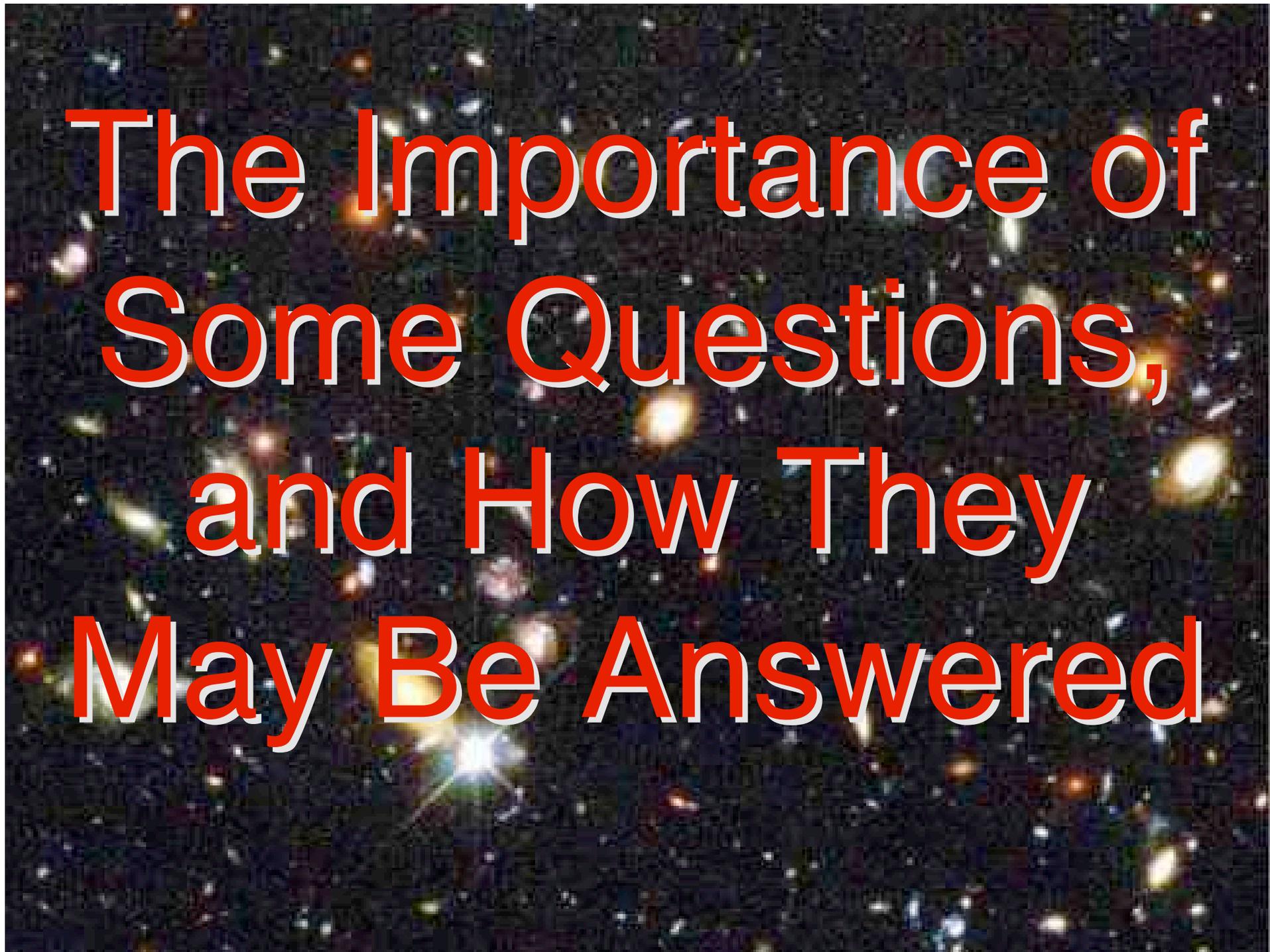
What is  $\theta_{13}$ ?

- Is the spectrum like  $\underline{=}$  or  $\underline{=}$  ?

- Do neutrino – matter interactions violate CP?

Is  $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \neq P(\nu_\alpha \rightarrow \nu_\beta)$  ?

- What can neutrinos and the universe tell us about one another?
- Is CP violation involving neutrinos the key to understanding the matter – antimatter asymmetry of the universe?
- What physics is behind neutrino mass?



The Importance of  
Some Questions,  
and How They  
May Be Answered

# Does $\bar{\nu} = \nu$ ?

That is, for each *mass eigenstate*  $\nu_i$ , does —

- $\bar{\nu}_i = \nu_i$  (Majorana neutrinos)

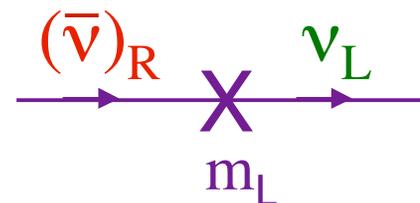
or

- $\bar{\nu}_i \neq \nu_i$  (Dirac neutrinos) ?

Equivalently, do neutrinos have *Majorana masses*? If they do, then the mass eigenstates are *Majorana neutrinos*.

# Majorana Masses

Out of, say, a left-handed neutrino field,  $\nu_L$ , and its charge-conjugate,  $\nu_L^c$ , we can build a **Majorana** mass term —

$$m_L \bar{\nu}_L \nu_L^c$$


*Quark* and *charged-lepton* Majorana masses are forbidden by electric charge conservation.

*Neutrino* Majorana masses would make the neutrinos very distinctive.

The objects  $\mathbf{v}_L$  and  $\mathbf{v}_L^c$  in  $m_L \overline{\mathbf{v}_L} \mathbf{v}_L^c$  are not the mass eigenstates, but just the neutrinos in terms of which the model is constructed.

$m_L \overline{\mathbf{v}_L} \mathbf{v}_L^c$  induces  $\mathbf{v}_L \leftrightarrow \mathbf{v}_L^c$  mixing.

As a result of  $K^0 \leftrightarrow \overline{K}^0$  mixing, the neutral K mass eigenstates are —

$$K_{S,L} \cong (K^0 \pm \overline{K}^0)/\sqrt{2} . \quad \overline{\overline{K}_{S,L}} = K_{S,L} .$$

As a result of  $\mathbf{v}_L \leftrightarrow \mathbf{v}_L^c$  mixing, the neutrino mass eigenstate is —

$$\mathbf{v}_i = \mathbf{v}_L + \mathbf{v}_L^c = \text{“ } \mathbf{v} + \overline{\mathbf{v}} \text{”} . \quad \overline{\overline{\mathbf{v}}_i} = \mathbf{v}_i .$$

To Determine If  
Neutrinos Have  
Majorana Masses

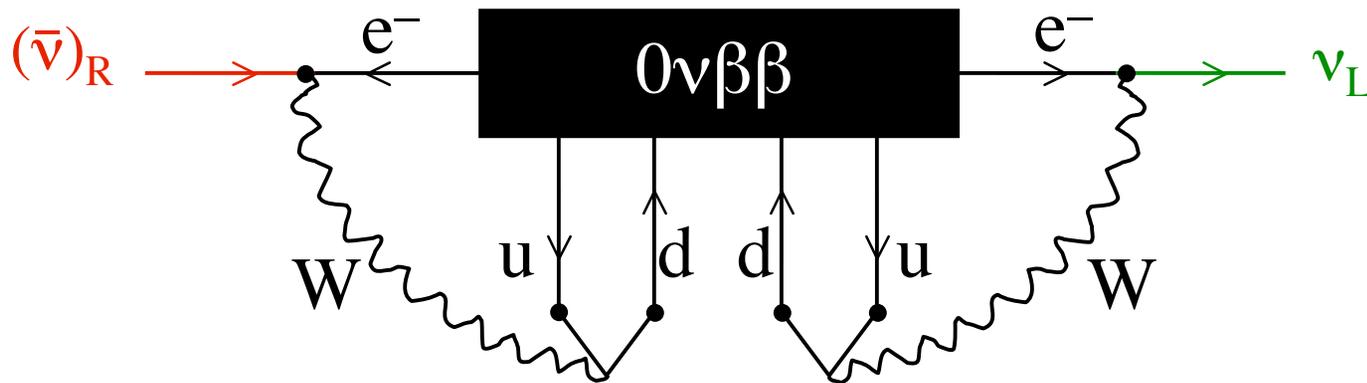
# The Promising Approach — Neutrinoless Double Beta Decay [ $0\nu\beta\beta$ ]



We are looking for a *small* Majorana neutrino mass. Thus, we will need *a lot* of parent nuclei (say, one ton of them).

Whatever diagrams cause  $0\nu\beta\beta$ , its observation would imply the existence of a Majorana mass term:

Schechter and Valle



$(\bar{\nu})_R \rightarrow \nu_L$  : A Majorana mass term

$\therefore 0\nu\beta\beta \rightarrow \bar{\nu}_i = \nu_i$

# The Central Role of $\theta_{13}$

Both CP violation and our ability to tell whether the spectrum is normal or inverted depend on  $\theta_{13}$ .

If  $\sin^2 2\theta_{13} > 10^{-(2-3)}$ , we can study both of these issues with intense but conventional accelerator  $\nu$  and  $\bar{\nu}$  beams, produced via  $\pi^+ \rightarrow \mu^+ + \nu_{\mu}$  and  $\pi^- \rightarrow \mu^- + \bar{\nu}_{\mu}$ .

Determining  $\theta_{13}$  is an important step.

# How $\theta_{13}$ May Be Measured

*Reactor* neutrino experiments are the cleanest way.

---

*Accelerator* neutrino experiments can also probe  $\theta_{13}$  .

Now it is entwined with other parameters.

In addition, accelerator experiments can probe *whether the mass spectrum is normal or inverted*, and look for *CP violation*.

All of this is done by studying  $\nu_{\mu} \rightarrow \nu_e$  and  $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$  while the beams travel hundreds of kilometers.

# The Mass Spectrum: $\underline{\underline{=}}$ or $\underline{=}$ ?

Generically, grand unified models (GUTS) favor —

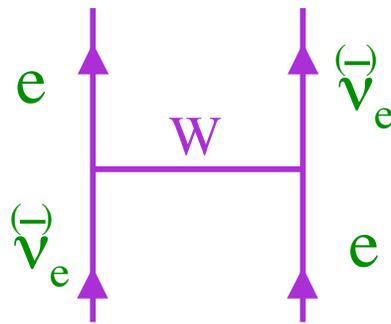
$\underline{\underline{=}}$

GUTS relate the **Leptons** to the **Quarks**.

$\underline{\underline{=}}$  is un-quark-like, and would probably involve a lepton symmetry with no quark analogue.

# How To Determine If The Spectrum Is Normal Or Inverted

Exploit the fact that, in matter,



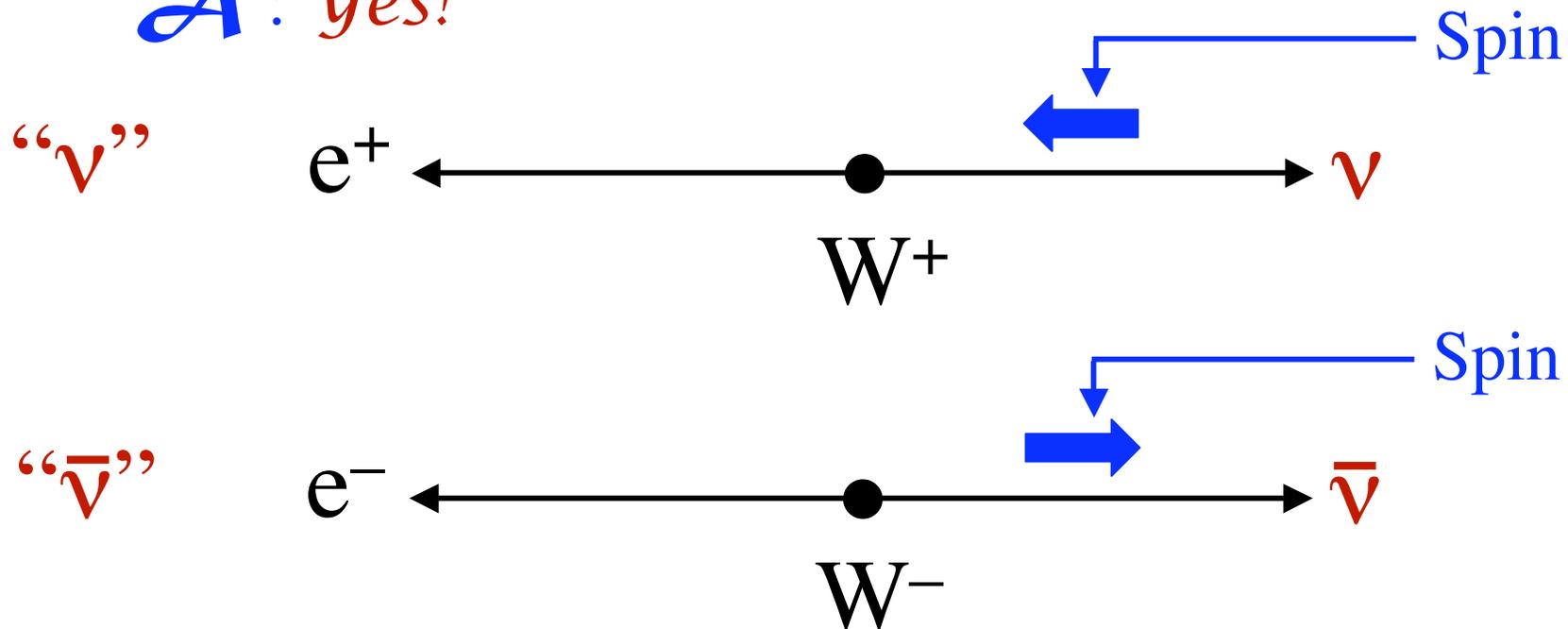
affects  $\nu$  and  $\bar{\nu}$  oscillation (*differently*), and leads to —

$$\frac{P(\nu_\mu \rightarrow \nu_e)}{P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \begin{cases} > 1 ; \equiv \\ < 1 ; \equiv \end{cases} \quad \text{Note fake } \mathcal{CP}$$

*Note dependence on the mass ordering*

**Q** : Does matter still affect  $\nu$  and  $\bar{\nu}$  differently when  $\bar{\nu} = \nu$ ?

**A** : Yes!



The weak interactions violate *parity*. Neutrino – matter interactions depend on the neutrino *polarization*.

# Do Neutrino Interactions Violate CP?

The observed  $\not{CP}$  in the weak interactions of *quarks* cannot explain the *Baryon Asymmetry* of the universe.

Is *leptonic*  $\not{CP}$ , through *Leptogenesis*, the origin of the *Baryon Asymmetry* of the universe?

(Fukugita, Yanagida)

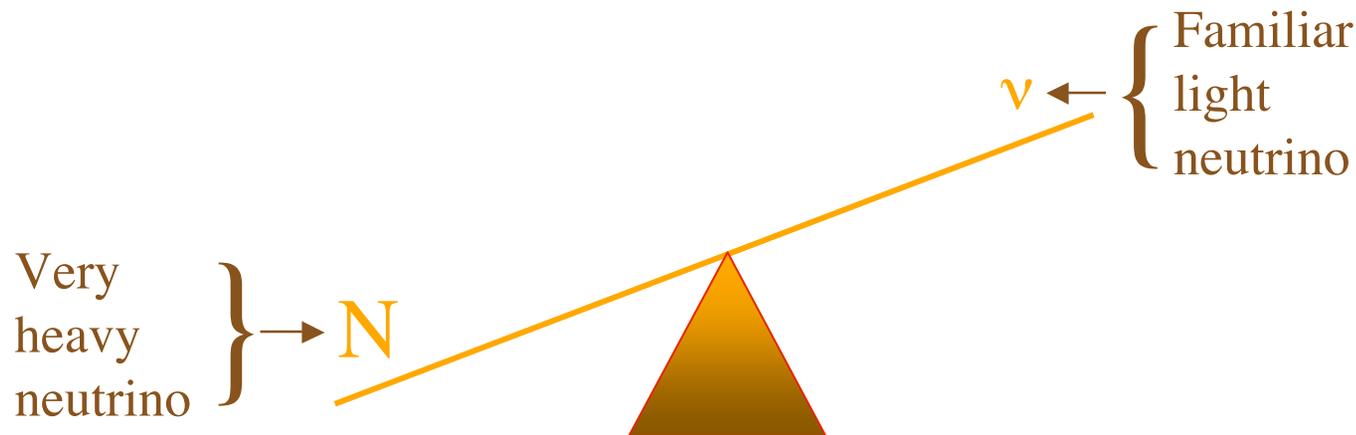
(Wilfried Buchmueller)  
Leading contributor

# *Leptogenesis In Brief*

The most popular theory of why neutrinos are so light is the —

## See-Saw Mechanism

(Yanagida; Gell-Mann, Ramond, Slansky; Minkowski)



The *very* heavy neutrinos **N** would have been made in the hot Big Bang.

The heavy neutrinos  $N$ , like the light ones  $\nu$ , are Majorana particles. Thus, an  $N$  can decay into  $\ell^-$  or  $\ell^+$ .

*If neutrino oscillation violates CP, then quite likely so does  $N$  decay. In the See-Saw, these two CP violations have a common origin.*

Then, in the early universe, we would have had different rates for the CP-mirror-image decays –

$$N \rightarrow \ell^- + \dots \quad \text{and} \quad N \rightarrow \ell^+ + \dots$$

This would have led to unequal numbers of **leptons** and **antileptons** (*Leptogenesis*).

Then, Standard-Model *Sphaleron* processes would have turned  $\sim 1/3$  of this leptonic asymmetry into a *Baryon Asymmetry*.

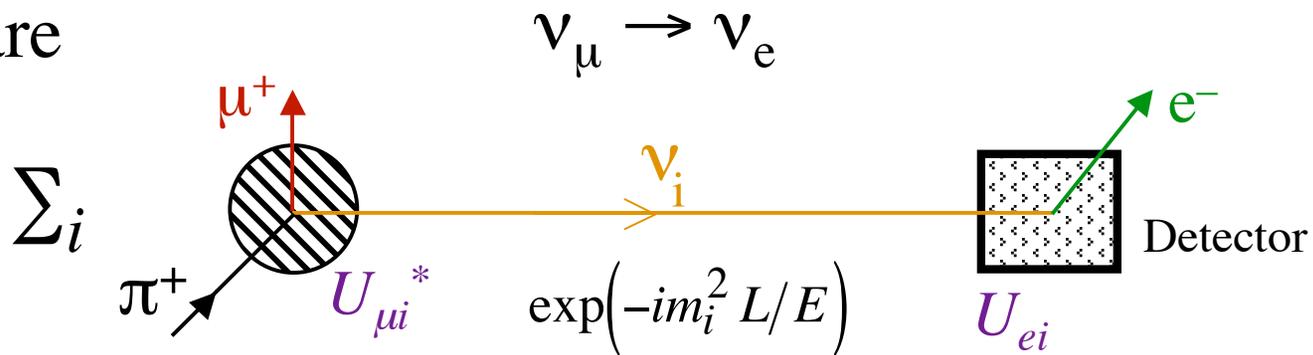
# How To Search for ~~CP~~ In Neutrino Oscillation

Look for  $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \neq P(\nu_\alpha \rightarrow \nu_\beta)$

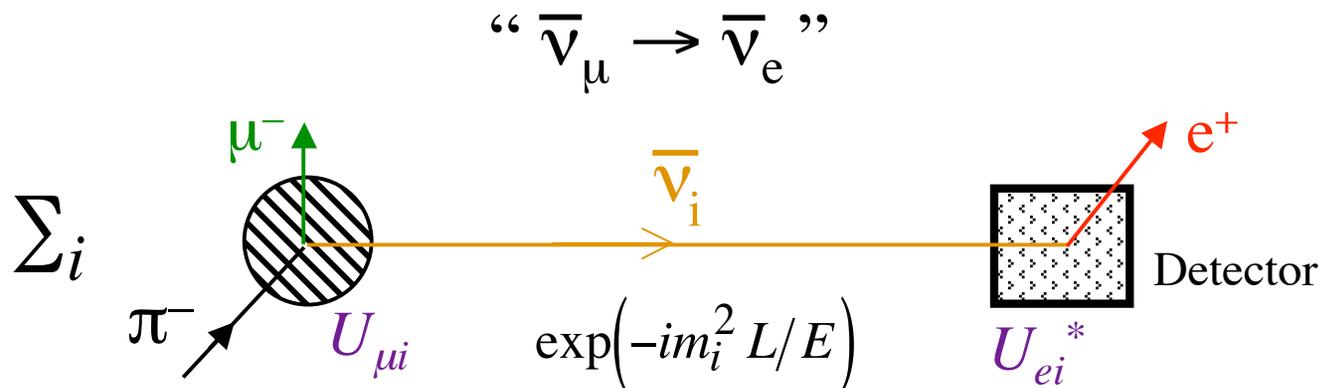
**Q** : Can CP violation still lead to  $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \neq P(\nu_\mu \rightarrow \nu_e)$  when  $\bar{\nu} = \nu$ ?

**A** : Certainly!

Compare



with



# Separating $\cancel{CP}$ From the Matter Effect

Genuine  $\cancel{CP}$  and the matter effect  
both lead to a difference between  
 $\nu$  and  $\bar{\nu}$  oscillation.

But genuine  $\cancel{CP}$  and the matter effect depend  
quite differently from each other on  $L$  and  $E$ .

One can disentangle them by making oscillation  
measurements at different  $L$  and/or  $E$ .

# Accelerator ( $\bar{\nu}$ ) Oscillation Probabilities

With  $\alpha \equiv \Delta m_{21}^2 / \Delta m_{31}^2$ ,  $\Delta \equiv \frac{\Delta m_{31}^2 L}{4E}$ , and  $x \equiv \frac{2\sqrt{2}G_F N_e E}{\Delta m_{31}^2}$  —

$$P[\nu_\mu \rightarrow \nu_e] \cong \sin^2 2\theta_{13} T_1 - \alpha \sin 2\theta_{13} T_2 + \alpha \sin 2\theta_{13} T_3 + \alpha^2 T_4 ;$$

Atmospheric
CP-odd interference

$$T_1 = \sin^2 \theta_{23} \frac{\sin^2[(1-x)\Delta]}{(1-x)^2}, \quad T_2 = \sin \delta \sin 2\theta_{12} \sin 2\theta_{23} \sin \Delta \frac{\sin(x\Delta)}{x} \frac{\sin[(1-x)\Delta]}{(1-x)},$$

CP-even interference
Solar

$$T_3 = \cos \delta \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \frac{\sin(x\Delta)}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}, \quad T_4 = \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(x\Delta)}{x^2}$$

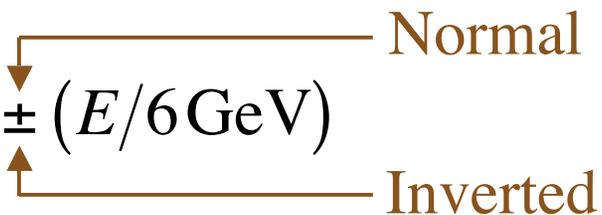
$$P[\bar{\nu}_\mu \rightarrow \bar{\nu}_e] = P[\nu_\mu \rightarrow \nu_e] \text{ with } \delta \rightarrow -\delta \text{ and } x \rightarrow -x.$$

(Cervera *et al.*, Freund, Akhmedov *et al.*)

# Strategies

The matter-effect parameter  $x$  has  $|x| \approx E/12 \text{ GeV}$ .

At  $L/E$  of the 1<sup>st</sup> “atmospheric” oscillation peak, and  $E \sim 1 \text{ GeV}$ , the effect of matter on the *neutrino* atmospheric oscillation term ( $\sin^2 2\theta_{13} T_1$ ) is —

$$1/(1-x)^2 \cong 1 \pm (E/6 \text{ GeV})$$


At fixed  $L/E$ , genuine ~~CP~~ effects do not change with  $E$ , but the matter effect grows, **enhancing** (**suppressing**) the oscillation if the hierarchy is **Normal** (**Inverted**).

If  $E \rightarrow E/3$  at fixed  $L$ , we go from the 1<sup>st</sup> atmospheric oscillation peak to the 2<sup>nd</sup> one.

When  $E \rightarrow E/3$  at fixed  $L$ ,  ~~$\mathcal{CP}$~~  is tripled, but the matter effect is reduced by a factor of 3.

# Neutrino Vision at Fermilab

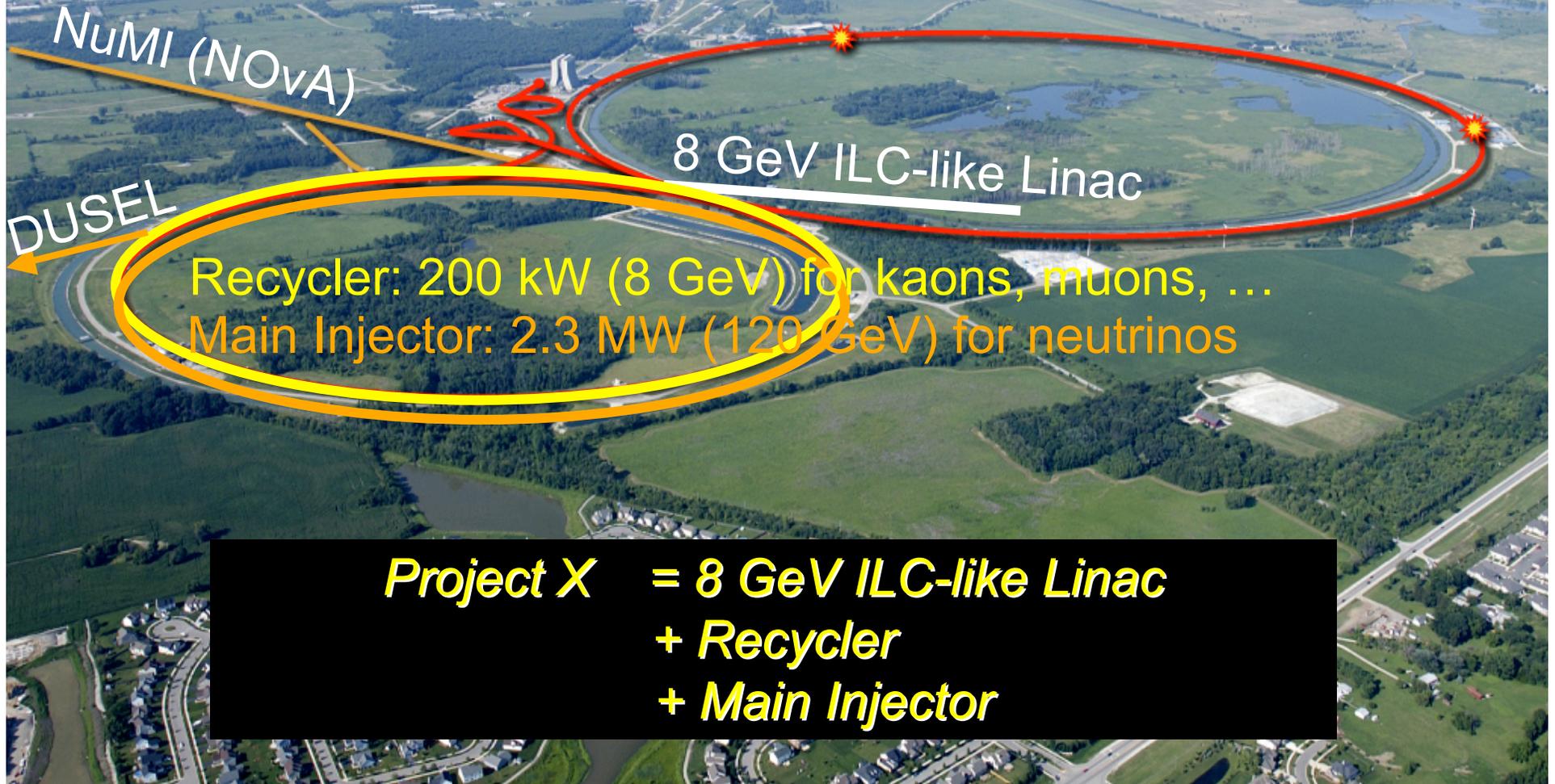
Develop a  
phased approach with  
ever increasing beam intensities  
and ever increasing detector capabilities

Probe Mixing, Mass Ordering, CP Violation

# The Intensity Frontier With Project X

Y-K Kim

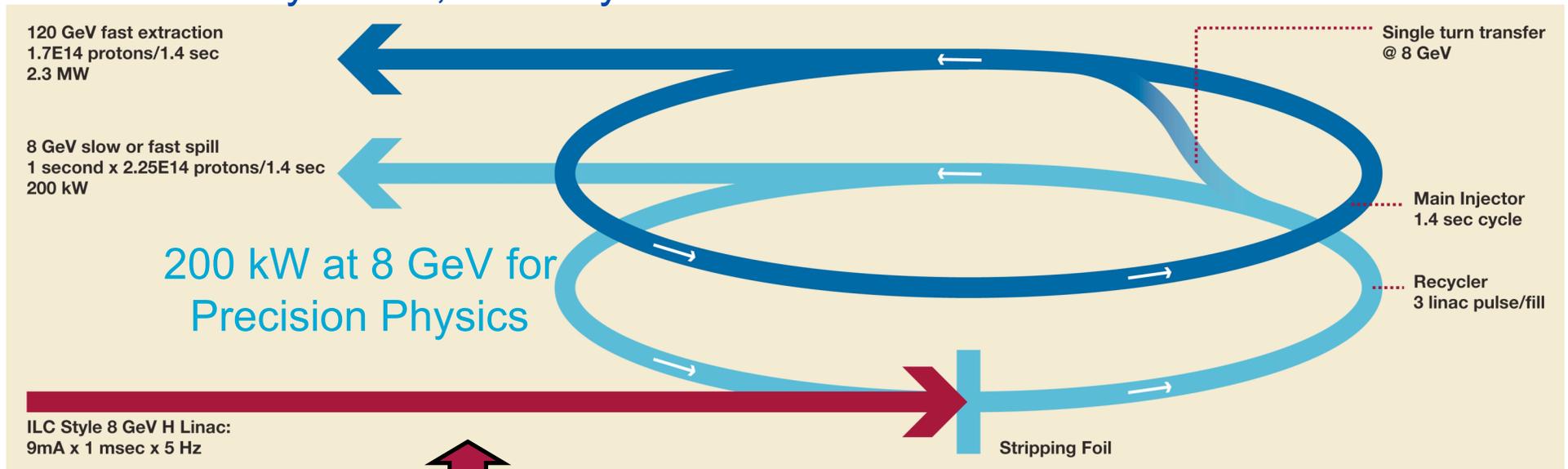
National Project with International Collaboration



# Project X: Properties

(Young-Kee Kim)

~2.3 MW at 120 GeV for Neutrino Science  
Initially NOvA, Possibly DUSEL later



8 GeV H<sup>-</sup> Linac with ILC Beam Parameters  
(9mA x 1msec x 5Hz)



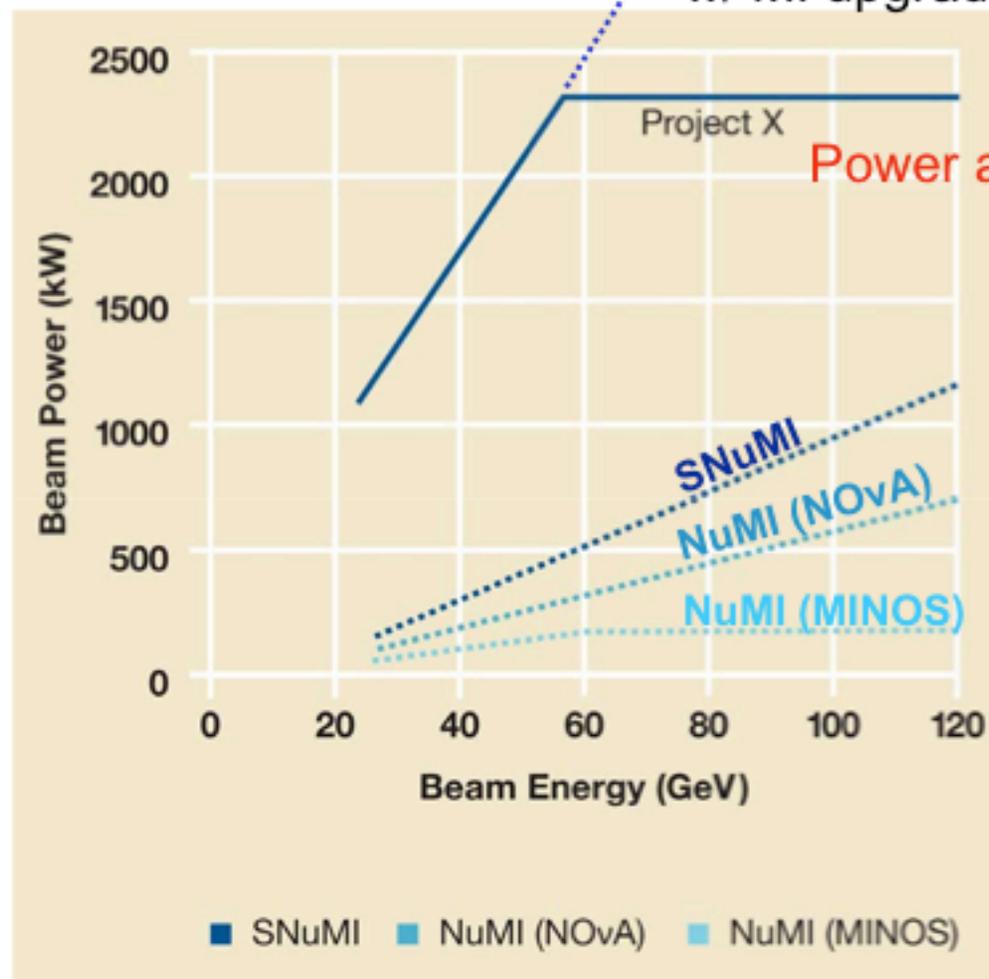
# Project X: Proton Beam Power

(Y-K Kim)

## Main Injector Protons

## Recycler 8 GeV Protons

with 120 GeV MI protons



200 kW (Project X)

0\* (SNUMI)

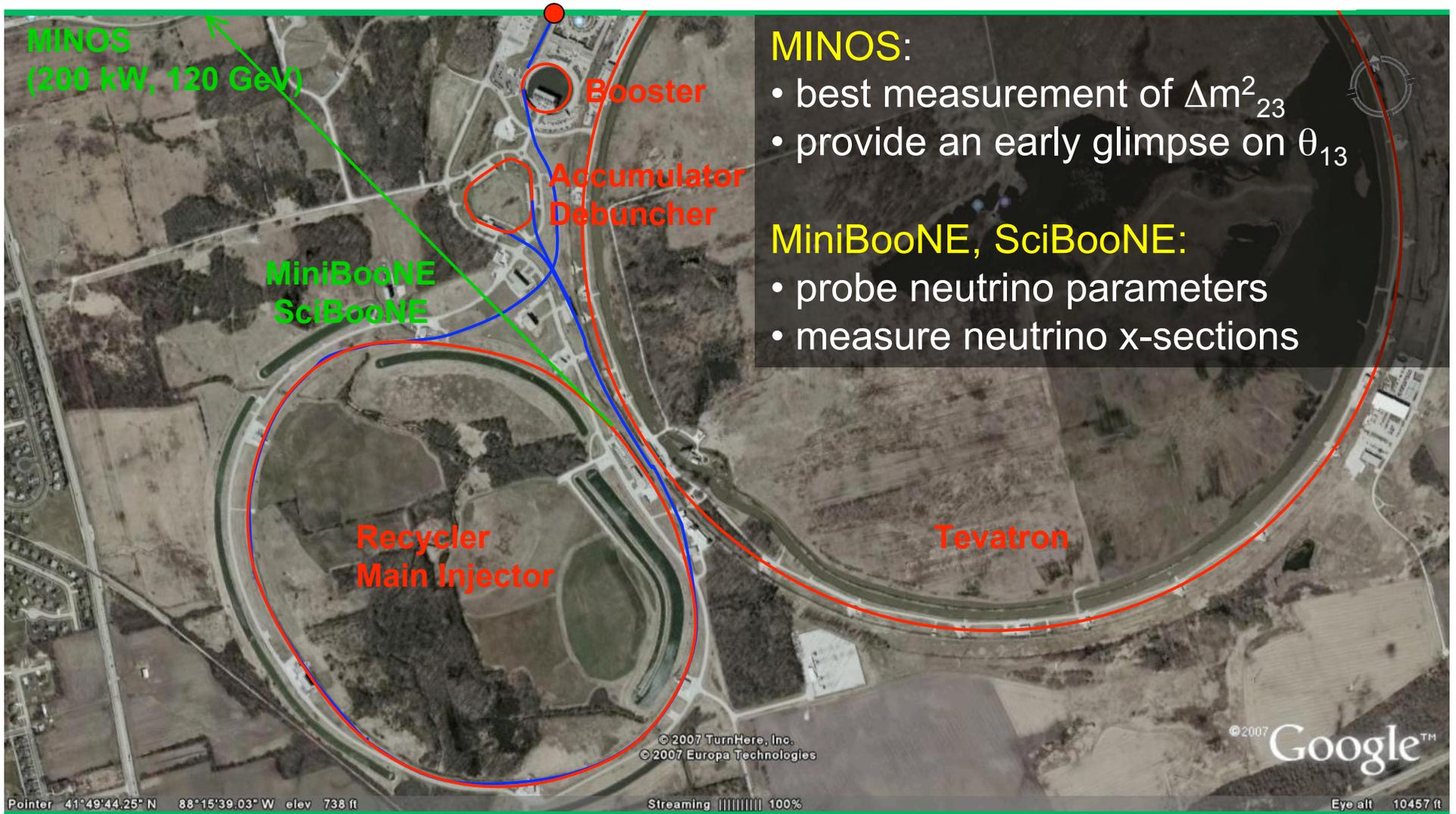
16 kW (NuMI-NOvA)

17 kW (NuMI-MINOS)

35-year-old injection  
(technical risk)

\* Protons could be made available at the expense of 120 GeV power.

# Present:



## MINOS:

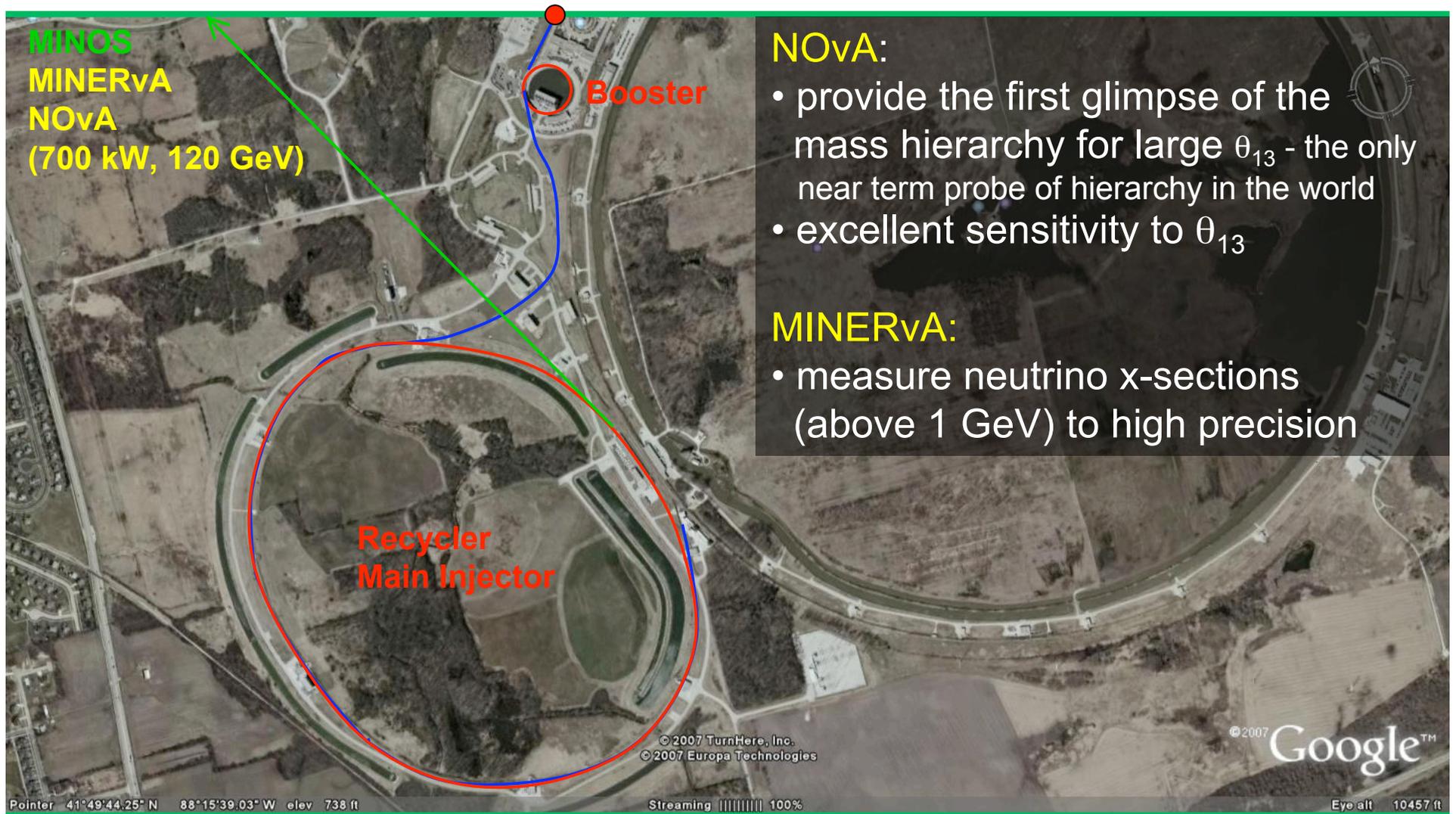
- best measurement of  $\Delta m^2_{23}$
- provide an early glimpse on  $\theta_{13}$

## MiniBooNE, SciBooNE:

- probe neutrino parameters
- measure neutrino x-sections

Y-K Kim

# Phase 1:



Y-K Kim

# The NO $\nu$ A Experiment

NO $\nu$ A Far Detector  
MINOS Far Detector

810 km

Minnesota

Ontario

Wisconsin

Iowa

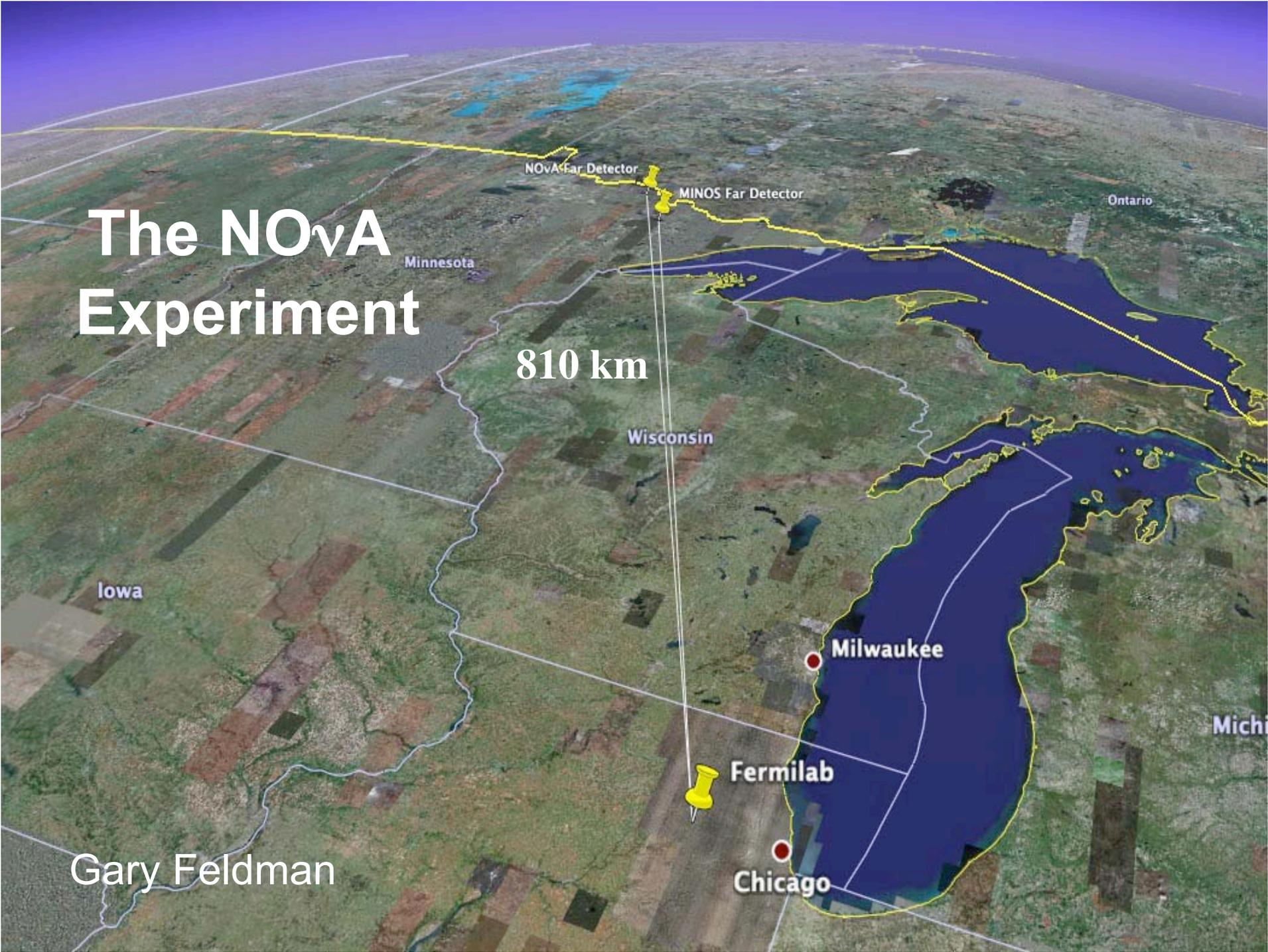
Milwaukee

Michi

Fermilab

Chicago

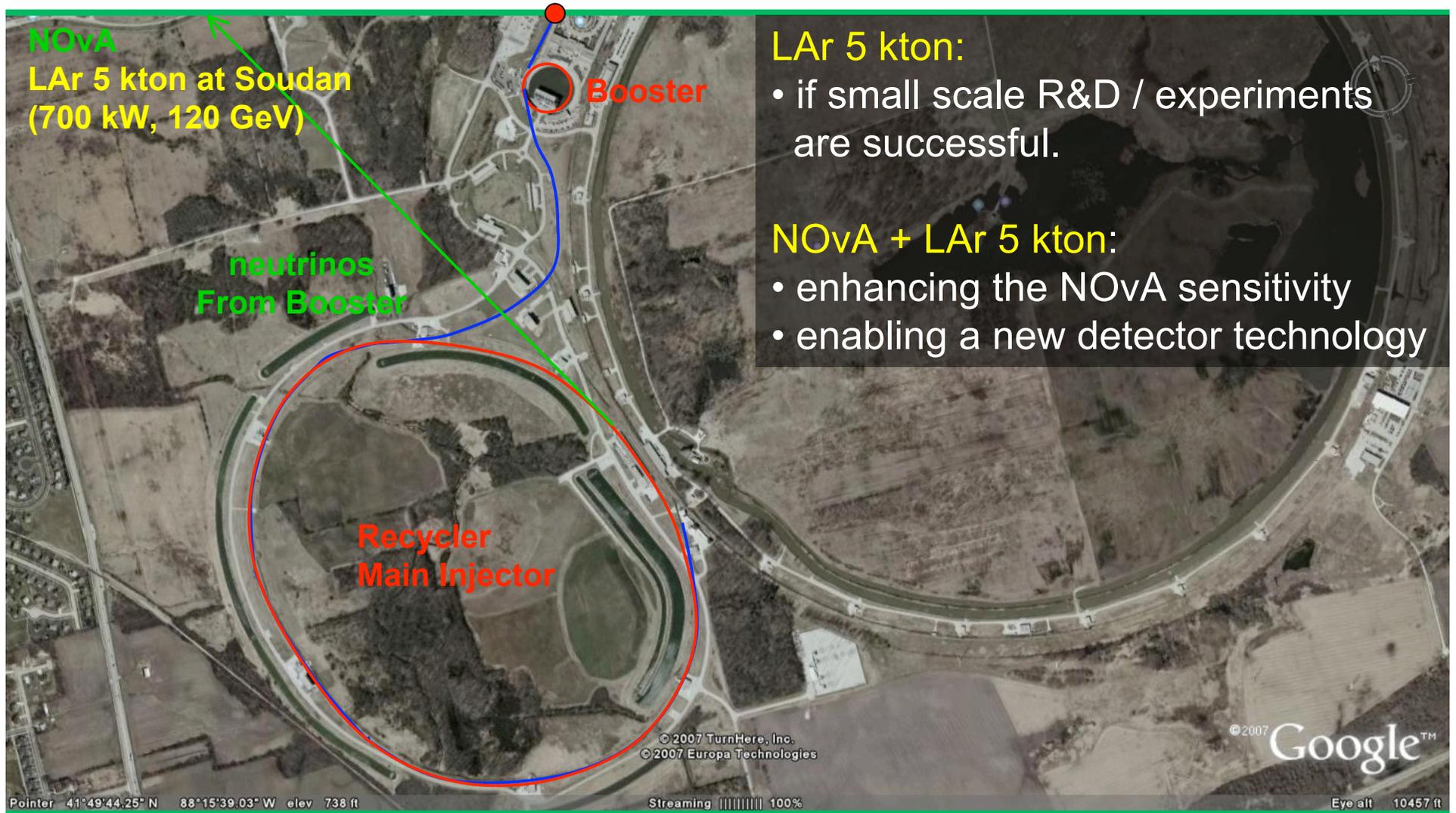
Gary Feldman



# NO $\nu$ A

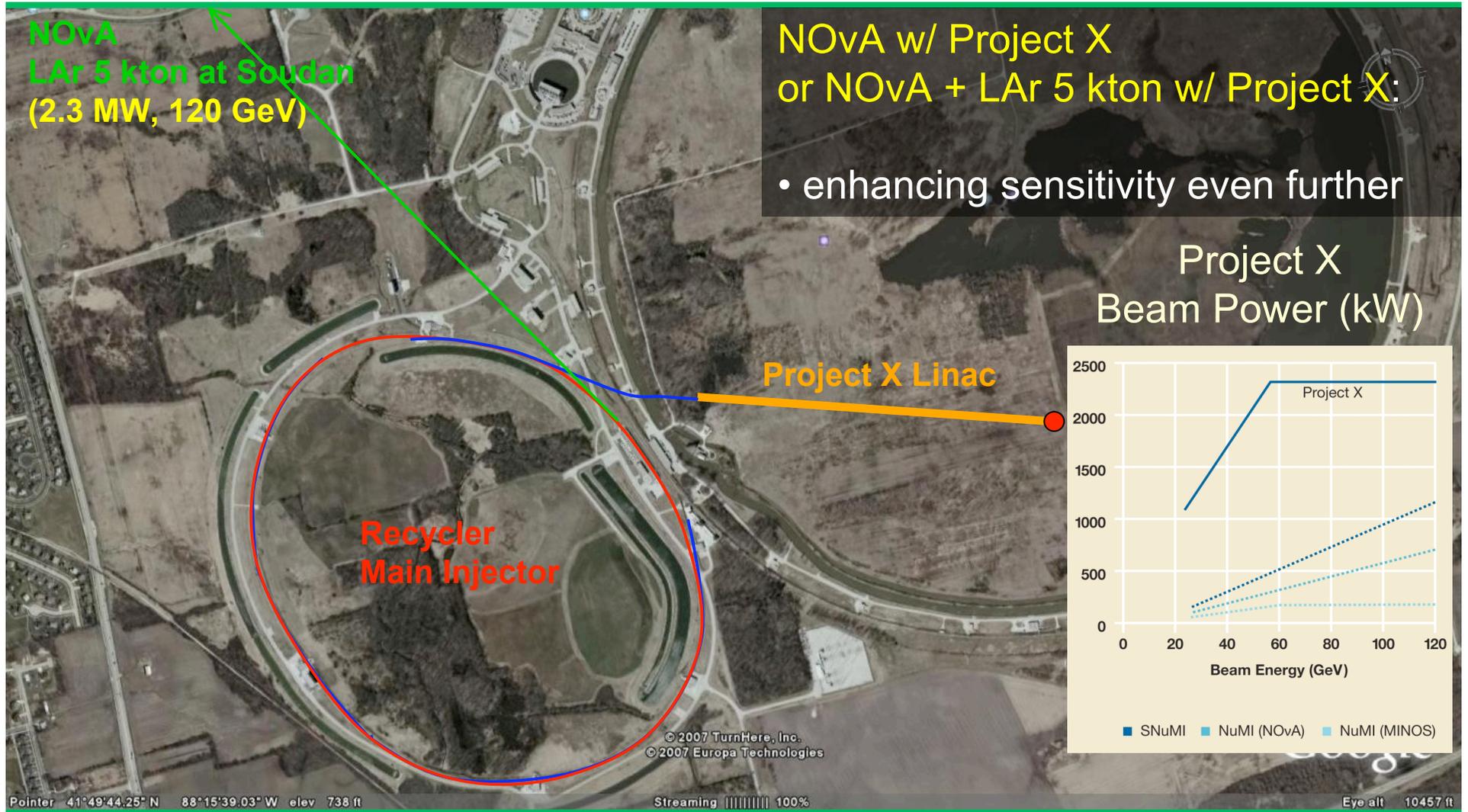
- A study of  $\nu_{\mu} \rightarrow \nu_e$  and  $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$
- $\sim 15$  kton liquid scintillator detector
- Off the axis of Fermilab's NuMI neutrino beamline
- $L = 810$  km;  $E \sim 2$  GeV ( *$L/E$  near 1<sup>st</sup> osc. peak*)
- *Main goal: Try to determine whether the spectrum is **Normal** or **Inverted***

# Phase 1.5:



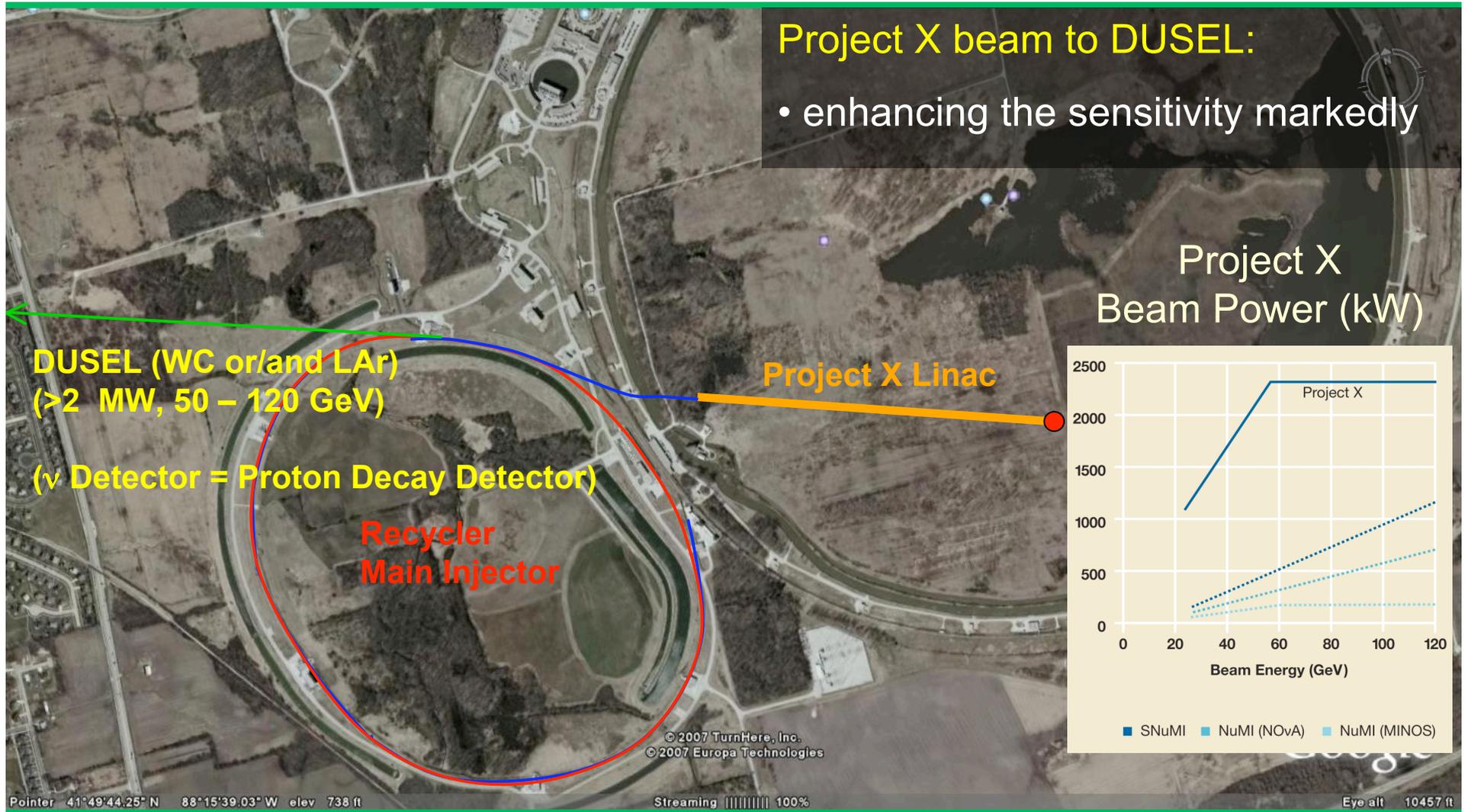
Y-K Kim

# Phase 2:



Y-K Kim

# Phase 3



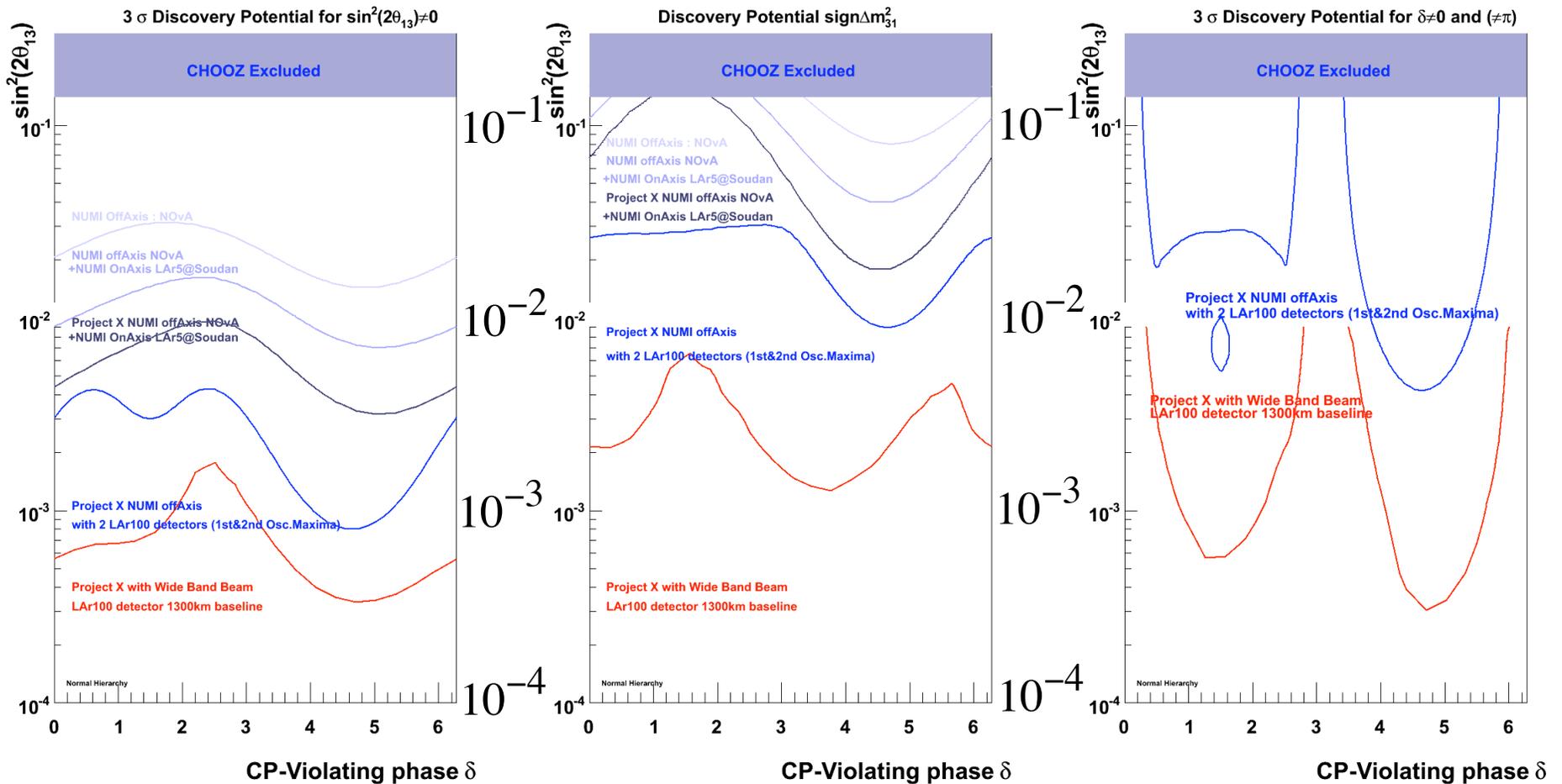
Y-K Kim

# The $3\sigma$ Reach of the Successive Phases

$\sin^2 2\theta_{13}$

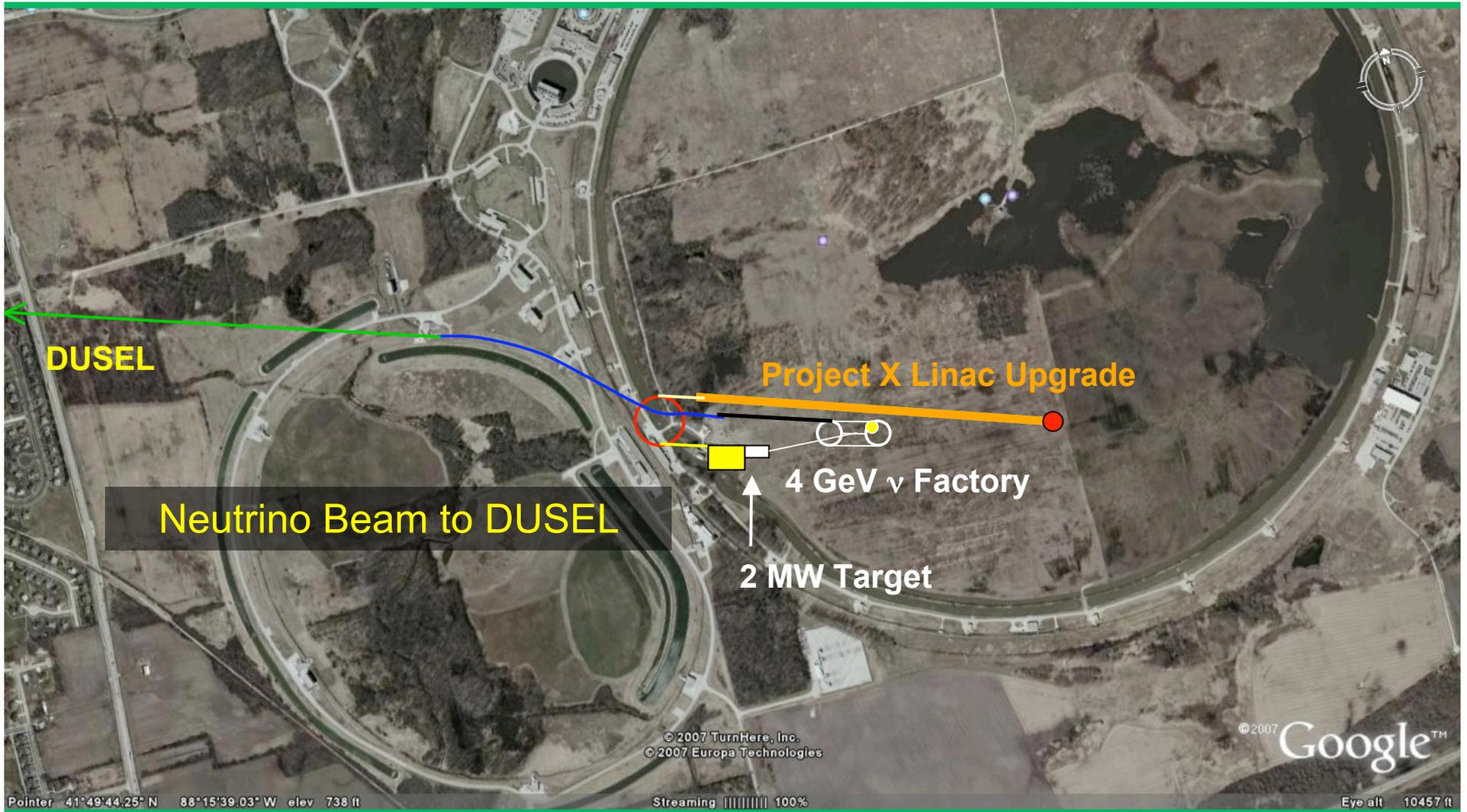
Mass Ordering

CP Violation



N. Saoulidou

# Toward “Proton Intensity Upgrade” Evolutionary Path to a Neutrino Factory



Y-K Kim

# *Summary*

*We have learned a lot about the neutrinos in the last decade.*

*What we have learned raises some very interesting questions.*

*We look forward to answering them.*