

# The Optics of the Dark Universe

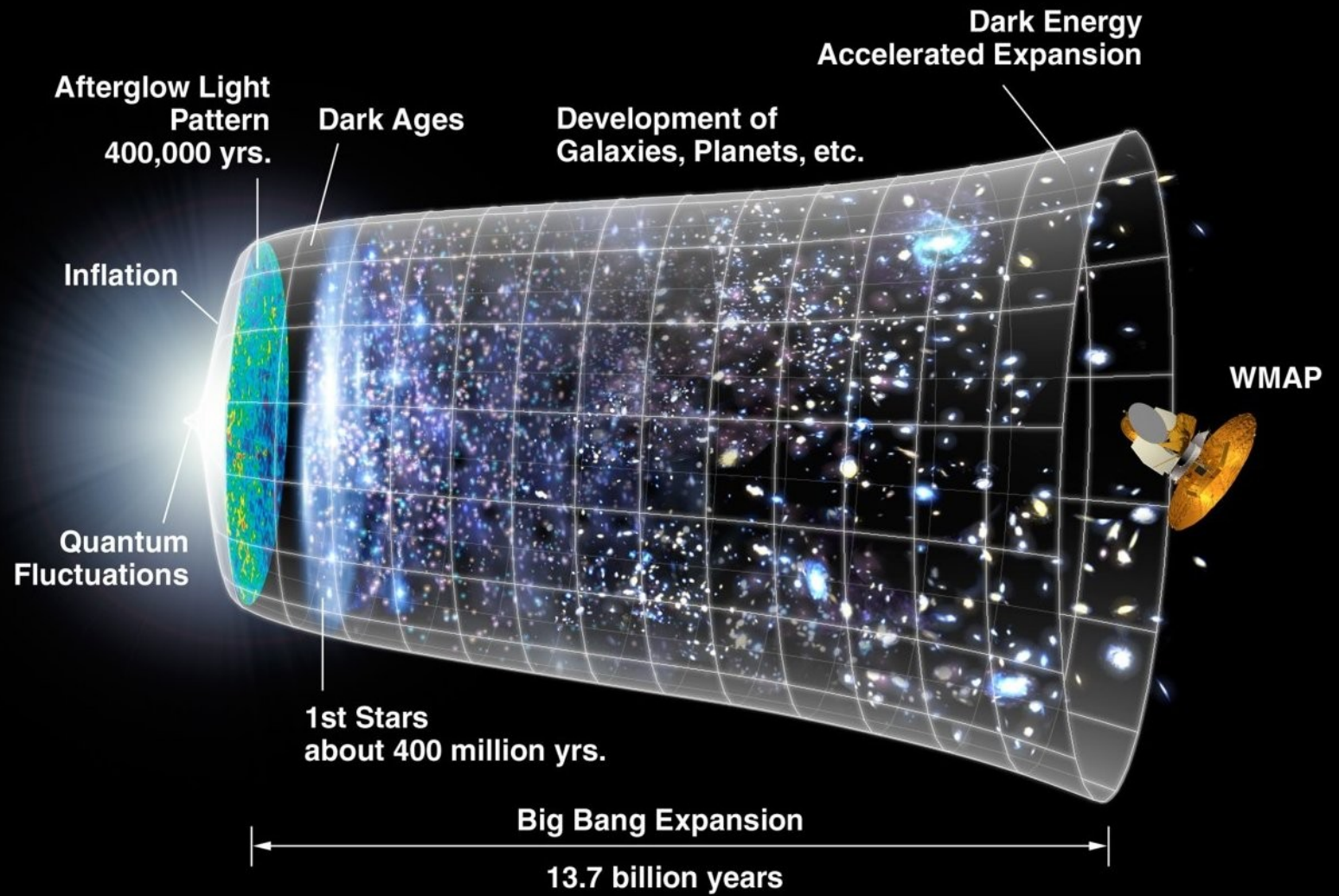
Colloquium Talk  
DESY Hamburg & Zeuthen  
February 8-9, 2011

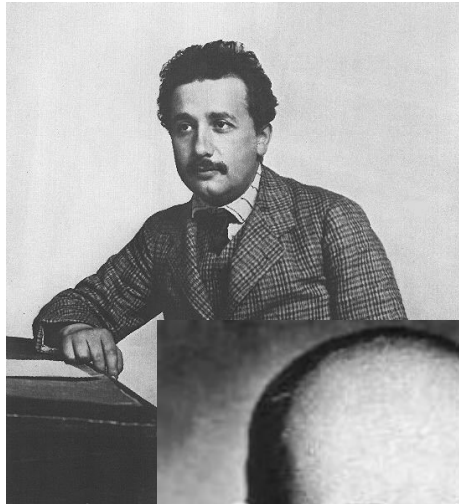
Matthias Bartelmann  
Zentrum für Astronomie  
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# The Optics of the Dark Universe

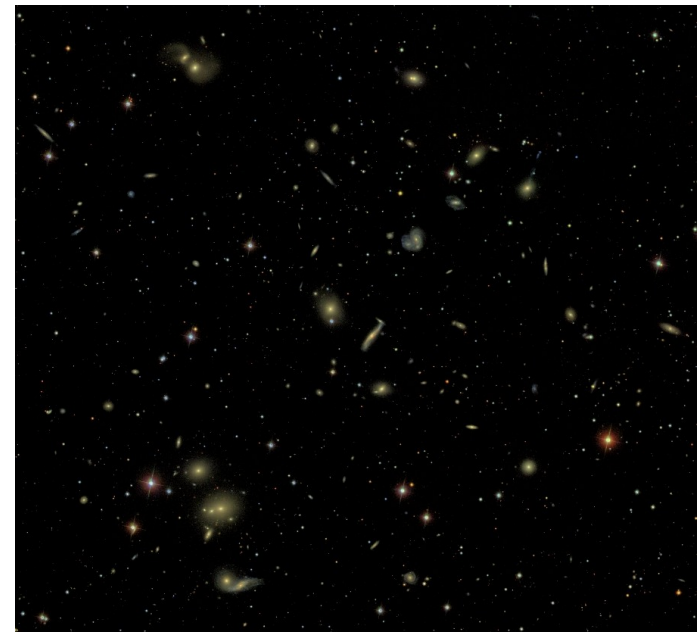
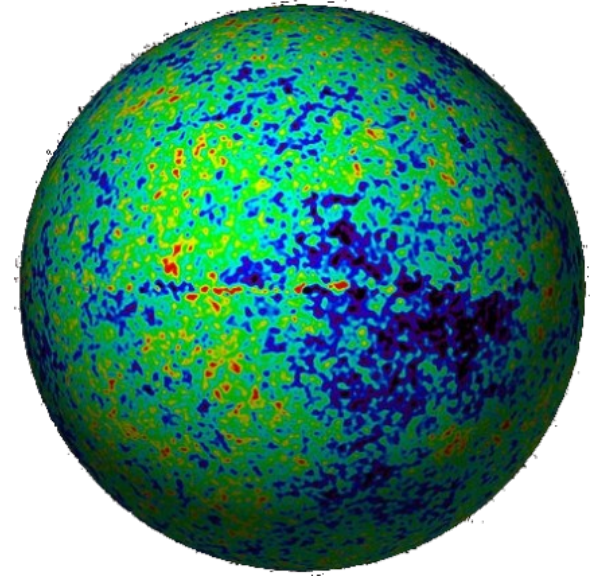
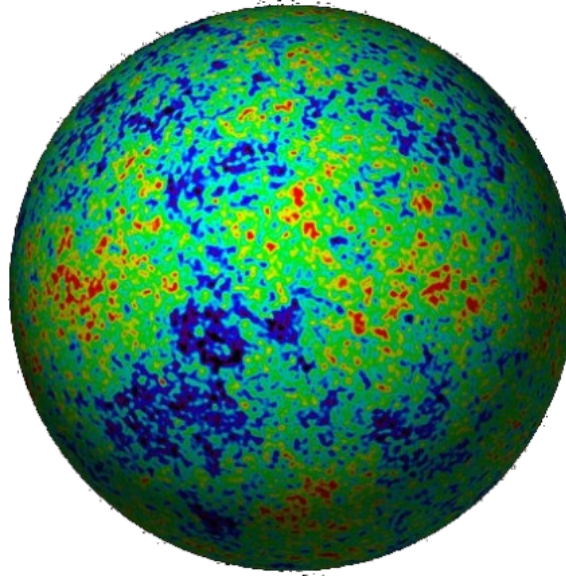
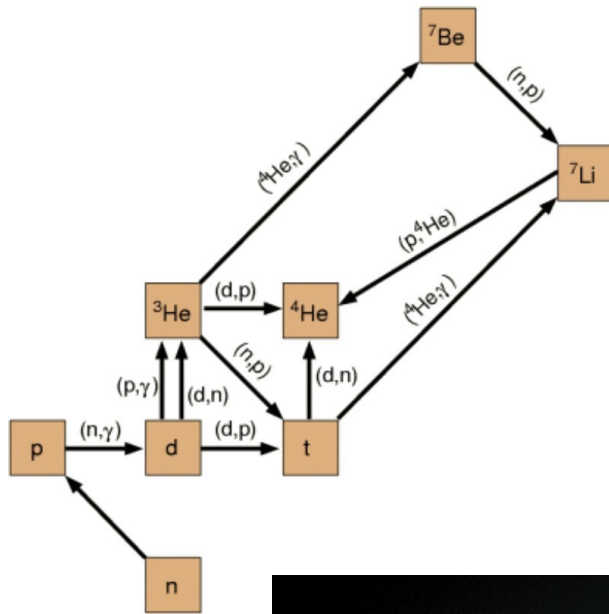
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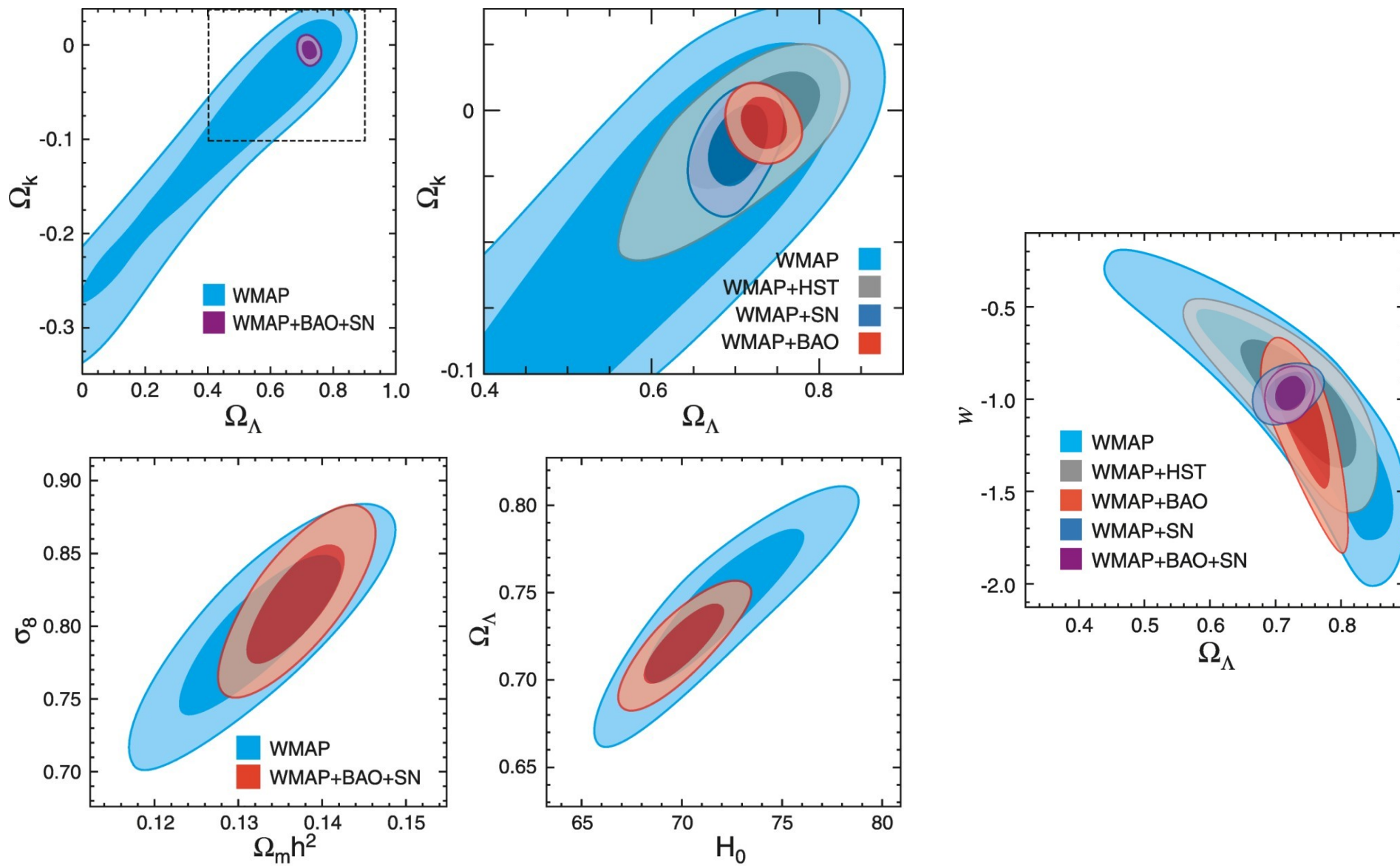
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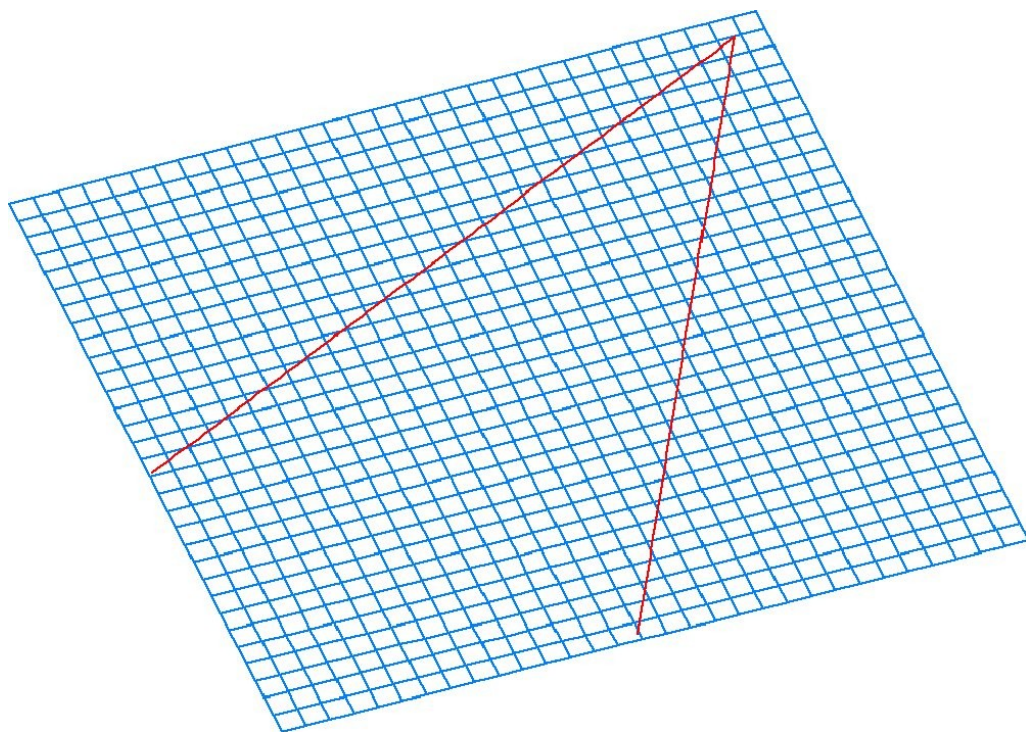


- Einstein's theory of General Relativity
- Symmetry assumptions:  
Friedmann-Lemaître models
- Parameters:
  - Expansion rate,  $H_0$
  - Density contributions,  $\Omega_i$
  - Cosmological constant,  $\Omega_\Lambda$
  - Possible further parameters

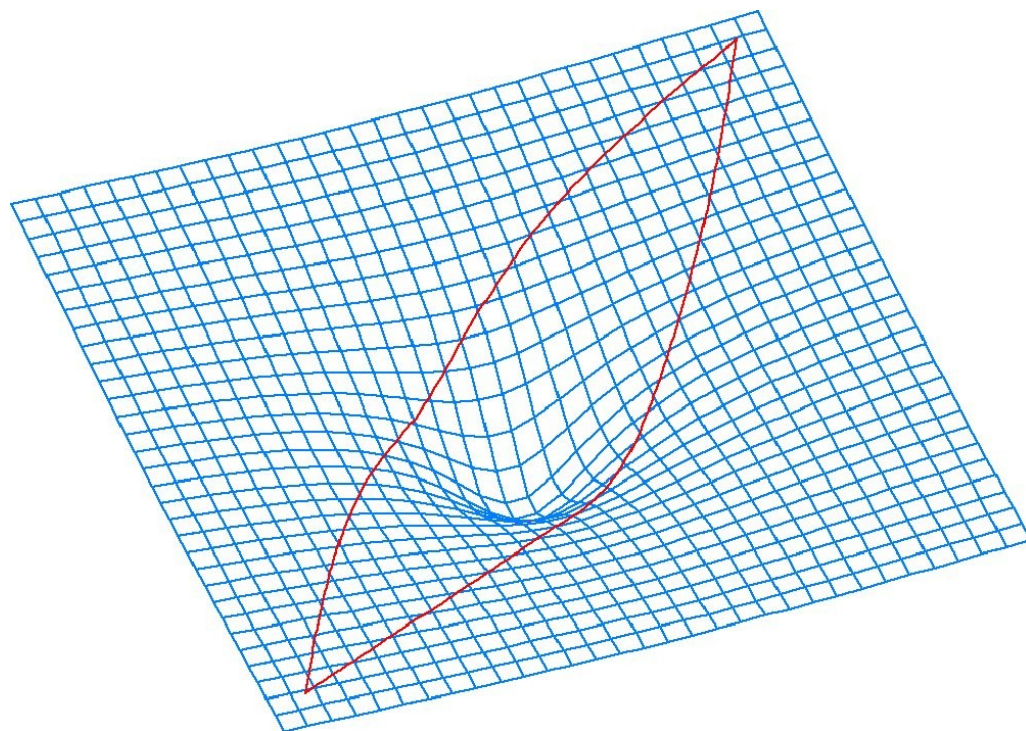


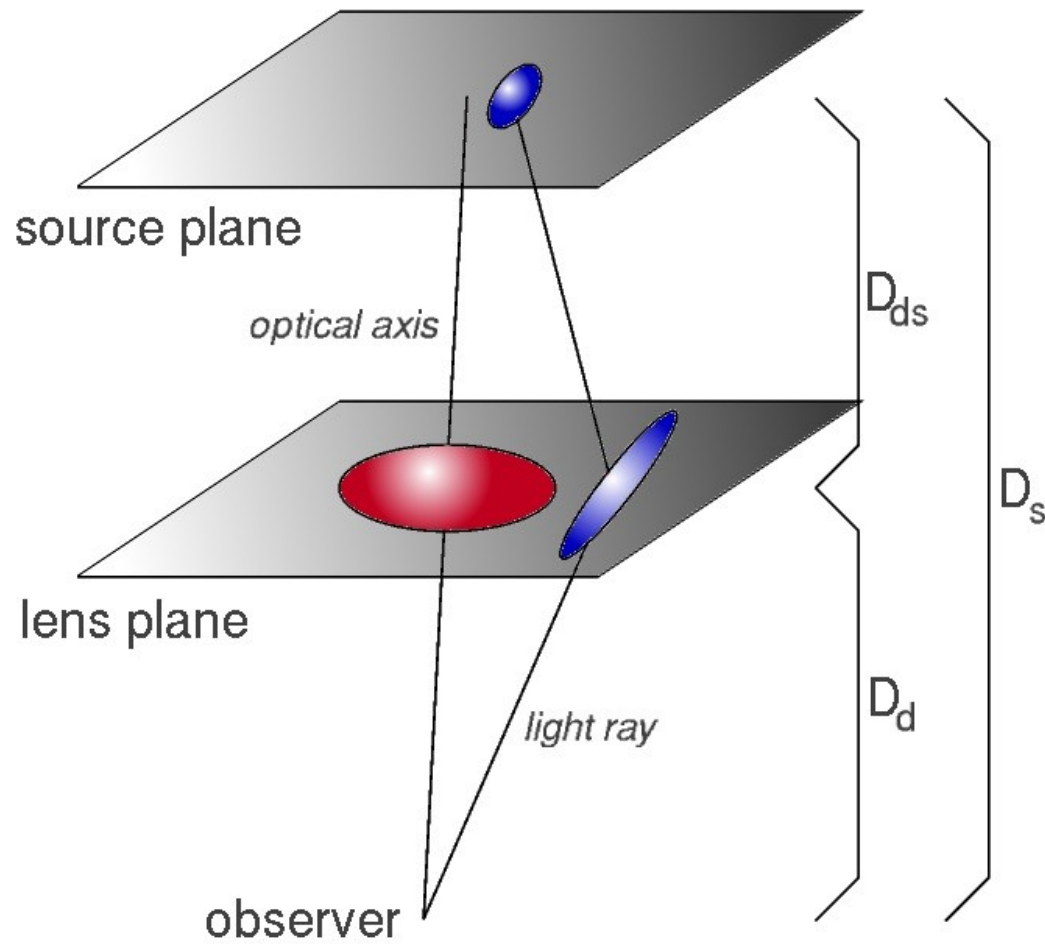


(Komatsu et al. 2008)



$$n = 1 - \frac{2\Phi}{c^2} > 1$$







Fermat's principle

$$0 = \delta\tau = \delta \left[ \int_a^b n(\vec{x}) \frac{|\mathrm{d}\vec{x}|}{c} \right]$$

Deflection angle, lensing potential

$$\vec{\alpha} = \vec{\nabla}\psi, \quad \psi = \frac{2}{c^2} \frac{D_{ds}}{D_d D_s} \int \Phi \, \mathrm{d}l$$

Lens equation

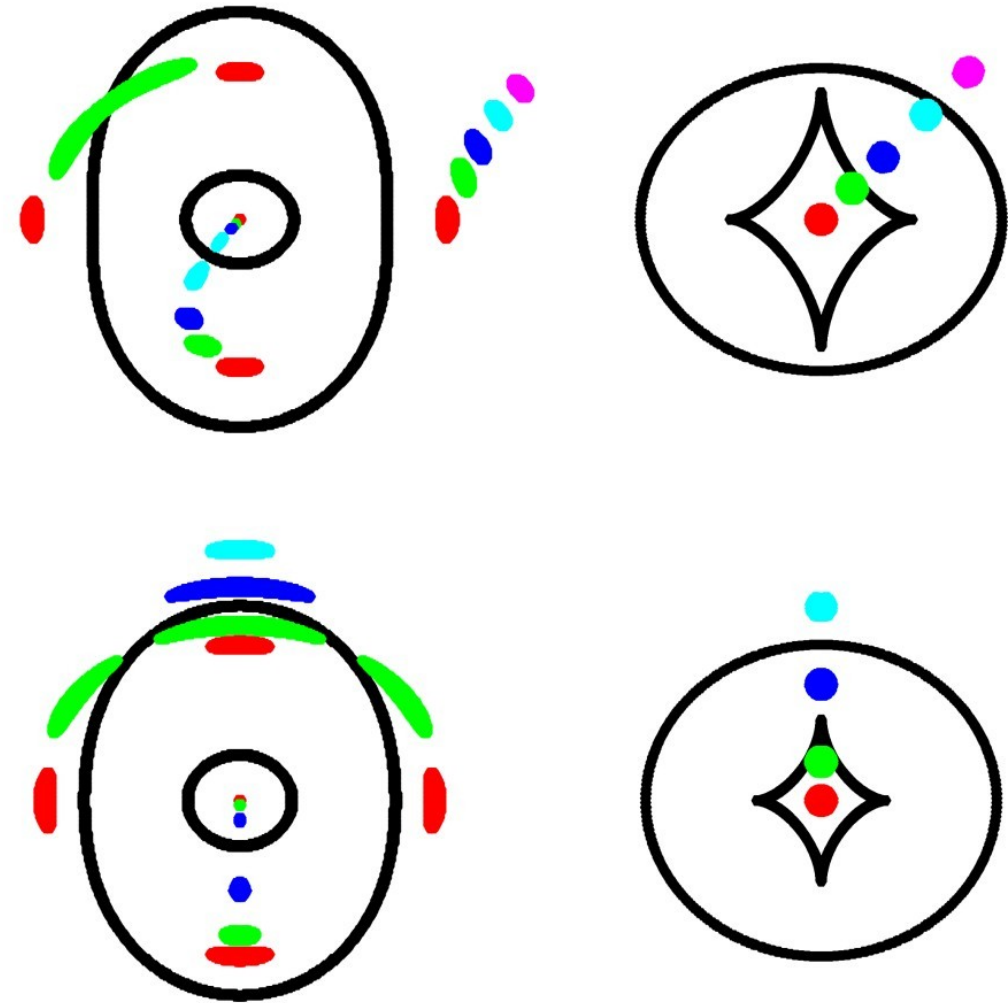
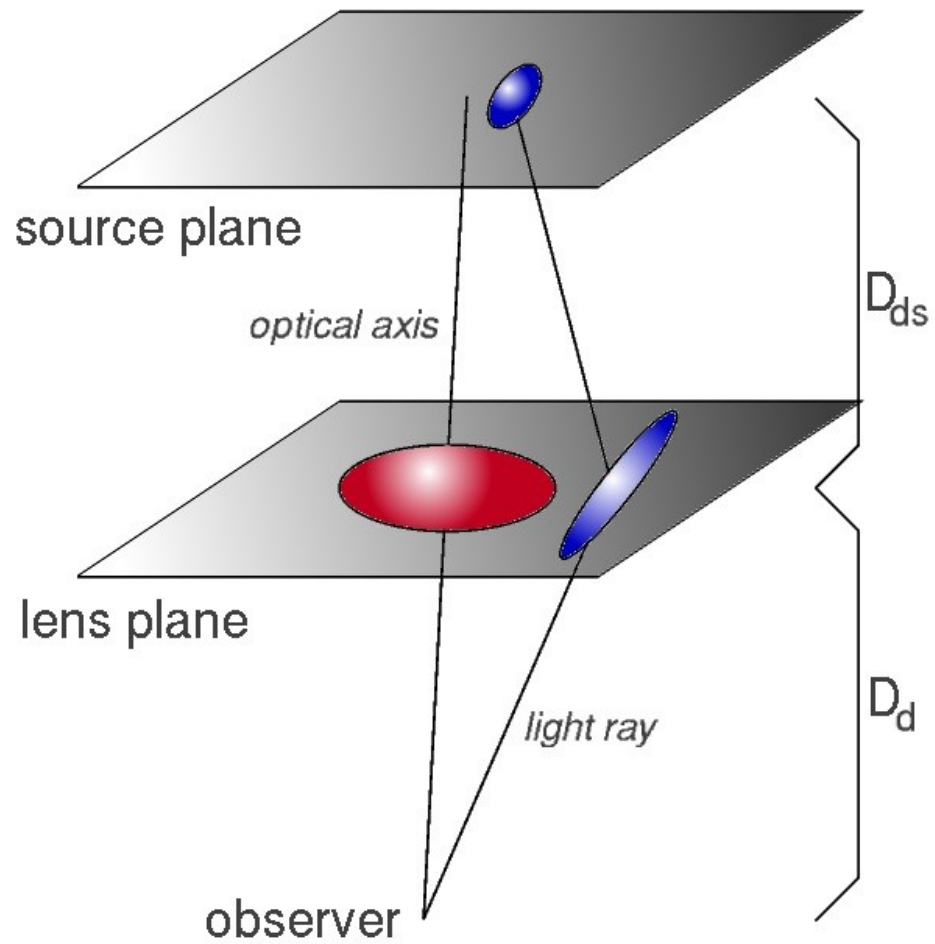
$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\mathcal{A} = \left( \frac{\partial \beta_i}{\partial \theta_j} \right) = \left( \delta_{ij} - \frac{\partial^2 \psi}{\partial \theta_i \partial \theta_j} \right)$$

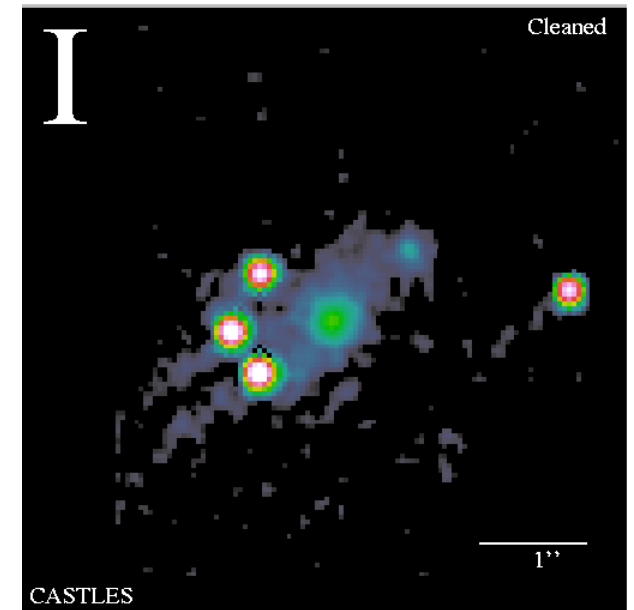
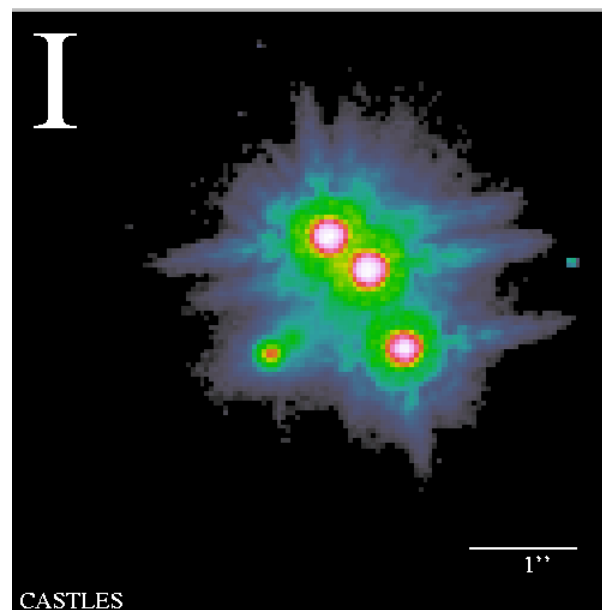
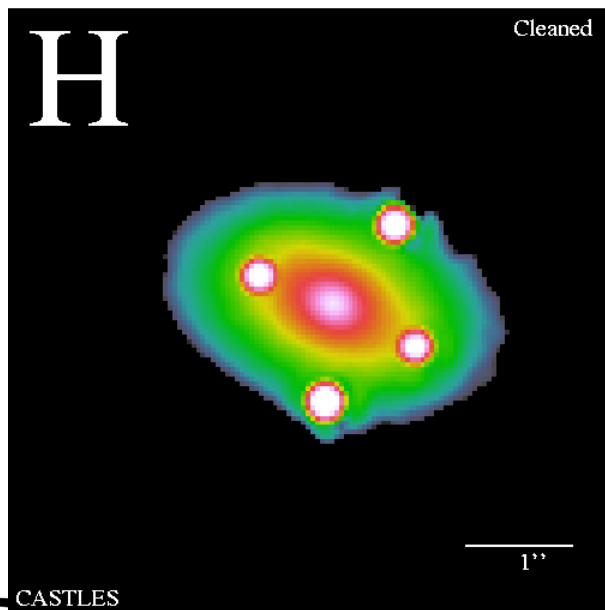
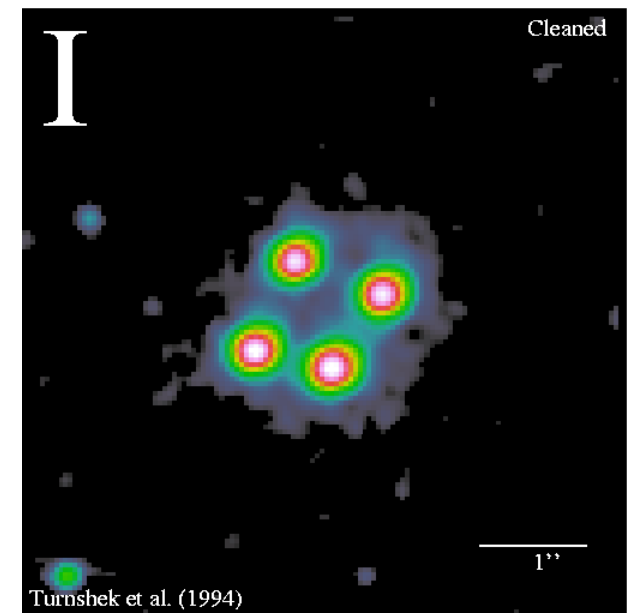
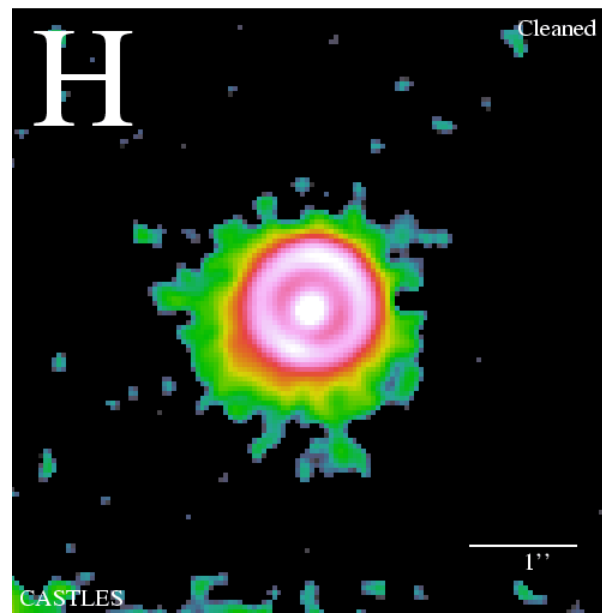
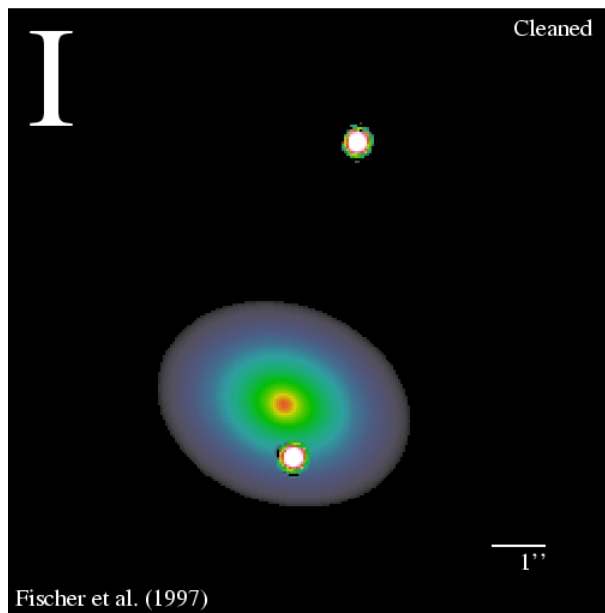
Convergence and shear

$$\partial := \partial_1 + \mathrm{i}\partial_2$$

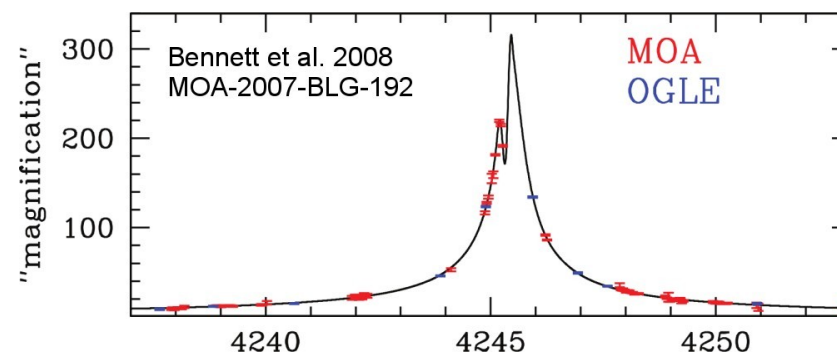
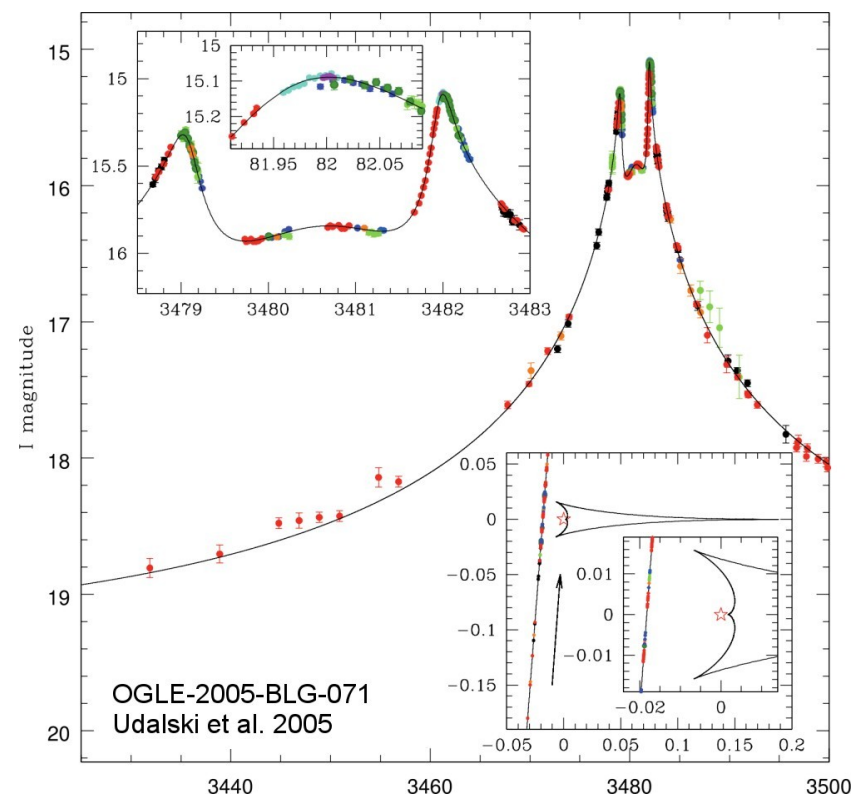
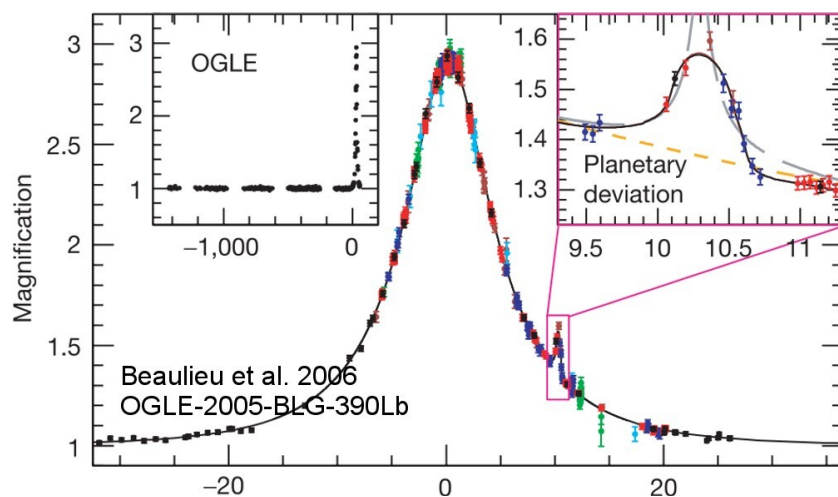
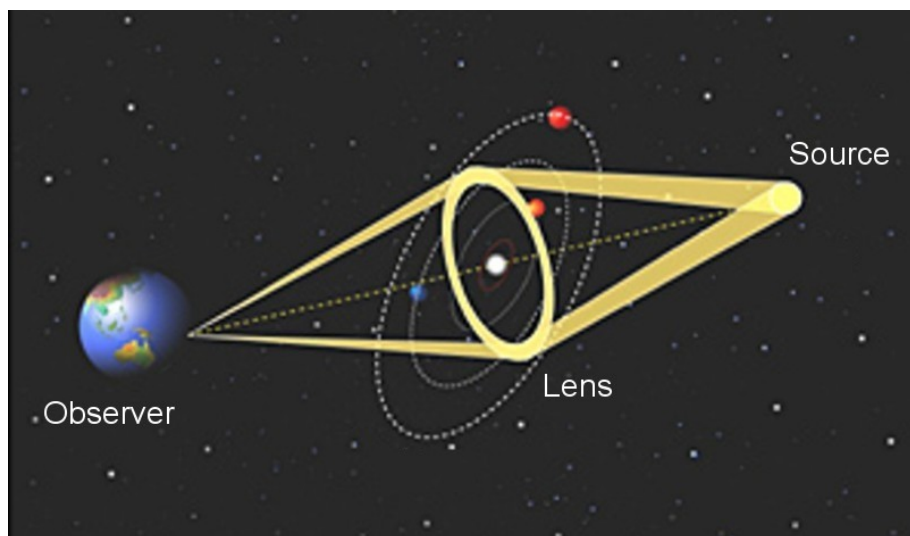
$$\kappa = \frac{1}{2} \partial^\dagger \partial \psi, \quad \gamma = \frac{1}{2} \partial^2 \psi$$

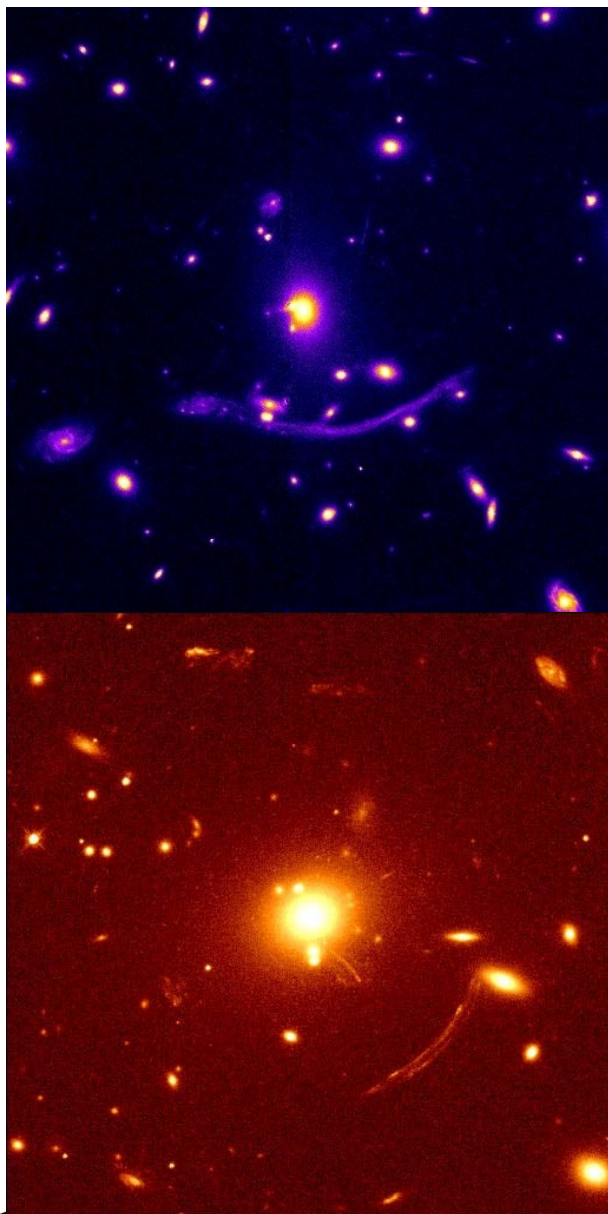






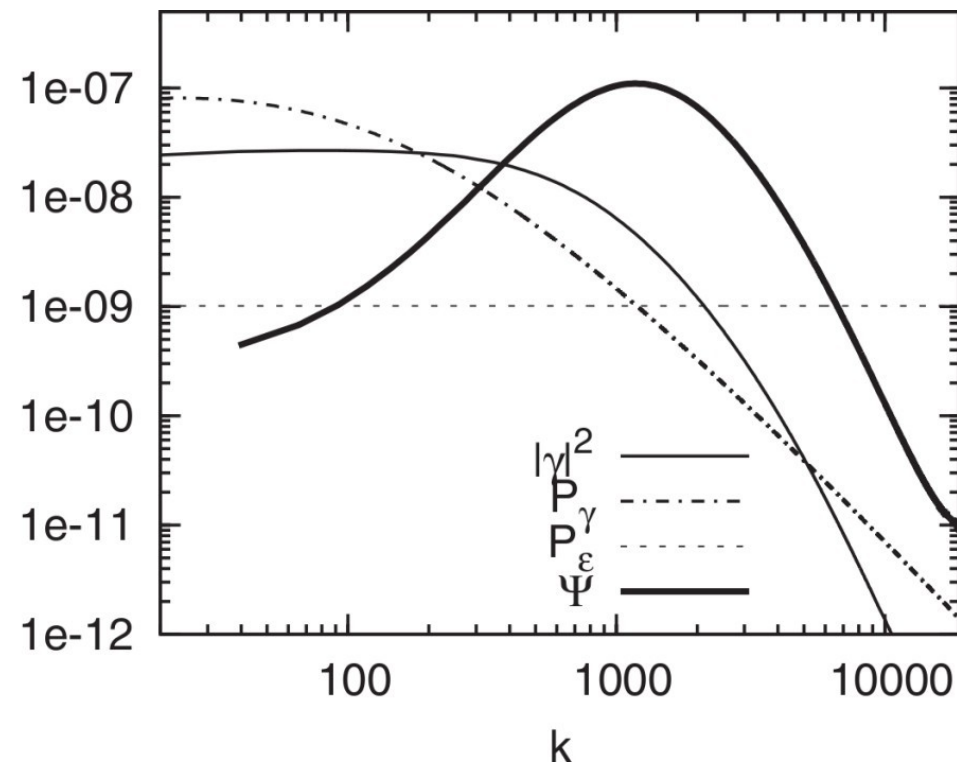
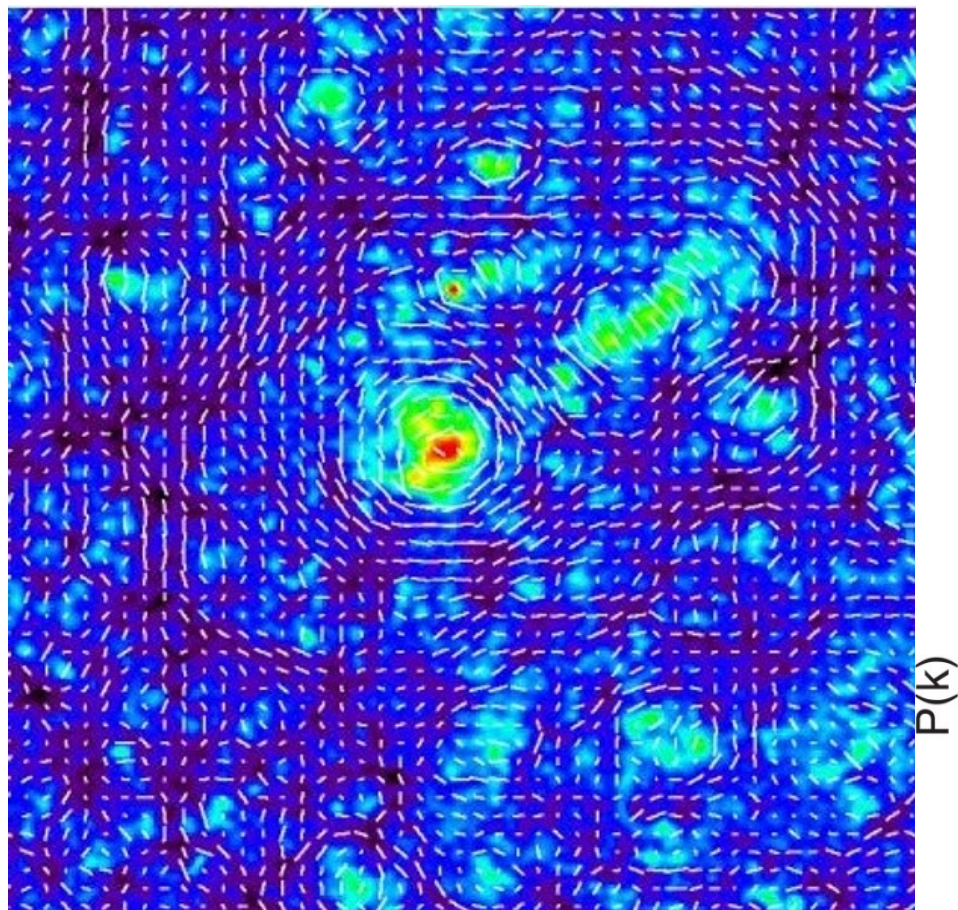
(Castles Collaboration)







- How frequent are bound structures composed of dark matter? Do dark haloes exist? Are they connected by filaments?
- How are dark-matter haloes structured and composed? What density profiles do they have, and how substructured are they?
- How do structures grow in the universe?  
What does this imply for dark energy?

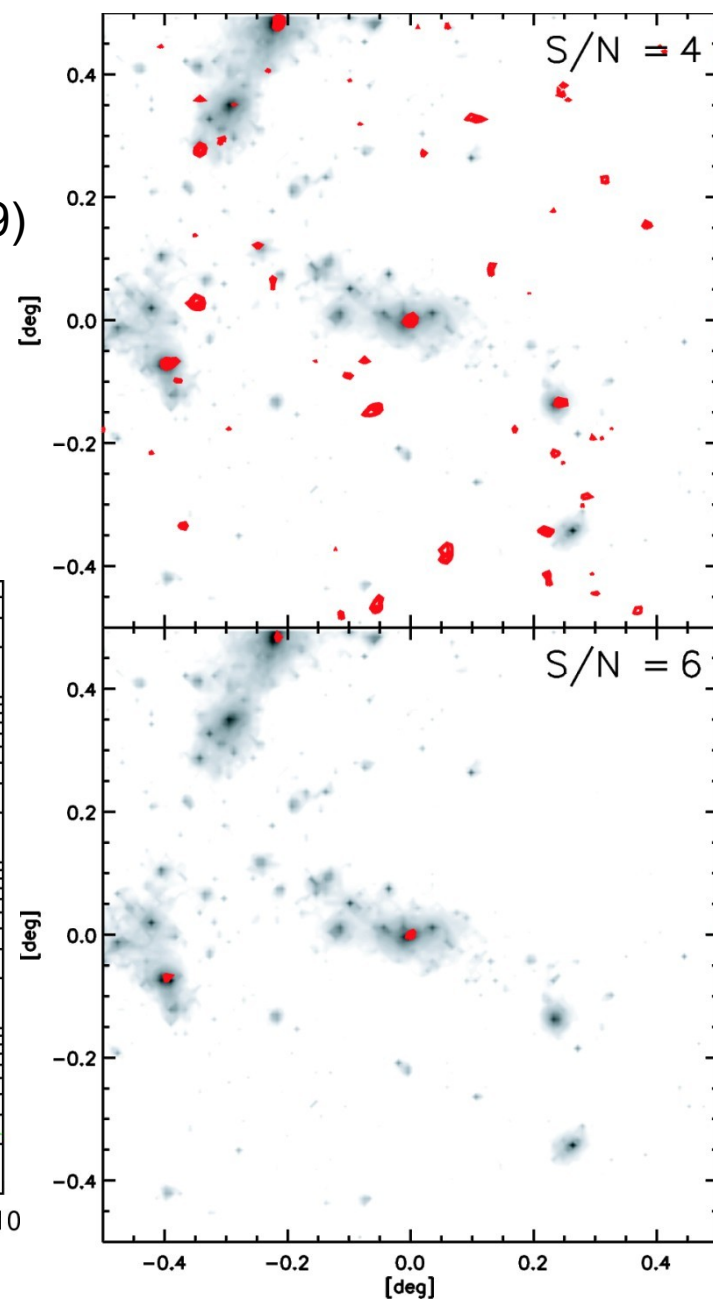
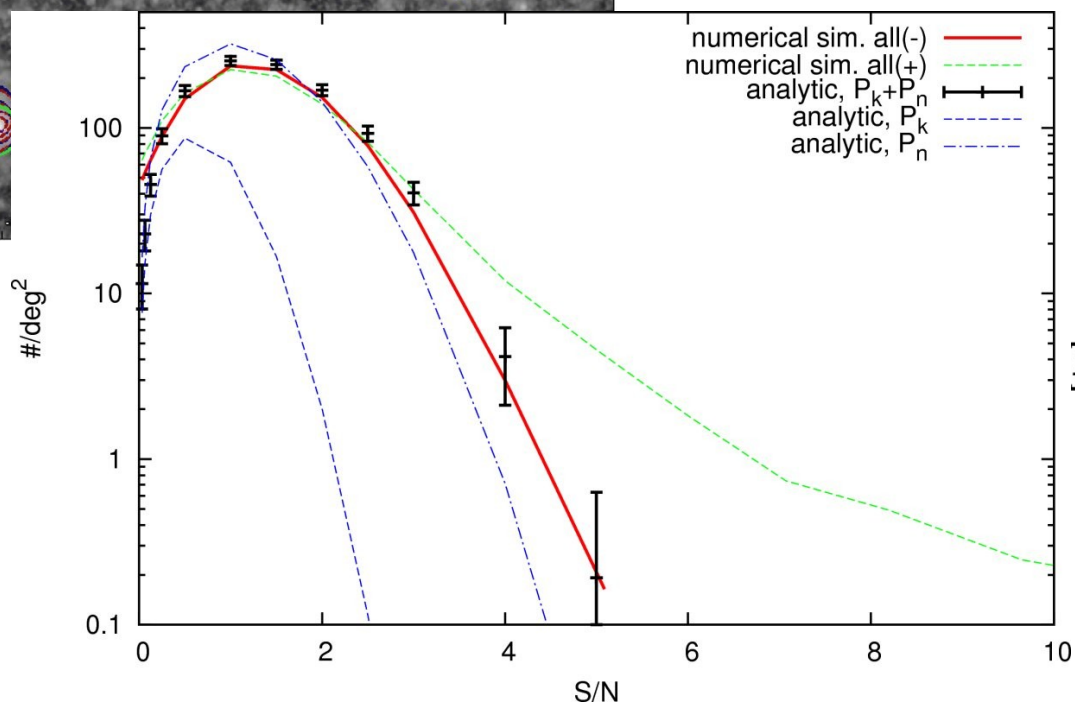
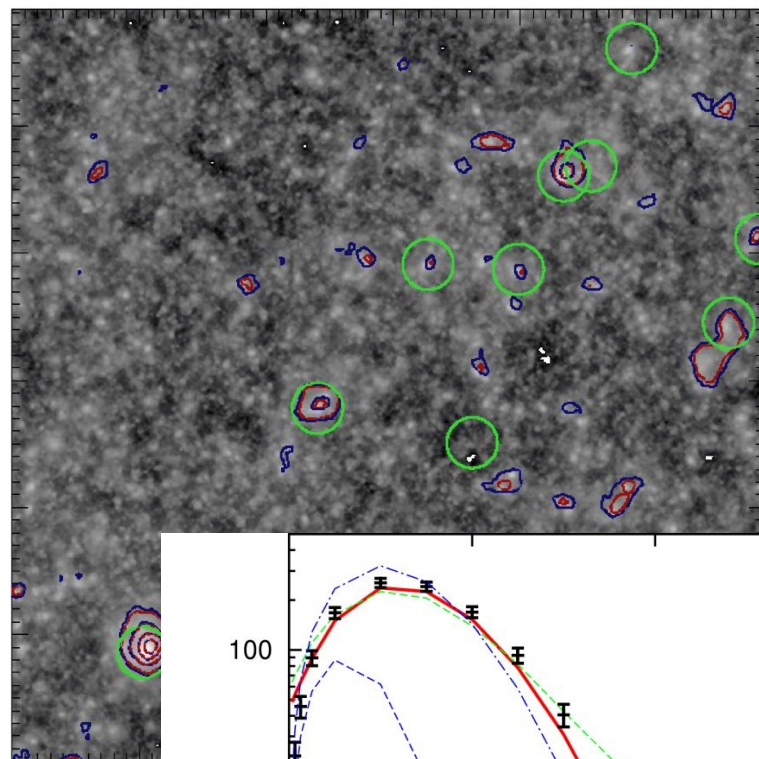


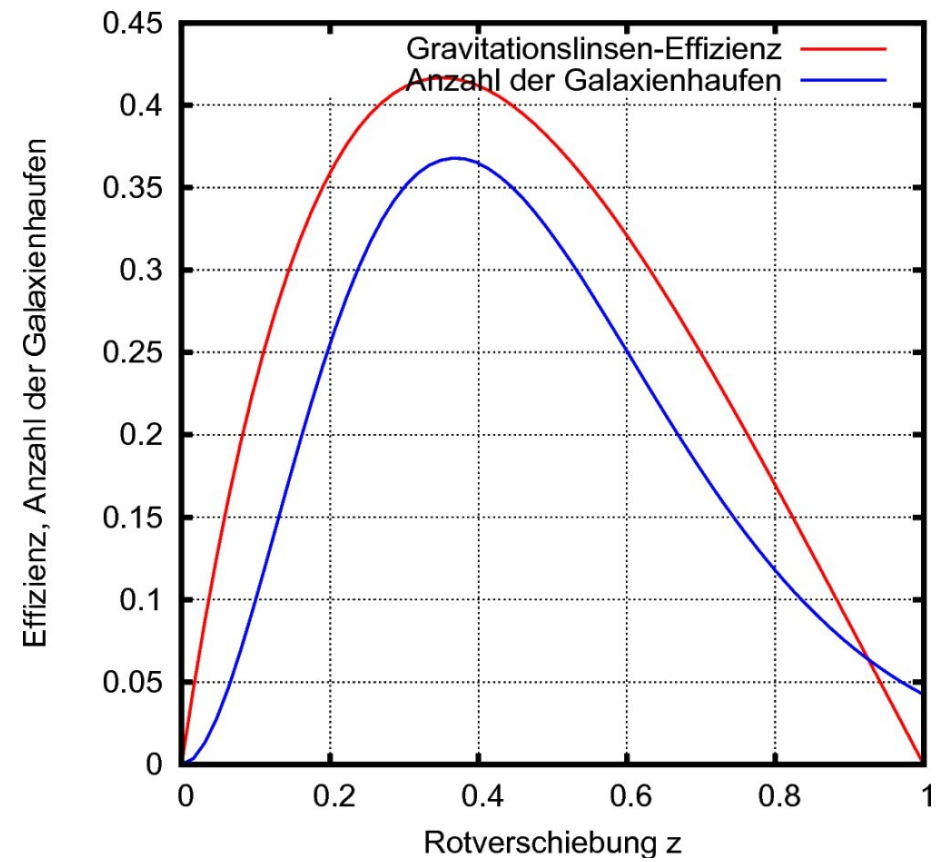
(Maturi et al. 2005)

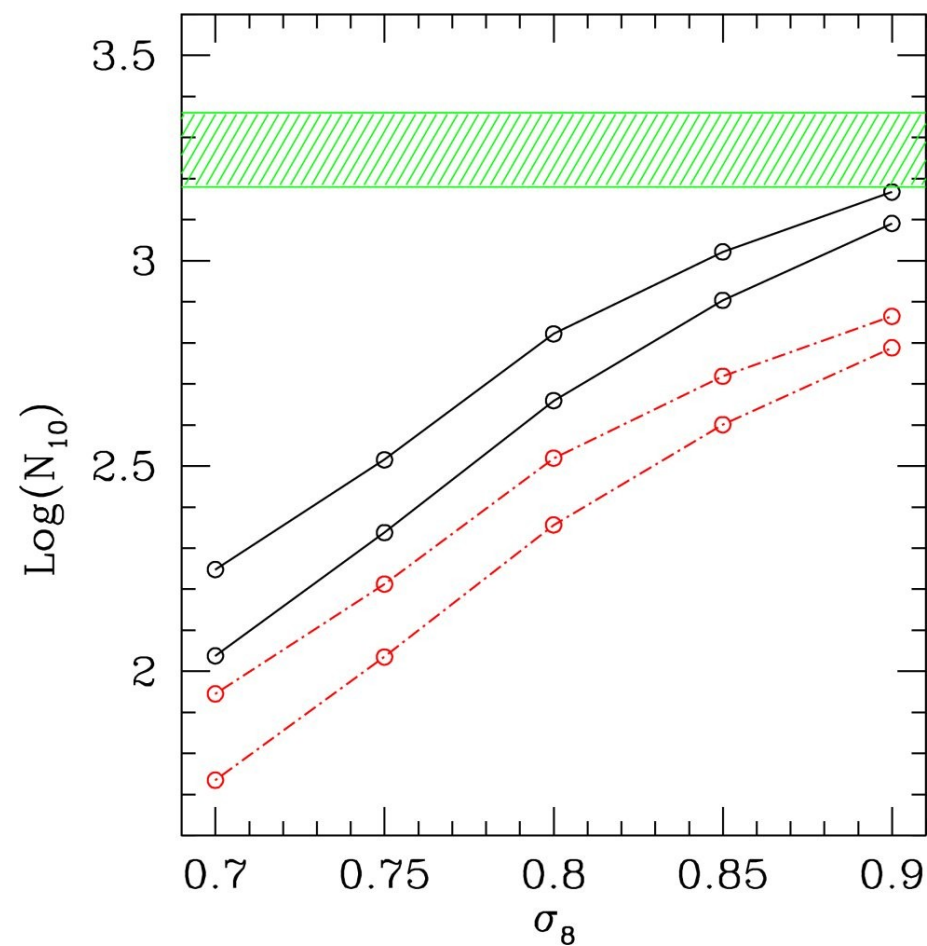




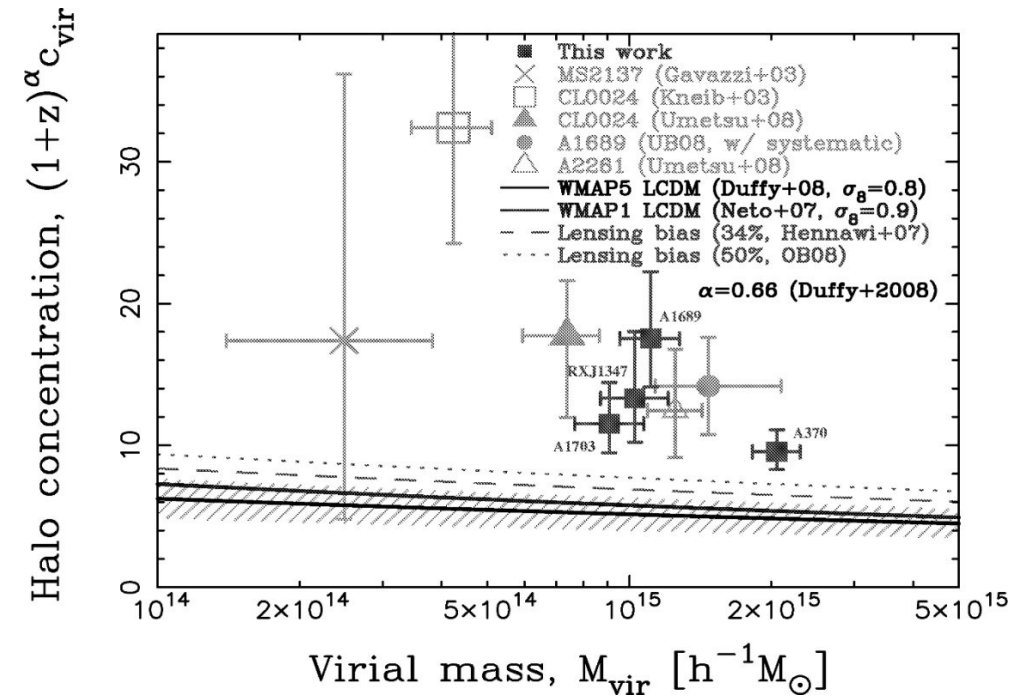
(Maturi et al. 2005  
Pace et al. 2007,  
Angrick et al. 2009)



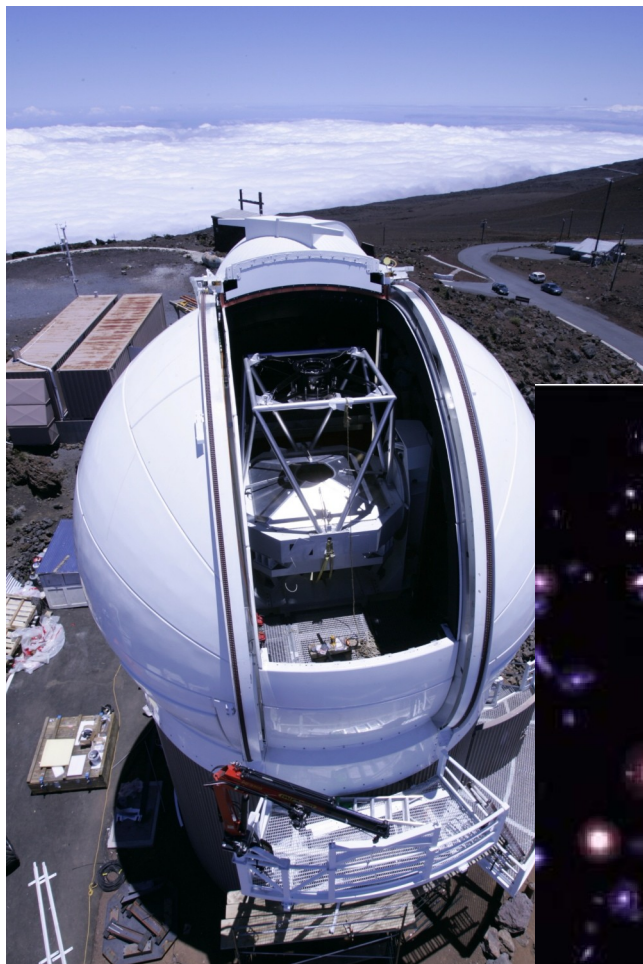




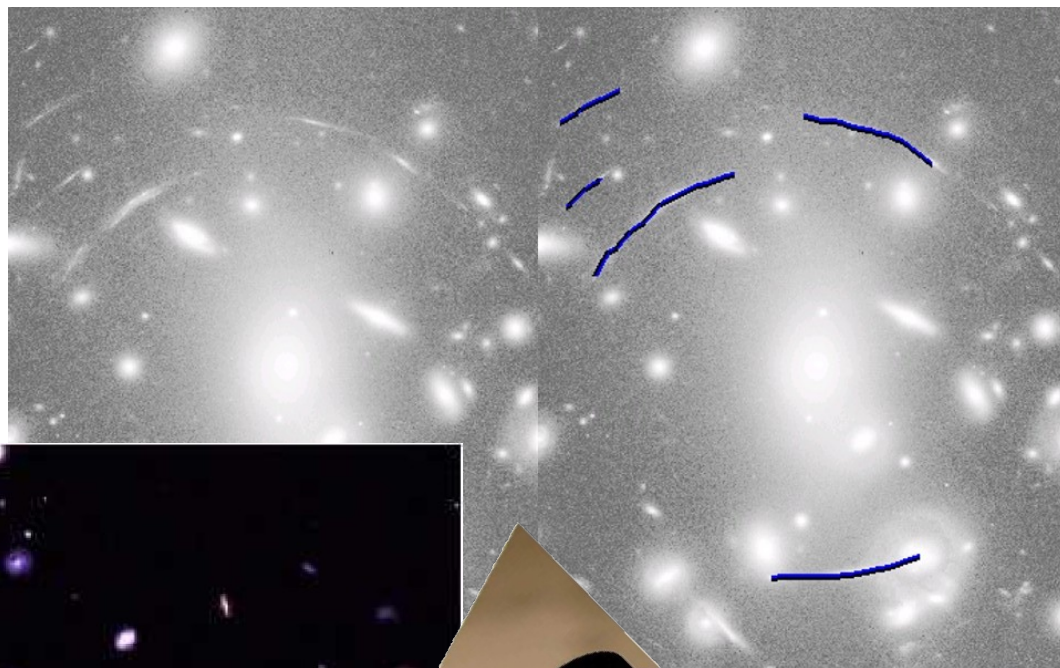
(Fedeli et al. 2006,  
Fedeli et al. 2008)



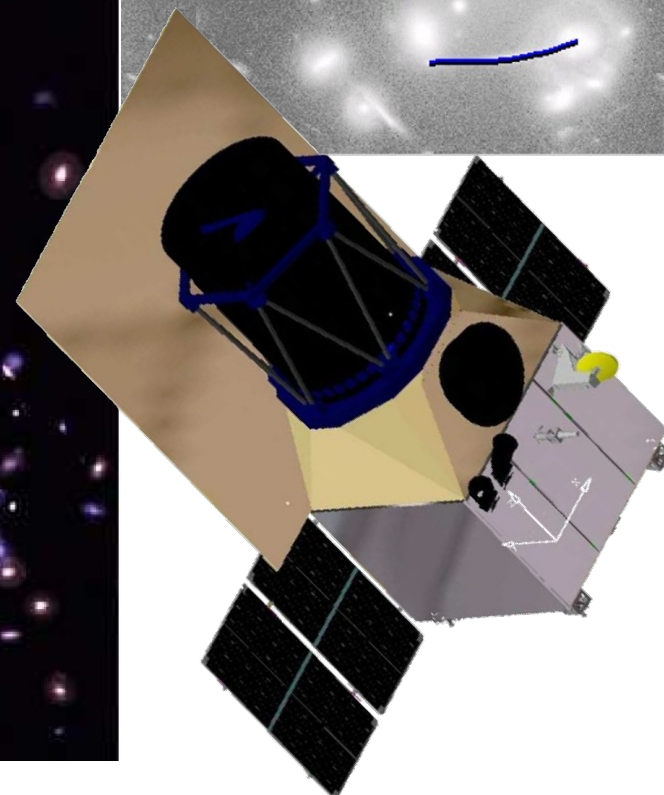
(Broadhurst et al. 2010)

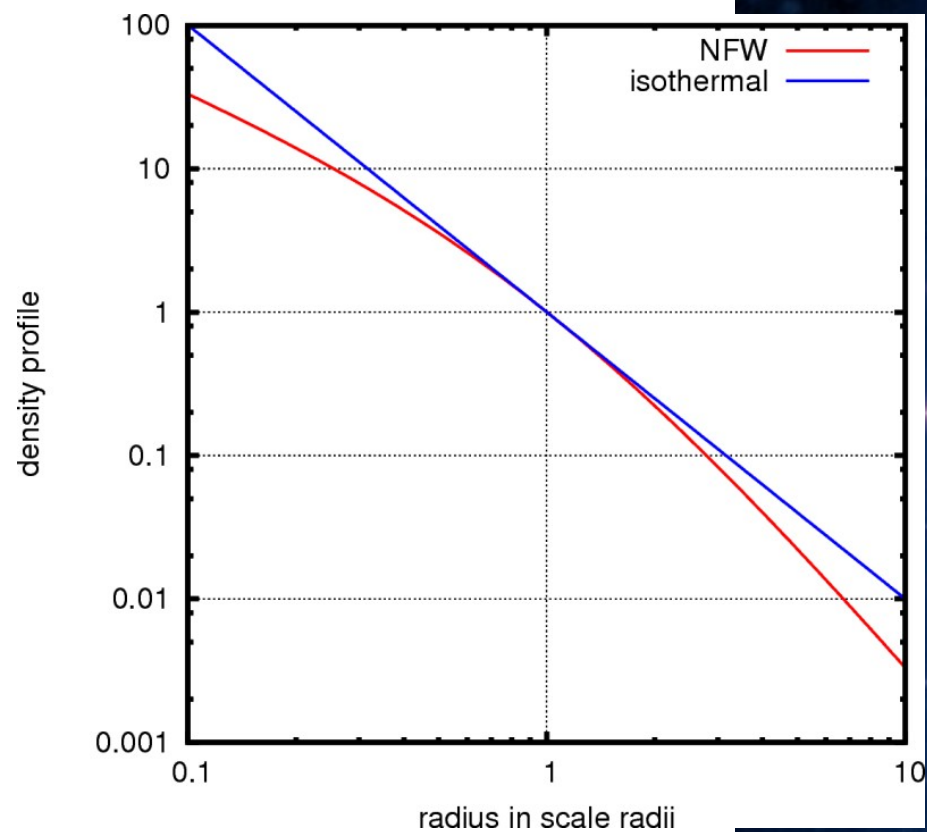


(Seidel  
et al.  
2007)



(Meneghetti  
et al. 2008)

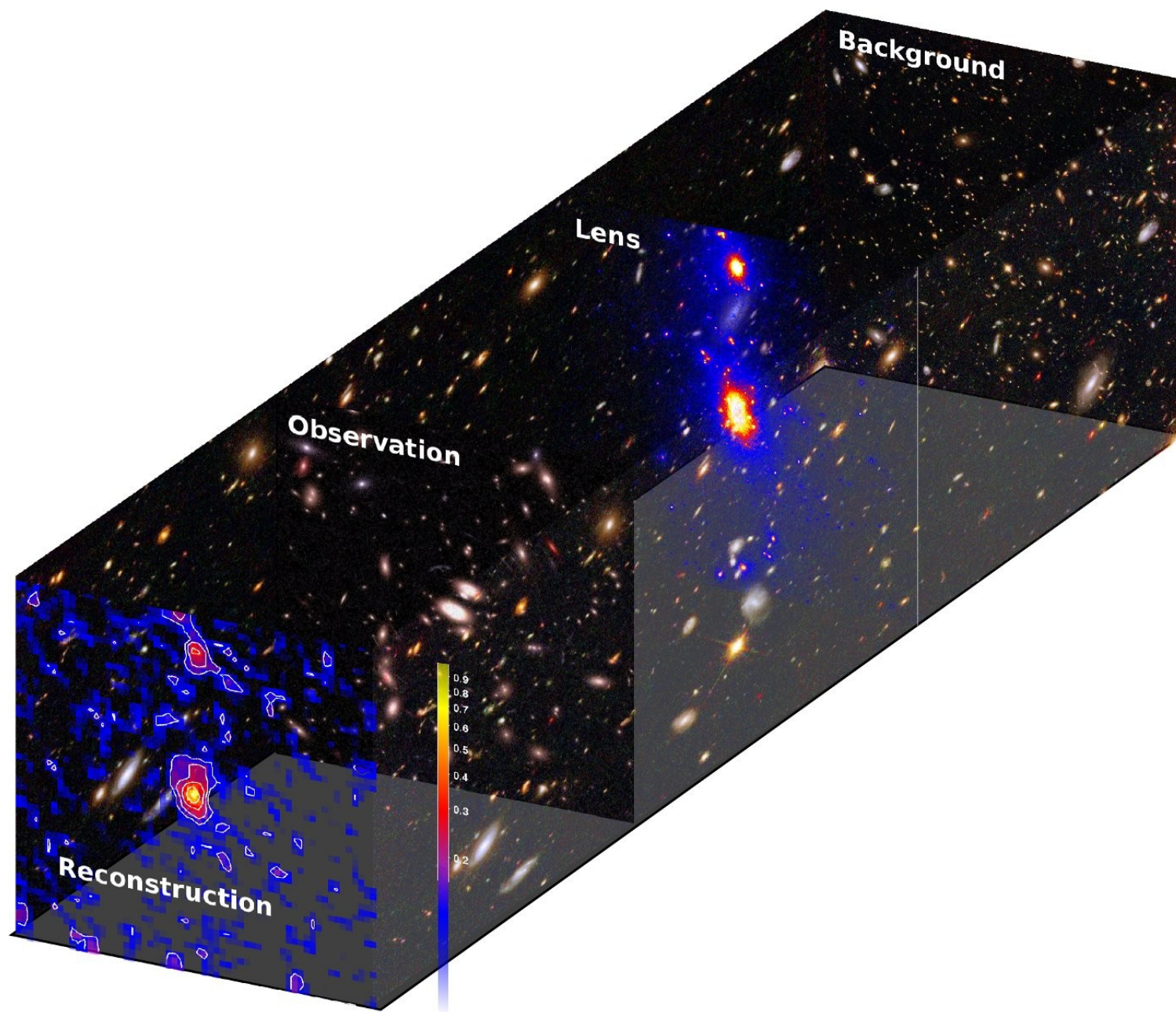




(V. Springel, Virgo Consortium)

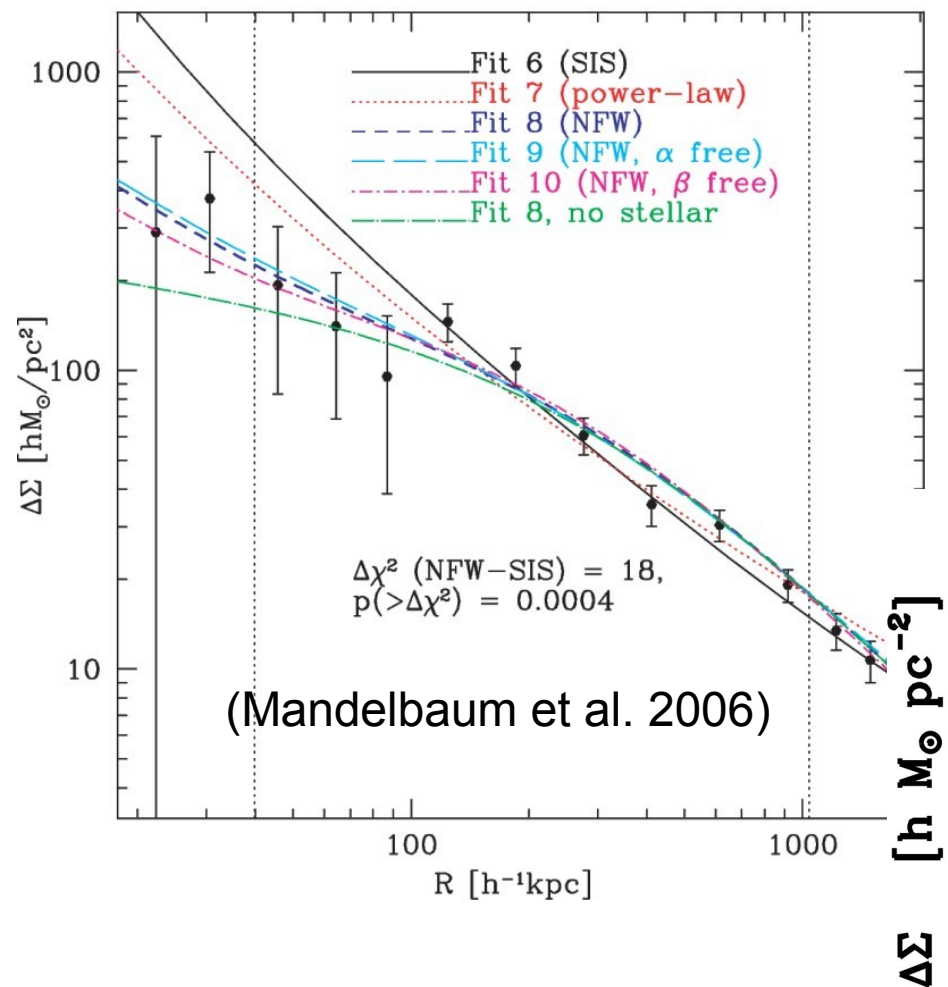


(Merten 2010)

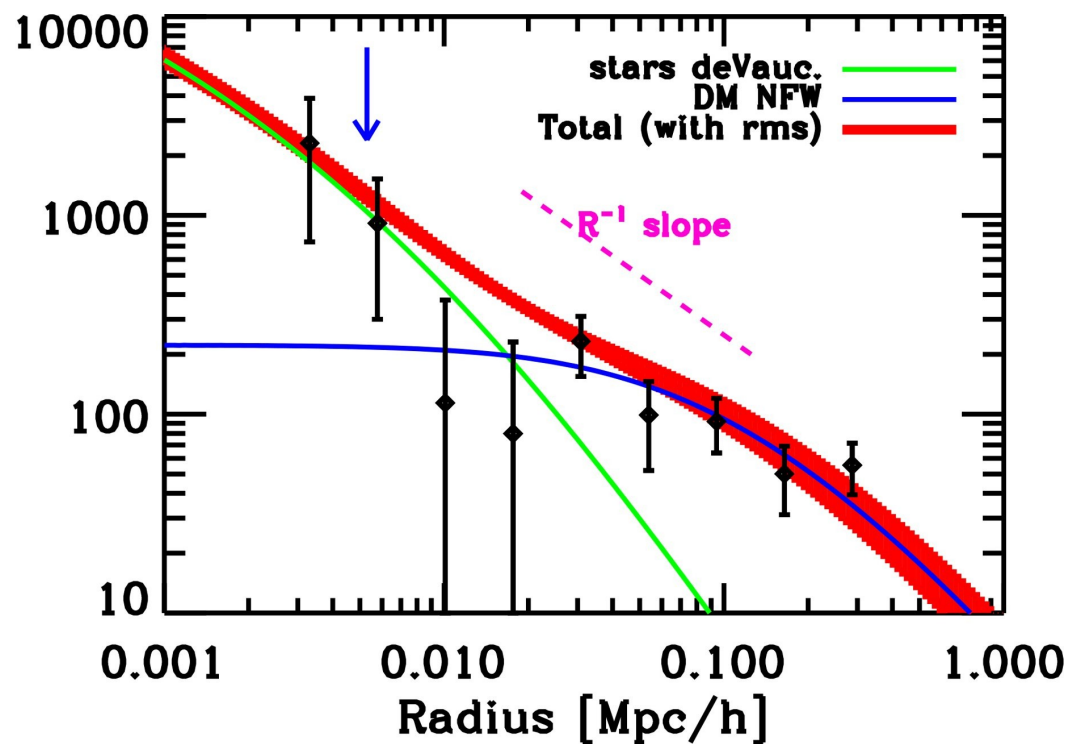




Lensing signal for bright LRG sample

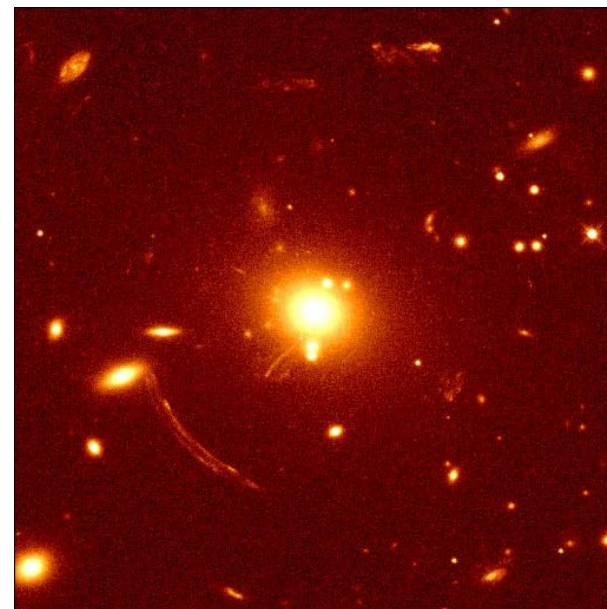
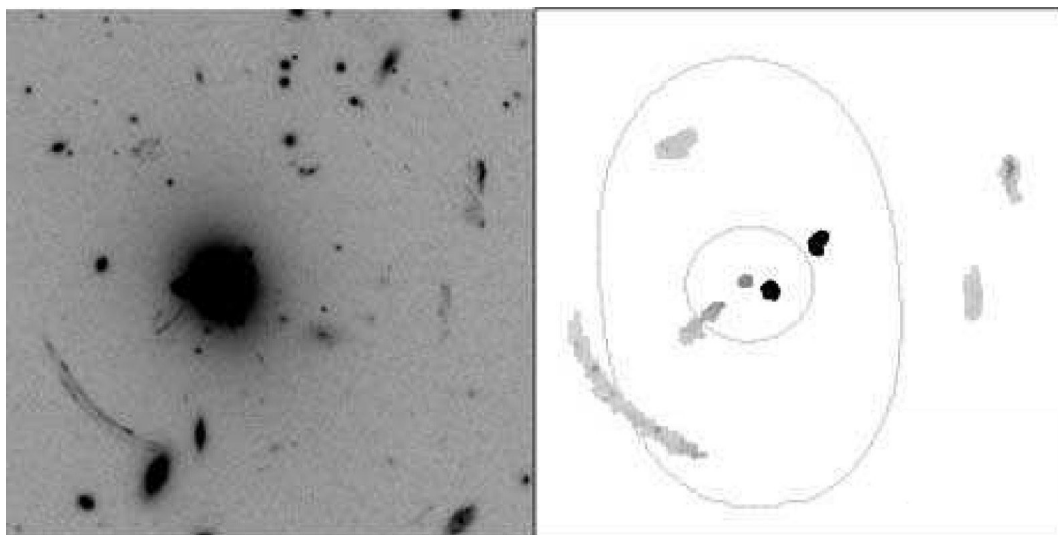
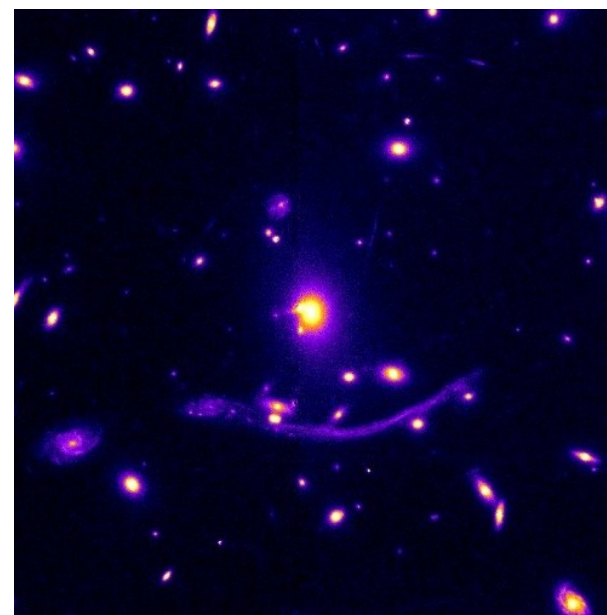
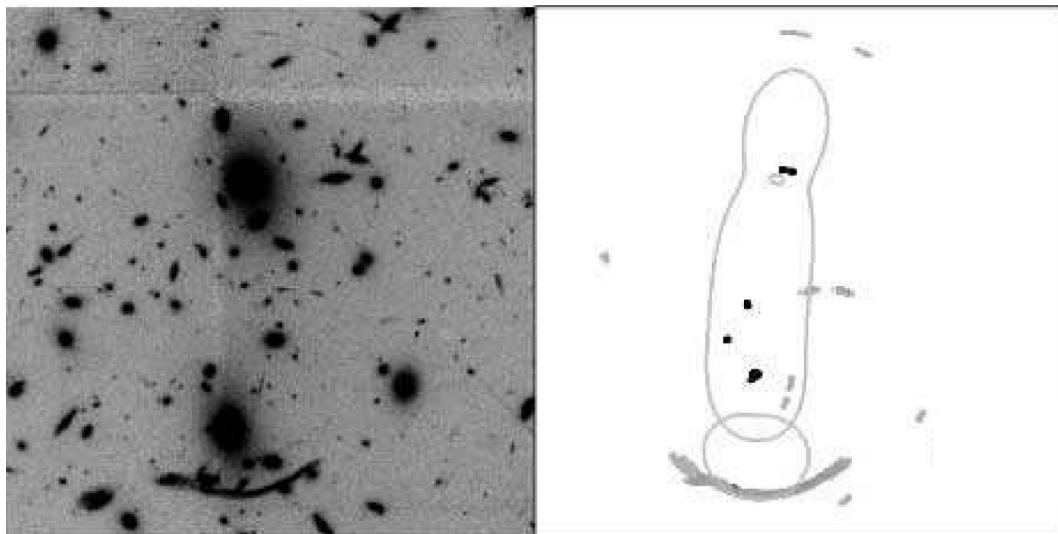


(Gavazzi et al. 2007)

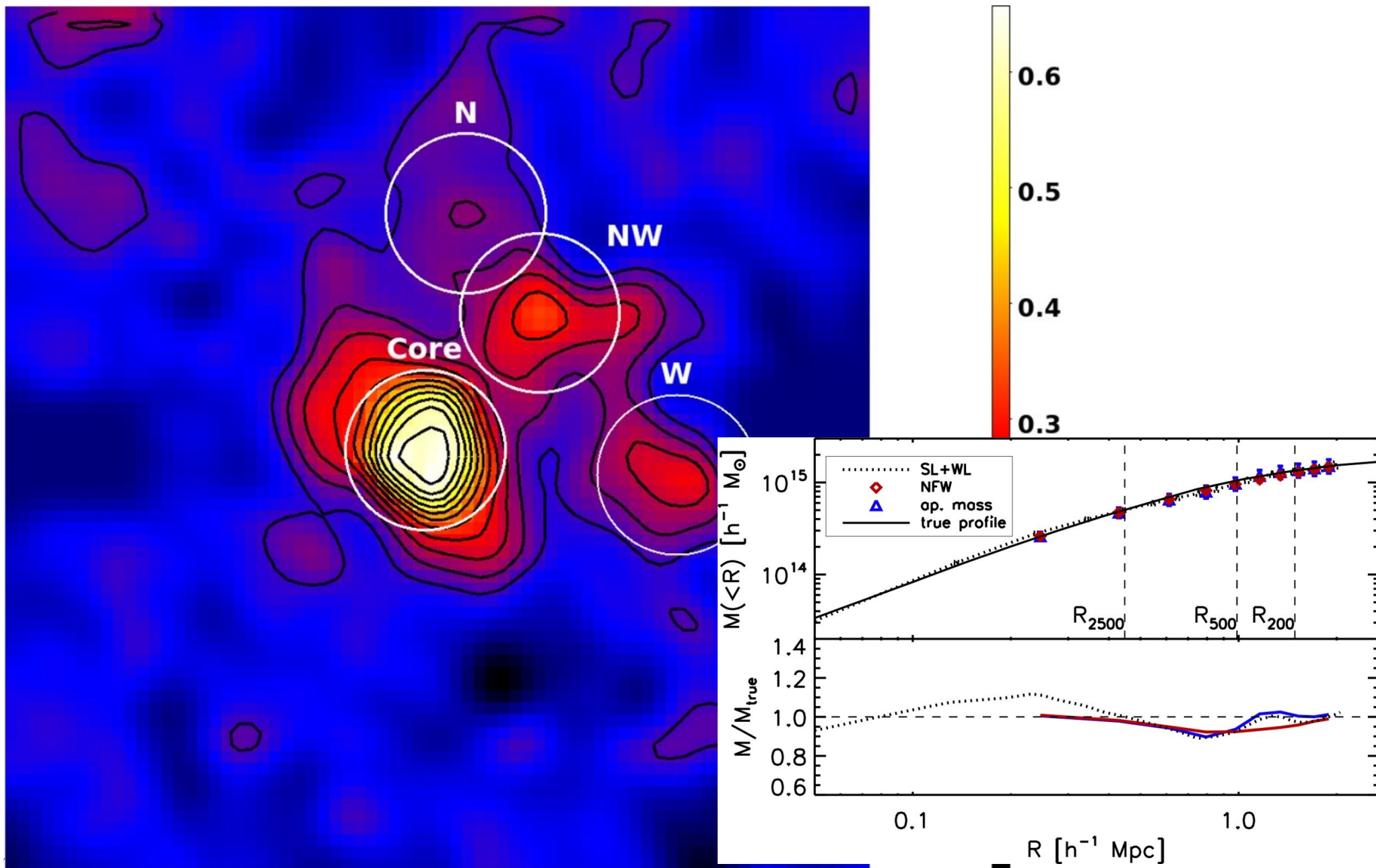




# Structure of dark-matter haloes

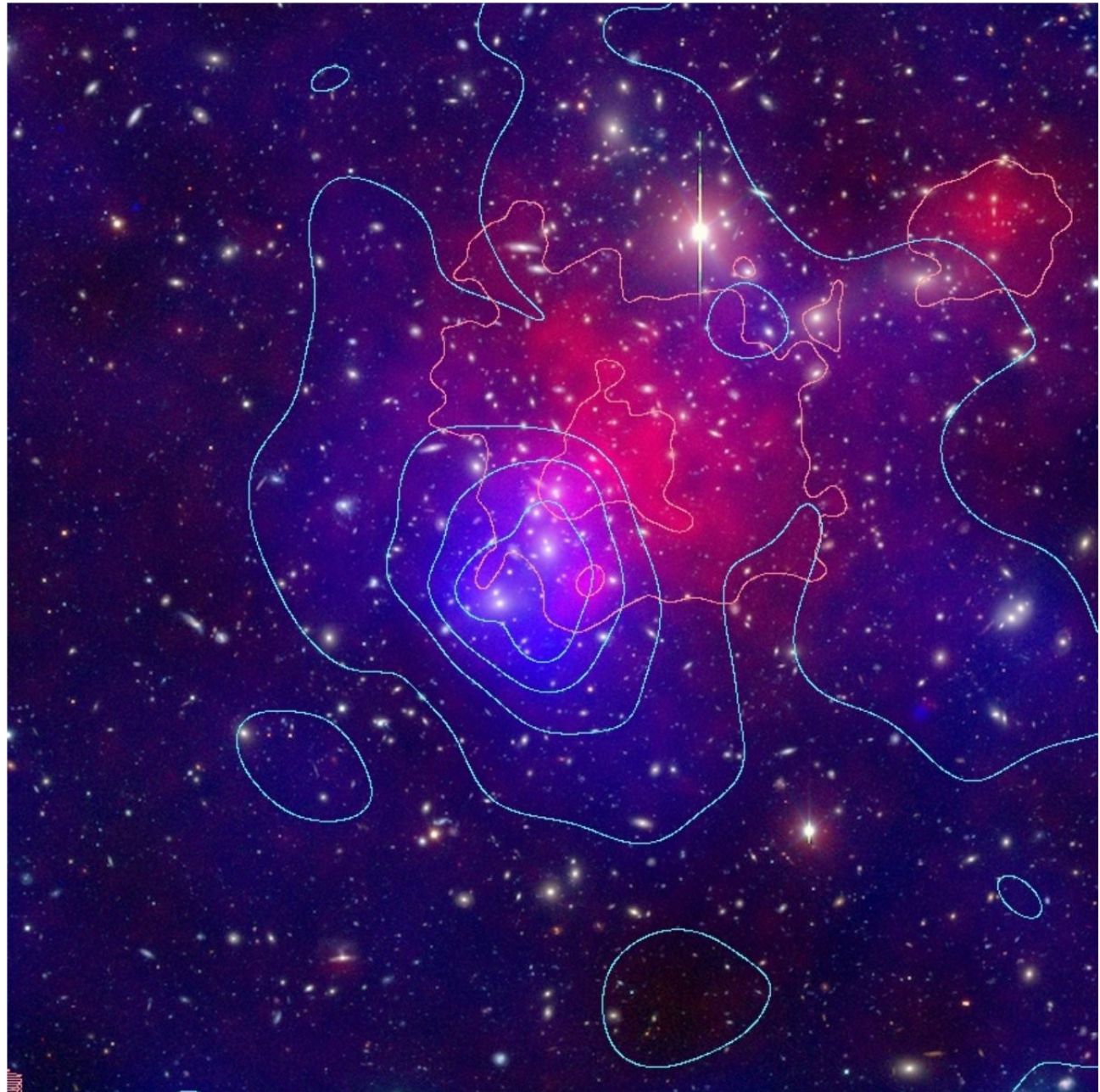


(Comerford et al. 2005)



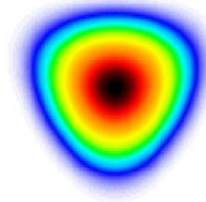
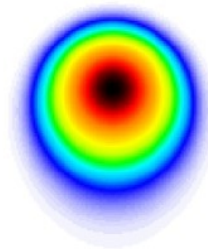
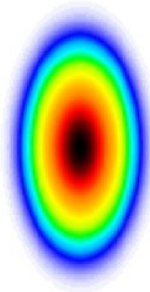
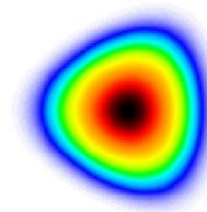
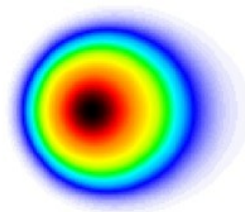
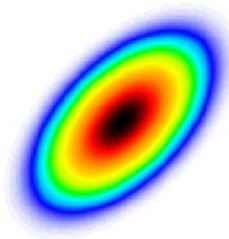


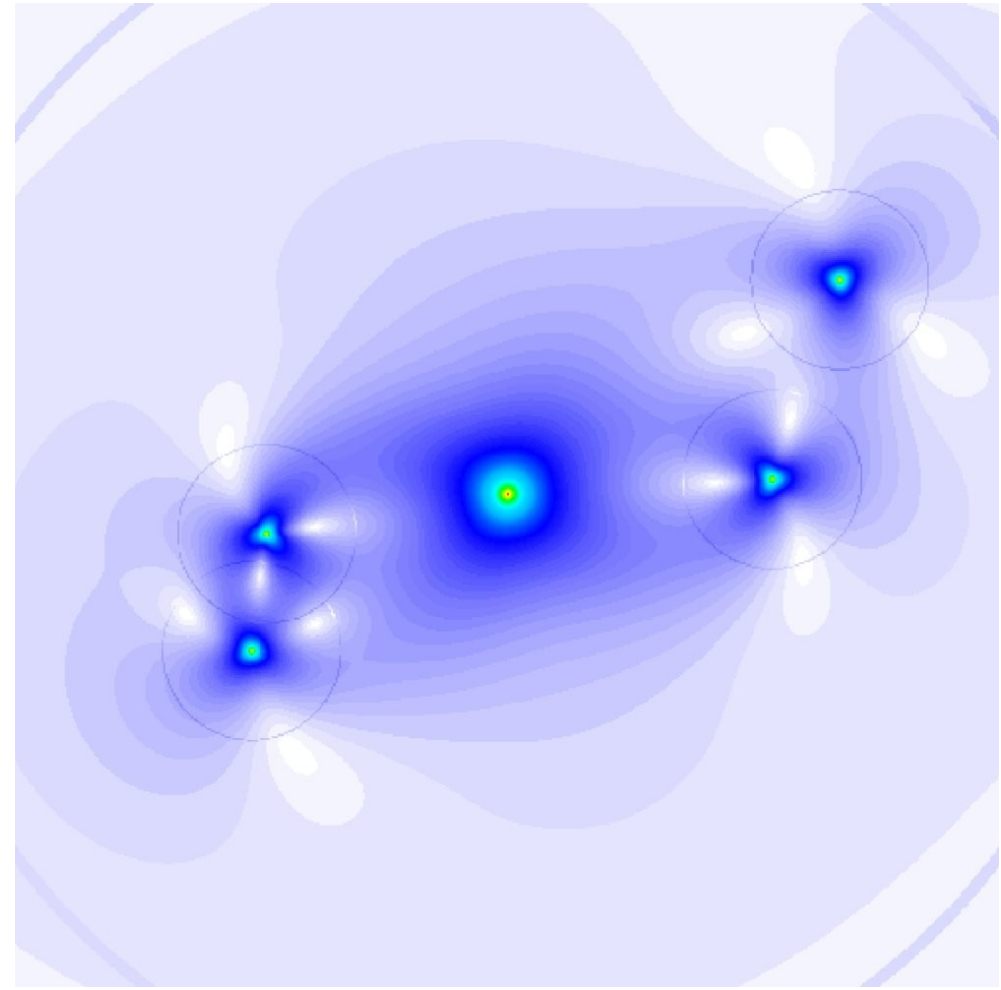
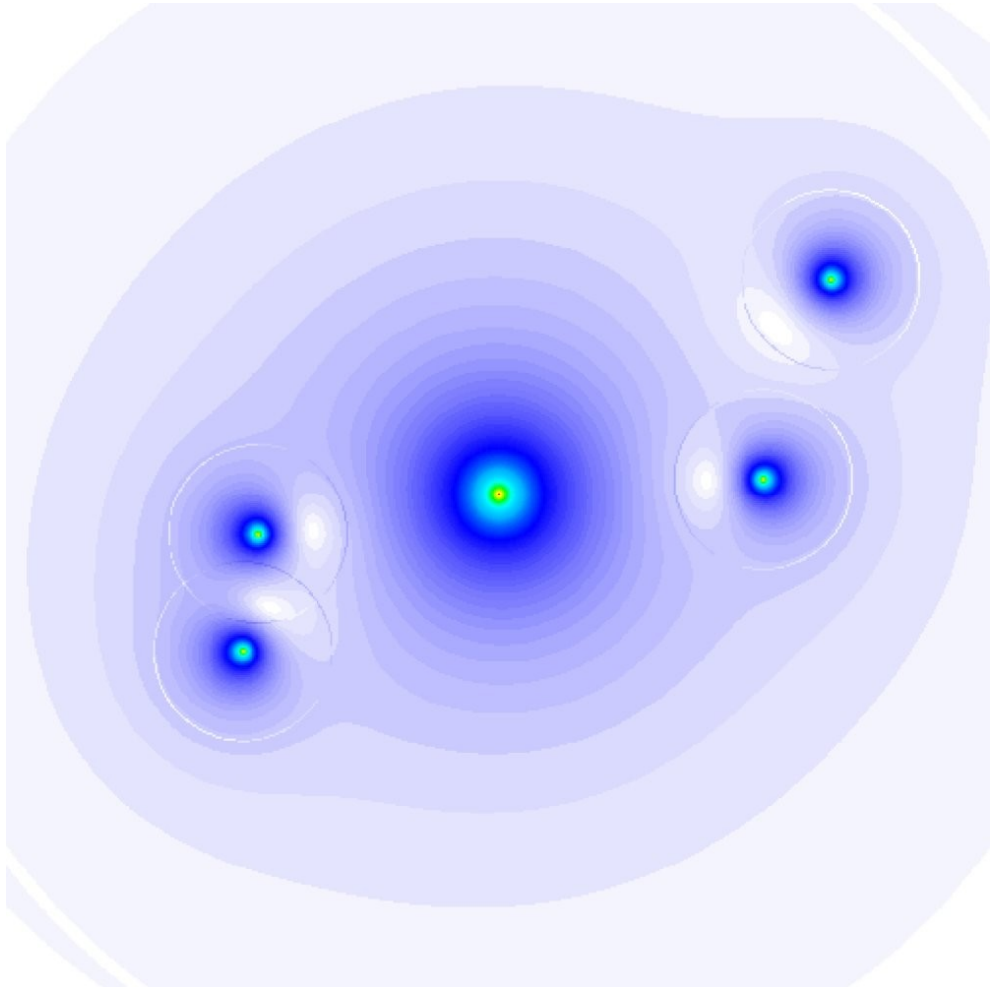
(Merten et al. 2011)





$$\kappa = \frac{1}{2} \partial^\dagger \partial \psi, \quad \gamma = \frac{1}{2} \partial^2 \psi \quad F = \frac{1}{2} \partial \partial^\dagger \partial \psi, \quad G = \frac{1}{2} \partial^3 \psi$$

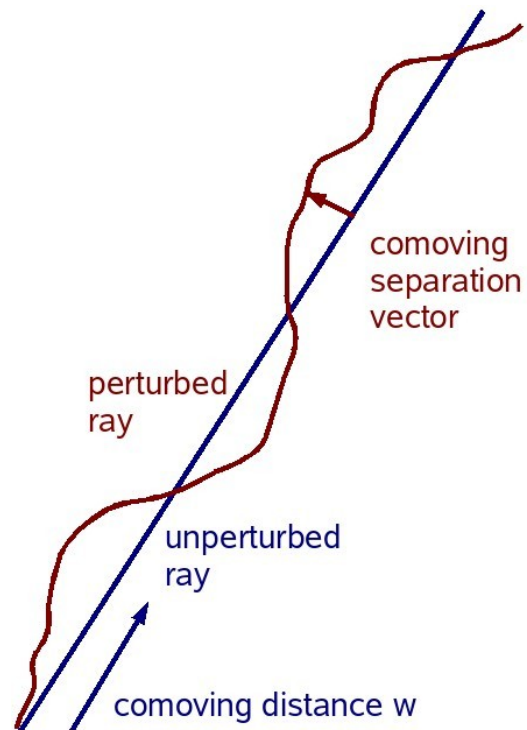
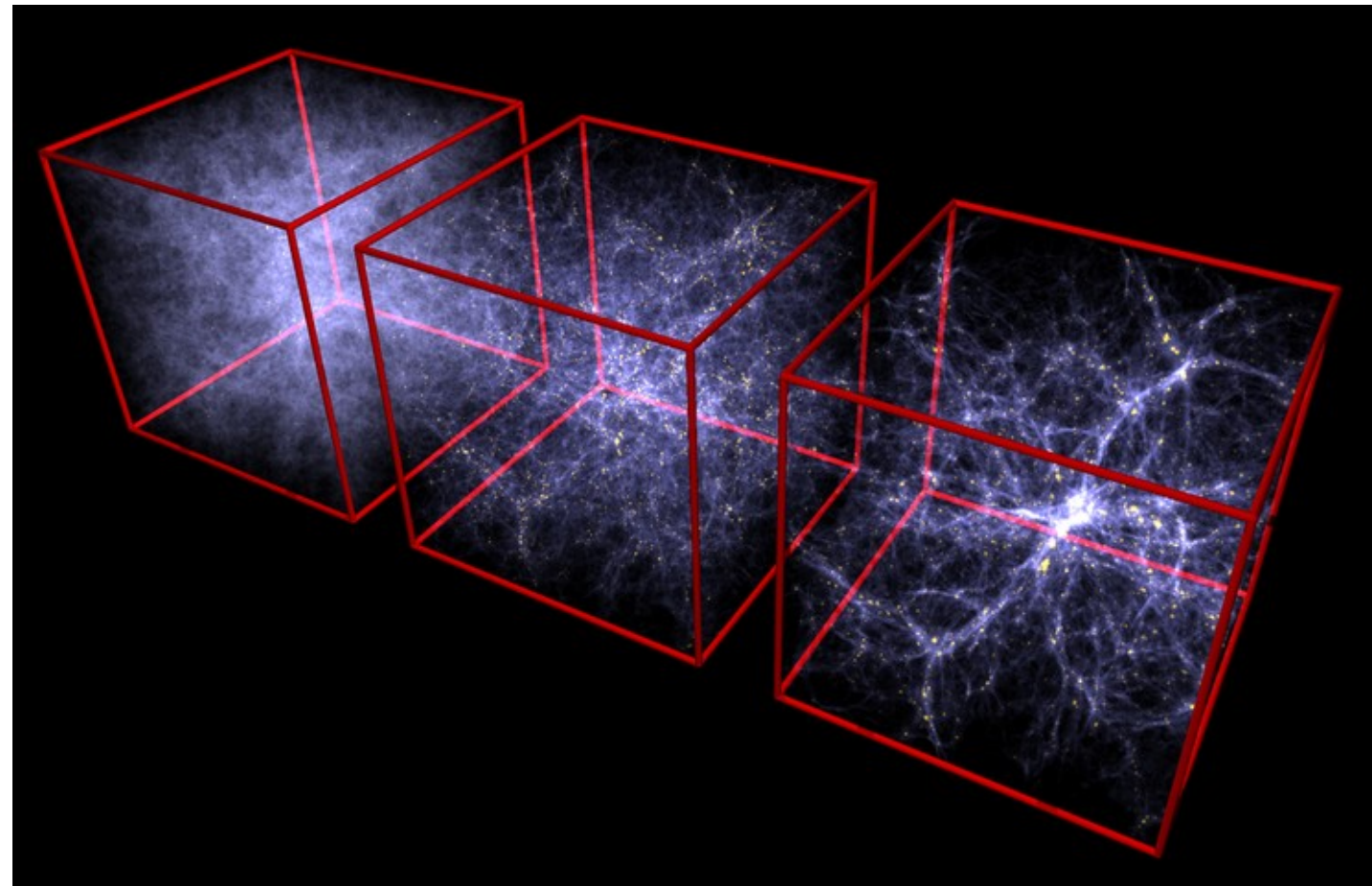




(Giocoli 2010)

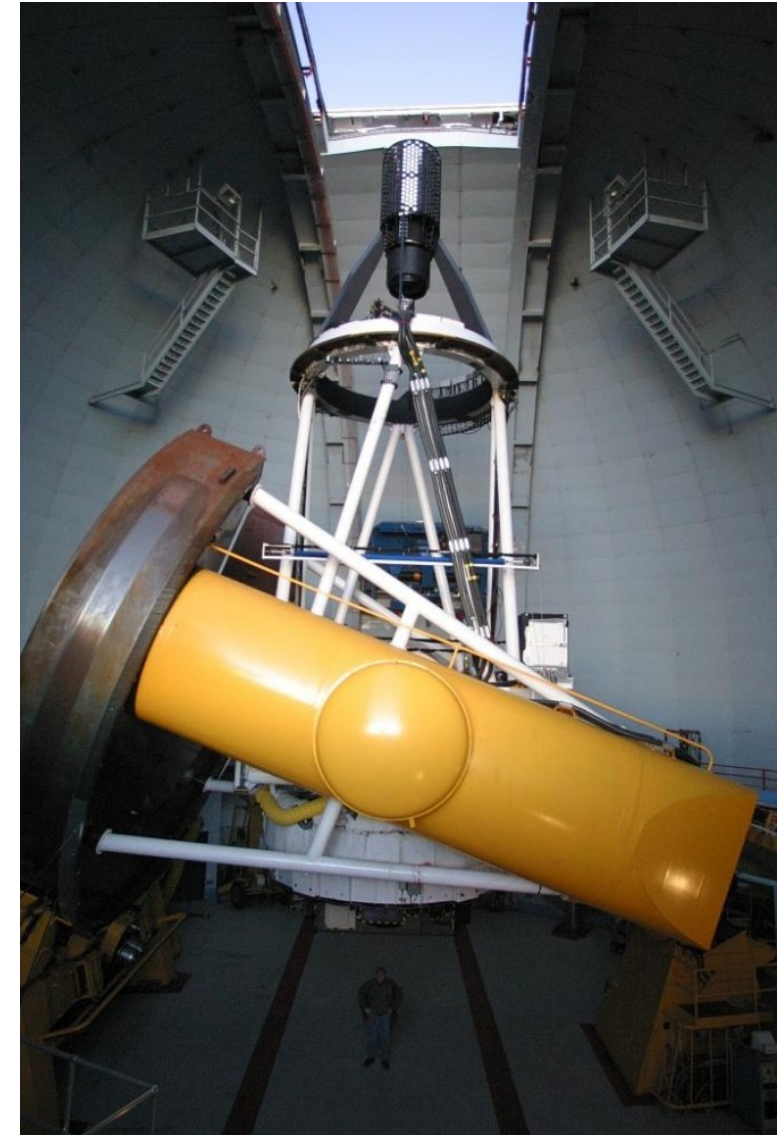
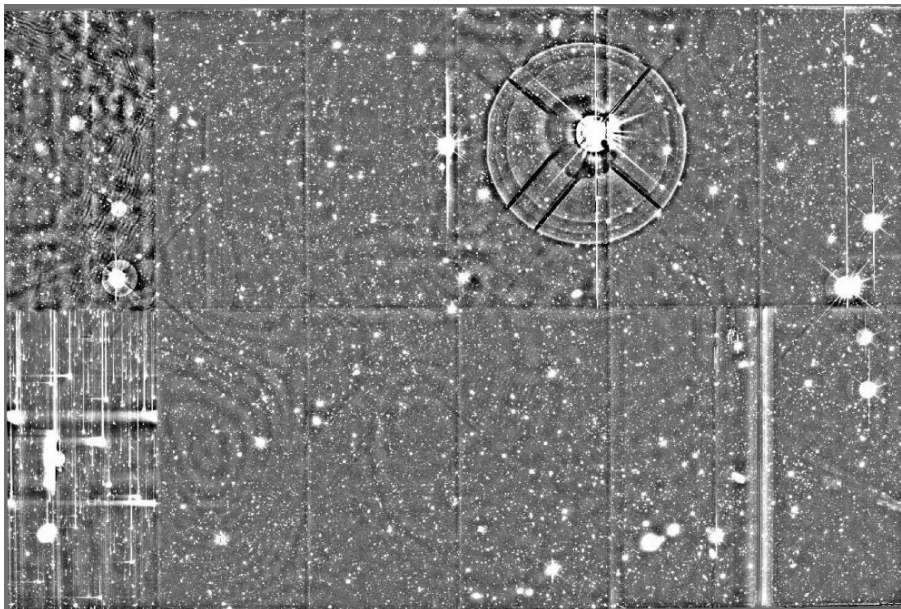


$$\psi = \frac{2}{c^2} \int \frac{D_{ds}}{D_d D_s} \Phi dz$$

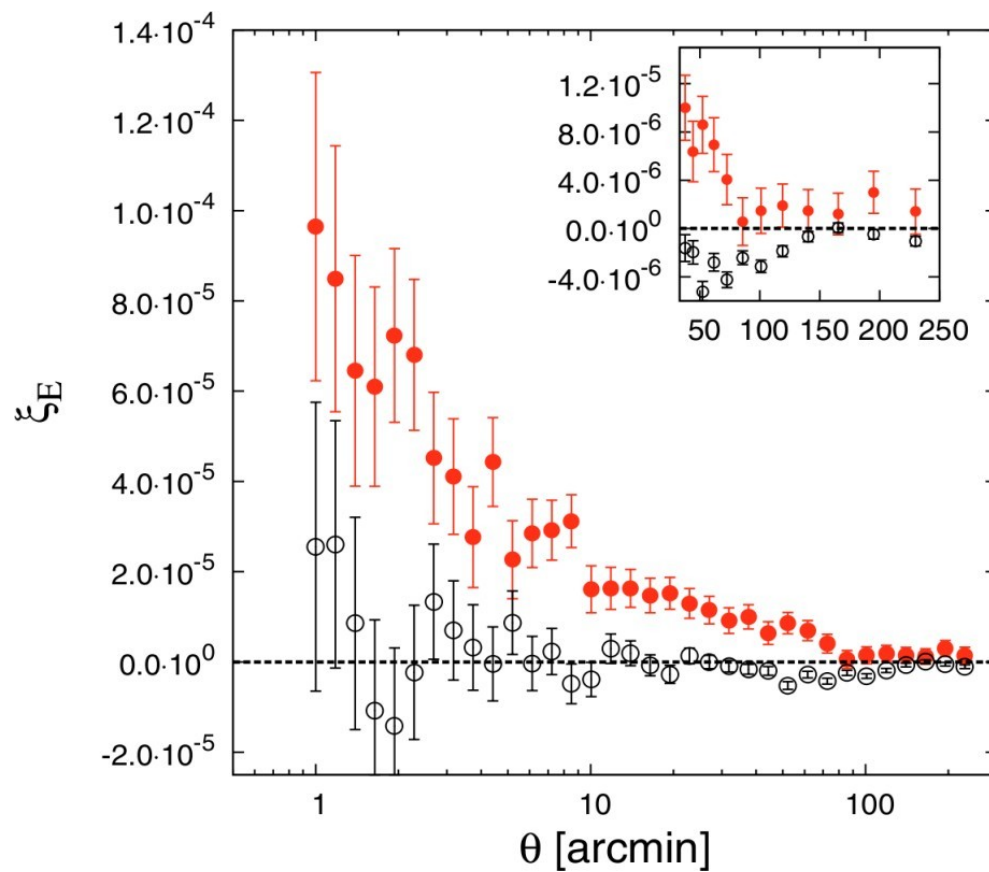


$$P_k(l) = \frac{8\pi G}{c^2} \int \left( \frac{D_{ds}}{D_s} \right)^2 P_{\delta\rho} \left( \frac{l}{D_d} \right) dz$$

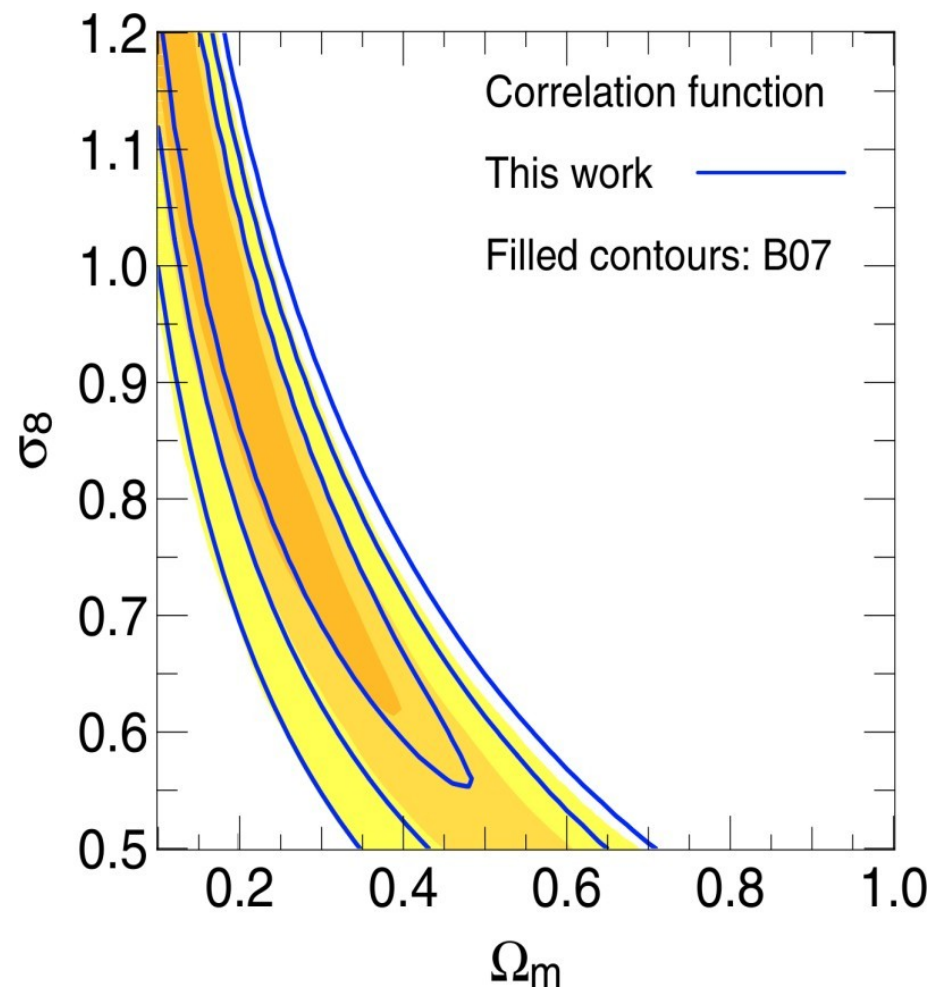
$$\xi_k(\phi) = \int_0^\infty \frac{l dl}{2\pi} P_k(l) J_0(l\phi)$$

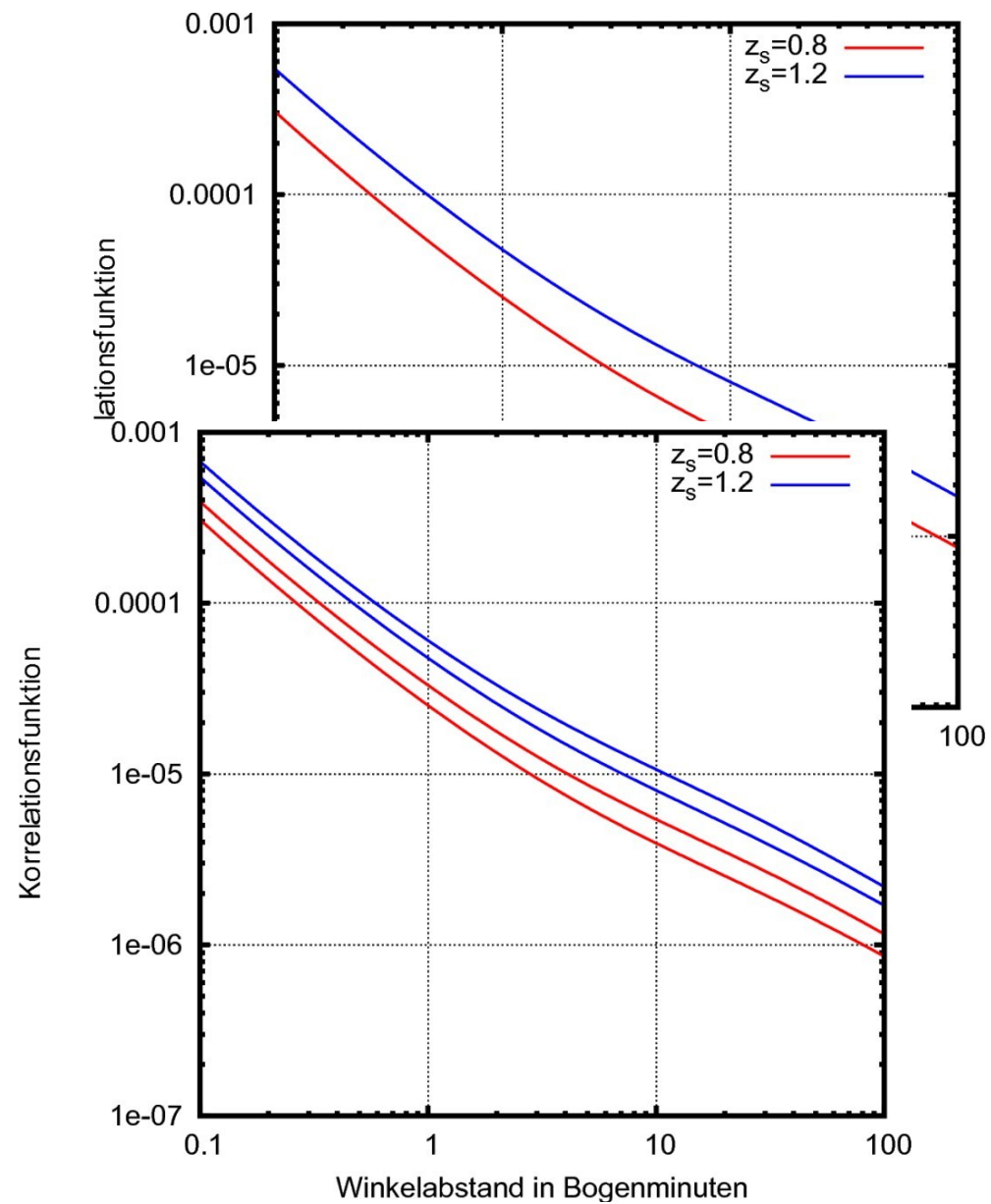
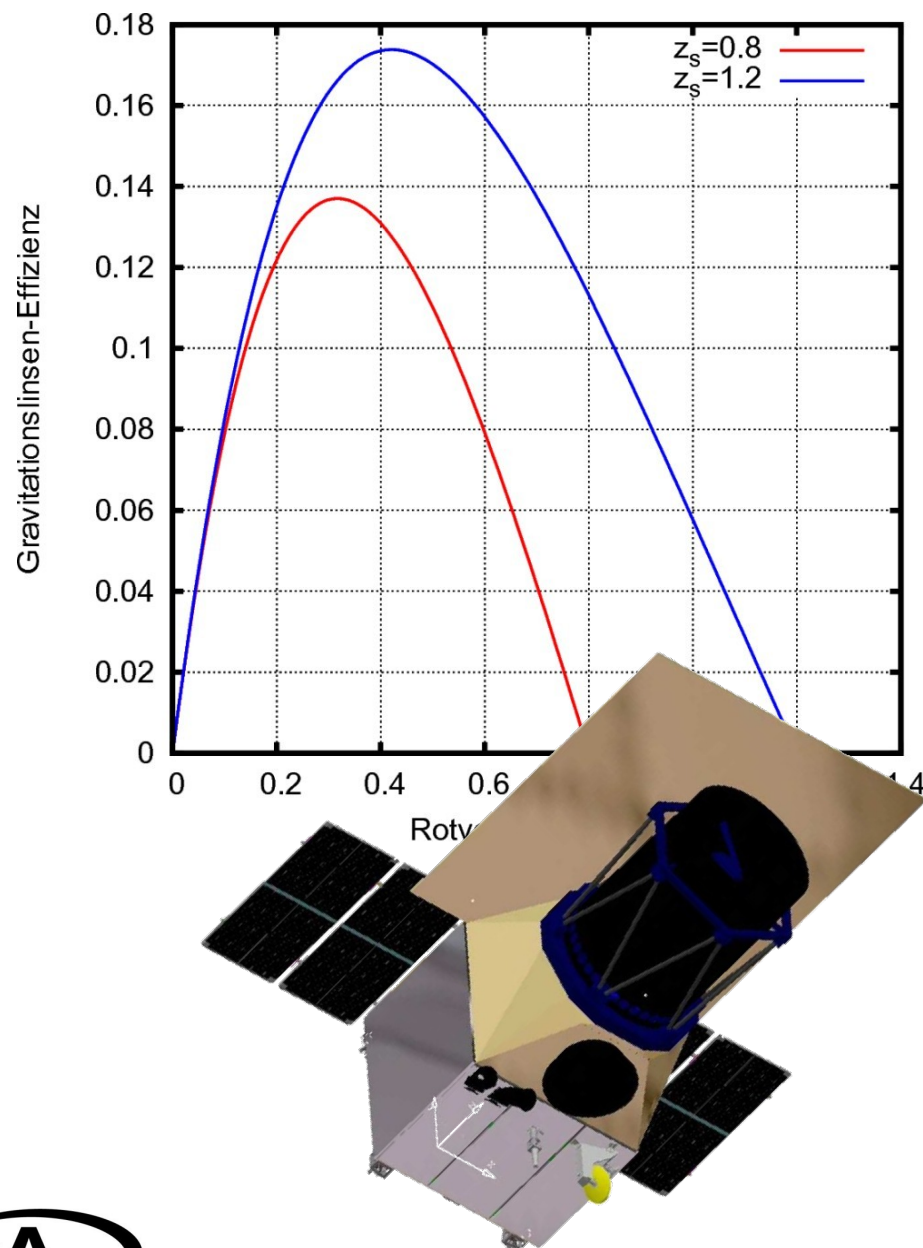


(CFHTLS, Mellier et al.)



(Fu et al. 2008)







(Carbone  
et al. 2008)

