

Warped Dimensions & the LHC

Raman Sundrum
Johns Hopkins University

OUTLINE

- A non-supersymmetric, but extra-dimensional approach to Hierarchy Problem.
- Comprehensively developed & studied
- Deep principles are at stake
- An unusual, challenging phenomenology to prepare for:

Heavy Resonances \rightarrow highly boosted
 t, b, W, Z, higgs .

(Mostly $t = c = 1$ units)

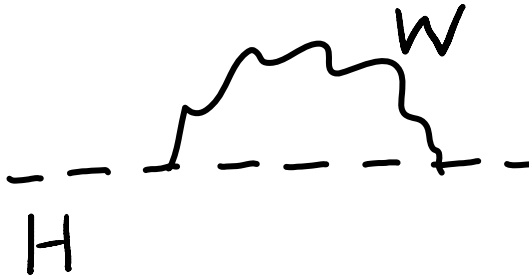
HIERARCHY PUZZLES of the SM

$$m_\nu \ll m_e \ll m_c \ll m_Z \ll M_{\text{GUT}}, M_{\text{Pl}}$$

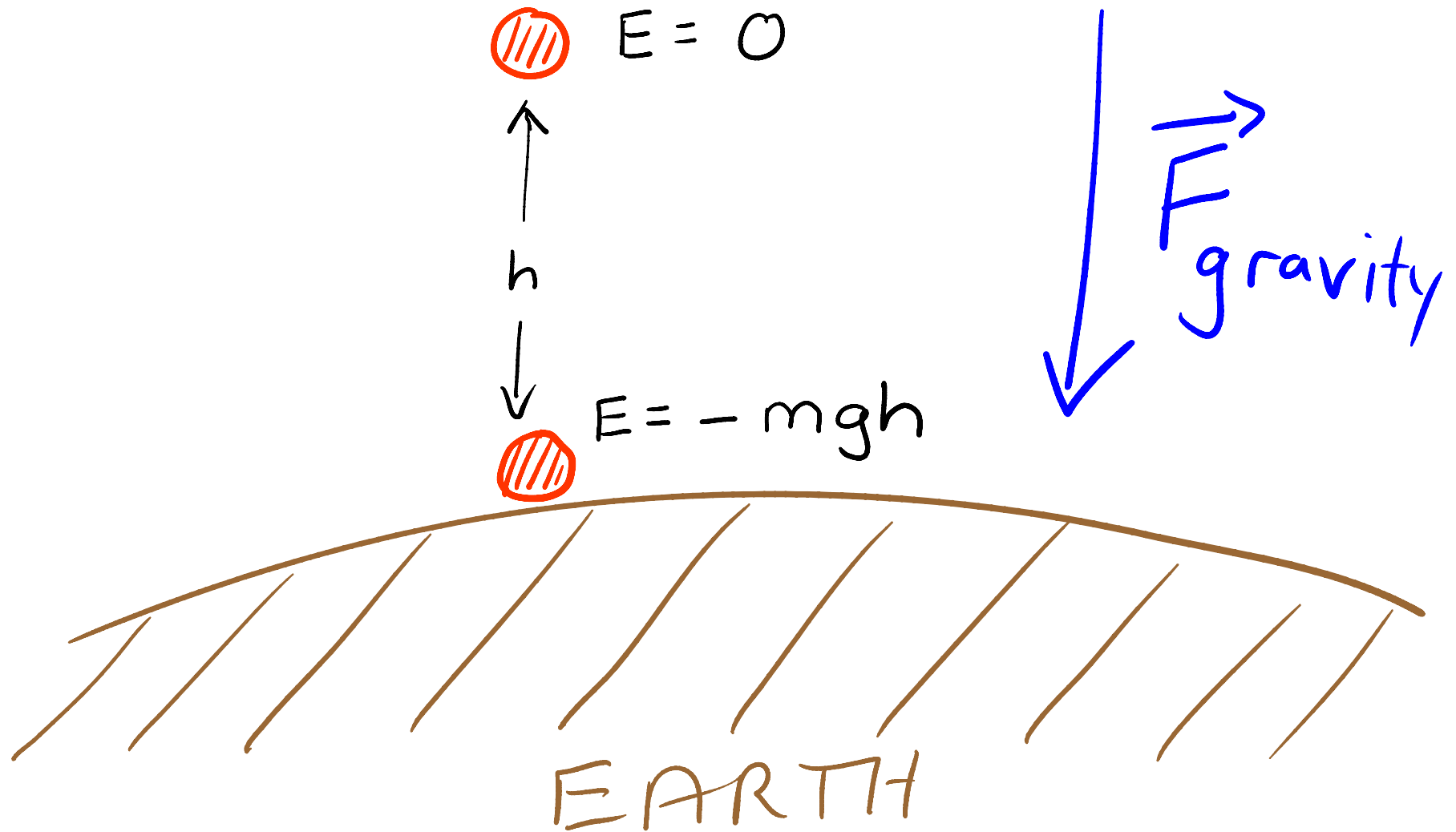
$$V_{td}^{\text{CKM}} \ll V_{ud}^{\text{CKM}}$$

Flavor Hierarchies

The
Hierarchy
Problem:

Radiative Corrections, , tend
to drive m_Z to the highest scales.

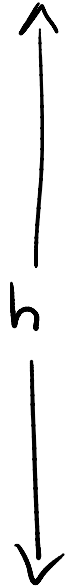
NEWTONIAN GRAVITY



GENERAL RELATIVITY



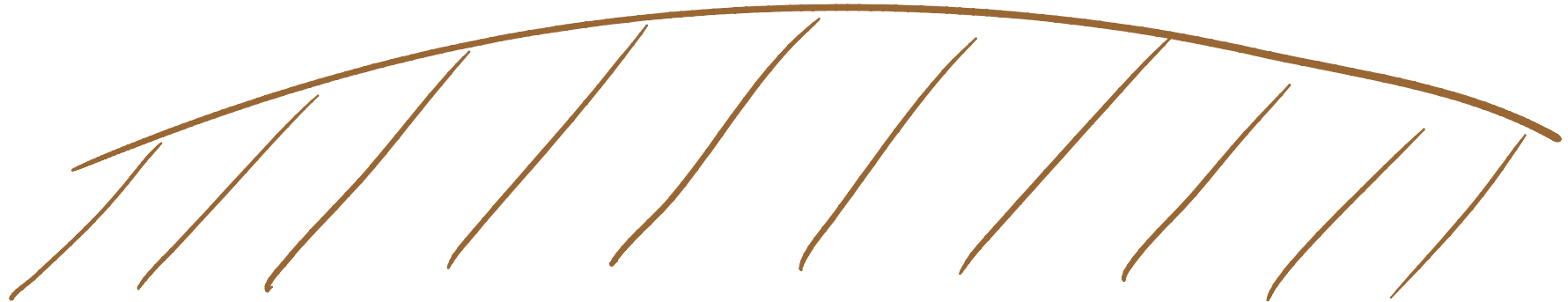
tick, tick, tick



$$\Delta t_{\text{low}} = \frac{\Delta t_{\text{high}}}{1 - gh}$$

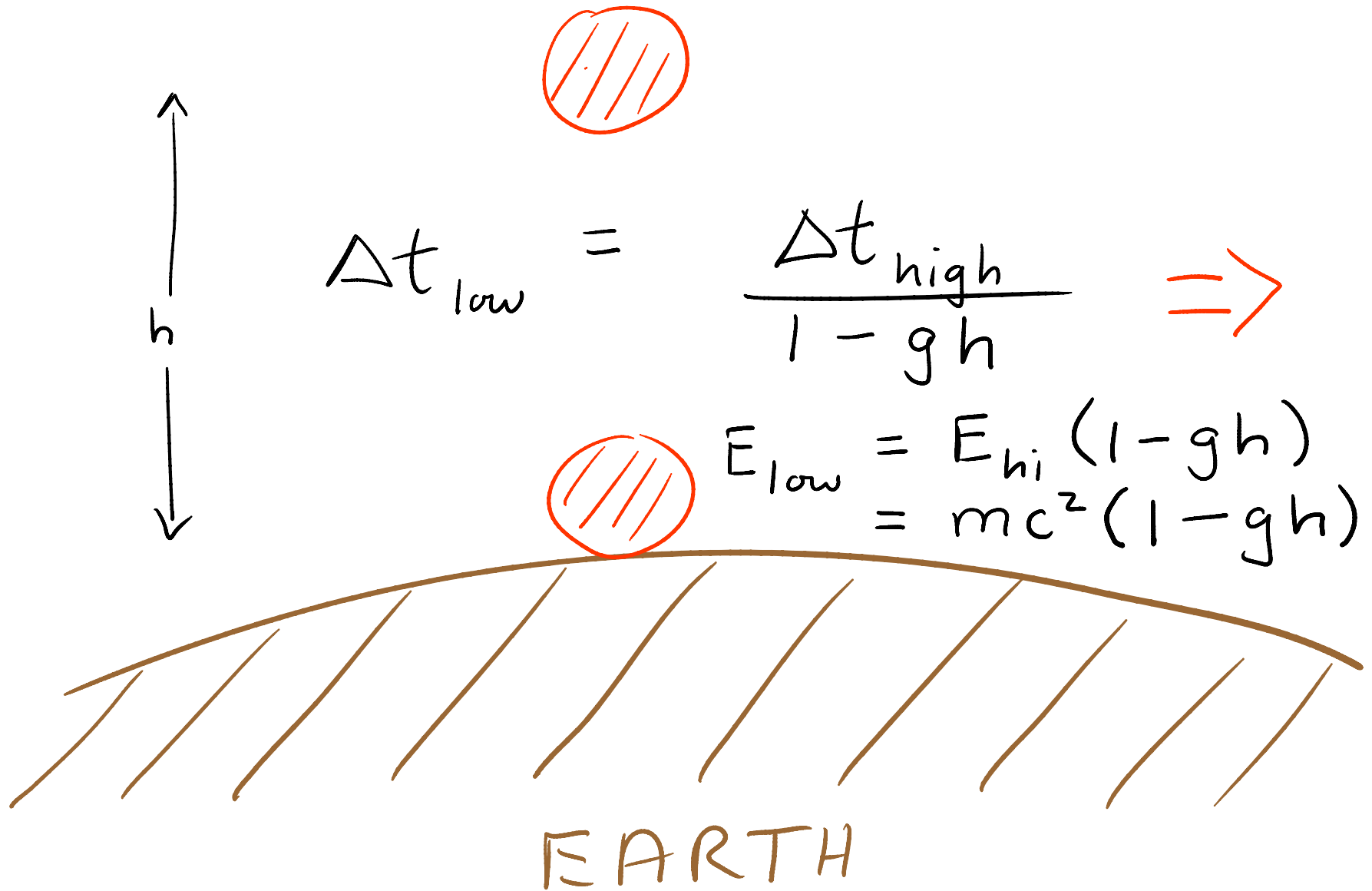


tick - tick - tick

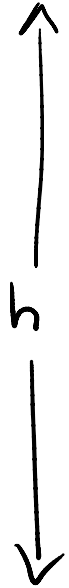
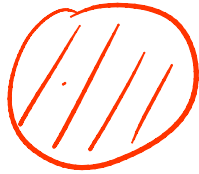


EARTH

GRAVITATIONAL REDSHIFT



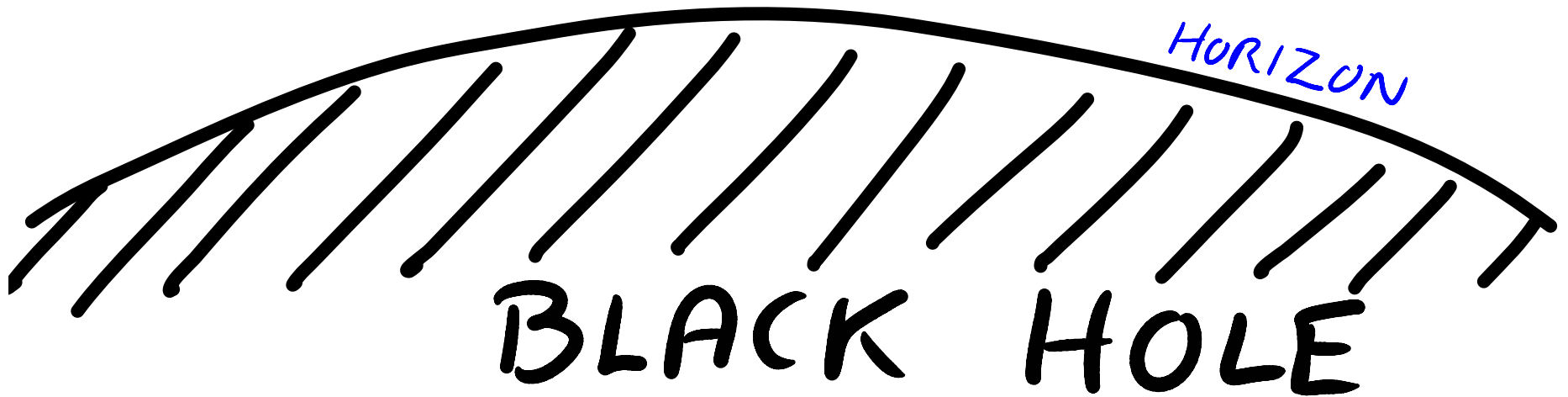
GRAVITATIONAL REDSHIFTS CAN BE BIG!



$$\Delta t_{\text{low}} = \frac{\Delta t_{\text{high}}}{\sqrt{1 - \frac{R_{\text{horizon}}}{r}}} \Rightarrow$$



$$E_{\text{low}} = E_{\text{high}} \sqrt{1 - \frac{R_{\text{horizon}}}{r}}$$
$$= mc^2 \sqrt{1 - R_{\text{horizon}}/r}$$

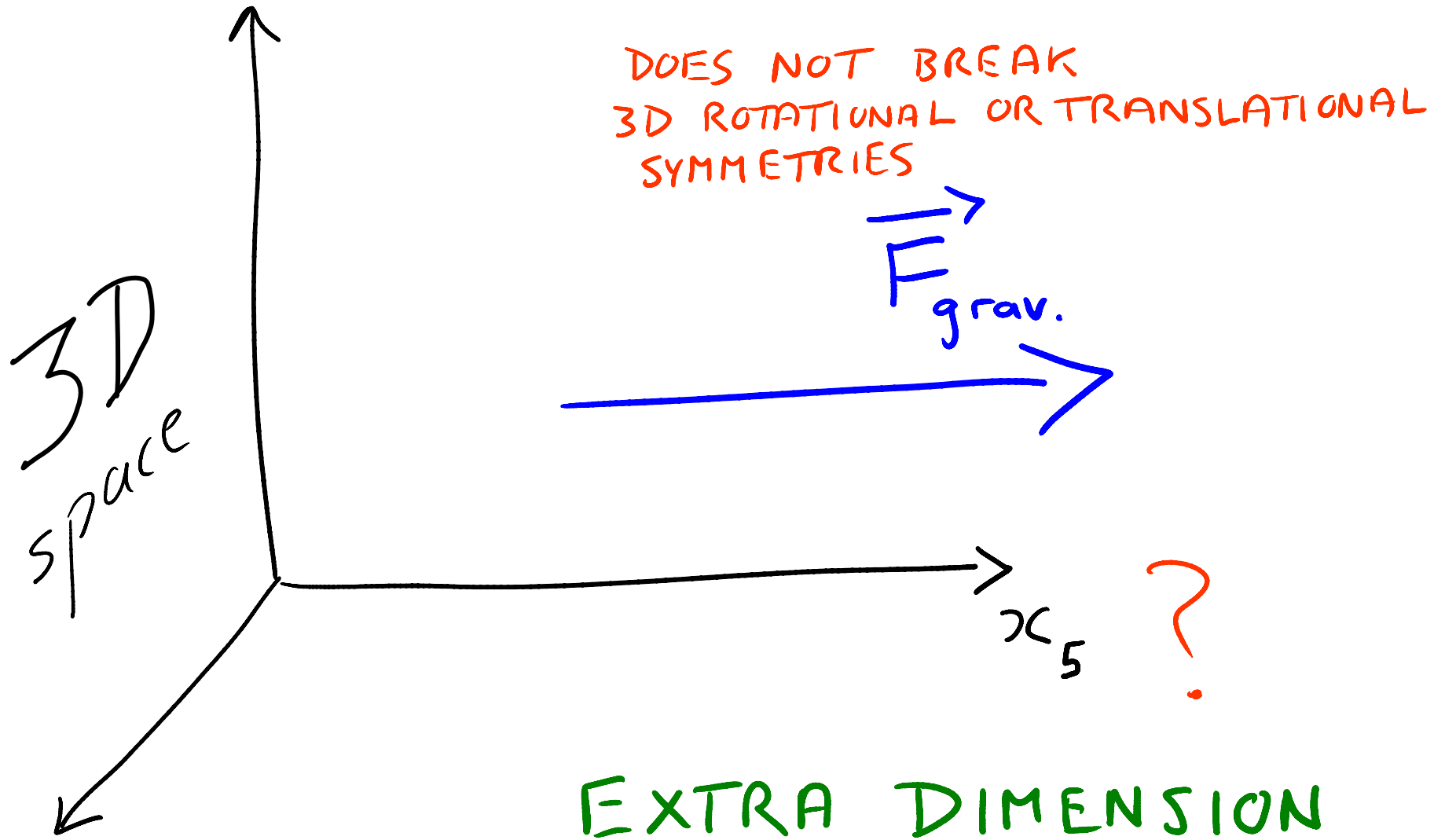


CAN BIG REDSHIFTS
EXPLAIN BIG MASS
HIERARCHIES?

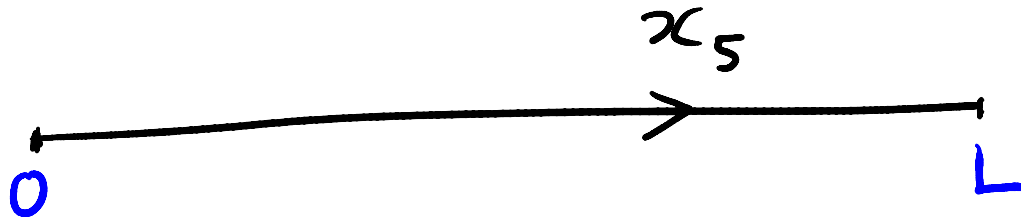
BUT WHICH

WAY IS DOWN?

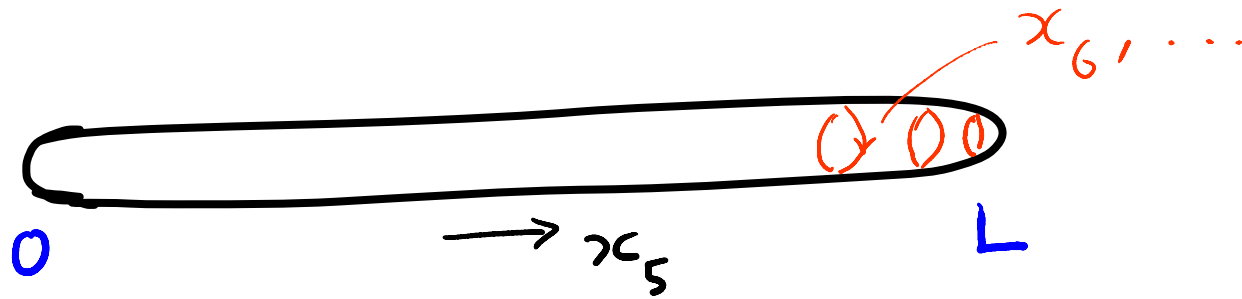
A NEW DIRECTION



THE ENDS OF THE UNIVERSE



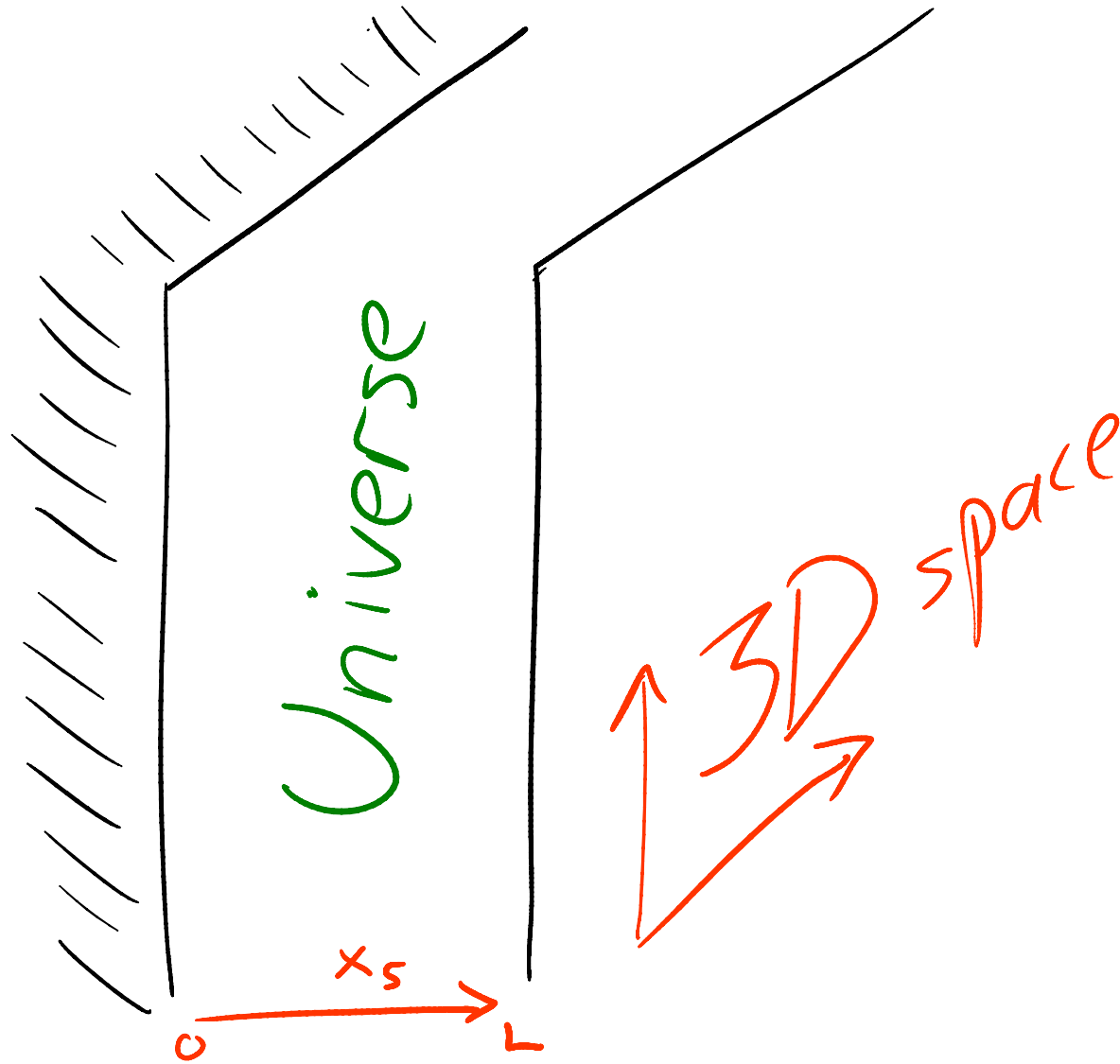
THE ENDS OF THE UNIVERSE



CAN BE SMOOTH

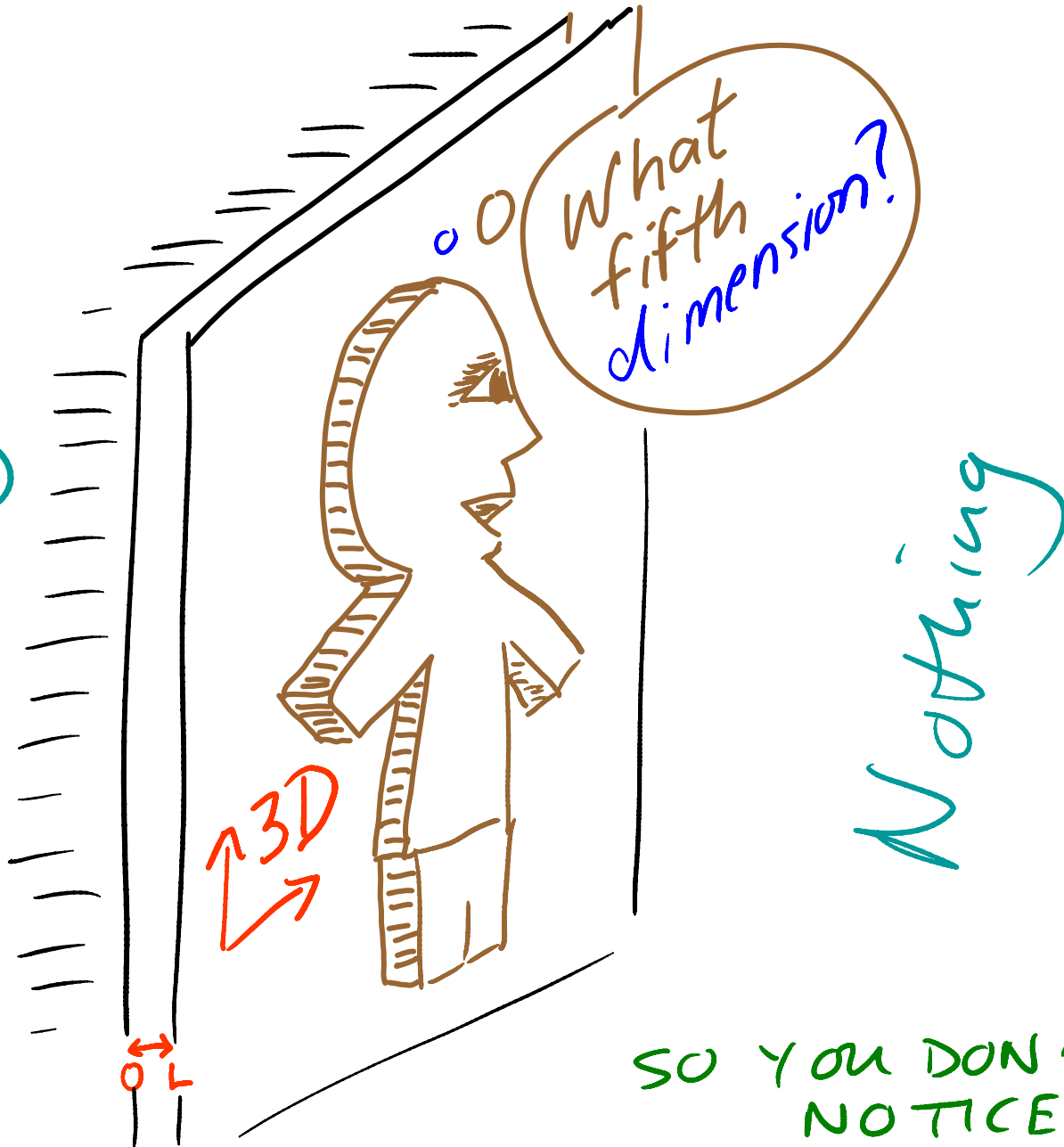
SUCH AS IN SOME
STRING THEORY CONSTRUCTIONS

THE ENDS OF THE UNIVERSE



THE FIFTH DIMENSION IS SMALL...

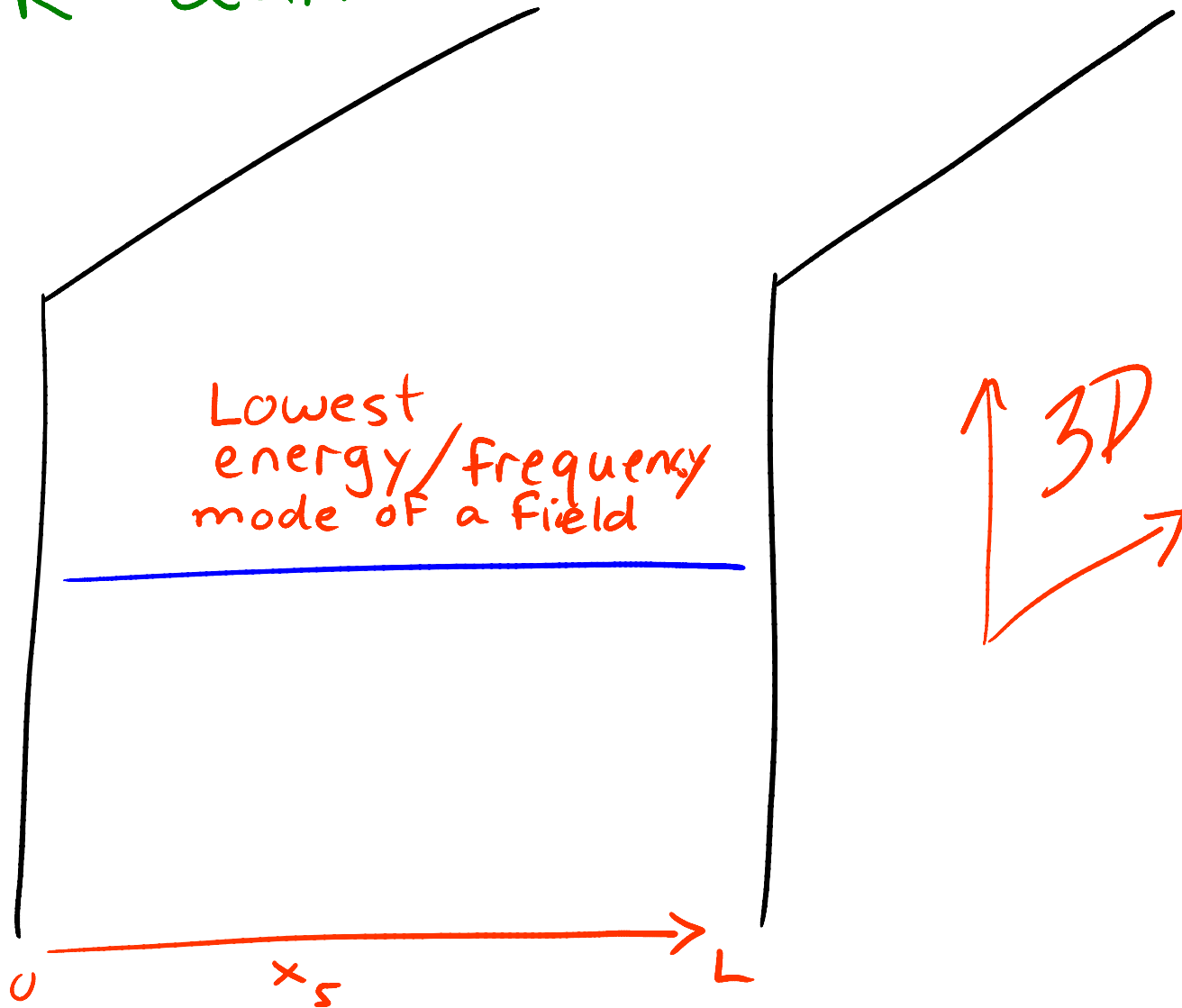
Nothing



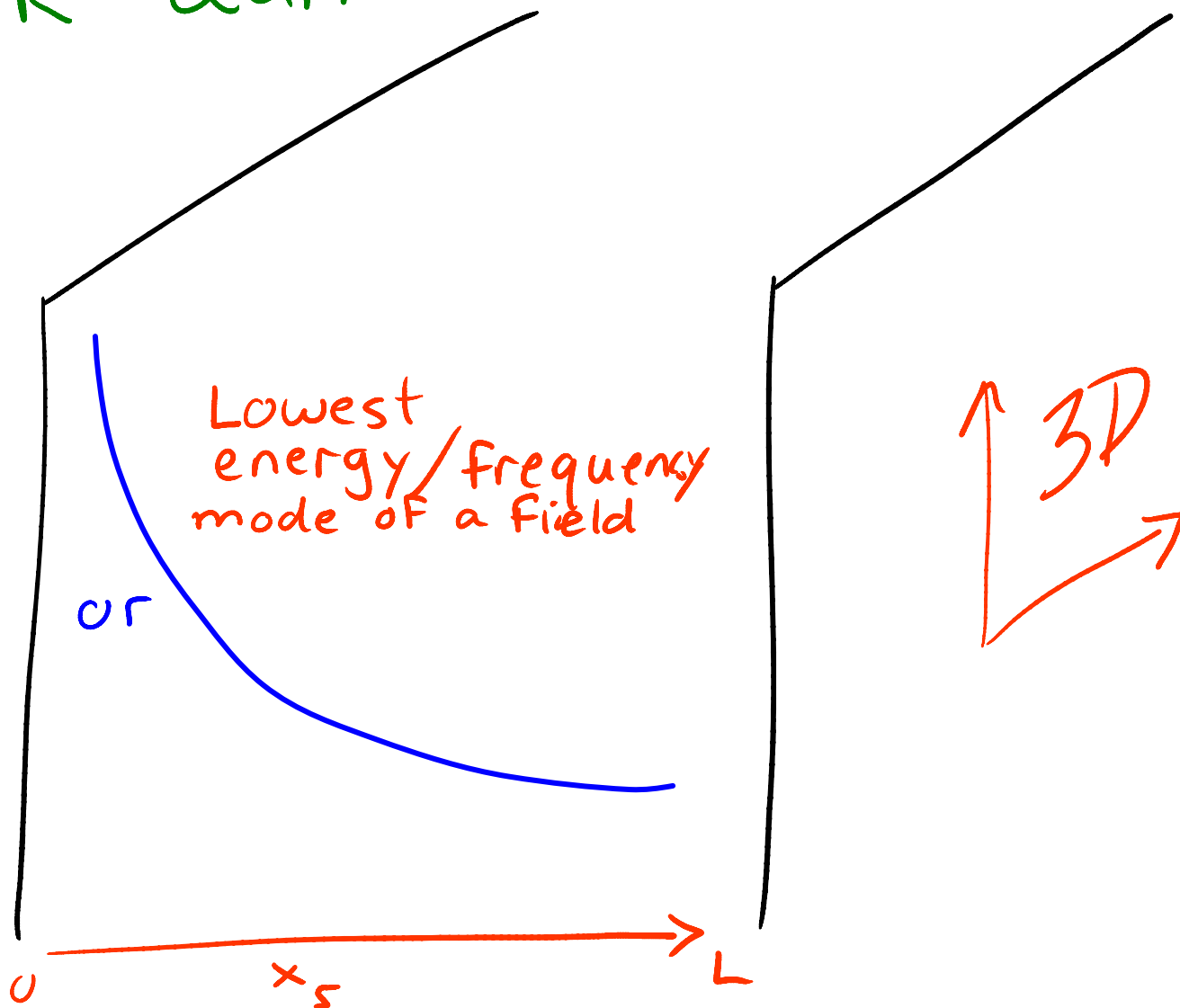
Nothing

SO YOU DON'T NOTICE IT

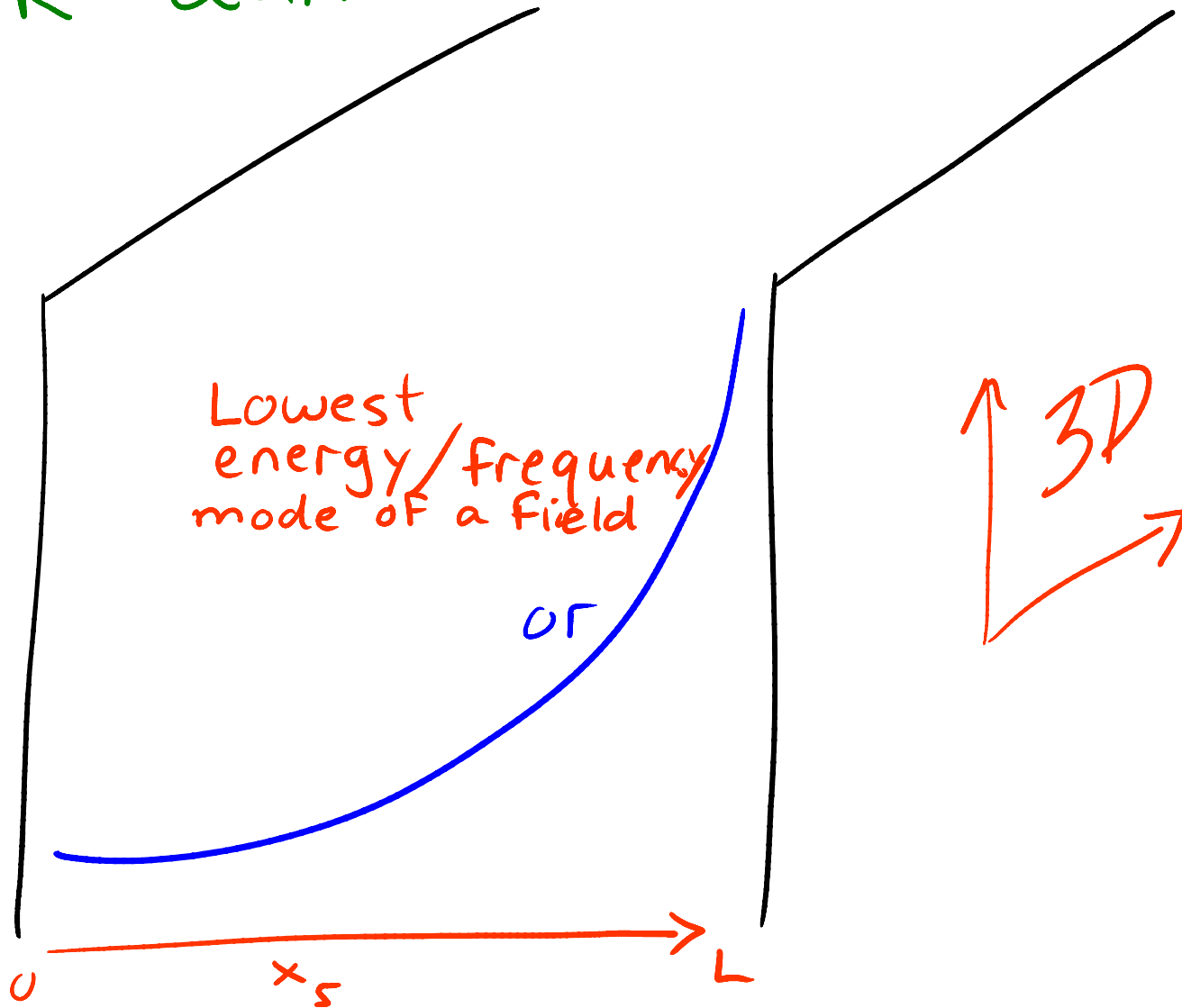
A COSMIC WAVE GUIDE FOR QUANTUM FIELDS



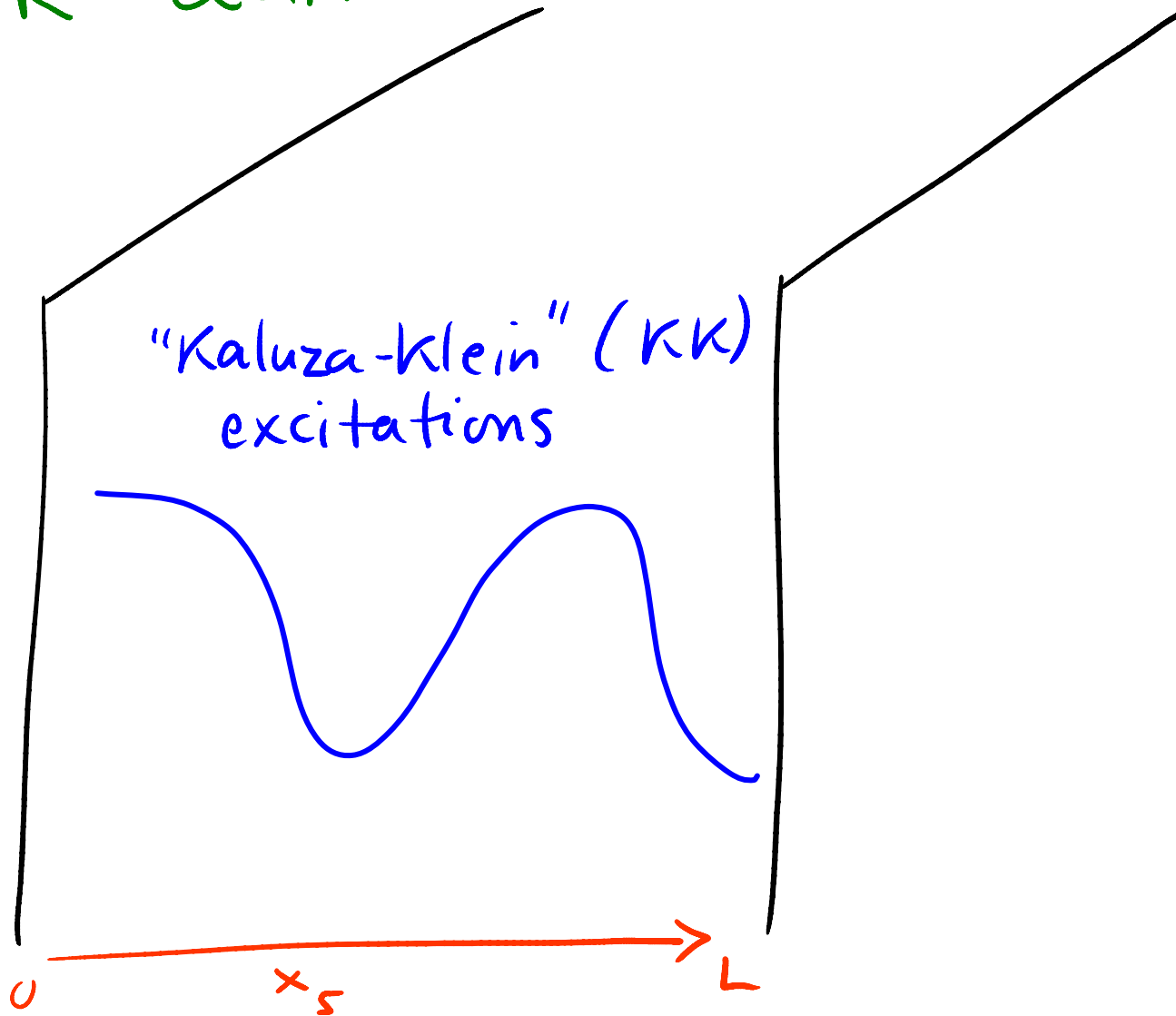
A COSMIC WAVE GUIDE FOR QUANTUM FIELDS



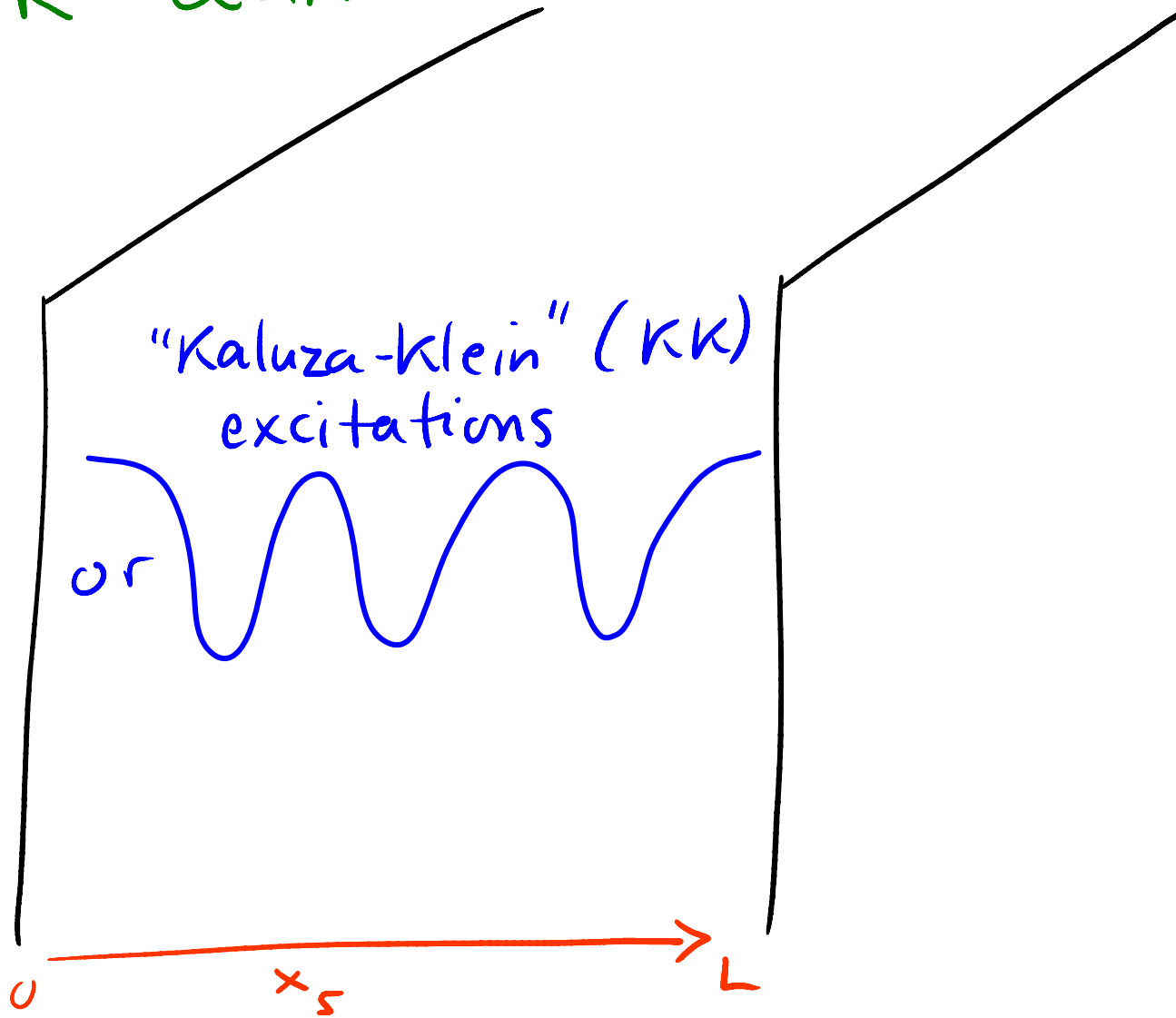
A COSMIC WAVE GUIDE FOR QUANTUM FIELDS



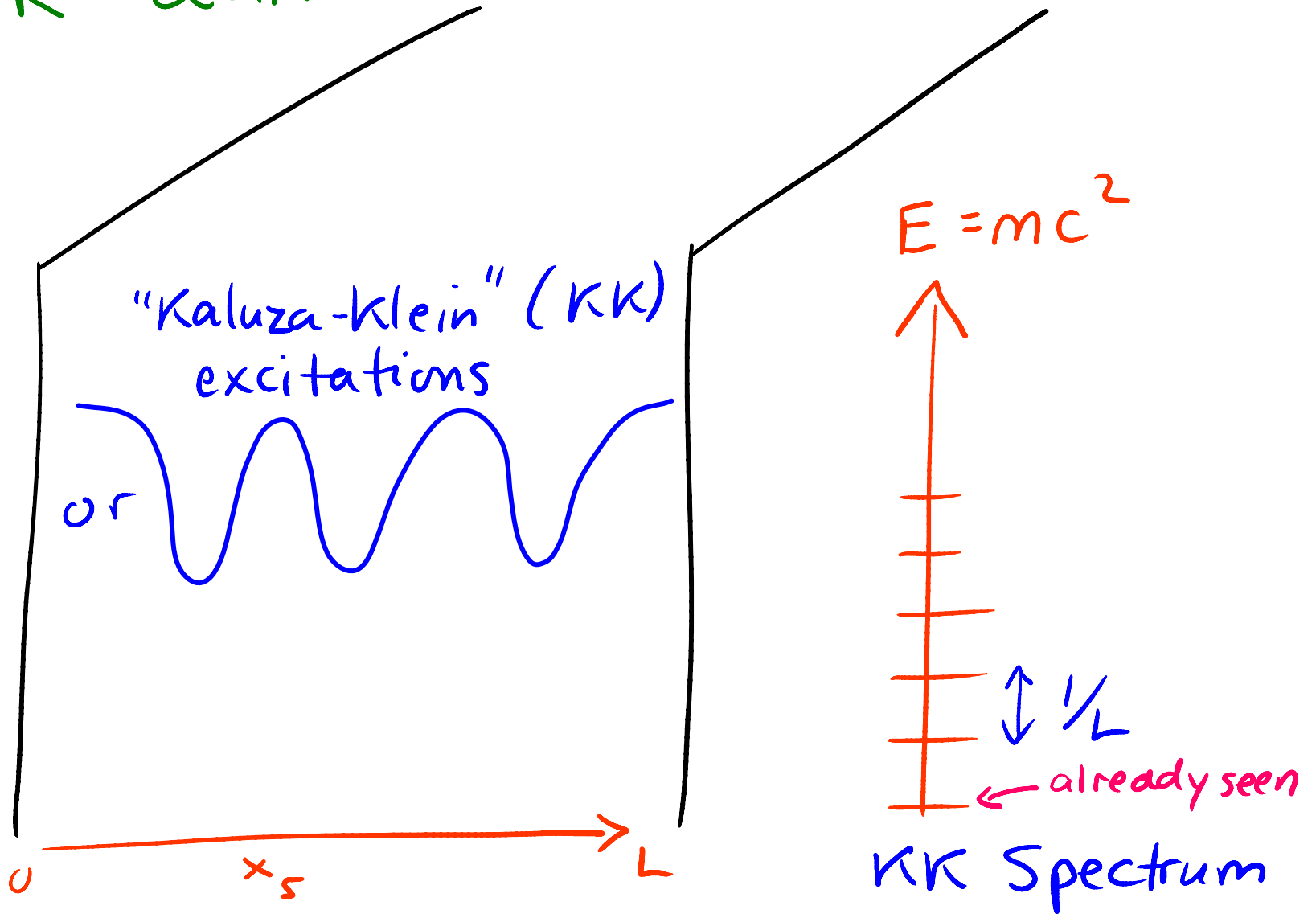
A COSMIC WAVE GUIDE FOR QUANTUM FIELDS



A COSMIC WAVE GUIDE FOR QUANTUM FIELDS



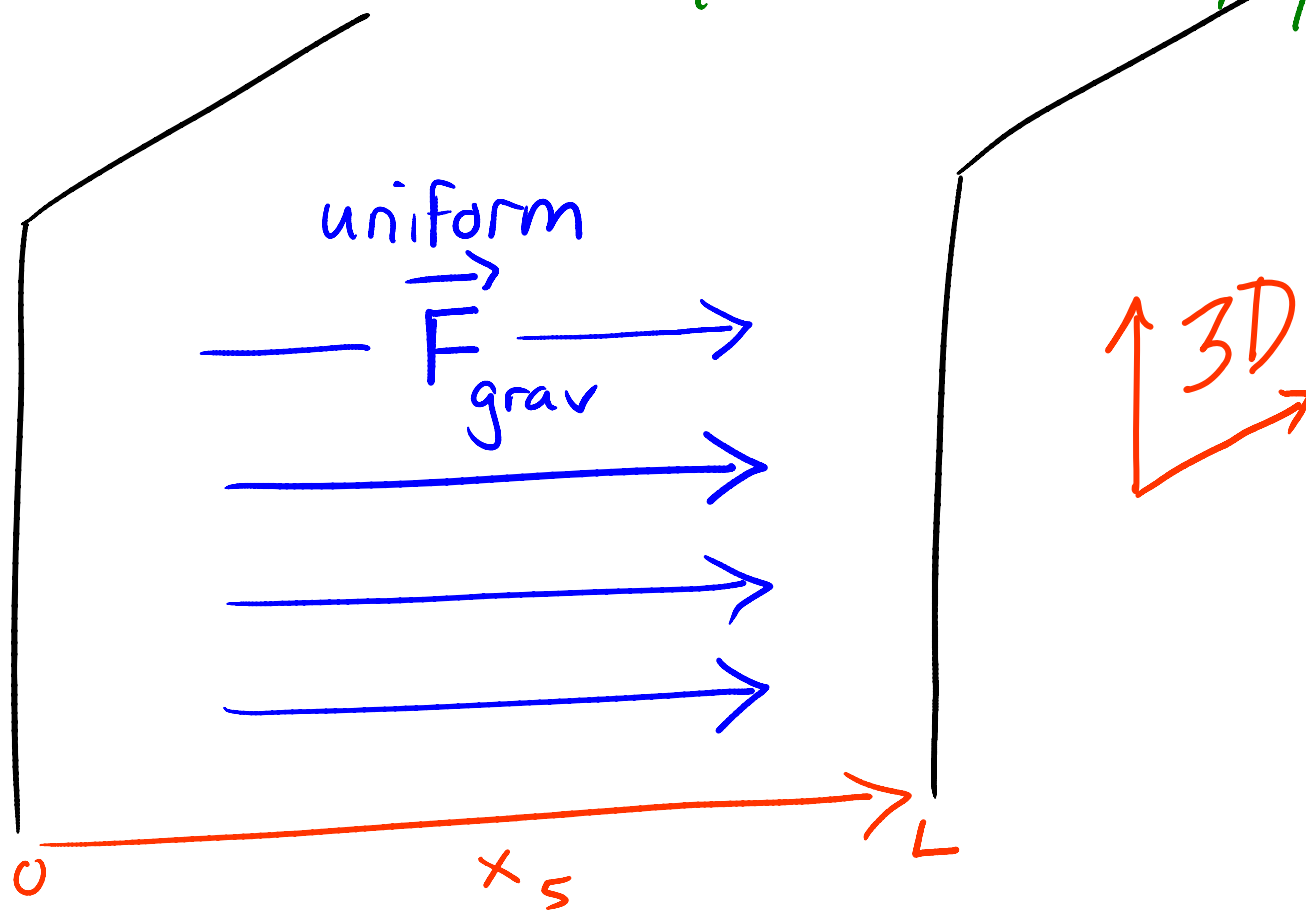
A COSMIC WAVE GUIDE FOR QUANTUM FIELDS



RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

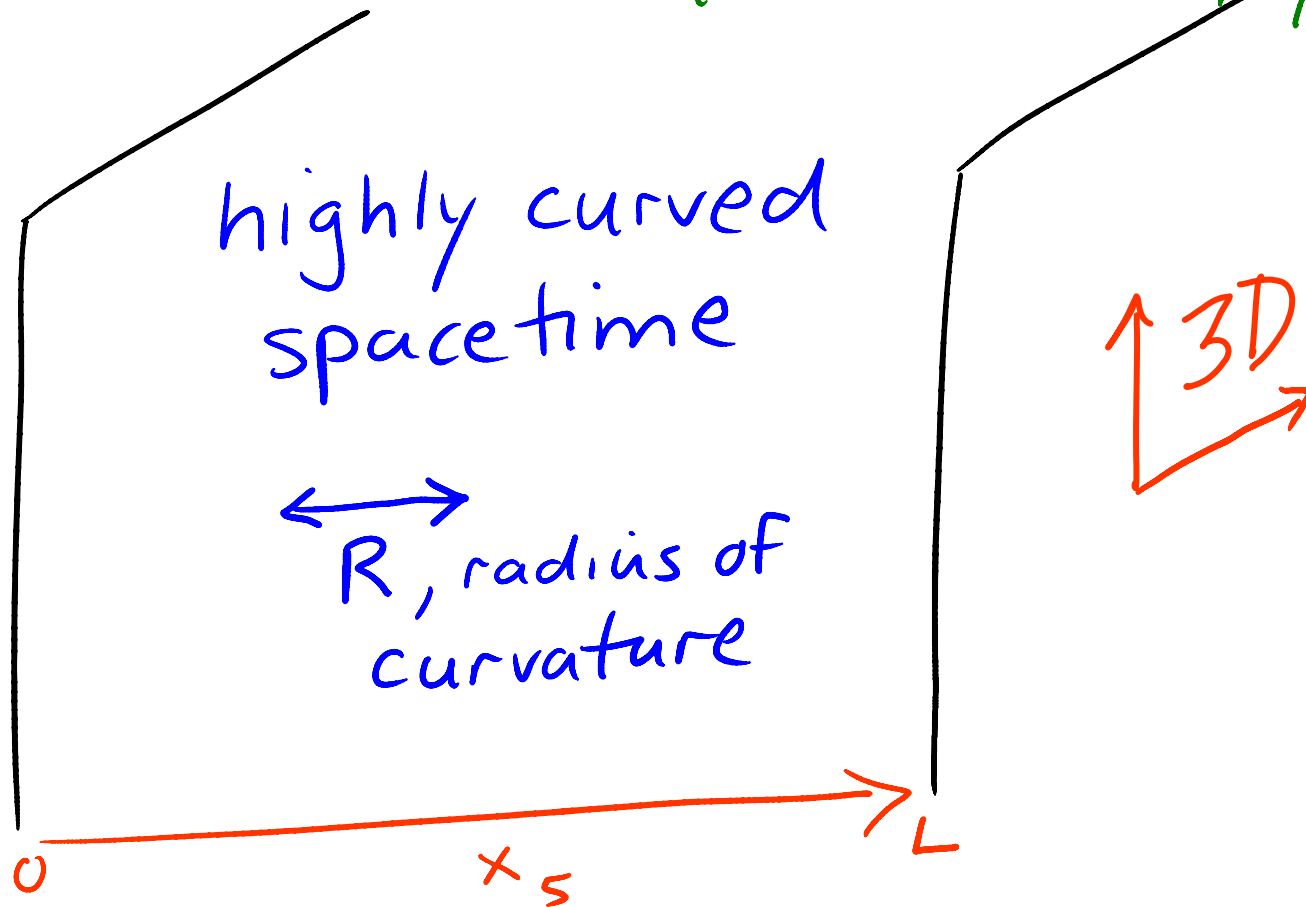
Higher-dimensional Einstein Equations robustly yield...



RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

Higher-dimensional Einstein Equations robustly yield...



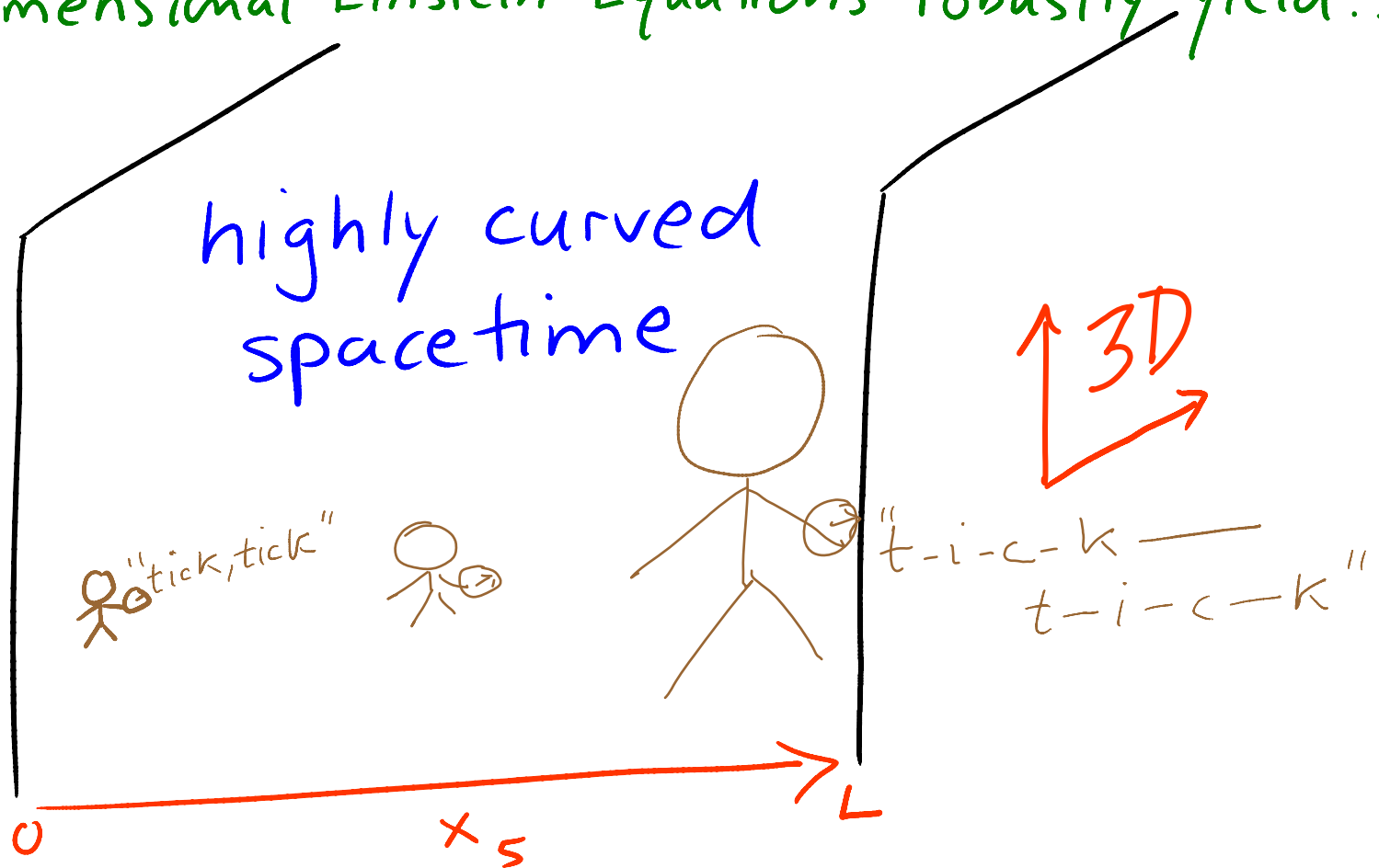
$L \sim 10^{15} \times R$ readily occurs in solutions

Goldberger, Wise '99

RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

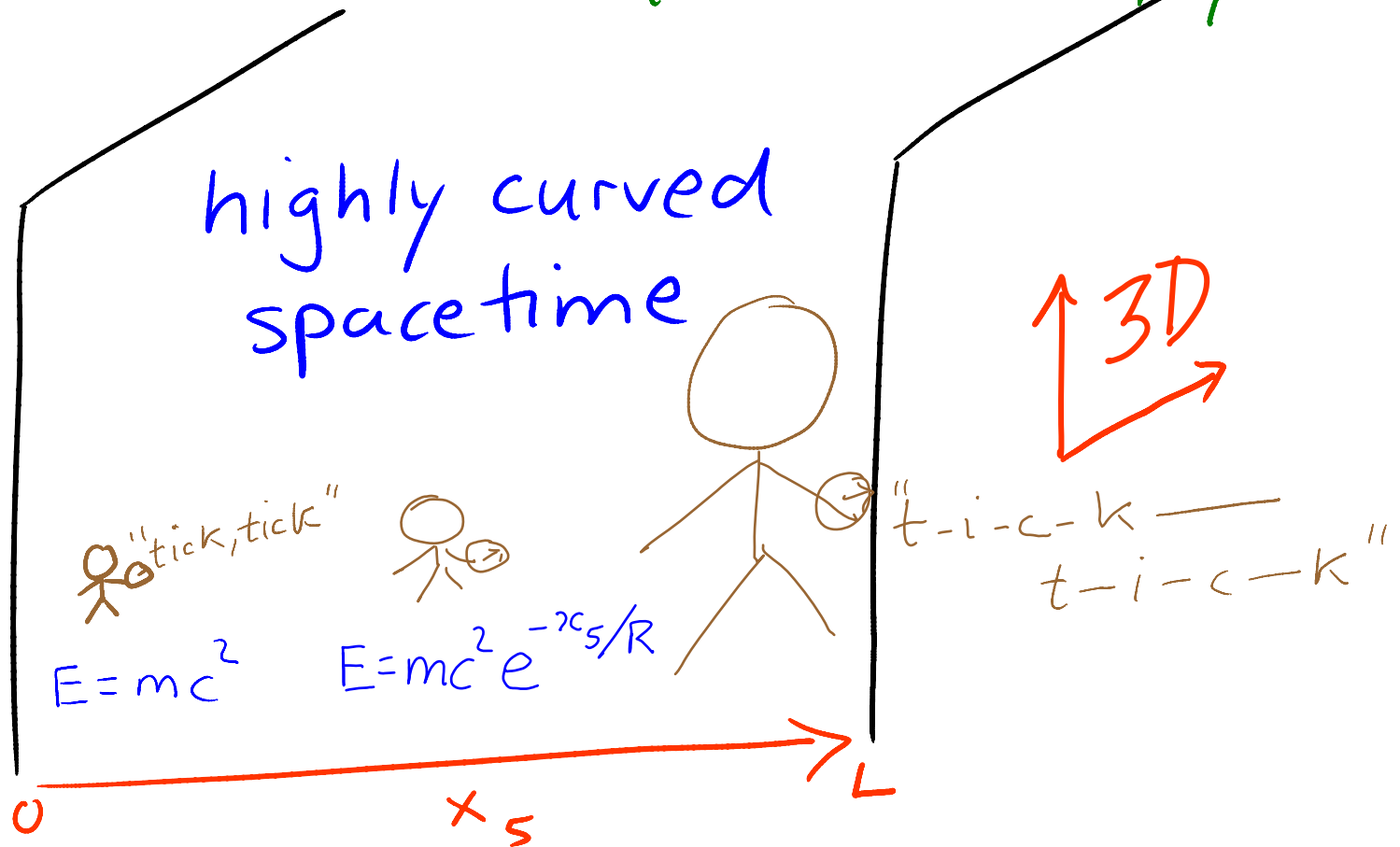
Higher-dimensional Einstein Equations robustly yield...



RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

Higher-dimensional Einstein Equations robustly yield...

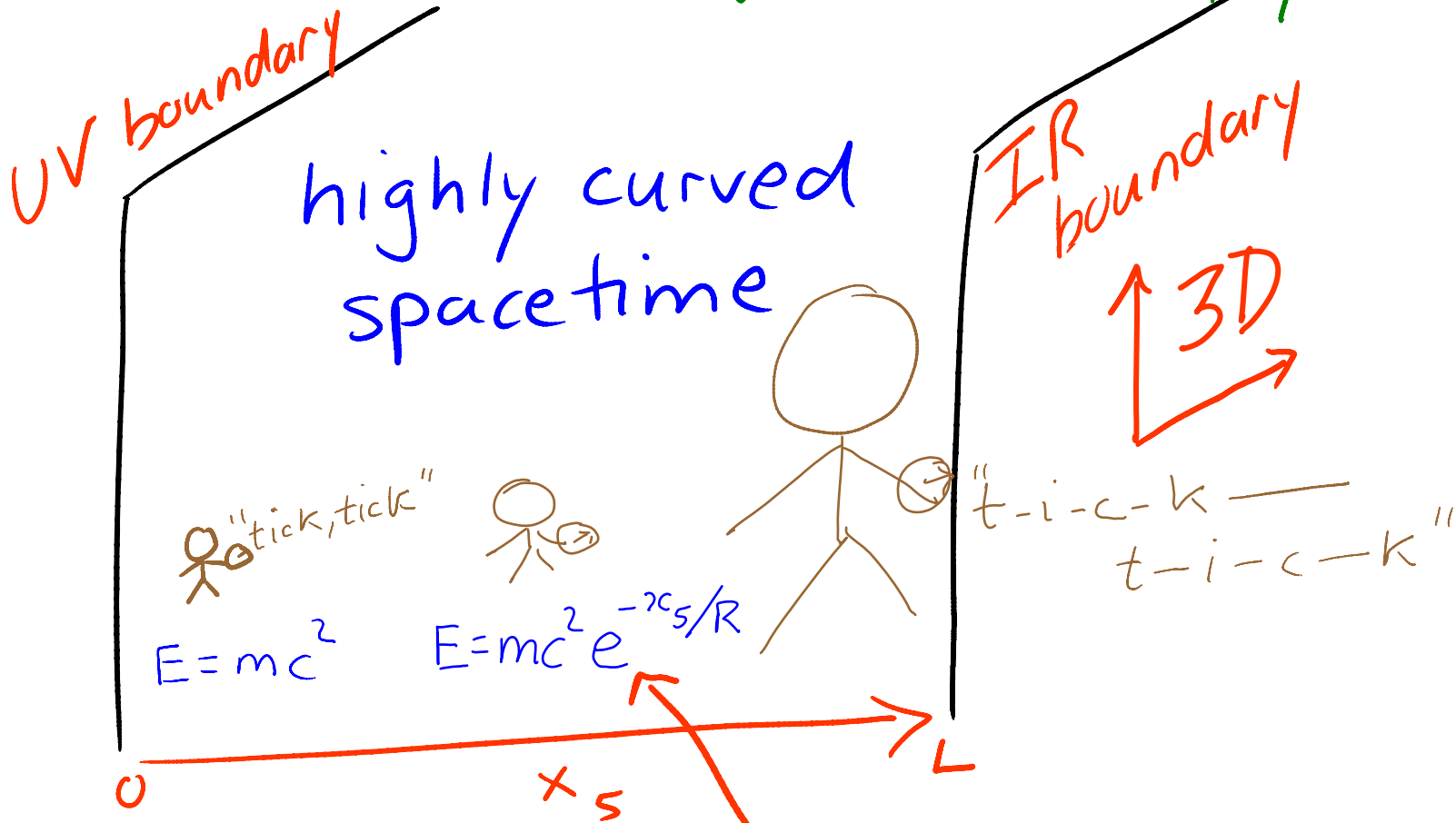


... Exponential
Gravitational Redshifts

RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

Higher-dimensional Einstein Equations robustly yield...

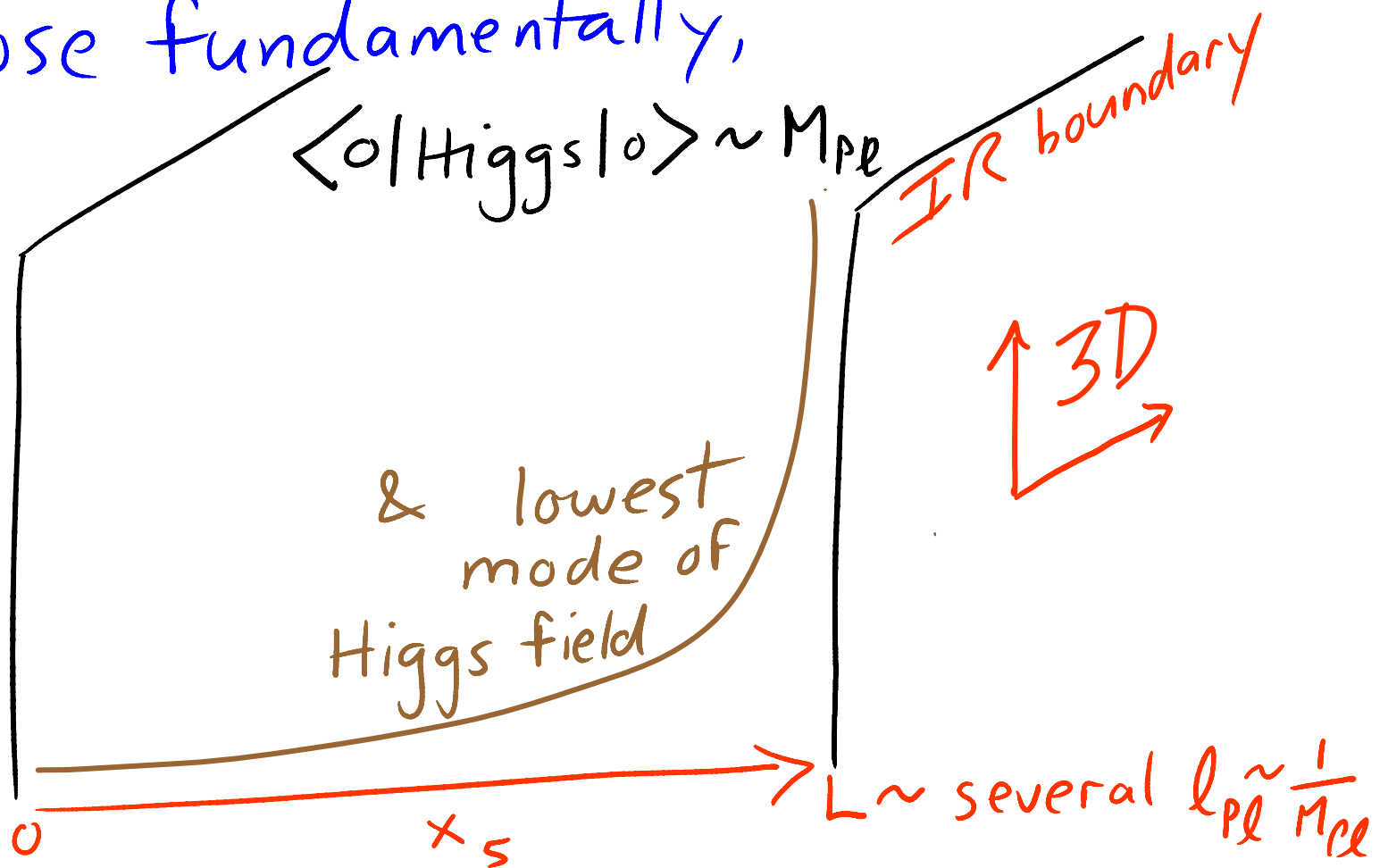


... Exponential Redshift "Warp factor"

RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

Suppose fundamentally,

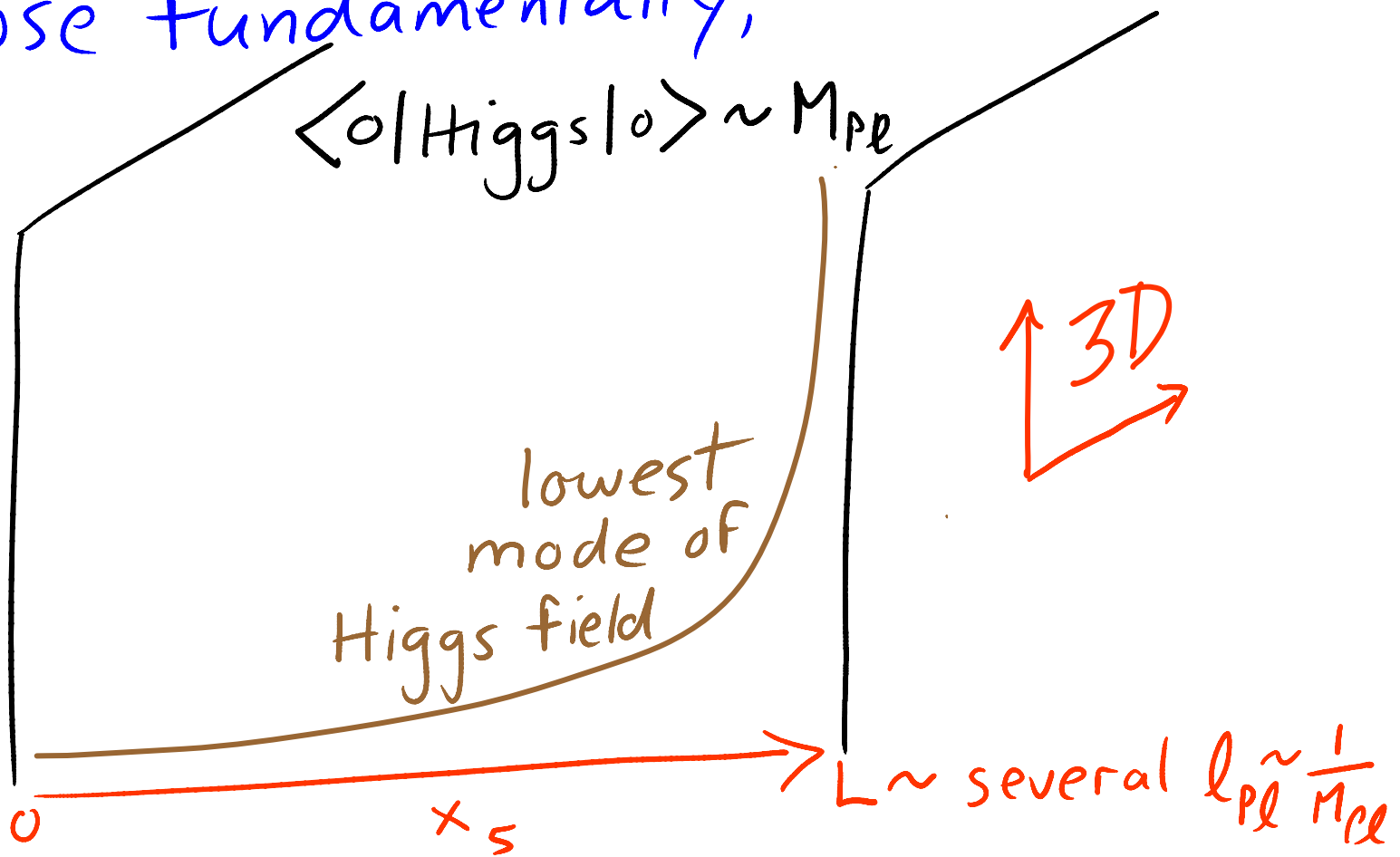


Effectively $\langle 0 | \text{Higgs} | 0 \rangle \sim M_{Pl} e^{-L/R}$
sets max. SM masses (m_Z, m_{top})

RANDALL-SUNDRUM I MODEL (RSI)

Randall, Sundrum '99

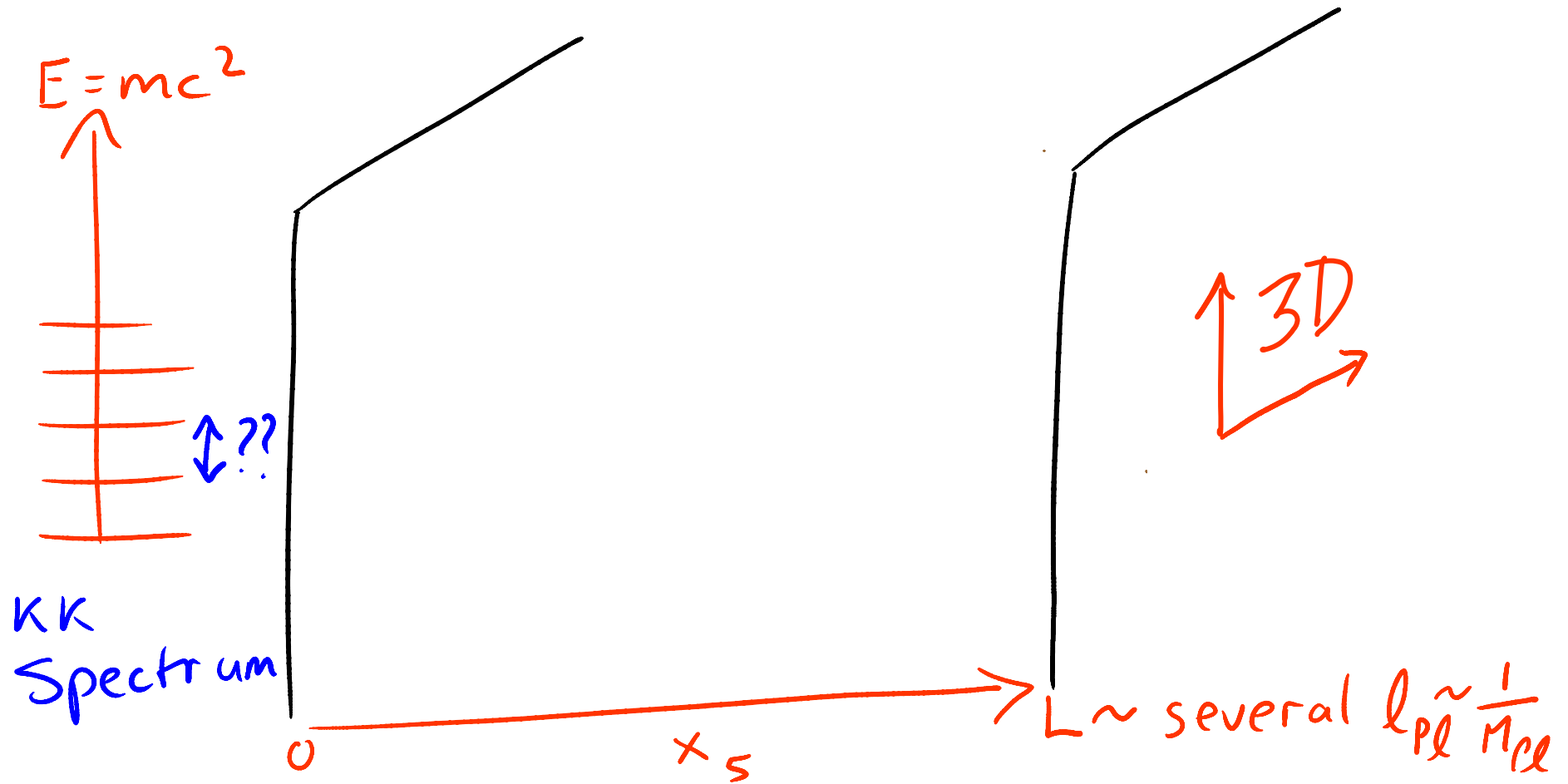
Suppose fundamentally,



Effectively $\langle 0 | \text{Higgs} | 0 \rangle \sim M_{Pl} e^{-L/R} \sim 100\text{'s GeV}$
sets max. SM masses (m_Z, m_{top}) for $L/R \sim 30$

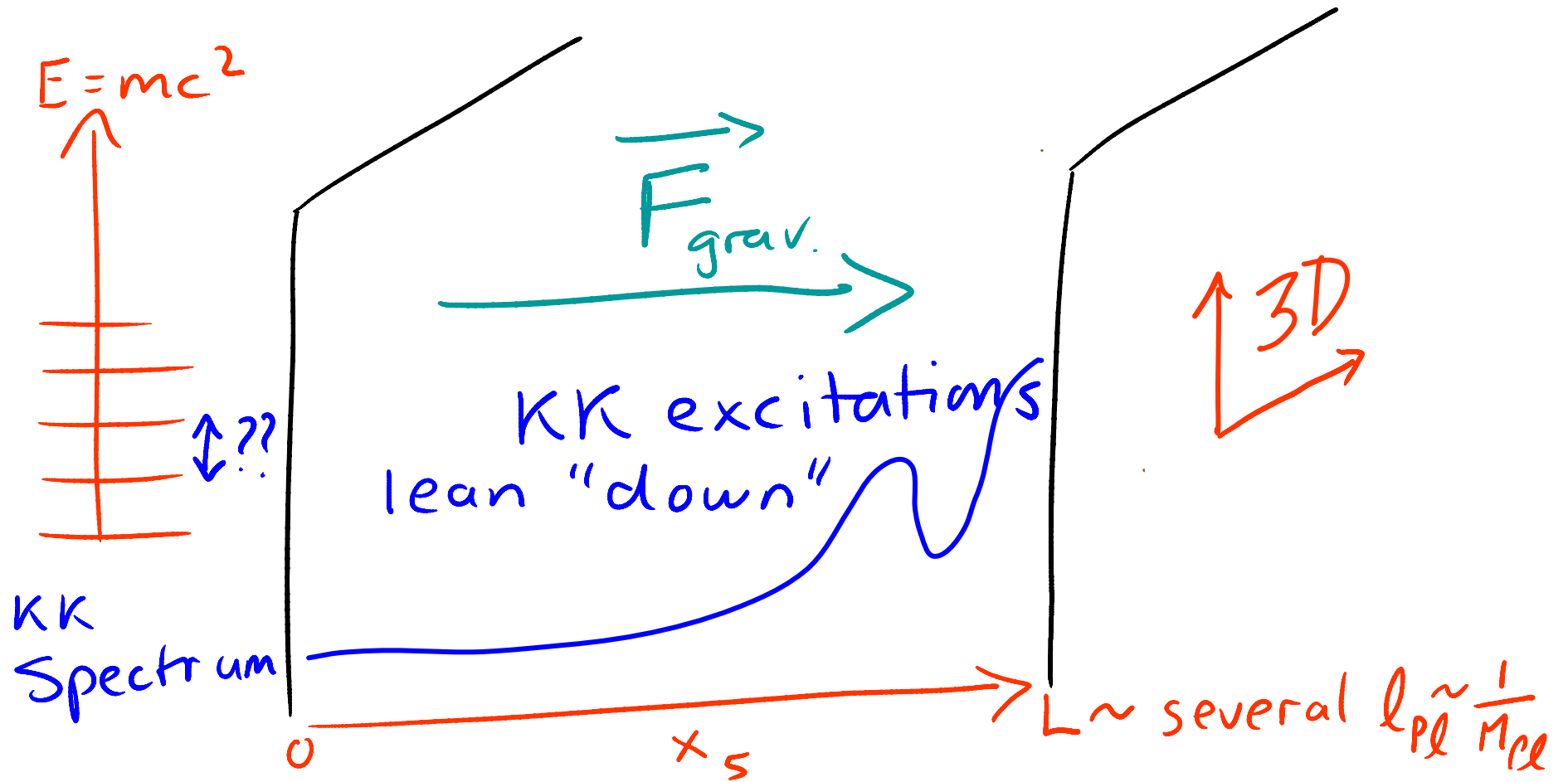
KALUZA-KLEIN EXCITATIONS IN RS1

are not at $1/L \approx 1/l_{Pl} \equiv M_{Pl}$



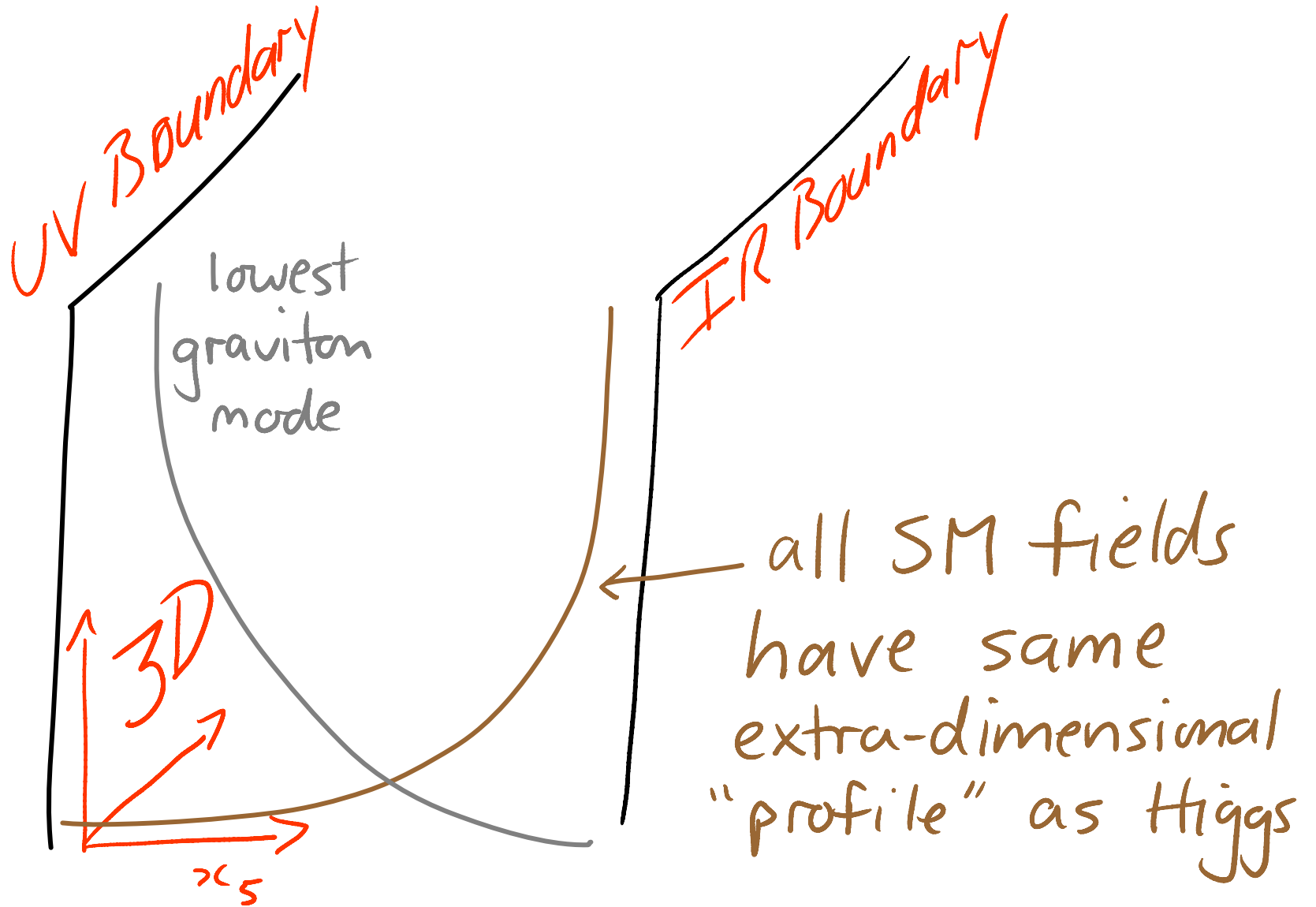
KALUZA-KLEIN EXCITATIONS IN RS1

are not at $1/L \approx 1/l_{pl} \equiv M_{pl}$

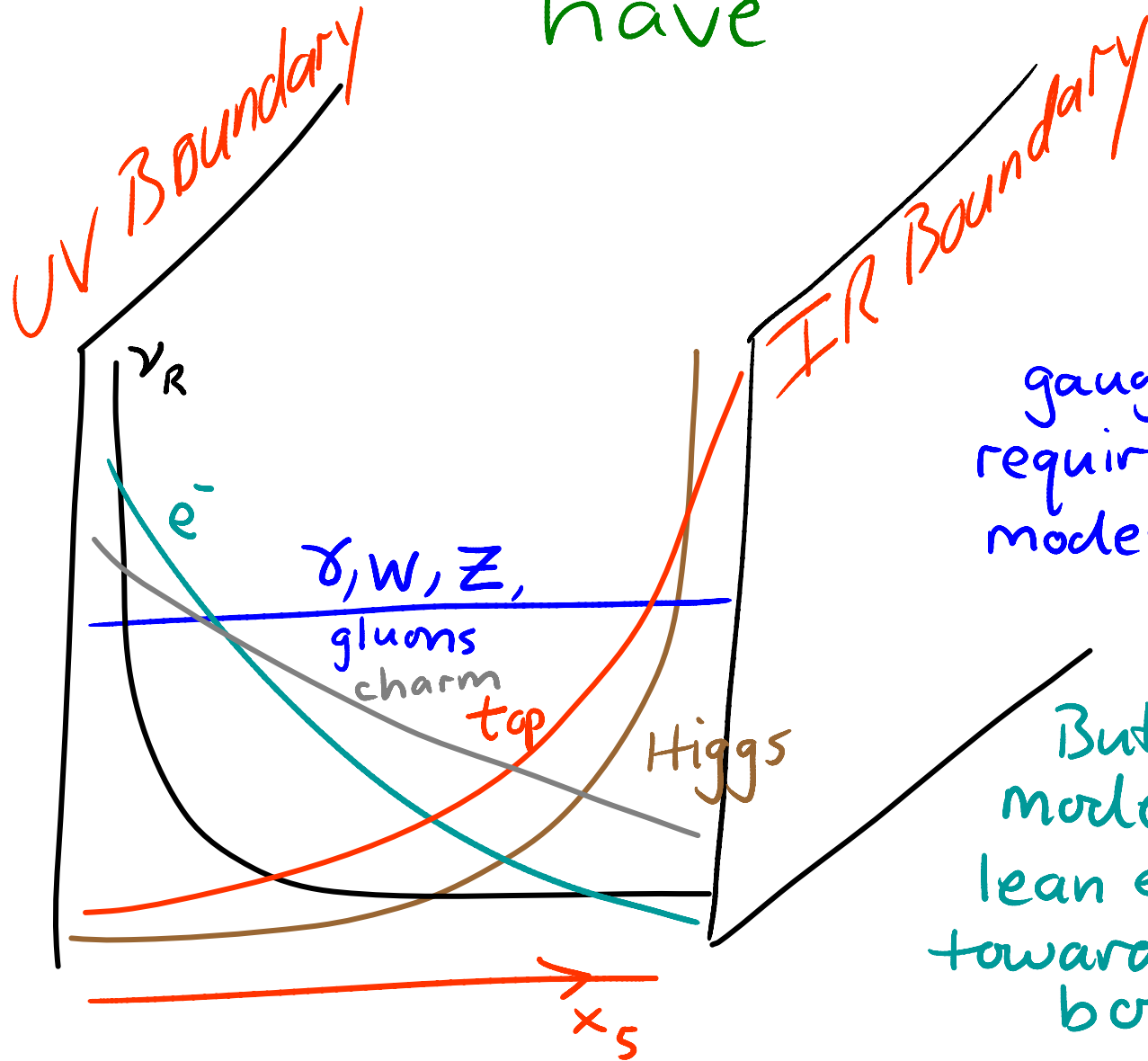


& are redshifted, $E_{KK} = m_{KK} c^2 \sim \frac{e^{-L/R}}{L} \sim \text{TeV}$

ORIGINAL RS1



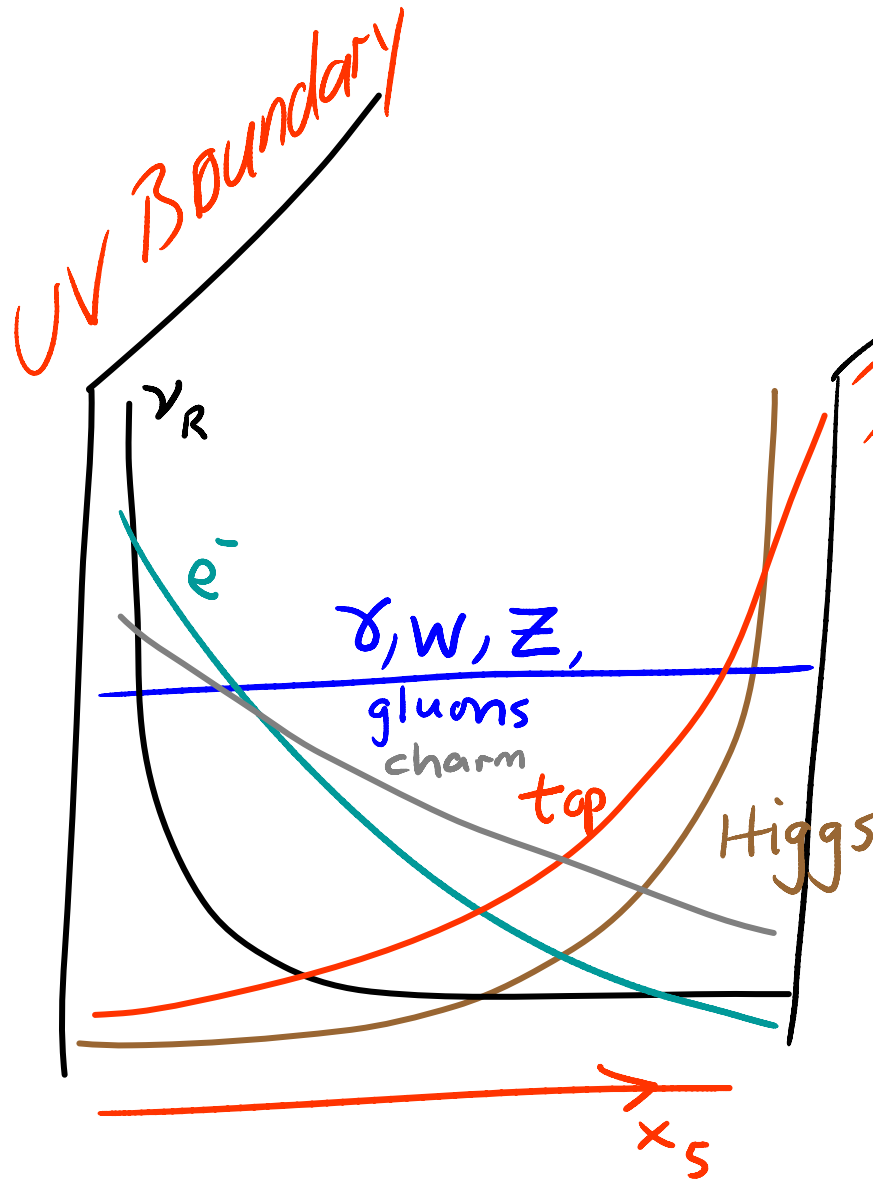
MODERN VARIANTS have



gauge invariance
requires gauge
modes to be
"flat"

But matter
modes tend to
lean exponentially
towards a
boundary

5D CHAOS = 4D COSMOS



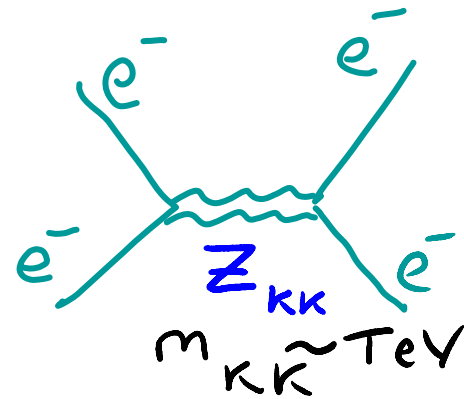
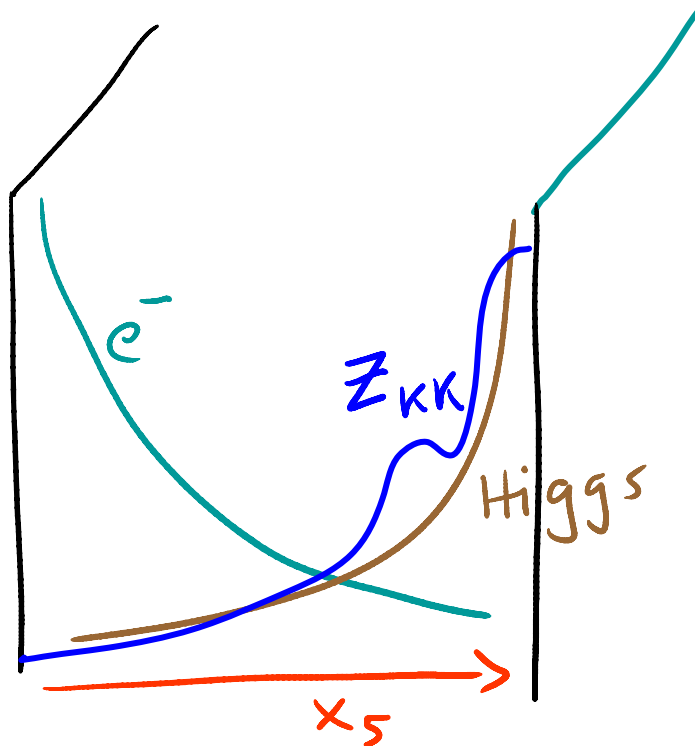
Flavor Hierarchies from extra-dimensional wavefunction overlaps with Higgs

(Arkani-Hamed, Schmaltz '00)
Grossman, Neubert '00
Gherghetta, Pomarod '00
Huber, Shafi '01
Agashe, Okui, Sundrum '08
⋮

PRECISION TESTS

≡ virtual sensitivity to
KK excitations

Compositeness tests



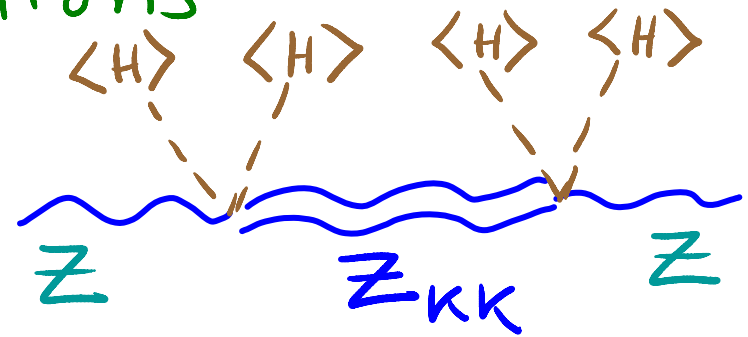
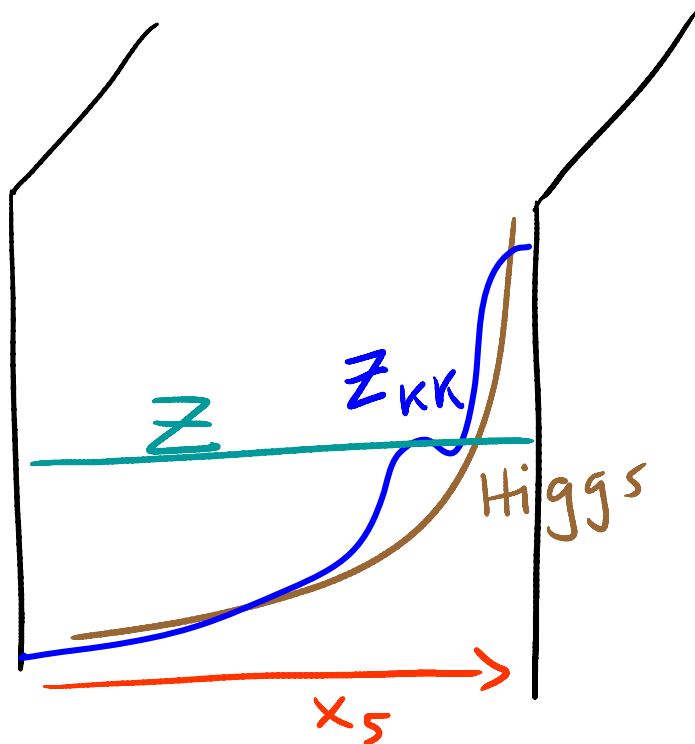
suppressed by
small $e^- - Z_{kk}$
overlap

$\sim e^- - \text{Higgs overlap.}$

PRECISION TESTS

≡ virtual sensitivity to
KK excitations

Electroweak tests:



requires extending
5D gauge symmetry

$$SU(3) \times SU(2)_L \times U(1)_Y$$

$$\rightarrow SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_X$$

Agashe, Delgado, May, Sundrum '03

Even then, $m_{KK} \gtrsim 3 \text{ TeV}$.

based on long history...

Davoudiasl, Hewett, Rizzo '00

Chang et. al '00

Huber, Shafi '01

Huber, Lee, Shafi '02

Csaki, Erlich, Terning '02

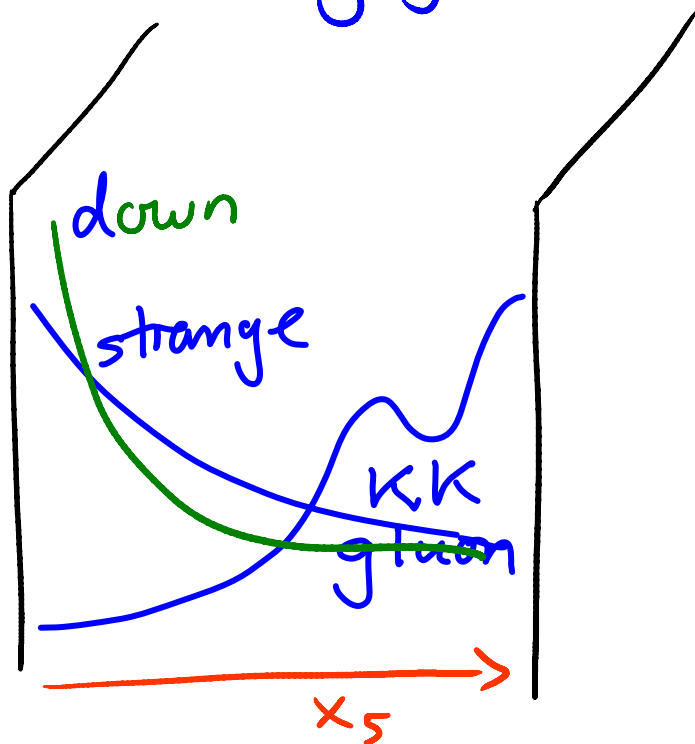
Hewett, Petriello, Rizzo '02

Burdman '02

PRECISION TESTS

≡ virtual sensitivity to
KK excitations

Flavor-changing tests: have virtual sensitivity to extremely high mass scales



suppressed again by
wavefunction overlaps

Agashe, Perez, Soni '04

$$m_{KK} \gtrsim 3 \text{ TeV}$$

PRECISION TESTS

≡ virtual sensitivity to
KK excitations

~~CP~~ tests in flavor-changing
+ edm's (also worrying
for SUSY)

Agashe, Perez, Soni '05

Csaki, Falkowski, Weiler '08

Casagrande, Goertz, Haisch, Neubert, Pfoh '08

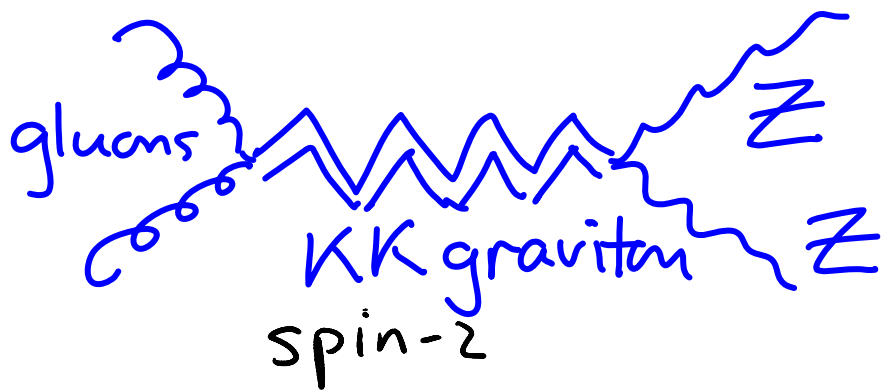
Blanke, Buras, Duling, Gori, Weiler '09; Agashe, Azarov, Zhu '09

Gedalia, Isidori, Perez; Blum, Grossman, Nir, Perez '09

$m_{KK} \gtrsim 5-10 \text{ TeV}$ in dominant part of
parameter space,

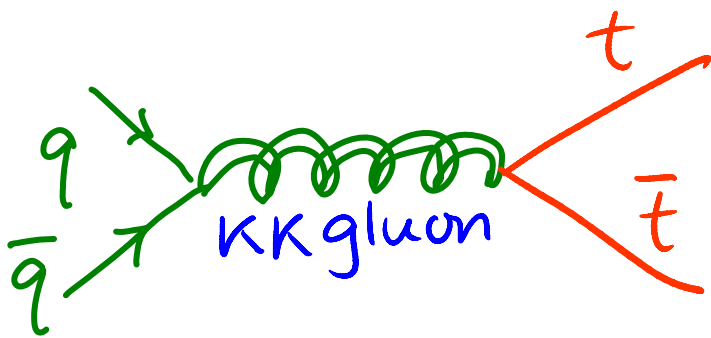
OR still missing some special ~~CP~~ mechanism.

KK RESONANCES $\lesssim 3\text{TeV}$ @ LHC $_{14\text{TeV}}$



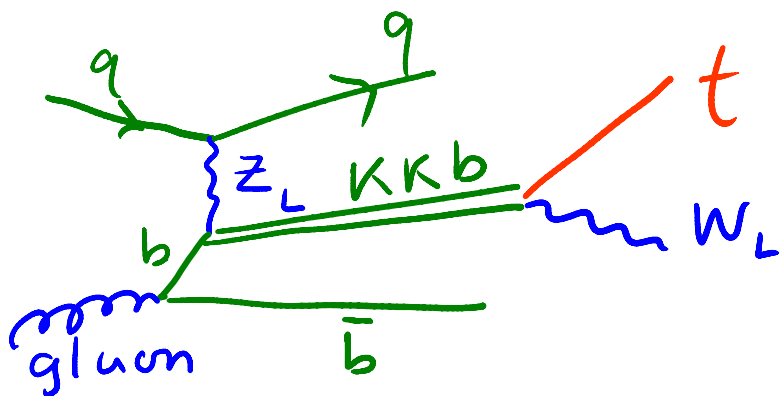
$$\sigma(pp \rightarrow Z_{KK}^{TeV} \rightarrow ZZ) \sim 5-10\text{fb}$$

Fitzpatrick, J. Kaplan, Randall,
L. Wang '07
Agashe, Davoudiasl, Perez, Soni
'07



$$\sigma(pp \rightarrow Z_{KK}^{TeV} \rightarrow t\bar{t}) \sim 100\text{fb}$$

Agashe, Belyaev, Krupovnickas,
Perez, Virzi '06
Lillie, Randall, Wang '07

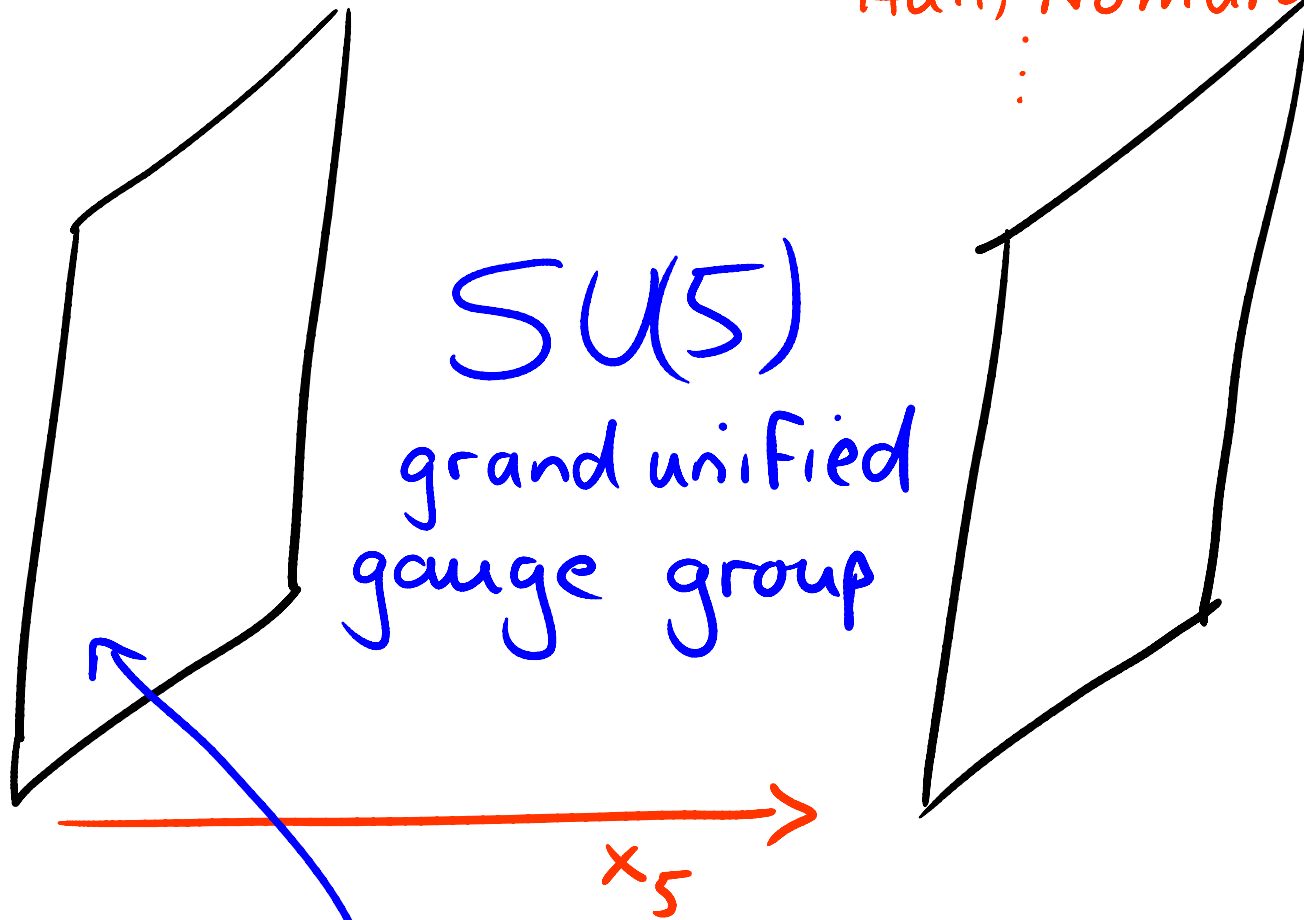


$$\sigma(pp \rightarrow \bar{b} b_{KK}^{1.5\text{TeV}} \rightarrow \bar{b} t W_L) \sim 10\text{fb}$$

similar to Little Higgs
"top partner".

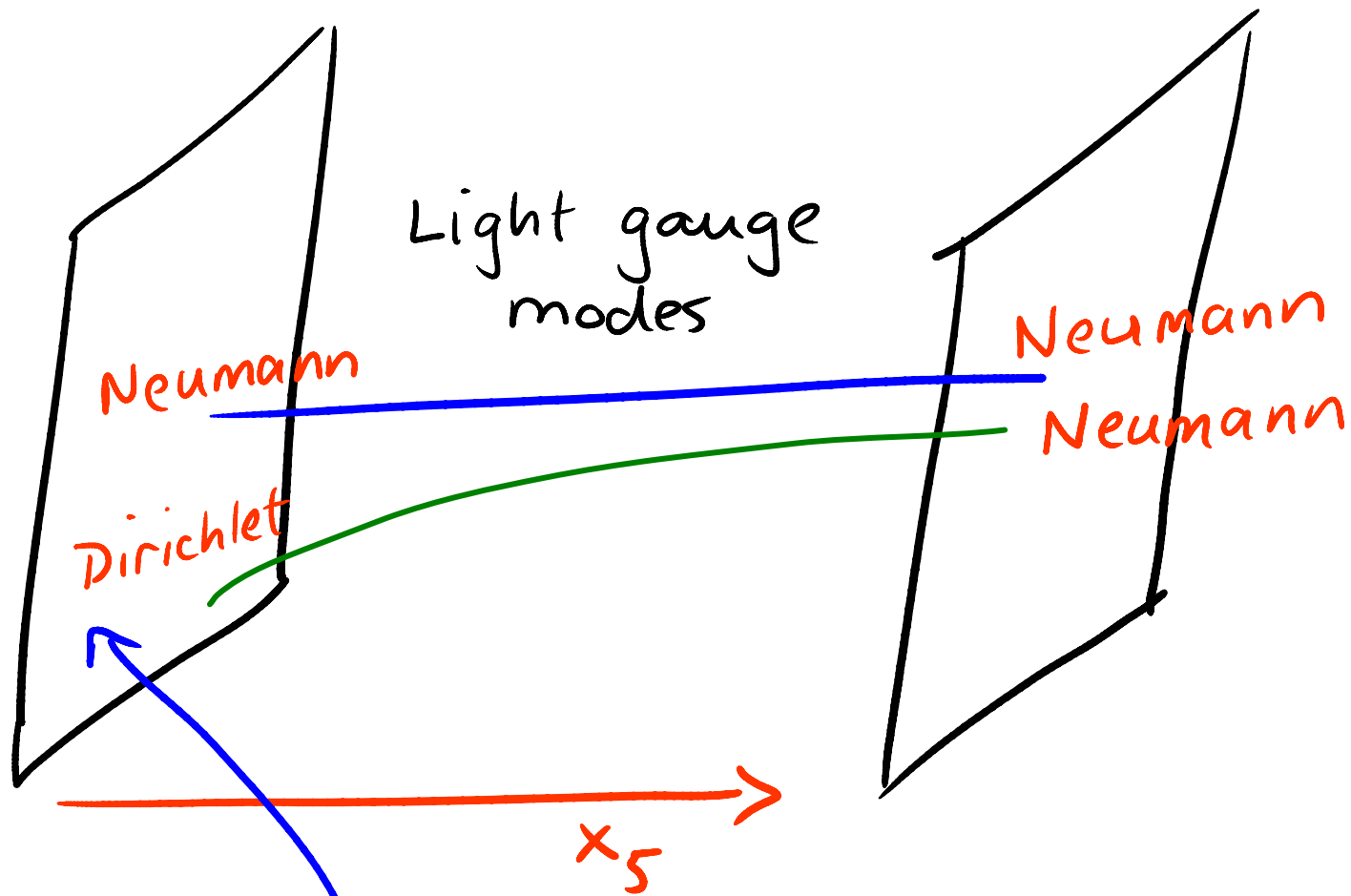
(ORBIFOLD) UNIFICATION

Kawamura '00
Hall, Nomura '01
⋮



broken by extra-dimensional boundary condition $\rightarrow SU(3) \times SU(2)_L \times U(1)_Y$

(ORBIFOLD) UNIFICATION

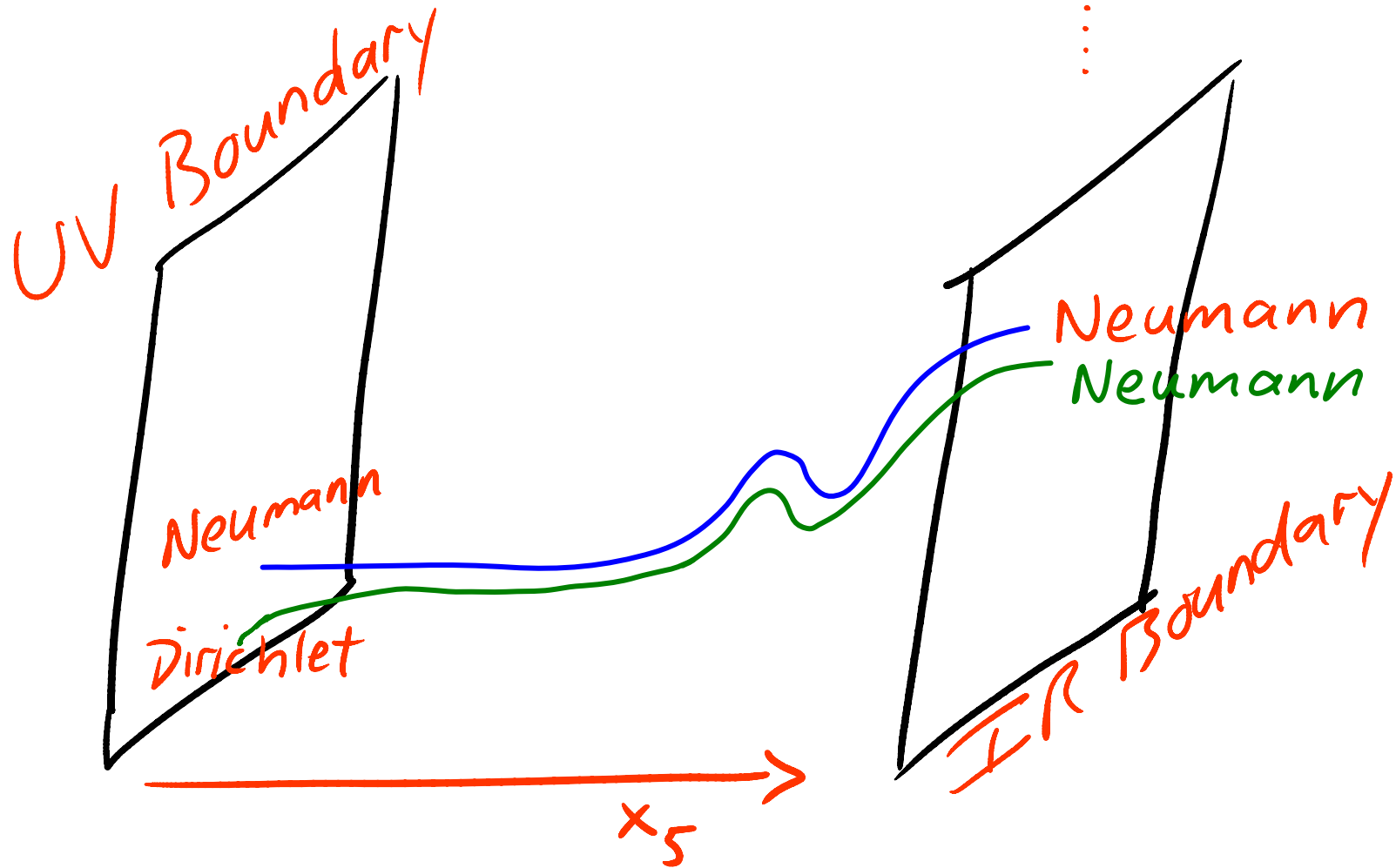


broken by extra-dimensional boundary condition $\rightarrow SU(3) \times SU(2)_L \times U(1)_Y$

WARPED UNIFICATION

Pomared '00

⋮

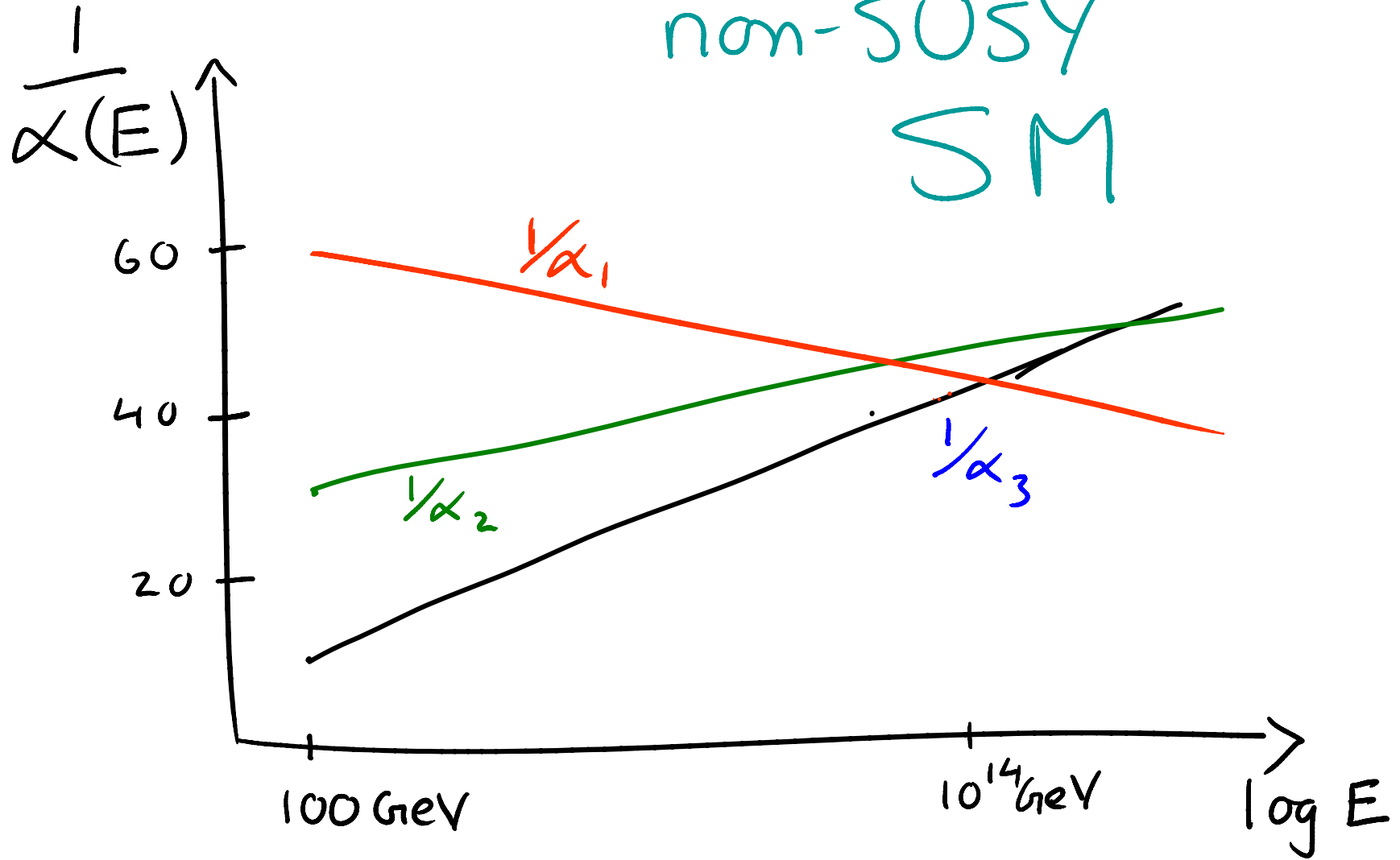


KK modes remain \cong unified at several TeV, insensitive to UV boundary.

Gauge Coupling Unification

non-SUSY

SM

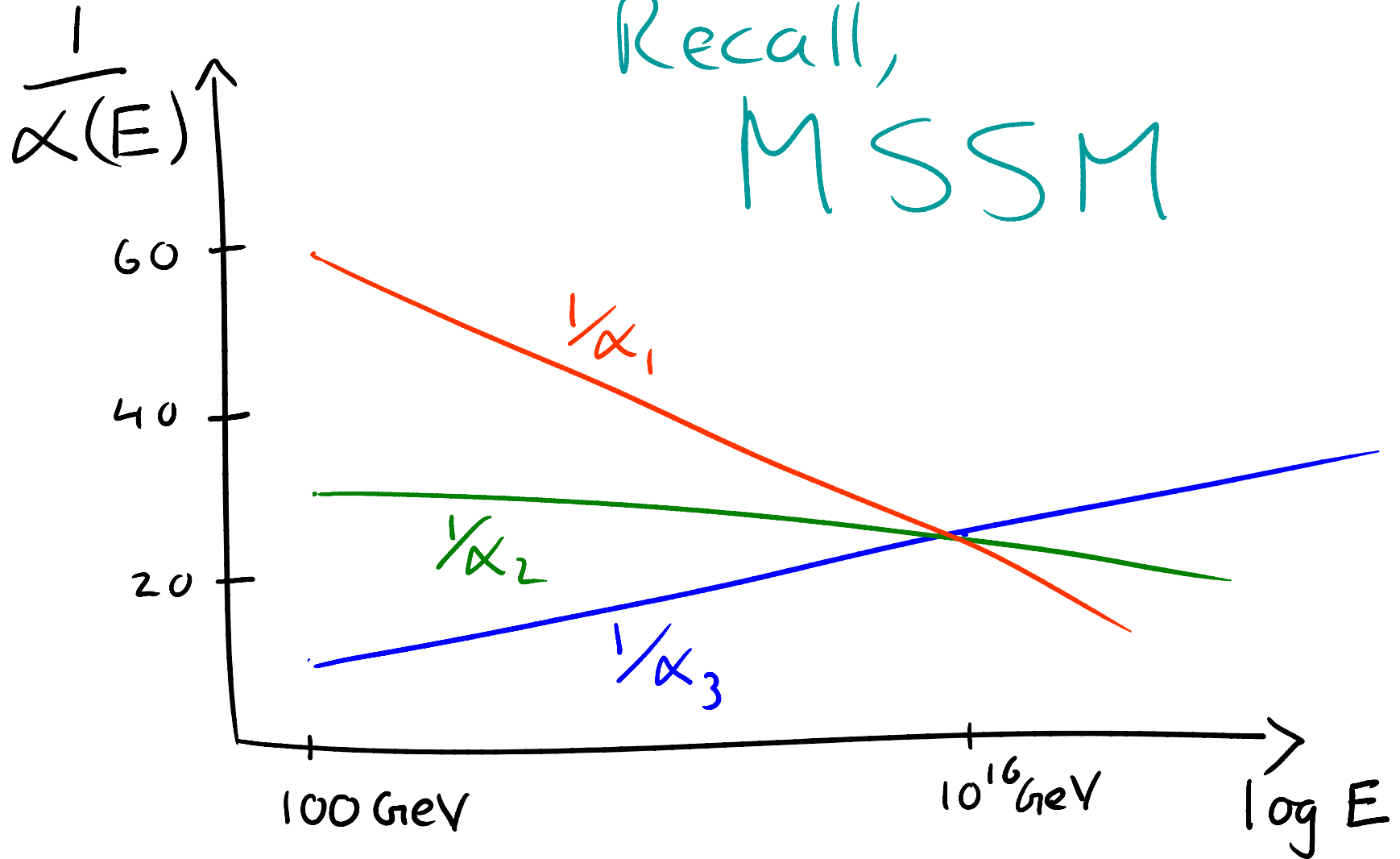


intriguing but not precise

Gauge Coupling Unification

Recall,

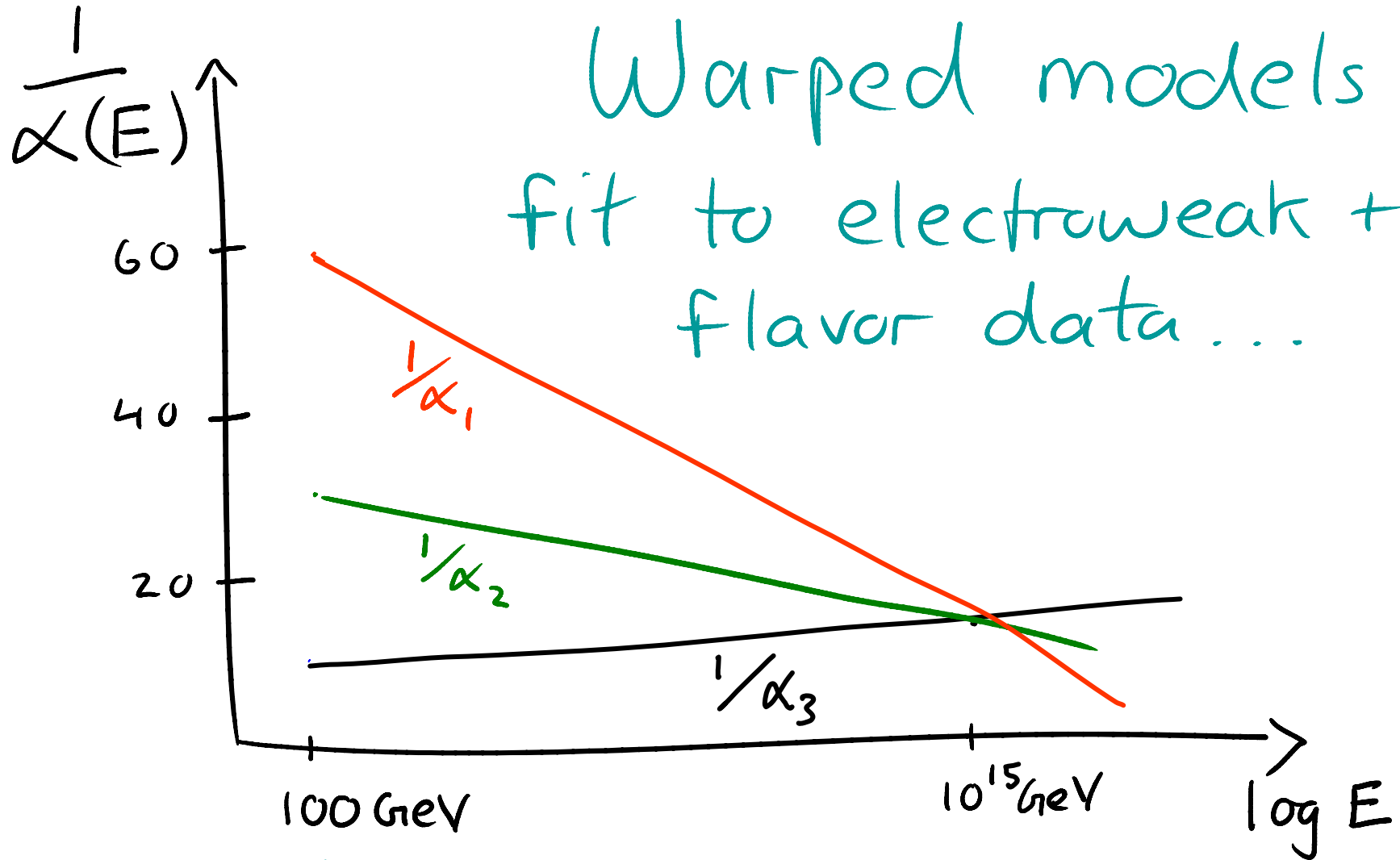
MSSM



gives precision unification

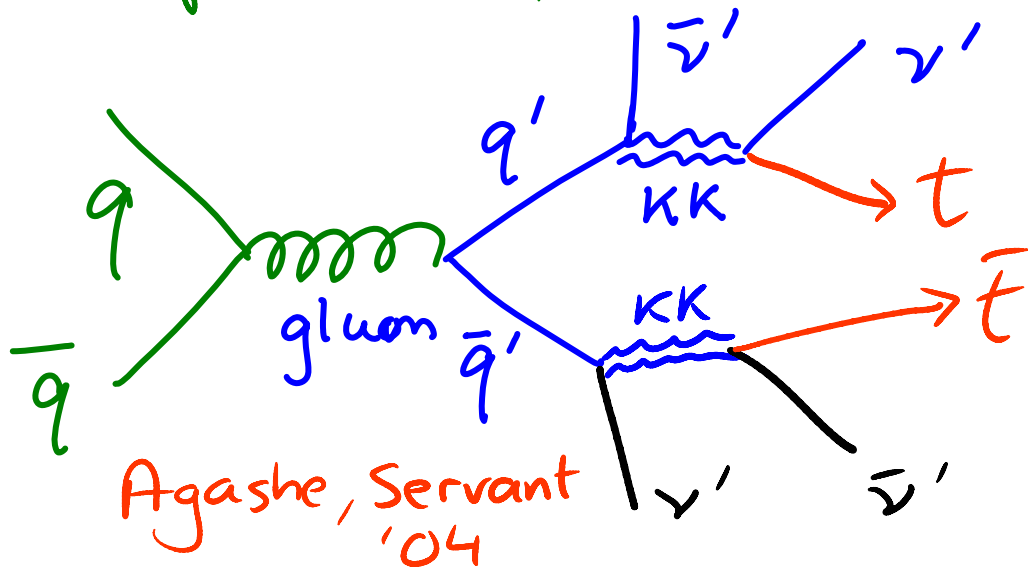
Gauge Coupling Unification

Warped models
fit to electroweak +
flavor data...



... also give precision unification!
Agashe, Contino, Sundrum '05

Such extra structure in Warped theory \rightarrow "Light" exotics $< \text{TeV}$

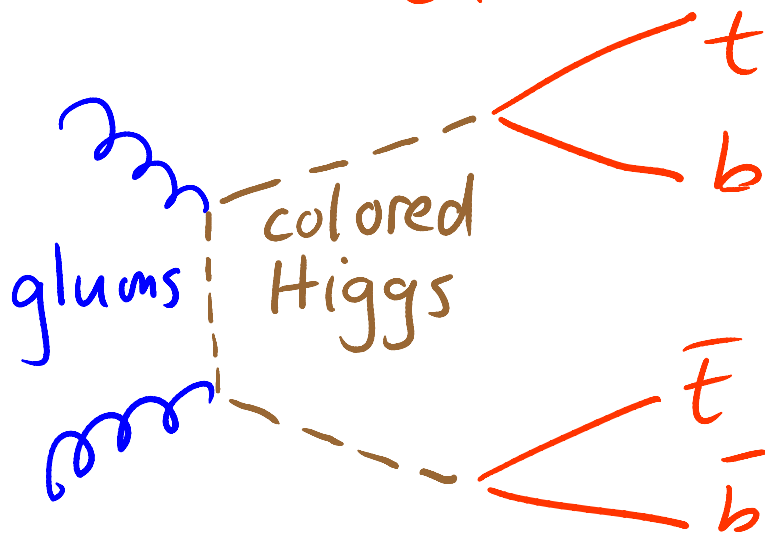


$$\sigma(pp \rightarrow \bar{q}' q' \rightarrow \bar{t} t + \cancel{E})$$

500 GeV each

$\sim 3000 \text{ fb}$

Exotic ν' stable, good WIMP dark matter



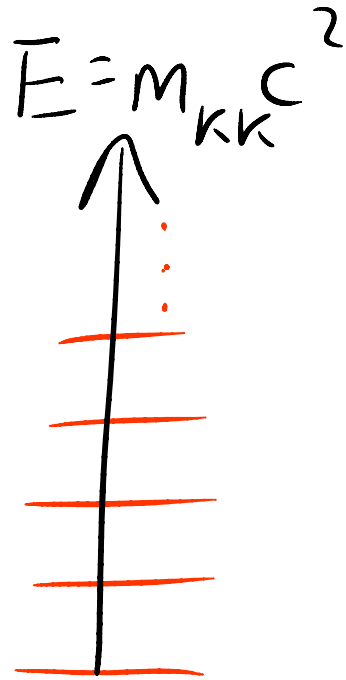
$$\sigma(pp \rightarrow \bar{H}_{col.} H_{col.} \rightarrow t \bar{t} b \bar{b})$$

500 GeV each

$\sim 500 \text{ fb}$

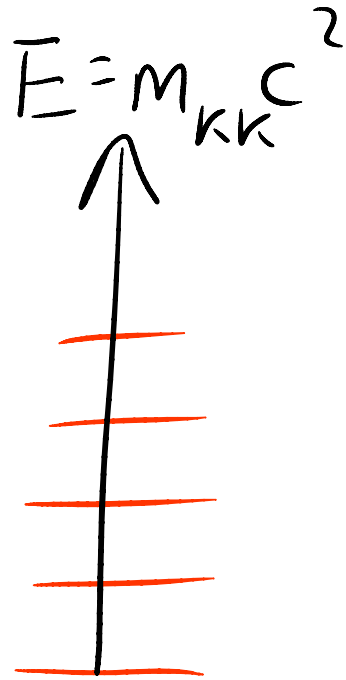
Contino, Kramer, Son, Sundrum (in progress)

AdS/CFT DUALITY

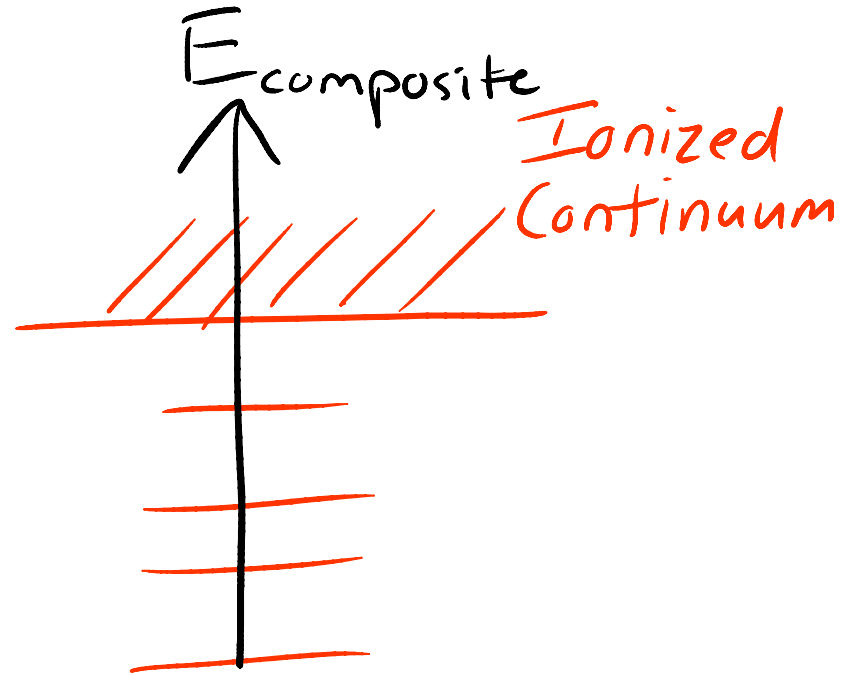


Warped
KK Spectrum

AdS/CFT DUALITY

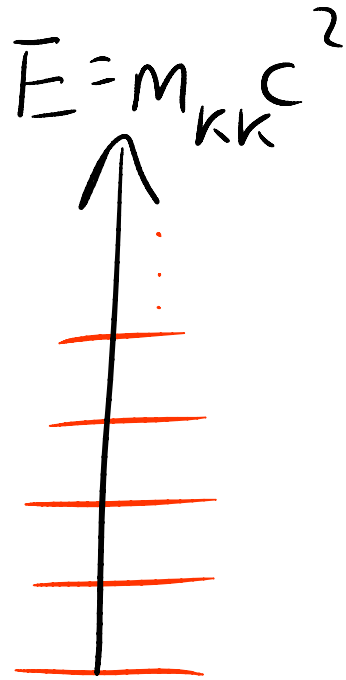


Warped
KK Spectrum

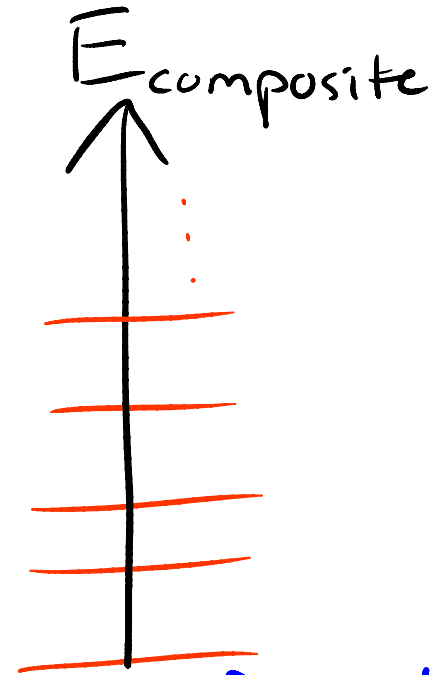


Bound State
Spectrum

AdS/CFT DUALITY

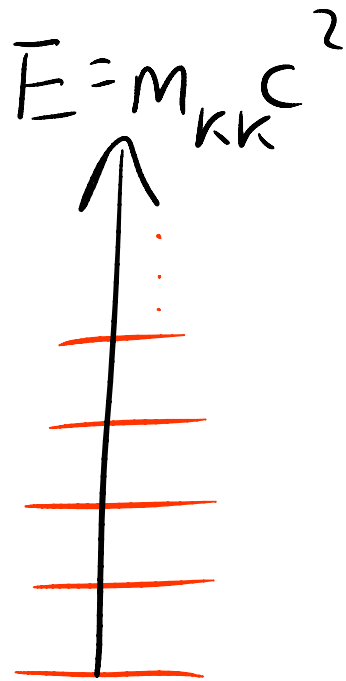


Warped
KK Spectrum

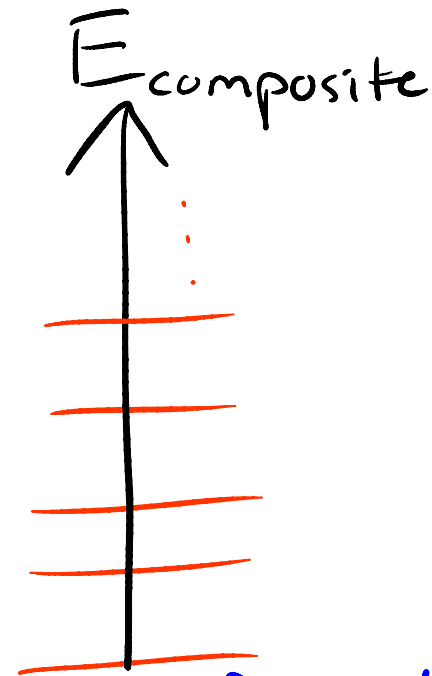


Confined
Bound State
Spectrum

AdS/CFT DUALITY



Warped
KK Spectrum



Confined
Bound State
Spectrum

Maldacena '98 ; Gubser, Klebanov, Polyakov '98 ; Witten '98
H. Verlinde '00 ; Gubser '01 ; Arkani-Hamed, Porrati, Randall '01
Rattazzi, Zaffaroni '01 ; Perez-Victoria '01

AdS/CFT DUALITY

Theories of Warped Dimensions have very similar "DNA" to Theory of Strong Nuclear Force, despite appearances.

Warped Dimensions \equiv calculable variants of theories of Higgs Compositeness

see eg. Georgi, Kaplan '84
D.B. Kaplan '91

~~OUTLINE~~ CONCLUSIONS

- A non-supersymmetric, but extra-dimensional approach to Hierarchy Problem.
- Comprehensively developed & studied
- Deep principles are at stake
- An unusual, challenging phenomenology to prepare for:

Heavy Resonances \rightarrow highly boosted
 t, b, W, Z, higgs .